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India's Number 1 Education App

## MATHS

## BOOKS - ZEN MATHS (KANNADA

## ENGLISH)

## CO-ORDINATE GEOMETRY

## Illustrative Example

1. Find a point on the $X$-axis equidistant from $A$
$(5,4)$ and $B(-2,3)$.
2. If distances of a point ( $\mathrm{x}, \mathrm{y}$ ) are equidistant from $(a+b, b-a)$ and $(a-b, a+b)$, prove that $b x$ $=a y$.

## - Watch Video Solution

3. Show that the points $(12,8),(-2,6)$, and $(6,0)$ are vertices of a right-angled triangle.

## D Watch Video Solution

4. Find a relation between $x$ and $y$ such that the point ( $x, y$ ) is equidistant from the point (3,
$6)$ and ( $-3,4$ ).

## D Watch Video Solution

5. Show that the points $(0,-1),(2,1),(0,3)$, and $(-2,1)$ are the corners of a square.
6. Show that the points $(1,-1),(5,2)$, and $(9,5)$ are collinear.

## D Watch Video Solution

7. Points $A(-1, y)$ and $B(5,7)$ lie on the circumference of a circle with centre $\mathrm{O}(2,-3 y)$.

Find $y$. Hence find the radius of the circle.

- Watch Video Solution

8. Find the coordinates of the circumcentre of
a triangle whose vertices are (8, 6), (8, - 2), and
(2-2). Also find its circumradius.

## D Watch Video Solution

9. Find the coordinates of the points of trisection of the line segment joining (4, -1) and ( $-2,-3$ ).
10. Find the midpoint of the line joining $(3,-8)$
and (2,-2). Midpoint $M$ of line joining $A(3,-8)$ and $B(2,-2)$ is

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11. In what ratio is the line joining, $A(4,4)$ and
$B(7,7)$ divided byP(F,-1)7

- Watch Video Solution

12. Determine theratio in which $P(m, 6)$ divides
$A B$ where $A(-4,3)$ and $B(2,8)$. Findm.

## D Watch Video Solution

13. Determine the ratio in which $2 x+3 y+7$
divides the line joining of $A(3,4)$ and $B(7,8)$.
Find the point.

D Watch Video Solution
14. Prove that $(4,-1),(6,0),(7,2)$, and $(5,1)$ are the vertices of a rhombus but not a square.

## D Watch Video Solution

15. IF the coordinates of the midpoints of the sides of a triangle are (1, 2), (0, -1), and (2,-1), find vertices of triangle.

## D Watch Video Solution

16. If the midpoint of the line joining $(3,4)$ and $(K, 7)$ is $(y)$ and $2 x+2 y+1=0$, find $K$.

D Watch Video Solution
17. Find the area of the triangle formed by points (3, 4, (2-1), and (4,-6).

## - Watch Video Solution

18. Check if $-5,1$ ), ( 5,5 ), and ( 10,7 ) are collinear.

## - Watch Video Solution

19. Find $x$ for which ( $a, 0$ ), ( $0, b$ ), and ( $3 a, x$ ) $(a \neq 0)$ lie on a line.

## D Watch Video Solution

## Textual Exercise Exercise 71

1. Find the distance between the following pairs of points :
$(2,3),(4,1)$

## - Watch Video Solution

2. Find the distance between the points $(0,0)$ and $(36,15)$.

## D Watch Video Solution

3. Determine if the points $(1,5),(2,3)$ and $(-2$,
-11) are collinear.

- Watch Video Solution

4. Check whether (5, -2), $(6,4)$ and $(7,2)$ aare the vertices of as isoceles triangle.

## - Watch Video Solution

5. Name the type of quadrilateral formed, if any by the following points, and give reasons for your answer :
$(-3,5),(3,1),(0,3),(-1,-4)$

D Watch Video Solution
6. Find the point on the $x$-axis which is equidistant from (2, -5 ) and ( $-2,9$ ).

## D Watch Video Solution

7. Find the values of $y$ for which the distance between the points $P(2,-3)$ and $Q(10, y)$ is 10 units.
8. If $\mathrm{Q}(0,1)$ is equidistant from $\mathrm{P}(5,-3)$ and $\mathrm{R}(\mathrm{x}$,

6 ), find the values of $x$. Also find the distance QR and PR.

## - Watch Video Solution

9. Find a relation between $x$ and $y$ such that
the point ( $x, y$ ) is equidistant from the point ( 3 ,
$6)$ and ( $-3,4$ ).

