

MATHS

BOOKS - ZEN MATHS (KANNADA ENGLISH)

CO-ORDINATE GEOMETRY

Illustrative Example

1. Find a point on the X-axis equidistant from A (5,4) and B(-2,3).

2. If distances of a point (x, y) are equidistant from (a +b, b-a) and (a- b, a + b), prove that bx = ay.



3. Show that the points (12, 8), (-2,6), and (6, 0) are vertices of a right-angled triangle.



4. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4).



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5. Show that the points (0,-1), (2, 1), (0, 3), and (-2, 1) are the corners of a square.



6. Show that the points (1,-1), (5,2), and (9,5) are collinear.



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7. Points A (-1, y) and B (5, 7) lie on the circumference of a circle with centre O (2,-3y).

Find y. Hence find the radius of the circle.



8. Find the coordinates of the circumcentre of a triangle whose vertices are (8, 6), (8, - 2), and (2-2). Also find its circumradius.



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9. Find the coordinates of the points of trisection of the line segment joining (4, -1) and (-2, -3).



10. Find the midpoint of the line joining (3,-8) and (2,-2). Midpoint M of line joining A (3,-8) and B (2,-2) is



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11. In what ratio is the line joining, A (4, 4) and B (7, 7) divided byP(F,-1)7



12. Determine theratio in which P (m, 6) divides AB where A (-4,3) and B(2,8). Findm.



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13. Determine the ratio in which 2x + 3y +7 divides the line joining of A (3,4) and B (7, 8). Find the point.



14. Prove that (4,-1), (6, 0), (7,2), and (5,1) are the vertices of a rhombus but not a square.



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15. IF the coordinates of the midpoints of the sides of a triangle are (1, 2), (0, -1), and (2,-1), find vertices of triangle.



16. If the midpoint of the line joining (3,4) and



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(K, 7) is (y) and 2x + 2y + 1 = 0, find K.

17. Find the area of the triangle formed by points (3, 4, (2-1), and (4,-6).



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18. Check if -5,1), (5, 5), and (10, 7) are collinear.



19. Find x for which (a, 0), (0, b), and (3a, x) $(a \neq 0)$ lie on a line .



Textual Exercise Exercise 7 1

1. Find the distance between the following pairs of points:

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(2,3), (4,1)

and (36, 15).



3. Determine if the points (1, 5), (2, 3) and (-2,

2. Find the distance between the points (0, 0)

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-11) are collinear.

4. Check whether (5, -2), (6, 4) and (7, 2) aare the vertices of as isoceles triangle.



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5. Name the type of quadrilateral formed, if any by the following points, and give reasons for your answer:

(-3, 5), (3, 1), (0, 3), (-1, -4)



6. Find the point on the x-axis which is equidistant from (2, -5) and (-2, 9).



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7. Find the values of y for which the distance between the points P(2, -3) and Q(10, y) is 10 units.



8. If Q(0, 1) is equidistant from P(5, -3) and R(x, 6), find the values of x. Also find the distance QR and PR.



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9. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4).



Textual Exercise Exercise 7 2

1. Find the corrdinates of the point which divides the join of (-1, 7) and (4, -3) into the ratio 2:3 internally.



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2. Find the coordinates of the points of trisection of the line segment joining A(4, -1) and B(-2, -3).



3. To conduct Sports Day activities, in your rectangu- lar shaped school ground ABCID, lines have been drawn with chalk powder at a distance of 1m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in the following figure. Niharika runs 1/4th the distance AD on the 2^{nd} line and posts a green tlag. Preet runs 1/5th the distance AD on the eighth line and posts a red tlag What is the distance between both the flags? If Rashmi has to post a blue flag

exactly halfway between the line segment joining the two flags, where should she post her flag?



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4. Find the ratio in which the line segment joining the points (-3, 10) and (6, -8) is divided by (-1, 6).



5. Find the ratio in which the line segment joining A(1, -5) and B(-4, 5) is divided by the x-axis. Also find the coordinates of the point of division.



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6. If (1, 2), (4, y), (x, 6) and (3, 5) are the vertices of a parallelogram taken in order, find x and y.



7. Find the coordinates of a point A, where AB is the diameter of a circle whose centre is (2, -3) and B is (1, 4).



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8. If A and B are (-2, -2) and (2, -4), respectively, find the coordinates of P such that AP $= \frac{3}{7}AB \text{ and P lies on the line segment AB.}$



9. Find the coordinates of the points which divide the line segment joining A(-2, 2) and B(2, 8) into four equal parts.



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10. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-2, -1) taken in order. [Hint : Area of a rhombus $=\frac{1}{2}$ (product of its diagonals)].



