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India's Number 1 Education App

## MATHS

## BOOKS - ZEN MATHS (KANNADA ENGLISH)

## TRIANGLES

Illustrative Examples

1. In the figure, $P R|\mid R C$ and $Q R| \mid B D$. Prove that $P Q|\mid C D$.

2. In the given figure $D E \| B C$ and $C D \| B F$ prove that $A C^{2}=A E \times A F$.

3. In the figure, $A B \perp B C$ and $D E \perp A C$. Prove that $\triangle A B C \sim \triangle A E D$.

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4. In the given figure $P$ is the midpoint of $B C$ and $Q$ is the midpoint of $A P$. If $B Q$ when produced meets $A C$ at $R$, prove that $R A=\frac{1}{3} C A$.

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5. In the given figure, $A D=3 \mathrm{~cm}, \mathrm{AE}=5 \mathrm{~cm}, \mathrm{BD}=4 \mathrm{~cm}, \mathrm{CE}=4 \mathrm{~cm}$, $C F=2 \mathrm{~cm}, \mathrm{BF}=2.5 \mathrm{~cm}$, then find the pair of parallel lines and hence their lengths.

6. In the $\triangle A B C$, altitudes $A D$ and $C E$ intersect each other at point P. Prove that

## i] $\triangle A P E \sim \Delta C P D$

ii] $A P \times P D=C P \times P E$
iii] $\triangle A D B \sim \Delta C E B$
iv] $A B \times C E=B C \times A D$

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7. In the figure $\left\lfloor Q P R=\left\lfloor U T S=90^{\circ}\right.\right.$ and $P R| | T S$. Prove that $\triangle P Q R \sim \triangle T U S$.


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8. In the figure $\frac{A O}{O C}=\frac{B O}{O D}=\frac{1}{2}$ and $\mathrm{AB}=5 \mathrm{~cm}$. Find DC

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9. If the area of two similar triangles is in the ratio $25: 64$, find the of their corresponding sides.
10. $\mathrm{D}, \mathrm{E}$ and F are the mid-points of sides of $\Delta A B C . \mathrm{P}, \mathrm{Q}, \mathrm{R}$ are the mid-points of sides DEF. This process of marking the mid-points and forming a new triangle is continued. How are the areas of these triangles related?

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11. In areas of two similar triangles $A B C$ and $P Q R$ are in the ratio 9
: 16. If $B C=4.5 \mathrm{~cm}$. Find the length of $Q R$.

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12. $\triangle A B C$ and $\triangle B D E$ are two equilateral triangles and $B D=D C$. Find the ratio between areas of $\triangle A B C$ and $\triangle B D E$.


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13. AD is altitude of equilateral $\triangle A B C$. On AD as base, another equilateral triangle ADE is constructed. Prove that $\frac{\text { Area of } \triangle A D E}{\text { Area of } \triangle A B C}=\frac{3}{4}$.

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14. The lengths of diagonals of a rhombus are 24 cm and 32 cm .

Calculate the altitide of the rhombus.

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15. The sides AB and AC and the perimeter $P_{1}$ of $\triangle A B C$ are respectively three times the corresponding sides DE and DF and the perimeter $P_{2}$ of $\triangle D E F$. Are the two triangles similar? If yes, find $\frac{\operatorname{ar}(\triangle A B C)}{\operatorname{ar}(\triangle D E F)}$.

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16. In the rectangle $W X Y Z, X Y+Y Z=17 \mathrm{~cm}$ and $X Z+Y W=26$.

Calculate the length and breadth of the rectangle.
17. An insect 8 m away from the foot of a lamp post 6 m tall, crawls towards it. After moving through a distance, its distance from the top of the lamp post is equal to the distance it has moved. How far is the insect away from the foot of the lamp post?

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18. In $\triangle A B C, \mathrm{C}$ is a point on BD such that $\mathrm{BC}: \mathrm{CD}=1: 2$ and $\triangle \mathrm{ABC}$ is an equilateral triangle Prove that $A D^{2}=7 A C^{2}$

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19. In $\triangle A B C, C D \perp A B, C A=2 A D, B D=3 A D$. Prove that $\left\lfloor B C A=90^{\circ}\right.$.
20. In the figure, $A B \perp B C$ and $D E \perp A C$. Prove that $\triangle A B C \sim \triangle A E D$.

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21. In the given figure $\left\lfloor B A C=90^{\circ}\right.$.

Prove that:
a] $\Delta A G F \sim \Delta B D G$
b] $\triangle A G F \sim \Delta E F C$
c] $\Delta B D G \sim \Delta E F C$
d] $D E^{2}=B D \times E C$
22. $A B C$ is a right angled triangle. Points $D$ and $E$ trisect $B C$. Prove that $8 A E^{2}=3 A C^{2}+5 A D^{2}$.

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23. In an equilateral triangle $\mathrm{ABC}, A D \perp B C$. Prove that $A D^{2}=3 B D^{2}$.