## - Watch Video Solution

Textual Exercise Exercise 72

1. Find the corrdinates of the point which divides the join of $(-1,7)$ and (4, -3 ) into the ratio 2 : 3 internally.

## - Watch Video Solution

2. Find the coordinates of the points of trisection of the line segment joining
$A(4,-1)$ and $B(-2,-3)$.
3. To conduct Sports Day activities, in your rectangu- lar shaped school ground ABCID,
lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been
placed at a distance of 1 m from each other along $A D$, as shown in the following figure.

Niharika runs $1 / 4$ th the distance $A D$ on the $2^{\text {nd }}$
line and posts a green tlag. Preet runs 1/5th
the distance AD on the eighth line and posts a red tlag What is the distance between both
the flags? If Rashmi has to post a blue flag
exactly halfway between the line segment joining the two flags, where should she post her flag?

## D Watch Video Solution

4. Find the ratio in which the line segment
joining the points $(-3,10)$ and $(6,-8)$ is divided by $(-1,6)$.
5. Find the ratio in which the line segment joining $A(1,-5)$ and $B(-4,5)$ is divided by the $x-$ axis. Also find the coordinates of the point of division.

## - Watch Video Solution

6. If $(1,2),(4, y),(x, 6)$ and $(3,5)$ are the vertices of a parallelogram taken in order, find x and y .

## - Watch Video Solution

7. Find the coordinates of a point $A$, where $A B$
is the diameter of a circle whose centre is (2,
$-3)$ and $B$ is (1, 4).

## D Watch Video Solution

8. If $A$ and $B$ are $(-2,-2)$ and ( $2,-4$ ), respectively,
find the coordinates of $P$ such that $A P$ $=\frac{3}{7} A B$ and P lies on the line segment AB .
9. Find the coordinates of the points which divide the line segment joining $A(-2,2)$ and $B(2$, 8) into four equal parts.

## D Watch Video Solution

10. Find the area of a rhombus if its vertices are $(3,0),(4,5),(-1,4)$ and $(-2,-1)$ taken in order.
[Hint : Area of a rhombus $=\frac{1}{2}$ (product of its diagonals)].

## - Watch Video Solution

Textual Exercise Exercise 73

1. Find the area of the triangle whose vertices are:
(i) $(2,3),(-1,0),(2,-4)(i i)(-5,-1),(3,-5),(5,2)$

## - Watch Video Solution

2. In each of the following find the value of ' $k$ ' for which the points are collinear .

$$
(8,1),(k,-4),(2,-5)
$$

3. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are ( $0,-1$ ), (2, 1) and ( 0 ,
3). Find the ratio of this area to the area of the given triangle.

## - Watch Video Solution

4. Find the area of the quadrilateral whose vertices, taken in order are $(-4,-2),(-3,-5),(3,-2)$

## D Watch Video Solution

5. You have studied in Class IX, (Chapter 9,

Example 3), that a median of a triangle divides
it into two triangles of equal areas. Verify this
result for $\Delta A B C$ whose vertices are $\mathrm{A}(4,-6)$, $B(3,-2)$ and $C(5,2)$.

## - Watch Video Solution

## Textual Exercise Exercise 74

1. Determine the ratio in which the line $2 x+y-$

4 = 0 divides the line segment joining the points $A(2,-2)$ and $B(3,7)$.


- Watch Video Solution

2. Find a relation between x and y if the points $(x, y),(1,2)$ and $(7,0)$ are collinear.

## - Watch Video Solution

3. Find the centre of a circle passing through the points (6, -6$),(3,-7)$ and $(3,3)$.

## D Watch Video Solution

4. The two opposite vertices of a square are
$(-1,2)$ and $(3,2)$. Find the coordinates of the other two vertices.
5. The Class $X$ students of a secondary school in Krishinagar have been alloted a rectangular plot of land for their gardening activity . Sapling of Gul mohar is planted on the boundary at a disatnce of 1 m from each other.

There is a triangular grassy lawn in the plot as shown in the figure. The students are to sow seeds of flowering plants on the remaining area of the plot.