Textual Exercise Exercise 7 3

1. Find the area of the triangle whose vertices are:



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2. In each of the following find the value of 'k' for which the points are collinear.

$$(8,1),(k,-4),(2,-5)$$



3. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.



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4. Find the area of the quadrilateral whose vertices, taken in order are (-4, -2), (-3, -5), (3, -2)

and (2, 3).



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5. You have studied in Class IX, (Chapter 9, Example 3), that a median of a triangle divides it into two triangles of equal areas. Verify this result for ΔABC whose vertices are A(4, -6), B(3, -2) and C(5, 2).



Textual Exercise Exercise 7 4

- 1. Determine the ratio in which the line 2x + y -
- 4 = 0 divides the line segment joining the points A(2, -2) and B(3, 7).



2. Find a relation between x and y if the points

(x, y), (1, 2) and (7, 0) are collinear.

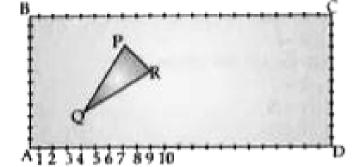
3. Find the centre of a circle passing through the points (6, -6), (3, -7) and (3, 3).



4. The two opposite vertices of a square are (-1,2) and (3, 2). Find the coordinates of the other two vertices.



5. The Class X students of a secondary school in Krishinagar have been alloted a rectangular plot of land for their gardening activity. Sapling of Gul mohar is planted on the boundary at a disatnce of 1m from each other. There is a triangular grassy lawn in the plot as shown in the figure. The students are to sow seeds of flowering plants on the remaining area of the plot.



(i) Taking A as origin, find the coordinates of the vertices of the triangle.

(ii) What will be the coordinates of the vertices of ΔPQR if C is the origin

Also calculate the areas of the triangles i these cases . What do you observe ?



and C (7,2). A line is drawn to intersect sides

6. The vertices of a \triangle ABC are A (4.6), B (1.5)

AB and AC at D and E respectively, such that

$$rac{AD}{AB} = rac{AE}{AC} = rac{1}{4}.$$
 Calculate the area of Δ

ADE and compare it with area of Δ ABC



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7. Let A (4, 2). B (6, 5) and C (1, 4) be the vertices of Δ ABC.

i The median from A meets BC at D. Find the coordinates of point D.



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8. ABCD is a rectangle formed by the points A (-1,-1), B(-1,4), C (5, 4) and D (5, -1). P, Q R and S are the mid-points of AB, BC, CD, and DA respectively. Is the quadrilateral PQRS is a square? a rectangle? or a rhombus? Justify your answer.



Zen Additional Questions Multiple Choice Questions

1. The distance between (a $\cos \theta$ + b $\sin \theta$,0) and (0,a $\sin \theta - b \cos \theta$) is

A.
$$a^2 + b^2$$

B.
$$a^2 - b^2$$

C.
$$\sqrt{a^2+b^2}$$

D.
$$\sqrt{a^2-b^2}$$

Answer: C



- **2.** The co ordinates of the point which is reflection of the point (-3, 5) in X axis are
 - A. (3,5)
 - B. (3,-5)
 - C. (-3,-5)
 - D. (-3,5)

Answer: C



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3. If point P(6,2) divides the line joining A (6,5) and B (4, y) in the ratio 3:4 then the value of y is

A. 4

B. 3

C. 2

D. 1

Answer: B



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4. The ratio in which the line segment (a_1,b_1) and $\mathsf{B}(a_2,b_2)$ is divided by Y-axis is

A.
$$-a_1 : a_2$$

B.
$$a_1 : a_2$$

C.
$$b_1 : b_2$$

D.
$$-b_1:b_2$$

Answer: A::B



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5. The length of the line segment joining A(2,3) and B is 10 units . If absc is a of B is 10, its ordinate can be

A. 3 or - 9

B.-3 or 9

C. 6 or 27

D. -6 or -27

Answer: C



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6. If the centroid of a triangle formed by the points a. b), (b, c), and (c a) is at the origin, then $a^3+b^3+c^3$ =

A. abc

B. 0

C.a+b+c

D. 3 abc

Answer: A::B::C



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7. The coordinates of a point on the X-axis which lie on the L bisector of the line segment joining (7, 6) and (-3, 4) are

A.(0,2)

B.(3,0)

C.(0,3)

D. (2,0)

Answer: B



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8. If (t, 2t), (-2, 6), and (3, 1) are collinear, t =