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## Textual Exercises Exercise 21

1. Fill in the blanks using the correct word given in brackets :

All circles are ( congruent, similar )

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2. Fill in the blanks using the correct word given in the brackets:

All squares are $\qquad$ [Similar, Congruent]

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3. Fill in the blanks using the correct word given in the brackets:

All _______triangles are similar. [isosceles, equilateral].

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4. Two polygons of the same number of sides are similar, if

Their corresponding sides are $\qquad$
5. Two polygons of the same number of sides are similar, if Their corresponding angles are $\qquad$ and

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6. Give two different examples of a pair of different radii of different length:
i] Similar figures
ii] Non-similar figures.
7. State whether the following quadrilaterals are similar or not:


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Textual Exercises Exercise 22

1. $E$ and $F$ are points on the sides $P Q$ and $P R$ respectively of a $\triangle P Q R$. For the following cases, state whether EF||QR.
i] $\mathrm{PE}=3.9 \mathrm{~cm}, \mathrm{EQ}=3 \mathrm{~cm}, \mathrm{PF}=3.6 \mathrm{~cm}$, and $\mathrm{FR}=2.4 \mathrm{~cm}$.
ii] $\mathrm{PE}=4 \mathrm{~cm}, \mathrm{QE}=4.5 \mathrm{~cm}, \mathrm{PF}=8 \mathrm{~cm}, \mathrm{RF}=9 \mathrm{~cm}$
iii] $P Q=1.28 \mathrm{~cm}, P R=2.56 \mathrm{~cm}, \mathrm{PE}=0.18 \mathrm{~cm}$, and $\mathrm{PF}=0.36 \mathrm{~cm}$.
2. In Fig, if $L M \| C B$ and $L N \| C D$, prove that $\frac{A M}{A B}=\frac{A N}{A D}$


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3. In Fig $D E\left|\mid A C\right.$ and $A E$. Prove that $\frac{B F}{F E}=\frac{B E}{E C}$


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4. In the figure $D E \| O Q$ and $D F \| O R$. Show that $E F|\mid Q R$.

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5. In Fig A, B and C are points on OP, OQ and OR respectively such that $A B|\mid P Q$ and $A C| \mid P R$. Show that $B C|\mid Q R$.


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6. Prove that a line drawn through the midpoint of one side of a triangle parallel to another side bisects the third side (using BPT).

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7. Prove that the line joining the midpoints of any two sides of a triangle is parallel to the third side.

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8. $A B C D$ is a trapezium in which $A B|\mid D C$. Its diagonals intersect each other at 0 .

Show that $\frac{A O}{B O}=\frac{C O}{D O}$

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9. The diagonals of a quadrilateral $A B C D$ intersect each other at the point $O$ such that $\frac{A O}{B O}=\frac{C O}{D O}$.

Show that ABCD is a trapezium.

## Textual Exercises Exercise 23

1. If the areas of two similar triangles are equal, prove that they are congruent.

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2. If the areas of two similar triangles are equal, prove that they are congruent.
3. State which pairs of triangles in Fig are similar. Write the similarity criterion used by you for answering the question also write the pairs of similar triangles in the symbolic form:


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4. If the areas of two similar triangles are equal, prove that they are congruent.

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5. 

In
the
figure
$\triangle O D C \sim \triangle O B A,\left\lfloor B O C=125^{\circ}\right.$ and $\left\lfloor C D O=70^{\circ}\right.$. Find
$\lfloor D O C,\lfloor D C O$, and $\lfloor O A B$.

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6. In Fig , if $\triangle A B E \angle \triangle A C D$, show that $\triangle A D E \sim \triangle A B C$


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7. In the figure altitudes AD and CE of $\triangle A B C$ intersect each other at the point P. Show that

1] $\triangle A E P \sim \Delta C D P$

2] $\triangle A B D \sim \Delta C B E$

## 3] $\triangle A E P \sim \Delta A D B$

4] $\triangle P D C \sim \Delta B E C$

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8. $E$ is a point on the side AD produced, of a parallelogram $A B C D$ and BE intersects CD at F . Show that $\triangle A B E \sim \triangle C F B$.

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9. In Fig, ABC and AMP are two right triangles, right angled at B and $M$ respectively. Prove that :
$\frac{C A}{P A}=\frac{B C}{M P}$


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10. CD and GH are respectively the bisectors of $\lfloor A C B$ and $\lfloor E G F$ such that D and H lie on sidea AB and FE of $\triangle A B C$ and $\triangle E F G$ respectively. If $\triangle A B C \sim \triangle F E G$, show that. i] $\frac{C D}{G H}=\frac{A C}{F G}$
ii] $\Delta C D B \sim \Delta H G E$
iii] $\Delta D C A \sim \Delta H G F$

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11. In the figure, $E$ is a point on side CB produced, of an isosceles triangle ABC , with $\mathrm{AB}=\mathrm{AC}$. If $A D \perp B C$ and $E F \perp A C$, prove that $\triangle A B D \sim \Delta E C F$.