(i) Taking A as origin, find the coordinates of the vertices of the triangle .
(ii) What will be the coordinates of the vertices of $\triangle P Q R$ if C is the origin

Also calculate the areas of the triangles ithese cases. What do you observe?
6. The vertices of a $\Delta \mathrm{ABC}$ are $\mathrm{A}(4,6), \mathrm{B}(1,5)$
and $C(7,2)$. A line is drawn to intersect sides
$A B$ and $A C$ at $D$ and $E$ respectively, such that $\frac{A D}{A B}=\frac{A E}{A C}=\frac{1}{4}$. Calculate the area of $\Delta$

ADE and compare it with area of $\triangle \mathrm{ABC}$

## - Watch Video Solution

7. Let $A(4,2)$. $B(6,5)$ and $C(1,4)$ be the vertices of $\Delta \mathrm{ABC}$.
i The median from A meets BC at D. Find the coordinates of point D.

## D Watch Video Solution

8. $A B C D$ is a rectangle formed by the points $A$
$(-1,-1), B(-1,4), C(5,4)$ and $D(5,-1) . P, Q R$ and $S$
are the mid-points of $A B, B C, C D$, and $D A$
respectively. Is the quadrilateral $P Q R S$ is a square? a rectangle? or a rhombus? Justify your answer.

## View Text Solution

## Zen Additional Questions Multiple Choice

## Questions

1. The distance between $(\mathrm{a} \cos \theta+\mathrm{b} \sin \theta, \mathrm{o})$ and $(0, a \sin \theta-b \cos \theta)$ is
A. $a^{2}+b^{2}$
B. $a^{2}-b^{2}$
C. $\sqrt{a^{2}+b^{2}}$
D. $\sqrt{a^{2}-b^{2}}$

## Answer: C

## D Watch Video Solution

2. The co ordinates of the point which is reflection of the point $(-3,5)$ in $X$ axis are
A. $(3,5)$
B. $(3,-5)$
C. $(-3,-5)$
D. $(-3,5)$

## D Watch Video Solution

## 3. If point $P(6,2)$ divides the line joining $A(6,5)$

and $B(4, y)$ in the ratio $3: 4$ then the value of $y$ is
A. 4
B. 3
C. 2
D. 1

Answer: B

## D Watch Video Solution

4. The ratio in which the line segment $\left(a_{1}, b_{1}\right)$
and $\mathrm{B}\left(a_{2}, b_{2}\right)$ is divided by Y -axis is
A. $-a_{1}: a_{2}$
B. $a_{1}: a_{2}$
C. $b_{1}: b_{2}$
D. $-b_{1}: b_{2}$

## D Watch Video Solution

5. The length of the line segment joining $A(2,3)$
and $B$ is 10 units. If absc is a of $B$ is 10 , its
ordinate can be
A. 3 or - 9
B. -3 or 9
C. 6 or 27
D. -6 or -27

Answer: C

## - Watch Video Solution

6. If the centroid of a triangle formed by the points $a . b),(b, c)$, and (c a) is at the origin, then $a^{3}+b^{3}+c^{3}=$
A. abc
B. 0
C. $a+b+c$
D. 3 abc

Answer: A::B::C

## D Watch Video Solution

7. The coordinates of a point on the $X$-axis
which lie on theL bisector of the line segment
joining $(7,6)$ and $(-3,4)$ are
A. $(0,2)$
B. $(3,0)$
C. $(0,3)$
D. $(2,0)$

Answer: B

## - Watch Video Solution

8. If $(t, 2 t),(-2,6)$, and $(3,1)$ are collinear, $t=$
A. $3 / 4$
B. $4 / 3$
C. $5 / 3$
D. $3 / 5$
9. Length of the median through C of $\Delta \mathrm{ABC}$ with $A(4,9) B(2,3)$, and $C(6,5)$ is
A. 5 units
B. $\sqrt{10}$ units
C. 25 units
D. 10 units

Answer: A
10. If $P(2,4), Q(0,3), R(3,6)$, and $S(5, y)$ are the vertices of a parallelogram PQRS, value of $y$ is
A. 7
B. 5
C. -7
D. -8

Answer:

D Watch Video Solution
11. The distance between the origin and coordinates of point $(x, y)$ is
A. $x^{2}+y^{2}$
B. $\sqrt{x^{2}-y^{2}}$
C. $x^{2}+y^{2}$
D. $\sqrt{x^{2}+y^{2}}$

Answer: B

## Zen Additional Questions Very Short Answer Vsa

 Type Questions1. Find the area of the triangle $\Delta \mathrm{ABC}$ with
$A(a, b+c), B(b, c+a)$, and $C(c, a+b)$.