A. 3/4

B.4/3

C.5/3

D.3/5

Answer: C::D

9. Length of the median through C of Δ ABC with A(4,9) B(2, 3), and C (6, 5) is

A. 5 units

B. $\sqrt{10}$ units

C. 25 units

D. 10 units

Answer: A



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10. If P(2, 4), Q(0, 3), R(3, 6), and S(5, y) are the vertices of a parallelogram PQRS, value of y is

A. 7

B. 5

 $\mathsf{C.}-7$

D. - 8

Answer:



11. The distance between the origin and coordinates of point (x,y) is

A.
$$x^2 + y^2$$

B.
$$\sqrt{x^2-y^2}$$

$$C. x^2 + y^2$$

D.
$$\sqrt{x^2+y^2}$$

Answer: B



Zen Additional Questions Very Short Answer Vsa Type Questions

1. Find the area of the triangle Δ ABC with A(a,b+c), B(b,c+a), and C(c, a+ b).



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2. Find the length of the median AD of Δ ABC with A(5,1) , B(1,5), and C(-3,-1).



3. Find the ratio in which the line segment PQ P(4, 5) and Q(3,7), is internally divided by the Yaxis.



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4. Find k if (2,1), (k,-1) and (-1,3) are collinear.



5. Find 'a' so that (3,a) lies on the line 2x - 3y = 5



6. Find k if the centroid of the triangle whose vertices are (2,k), (-5,2) and (3, 4) is (0,-2).



7. The endpoints of the diameter of a circle are

(2, 4) and (3-1). Find the radius of the circle.



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8. Find the distance between (0.5) and (-5.0).



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9. Find the point equidistant from (3, 8) and (-10,-5).

10. Plot these points on the Cartesian plane.

(i) A (-4,0) (ii)B (0,5) (iii) C (3 -4) (iv) D (-2,5) (v) E (-1,-1) (vi) F (3,5)



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11. A square of side 4 units lies in I Quadrant on the X-axis, with its one vertex at the origin.

Plot the coordinates of the other 3 vertices of the square.



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12. Draw the quadrilateral whose vertices are (1, 1), (24), (8,4), and (10, 1).



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13. Find distance between the pair of points given.

(i) $(a\sin lpha,\ -b\cos lpha), (\ -a\cos lpha, b\sin lpha)$

(ii) (a + b, b + c), (a - b, c - b)

(iii) (4, 10), (7 - 6)



14. Find the coordinates of the mid-point of the line joining the points (x_1, y_1) and (x_2, y_2) .



Zen Additional Questions Short Answer Sa Type Questions

1. Find the value (s) of x if distance between A (0, 0) and B (x,-4) is 5 units.



2. What is the distance of P (x, y) from the origin?



3. A line intersects y-axis and x-axis at the points P and Q respectively. If (2, 5) is the mid point of PQ then find the co ordinates of P and Q.



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4. If the distance between P (x, y) from A (5, 1) and B (-1,5) are equal, show that 3x = 2y.



5. Find the area of A ABC where A(-3/2, 3), B(6, -3/2, 3)

-2), and C(-3,4).



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6. Find k if A (k + 1, 24), B(3k, 2k + 3), and C(5k-1, 24)5k) are collinear.



7. Find the ratio in which x - y - 2 = 0 divides the line segment joining (8, -1) and (8, 9).



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8. The length of a line segment is $\sqrt{29}$ units. If one end is at (-3,5) and the ordinate of the other end is 7, show that the absciss is either 2 or -8.



9. Given P $\left(at^2,2at\right),Q\left(rac{a}{t^2},rac{-2a}{t}
ight)$, and S(a, 0) , show that $rac{1}{SP}+rac{1}{SQ}$ is independent of t



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10. Use a graph sheet to plot points P (-2, 2), Q (4, -2), and R (5, 2). Complete Δ PQR. Find the altitude drawn fromQ to PR from the graph. Also find the area of Δ PQR.



11. James started from a point X, 4 units away from the origin above the X-axis. He walked to the origin and turned right to Y, 3 units away. What are points X and Y? Locate them on the Cartesian plane. What is distance between X and Y?



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12. The base AB of an equilateral Δ ABC of side 2p lies along the X-axis such that the midpoint

of AB is at the origin and vertex C is above xaxis. Find coordinates of the vertices of Δ ABC.



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13. Plot points P (3, 8) and Q (3,-8). Join AOPQ. What kind of a Δ is it? Find its area.



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14. If A (3,y) is equidistant from P (8,-3) and Q(7, 6), find y and the distance AQ.

15. Find the values of y for which the distance between the points P(2, -3) and Q(10, y) is 10 units.



16. Find the equation of the perpendicular bisector of the line segment joining (7,1) and (3,5).

17. If P (2,2) is equidistant from A (-2, k) and B (-2k,-3), find k. Also find the length AP.



18. Find a point equidistant from A (-5, 4) and

B(-1,6). How many such points are there?



19. Show that (1, 0), (0, 1), (-3,4) are on a straight line.



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20. If P (x, y) lies on a circle whose centre is (3,-2) and radius is 3, show that $x^2 + y^2 - 6x + 4y + 4 = 0.$



21. The centre of a cicle is (2a, a -7). Find the values of aif the circle passes through (11, -9) and has a diameter of $10\sqrt{2}$ units .



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22. Prove that (2a, 4a), (2a, 6a), and (2a $+\sqrt{3}a$, 5a) are the vertices of an equilateral triangle.



23. Find the area of a triangle whose vertices are (1, -1), (-4, 6) and (-3, -5).



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24. Prove that the area of the triangle whose vertices are (t,t-2), (t+2,t+2), and (t+3,t) is independent of t.



25. Find the area of the quadrilateral ABCD whose vertices are A(1, 1), B(7,-3), C(12, 2), and D(7, 21).



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26. Show That (3, -2) is the 3rd verlex of a Δ ABC where A (2. 3), B (-2,1), and centroid is G (1, 2/3).



27. Find the area of a parallelogram ABCD if three of its vertices are A(2, 4), $B(2+\sqrt{3},5)$ and C(2, 6).



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28. Find the co - ordinates of points which divides the line segment joining the points A $(4,\,-3)$ and B (8,5) in the ratio $3\!:\!1$ internally



29. Find the distance between the points (2,3) and (4,1).



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30. Find the coordinates of the point which divides the line joining the points (1,6) and (4,3) in the ratio 1:2.



31. The points A(1, 1), B(3, 2) and C(5, 3)cannot be the vertices of the triangle ABD. Justify.



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32. If A(-2, -1) B(a, 0) C(4, b) and D(1, 2) are the vertices of a parallelogram. Find a and b



33. IfA(-5, 7), B (4, 5), C(-1,-6) and D (4,5) are the vertices of a quadrilateral. Find the area of quadrilateral.



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34. If the points A (k +1, 2k), B (3k, 2k + 3) and C (5k-1, 5k) are collinear, then find the value of k.



35. If the point P (x, y) is equidistant from the points A (a + b, b - a) and B(a - b, a + b). Prove that bx = ay.



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36. A (0,6), P (4,-3), and the origin O form a Δ OPA. Δ OPA is turned with its base OA on the Y-axis to form Δ OQA . What are the coordinates of Q? What is figure OPAQ? Is

 $\Delta OPA \cong \Delta OQA$? Give reason. Find the area of OPAQ.



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37. Find a and b if M (9a -2, -b) divides the line segment joining P (3a + 1,-3) and Q (8a, 5) in the ratio 3: 1.



38. Find the ratio in which (-4, 6) divides the line segment joining A (6, 10) and B (3,-8).



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39. Find the points of trisection of the line segment joining the points. i] (5,-6) and(-7,5) ii (2,-2) and (-7,4)



40. Three vertices of a parallelogram are (a + b ,a - b), (2a + b, 2a - b), and (a - b, a + b). Find the 4th vertex.



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41. A poin P divides the line segment joining A (3,-5) and B (- 4, 8) with $\frac{AP}{PB}$ = k. If p lies on the line x + y = 0 . Find k.



42. If the midpoints of the sides of a triangle are (3, 4) (4, 6), and (5,7), find the coordinates of the vertices of the triangle.



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43. In what ratio is the join of (-2, 2) and (4,5) cut by the axes of coordinates?



44. The vertices of \triangle ABC are A (1, 2), B (4, 6). and C (6, 14). AD bisects $\angle A$ and meets BC at D. Find the coordinates of D.



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45. Show that `(1,-1) , (-2,2) , (4,8) and (7,5) are the angular points of a rectangle.



46. The line segment joining (3,-4) and (1, 2) is trisected by P(a,-2) and Q (5/3, b). Find a and b.



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47. The centroid of a triangle ABC is (1, 2, 2) If the coordinates of A and B are (3, -5, 7) and (-1, 7, -6) respectively .

Find the coordinates of C.



48. The vertices of a Δ ABC are A (4,6), B (1, 5) and C (7,2). A line is drawn to intersect sides AB and AC at D and E respectively, such that

$$rac{AD}{AB} = rac{AE}{AC} = rac{1}{4}.$$
 Calculate the area of Δ

ADE and compare it with area of Δ ABC



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49. Prove that the median of Δ ABC divides it into two triangles of equal area. .