## D Watch Video Solution

2. Find the length of the median $A D$ of $\Delta A B C$ with $A(5,1), B(1,5)$, and $C(-3,-1)$.
3. Find the ratio in which the line segment $P Q$
$P(4,5)$ and $Q(3,7)$, is internally divided by the $Y$ axis.

## - Watch Video Solution

4. Find k if $(2,1),(\mathrm{k},-1)$ and $(-1,3)$ are collinear.

## - Watch Video Solution

## 5. Find 'a' so that ( $3, a$ ) lies on the line $2 x-3 y=5$

## - Watch Video Solution

6. Find k if the centroid of the triangle whose vertices are $(2, k),(-5,2)$ and $(3,4)$ is $(0,-2)$.

## - Watch Video Solution

7. The endpoints of the diameter of a circle are
$(2,4)$ and $(3-1)$. Find the radius of the circle.

- Watch Video Solution

8. Find the distance between ( 0,5 ) and $(-5,0)$.

## - Watch Video Solution

9. Find the point equidistant from $(3,8)$ and
$(-10,-5)$.

## - View Text Solution

10. Plot these points on the Cartesian plane.
(i) $A(-4,0)($ ii) $B(0,5)$ (iii) $C(3-4)$ (iv) $D(-2,5)(v) E$
$(-1,-1)(v i) F(3,5)$

## D Watch Video Solution

11. A square of side 4 units lies in I Quadrant on the X -axis, with its one vertex at the origin.

Plot the coordinates of the other 3 vertices of the square.

## D Watch Video Solution

12. Draw the quadrilateral whose vertices are
$(1,1),(24),(8,4)$, and (10, 1).

## - Watch Video Solution

13. Find distance between the pair of points given.
(i) $(a \sin \alpha,-b \cos \alpha),(-a \cos \alpha, b \sin \alpha)$
(ii) $(a+b, b+c),(a-b, c-b)$
(iii) $(4,10),(7-6)$

- Watch Video Solution

14. Find the coordinates of the mid-point of
the
line
joining
the
points
$\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$.

## Zen Additional Questions Short Answer Sa Type

 Questions1. Find the value (s) of $x$ if distance between $A$ $(0,0)$ and $B(x,-4)$ is 5 units.

## (D) Watch Video Solution

2. What is the distance of $P(x, y)$ from the origin?
3. A line intersects $y$-axis and $x$-axis at the points $P$ and $Q$ respectively. If $(2,5)$ is the mid point of $P Q$ then find the co ordinates of $P$ and Q.

## D Watch Video Solution

4. If the distance between $P(x, y)$ from $A(5,1)$ and $B(-1,5)$ are equal, show that $3 x=2 y$.
5. Find the area of $A$ ABC where $A(-3 / 2,3), B\{6$,
$-2)$, and $C(-3,4)$.

## - Watch Video Solution

6. Find k if $\mathrm{A}(\mathrm{k}+1,24), \mathrm{B}(3 \mathrm{k}, 2 \mathrm{k}+3)$, and $\mathrm{C}(5 \mathrm{k}-1$, 5k) are collinear.

## - Watch Video Solution

7. Find the ratio in which $x-y-2=0$ divides the line segment joining ( $8,-1$ ) and ( 8,9 ).

## D View Text Solution

8. The length of a line segment is $\sqrt{29}$ units. If one end is at $(-3,5)$ and the ordinate of the other end is 7 , show that the absciss is either 2 or-8.
9. Given $\mathrm{P}\left(a t^{2}, 2 a t\right), Q\left(\frac{a}{t^{2}}, \frac{-2 a}{t}\right)$, and $\mathrm{S}(\mathrm{a}$,

0 ), show that $\frac{1}{S P}+\frac{1}{S Q}$ is independent of $t$

## D Watch Video Solution

10. Use a graph sheet to plot points $P(-2,2), Q$
$(4,-2)$, and $R(5,2)$. Complete $\Delta P Q R$. Find the altitude drawn fromQ to PR from the graph.

Also find the area of $\triangle P Q R$.
11. James started from a point $X, 4$ units away
from the origin above the X -axis. He walked to
the origin and turned right to $\mathrm{Y}, 3$ units away.
What are points $X$ and $Y$ ? Locate them on the
Cartesian plane. What is distance between X and $Y$ ?

## D View Text Solution

12. The base $A B$ of an equilateral $\Delta A B C$ of side
$2 p$ lies along the $X$-axis such that the midpoint
of $A B$ is at the origin and vertex $C$ is above $x$ axis. Find coordinates of the vertices of $\Delta A B C$.

## D Watch Video Solution

13. Plot points $P(3,8)$ and $Q(3,-8)$. Join $A O P Q$.

What kind of a $\Delta$ is it ? Find its area.

## D Watch Video Solution

14. If $A(3, y)$ is equidistant from $P(8,-3)$ and
$Q(7,6)$, find $y$ and the distance $A Q$.
15. Find the values of $y$ for which the distance between the points $P(2,-3)$ and $Q(10, y)$ is 10 units.

## D Watch Video Solution

16. Find the equation of the perpendicular
bisector of the line segment joining (7,1) and
$(3,5)$.

## Watch Video Solution

17. If $P(2,2)$ is equidistant from $A(-2, k)$ and $B$ $(-2 k,-3)$, find $k$. Also find the length AP.

## D Watch Video Solution

18. Find a point equidistant from $A(-5,4)$ and $B(-1,6)$. How many such points are there?
19. Show that $(1,0),(0,1),(-3,4)$ are on a straight line.

## D Watch Video Solution

20. If $P(x, y)$ lies on a circle whose centre is
$(3,-2)$ and radius is 3 , show that $x^{2}+y^{2}-6 x+4 y+4=0$.

D Watch Video Solution
21. The centre of a cicle is (2a, a -7). Find the values ofa if the circle passes through (11, -9) and has a diameter of $10 \sqrt{2}$ units.

## - Watch Video Solution

22. Prove that (2a, 4a), ( $2 \mathrm{a}, 6 \mathrm{a}$ ), and ( $2 \mathrm{a}+\sqrt{3 a}$,
$5 a)$ are the vertices of an equilateral triangle.

## - Watch Video Solution

23. Find the area of a triangle whose vertices
are $(1,-1),(-4,6)$ and $(-3,-5)$.

## - Watch Video Solution

24. Prove that the area of the triangle whose vertices are ( $\mathrm{t}, \mathrm{t}-2$ ), $(\mathrm{t}+2, \mathrm{t}+2$ ), and $(\mathrm{t}+3, \mathrm{t})$
is independent of t .

- Watch Video Solution

25. Find the area of the quadrilateral $A B C D$ whose vertices are $A(1,1), B(7,-3), C(12,2)$, and $D(7,21)$.

## - Watch Video Solution

26. Show That (3, -2) is the 3rd verlex of a $\Delta$

ABC where $A(2.3), B(-2,1)$, and centroid is $G(1$, 2/3).
27. Find the area of a parallelogram $A B C D$ if three of its vertices are $A(2,4), B(2+\sqrt{3}, 5)$ and $C(2,6)$.

## D Watch Video Solution

28. Find the co - ordinates of points which
divides the line segment joining the points $A$
$(4,-3)$ and $B(8,5)$ in the ratio $3: 1$ internally
29. Find the distance between the points $(2,3)$ and (4,1) .

## D View Text Solution

30. Find the coordinates of the point which divides the line joining the points $(1,6)$ and $(4,3)$ in the ratio $1: 2$.

D Watch Video Solution
31. The points $A(1,1), B(3,2)$ and $C(5,3)$ cannot be the vertices of the triangle ABD . Justify.

## - Watch Video Solution

32. If $A(-2,-1) B(a, 0) C(4, b)$ and $D(1,2)$ are the
vertices of $a$ parallelogram. Find $a$ and $b$

## - Watch Video Solution

33. IfA(-5, 7), $B(4,5), C(-1,-6)$ and $D(4,5)$ are the
vertices of a quadrilateral. Find the area of quadrilateral.

## - View Text Solution

34. If the points $A(k+1,2 k), B(3 k, 2 k+3)$ and $C$
( $5 k-1,5 k$ ) are collinear, then find the value of $k$.

## D View Text Solution

35. If the point $P(x, y)$ is equidistant from the points $A(a+b, b-a)$ and $B(a-b, a+b)$. Prove that $b x=a y$.

## D Watch Video Solution

36. A $(0,6), \mathrm{P}(4,-3)$, and the origin O form a $\Delta$

OPA. $\triangle$ OPA is turned with its base OA on the $Y$ axis to form $\triangle$ OQA. What are the coordinates
of $Q$ ? What is figure OPAQ? Is
$\triangle O P A \cong \triangle O Q A$ ? Give reason. Find the area of OPAQ.