50. Find the value of a for which the area of the triangle formed by A(a, 2a), B(-2, 6), and C(3, 1) is 10 sq. units.



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51. If a $\neq b \neq$ 0, prove that points $(a,a^2),(b,b^2),$ and (0, 0) can never be collinear.



52. Prove that (a, 0), (0, b), and (1, 1) are collinear if $\frac{1}{a} + \frac{1}{b} = 1$.



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53. Find the values of a and b if P (9a-2,-b) divides the line segment A (3a +1,-3) and B (8a, 5) in the ratio 3:1.



54. The centre of a cicle is (2a, a -7). Find the values ofa if the circle passes through (11, -9) and has a diameter of $10\sqrt{2}$ units .



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55. For what value of k are (k, 2 2), (-k + 1, 2k), and (4-k, 6-2k) collinear?



56. The vertices of a Δ ABC are A (-3,2) , B (-1,-4) and C (5,2) . If M and N are the mid - points of AB and AC respectively show that 2 MN = BC .



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57. The vertices of a Δ ABC are A (-5,-1), B (3,-5), C (5,2). Show that the area of the Δ ABC is four times the area of the triangle formed by joining the mid-points of the sides of the triangle ABC.

Zen Additional Questions Long Answer La Type Questions

1. The vertices of AABC are A(4, 6), B(1, 5), and

C7, 2). A line is drawn to intersect sides AB and

AC at D and E respectively. Show that

$$rac{AD}{AB} = rac{AE}{AC} = rac{1}{4}.$$
 Find the area of Δ ADE

and compare it with Δ ABC.



2. The points A (6, 1), B (8, 2), and C 9, 4) are the three vertices of a parallelogram ABCD. If E is the midpoint of DC, find area of Δ ADE.



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3. If $D-\left(\frac{1}{5},\frac{5}{2}\right)$, E(7,3) and $F\left(\frac{7}{2},\frac{7}{2}\right)$ are the mid-point of the sides of Δ ABC , find the coordinates of Δ ABC.



4. The area of a triangle is 5 square units. Two of its vertices are (2,1) and (3,-2) and the third vertex lies on y = x + 3, find the third vertex.



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5. Find the coordinates of the centre of the circle passing through the point (0,0), (-2,1) and (-3,2). Also find the radius.



6. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.



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Zen Additional Questions Higher Order Thinking Skills Hots Questions 1. In what ratio does 4x +3y-13 0 divide the line segment joining (2, 1) and (1, 4)?



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2. Find the circumcentre of the triangle whose vertices are (0,0) $(3, \sqrt{3})$, and $(0, 2\sqrt{3})$.



3. Find the 4th vertex of a rhombus formed by (1,-1),(6, 1), and (8, 8).



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4. Find the coordinates of P which divides the line segment joining points A(1, 3) and B(3, 4) externally in the ratio 3:4.



5. If points (-3, 6), (-9, a), and (0, 15) are collinear, find 'a'.



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6. Check if the following points are collinear using section formula.

I] (-4, 6),(-6, 10), (3, -8) (ii) (1,-2), (2, 3), (-4,-3)



7. Find the perimeter and area of the quadrilaterals formed by the given point.s Mention the type of quadrilateral formed.

- (i) (0,3), (4,0), (0,-8), (-4,0)
- (ii) (5,0), (0,-5), (0,-9), (9, 0)
- (iii) (5, 3), (5, -3), (10, -6), (10, 6)



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- 8. Find the kind of quadrilateral formed by (1,
- 3),(0,8),(5,7), and (8,0).

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9. ABC is a triangle with vertices A(-8, 3), B(4, 5), C(-6,1). Find the vertices of a parallelogram in this Δ ABC sharing vertex B and having half the area of Δ ABC. Find the area of the paralelogram so formed.



10. Find the circumcentre of a triangle formed by (2,3), (1,-5), and (-1, 4).

11. Find λ if $2x - 27 + 5 + \lambda$ (3x - y + 4) = 0 passes through the midpoint of the line joining (2,3) and (4,9).



12. Find the point on the Y-axis equidistant from A(3, -6) and B(-2,5).



13. Find the coordinates of a point which divides the line joining points A(-3,2) and B(2, 6) in the ratio 3: 2.



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14. Let A(3,2), B(4, 1),C(3,1), and D(2, 4) be the vertices of a quadrilateral ABCD. Find the area of the quadrilateral formed by joining the midpoints of the sides of the quadrilateral ABCD.