## - Watch Video Solution

37. Find $a$ and $b$ if $M(9 a-2,-b)$ divides the line segment joining $P(3 a+1,-3)$ and $Q(8 a, 5)$ in the ratio 3: 1 .

- Watch Video Solution

38. Find the ratio in which $(-4,6)$ divides the line segment joining $A(6,10)$ and $B(3,-8)$.

## D View Text Solution

39. Find the points of trisection of the line segment joining the points. i] $(5,-6)$ and $(-7,5)$ ii (2,-2) and (-7,4)

## D Watch Video Solution

40. Three vertices of a parallelogram are $(a+b$
,a -b$),(2 \mathrm{a}+\mathrm{b}, 2 \mathrm{a}-\mathrm{b})$, and $(\mathrm{a}-\mathrm{b}, \mathrm{a}+\mathrm{b})$. Find
the 4th vertex.

## D Watch Video Solution

41. A poin $P$ divides the line segment joining $A$
$(3,-5)$ and $B(-4,8)$ with $\frac{A P}{P B}=k$. If p lies on
the line $x+y=0$. Find $k$.

- Watch Video Solution

42. If the midpoints of the sides of a triangle are $(3,4)(4,6)$, and $(5,7)$, find the coordinates of the vertices of the triangle.

## D Watch Video Solution

43. In what ratio is the join of $(-2,2)$ and $(4,5)$
cut by the axes of coordinates?

## D Watch Video Solution

44. The vertices of $\triangle \mathrm{ABC}$ are $\mathrm{A}(1,2), \mathrm{B}(4,6)$, and $C(6,14)$. $A D$ bisects $\angle A$ and meets $B C$ at $D$.

Find the coordinates of $D$.

## D Watch Video Solution

45. Show that ${ }^{`}(1,-1),(-2,2),(4,8)$ and $(7,5)$ are
the angular points of a rectangle.

## D Watch Video Solution

46. The line segment joining $(3,-4)$ and $(1,2)$ is trisected by $P(a,-2)$ and $Q(5 / 3, b)$. Find $a$ and $b$.

## D Watch Video Solution

47. The centroid of a triangle $A B C$ is $(1,2,2)$ If
the coordinates of $A$ and $B$ are
$(3,-5,7)$ and $(-1,7,-6)$ respectively.

Find the coordinates of $C$.

D Watch Video Solution
48. The vertices of a $\Delta \mathrm{ABC}$ are $\mathrm{A}(4,6), \mathrm{B}(1,5)$
and $C(7,2)$. A line is drawn to intersect sides
$A B$ and $A C$ at $D$ and $E$ respectively, such that $\frac{A D}{A B}=\frac{A E}{A C}=\frac{1}{4}$. Calculate the area of $\Delta$ ADE and compare it with area of $\triangle \mathrm{ABC}$

## - Watch Video Solution

49. Prove that the median of $\Delta \mathrm{ABC}$ divides it into two triangles of equal area. .
50. Find the value of a for which the area of the triangle formed by $\mathrm{A}(\mathrm{a}, 2 \mathrm{a}), \mathrm{B}(-2,6)$, and $C(3,1)$ is 10 sq. units.

## - Watch Video Solution

51. If a $\neq b \neq 0$, prove that points $\left(a, a^{2}\right),\left(b, b^{2}\right)$, and ( 0,0 ) can never be collinear.
52. Prove that $(a, 0),(0, b)$, and $(1,1)$ are collinear if $\frac{1}{a}+\frac{1}{b}=1$.

## D Watch Video Solution

53. Find the values of $a$ and $b$ if $P(9 a-2,-b)$ divides the line segment $A(3 a+1,-3)$ and $B(8 a$,
5) in the ratio 3:1.

## D Watch Video Solution

54. The centre of a cicle is ( $2 \mathrm{a}, \mathrm{a}-7$ ). Find the
values ofa if the circle passes through (11, -9)
and has a diameter of $10 \sqrt{2}$ units.

## - Watch Video Solution

55. For what value of $k$ are ( $k, 22$ ), ( $-k+1,2 k$ ), and ( $4-\mathrm{k}, 6-2 \mathrm{k}$ ) collinear?

## - Watch Video Solution

56. The vertices of a $\Delta \mathrm{ABC}$ are $\mathrm{A}(-3,2), \mathrm{B}(-1,-4)$
and $C(5,2)$. If $M$ and $N$ are the mid - points of
$A B$ and $A C$ respectively show that $2 M N=B C$.

## D Watch Video Solution

57. The vertices of a $\Delta \mathrm{ABC}$ are $\mathrm{A}(-5,-1), \mathrm{B}(3,-5)$,

C $(5,2)$. Show that the area of the $\Delta \mathrm{ABC}$ is four
times the area of the triangle formed by joining the mid-points of the sides of the triangle $A B C$.

# Zen Additional Questions Long Answer La Type 

 Questions1. The vertices of $A A B C$ are $A(4,6), B(1,5)$, and
$C 7,2$ ). A line is drawn to intersect sides AB and
AC at D and E respectively. Show that $\frac{A D}{A B}=\frac{A E}{A C}=\frac{1}{4}$. Find the area of $\Delta \mathrm{ADE}$ and compare it with $\Delta \mathrm{ABC}$.

## - Watch Video Solution

2. The points $A(6,1), B(8,2)$, and $C 9,4)$ are the three vertices of a parallelogram $A B C D$. If $E$ is the midpoint of $D C$, find area of $\Delta$ ADE.

## D Watch Video Solution

3. If $D-\left(\frac{1}{5}, \frac{5}{2}\right), E(7,3)$ and $F\left(\frac{7}{2}, \frac{7}{2}\right)$
are the mid-point of the sides of $\Delta A B C$, find the coordinates of $\triangle \mathrm{ABC}$.

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4. The area of a triangle is 5 square units. Two of its vertices are ( 2,1 ) and ( $3,-2$ ) and the third vertex lies on $y=x+3$, find the third vertex.

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5. Find the coordinates of the centre of the circle passing through the point $(0,0),(-2,1)$ and $(-3,2)$. Also find the radius.

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6. Find the area of the triangle formed by
joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0,
3). Find the ratio of this area to the area of the given triangle.

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## Zen Additional Questions Higher Order Thinking Skills Hots Questions

1. In what ratio does $4 x+3 y-130$ divide the line segment joining ( 2,1 ) and ( 1,4 )?

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2. Find the circumcentre of the triangle whose vertices are $(0,0)(3, \sqrt{3})$, and $(0,2 \sqrt{3})$.

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3. Find the 4th vertex of a rhombus formed by
$(1,-1),(6,1)$, and ( 8,8 ).

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4. Find the coordinates of $P$ which divides the
line segment joining points $A(1,3)$ and $B(3,4)$ externally in the ratio 3:4.

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5. If points $(-3,6),(-9, a)$, and $(0,15)$ are collinear, find 'a'.

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6. Check if the following points are collinear using section formula.

$$
\text { I] }(-4,6),(-6,10),(3,-8) \text { (ii) }(1,-2),(2,3),(-4,-3)
$$

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7. Find the perimeter and area of the quadrilaterals formed by the given point.s Mention the type of quadrilateral formed.
(i) $(0,3),(4,0),(0,-8),(-4,0)$
(ii) $(5,0),(0,-5),(0,-9),(9,0)$
(iii) $(5,3),(5,-3),(10,-6),(10,6)$

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8. Find the kind of quadrilateral formed by (1,
$3),(0,8),(5,7)$, and ( 8,0 ).
9. $A B C$ is a triangle with vertices $A(-8,3), B(4,5)$,
$C(-6,1)$. Find the vertices of a parallelogram in this $\triangle A B C$ sharing vertex $B$ and having half the area of $\Delta A B C$. Find the area ot the paralelogram so formed.

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10. Find the circumcentre of a triangle formed
by $(2,3),(1,-5)$, and ( $-1,4$ ).

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11. Find $\lambda$ if $2 x-27+5+\lambda(3 x-y+4)=0$ passes through the midpoint of the line joining $(2,3)$ and (4,9).

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12. Find the point on the $Y$-axis equidistant from $A(3,-6)$ and $B(-2,5)$.

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13. Find the coordinates of a point which divides the line joining points $A(-3,2)$ and $B(2,6$ ) in the ratio 3: 2 .

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14. Let $A(3,2), B(4,1), C(3,1)$, and $D(2,4)$ be the vertices of a quadrilateral $A B C D$. Find the area of the quadrilateral formed by joining the midpoints of the sides of the quadrilateral ABCD.

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