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12. Sides $A B$ and $B C$ and median $A D$ of a triangle $A B C$ are respectively proportional to sides $P Q$ and $Q R$ and median $P M$ of $\triangle P Q R$. Show that $\triangle A B C \sim \triangle P Q R$.
13. $D$ is a point on the side $B C$ of a triangle $A B C$ such that $\left\lfloor A D C=\left\lfloor B A C\right.\right.$. Show that $C A^{2}=C B . C D$.

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14. Sides $A B$ and $B C$ and median $A D$ of a triangle $A B C$ are respectively proportional to sides $P Q$ and $Q R$ and median $P M$ of $\triangle P Q R$. Show that $\triangle A B C \sim \triangle P Q R$.

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15. A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts shadow 28 m long.

Find the height of the tower.

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16. If $A D$ and $P M$ are median of triangles $A B C$ and $P Q R$ respectively where $\triangle A B C-\triangle P Q R$, prove that $\frac{A B}{P Q}=\frac{A D}{P M}$.

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1. Let $\triangle A B C \sim \triangle D E F$ and their areas be , respectively, $64 \mathrm{~cm}^{2}$ and $121 \mathrm{~cm}^{2}$. If $\mathrm{EF}=15.4 \mathrm{~cm}$, find BC

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2. Diagonals of a trapezium $A B C D$ with $A B \| D C$ intersect each other at the point $O$. If $A B=2 C D$, find the ratio of the areas of triangle AOB and COD.

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3. In the figure $A B C$ and $D B C$ are two triangles on the same base

BC . If AD intersects BC at 0 , show that $\frac{\operatorname{Area}(\triangle A B C)}{\operatorname{Area}(\triangle D B C)}=\frac{A O}{D O}$.
4. If the areas of two-similar triangles are equal, prove that the they are congruent.

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5. $D, E a n d F$ are respectively the mid - points of sides $A B, B C$ and $C A$ of $\triangle A B C$. Find the ratio of the areas of $\triangle D E F$ and $\triangle A B C$.

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6. Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.
7. Prove that the area of an equilateral triangle described on one side of a square is equal of half the area of the equilateral triangle described on one of its diagonals.

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8. $A B C$ and $B D F$ are two equilateral triangles such that $D$ is the mid -point of $B C$. Ratio of the areas of triangles $A B C$ and BDF is
A. $2: 1$
B. 1:2
C. $4: 1$
D. 1: 4

## Answer: C

9. Sides of two similar triangles are in the ratio 4:9 Areas of these triangles are in the ratio
A. $2: 3$
B. $4: 9$
C. $81: 16$
D. 16:81

## Answer: D

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## Textual Exercises Exercise 25

1. Sides of triangles are given below. Determine which of them are right triangles.

In case of a right triangle , write the length of its hypotenuse.
$7 \mathrm{~cm}, 24 \mathrm{~cm}, 25 \mathrm{~cm}$

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2. $P Q R$ is a triangle right angled at $P$ and $M$ is a point on $Q R$ such that $P M \perp Q R$. Show that $P M^{2}=Q M . M R$.

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3. In the figure ABD is a triangle right-angled at A and $A C \perp B D$.

Show that
i] $A B^{2}=B C \cdot B D$
ii] $A C^{2}=B C . D C$
iii] $A D^{2}=B D \cdot C D$

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4. $A B C$ is an isosceles triangle right-angled at $C$. Prove that $A B^{2}=2 A C^{2}$.

## ( Watch Video Solution

5. ABC is an isosceles triangle with $\mathrm{AC}=\mathrm{BC}$. If $A B^{2}=2 A C^{2}$, prove that $A B C$ is a right-angled triangle.
6. $A B C$ is an equilateral triangle of side $2 a$. Find each of its altitudes.

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7. Prove that sum of the squares of the side of a rhombus is equal to the to the sum of the squares of its diagonals.

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8. In the figure given below, $O$ is point in the interior of a triangle $\mathrm{ABC}, O D \perp B C, O E \perp A C$ and $O F \perp A B$. Show that
(i)

$$
O A^{2}+O B^{2}+O C^{2}+O D^{2}-O E^{2}-O F^{2}=A R^{2}+B D^{2}+C E^{2}
$$

(ii) $A F^{2}+B D^{2}+C E^{2}=A E^{2}+C D^{2}+B F^{2}$


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9. A ladder 10 m long reaches a window 8 m above the ground.

Find the distance of the foot of the ladder from base of the wall.
10. A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end. How far from the base of the pole should the stake be driven so that the wire will be taut?

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11. An aeroplane leaves an airport and files due north at a speed of 1000 km per hour. At the same time, another aeroplane leaves the same airpot and flies due west at a speed of 1200 km per hour .How far apart will be the two planes after $1 \frac{1}{2}$ hours ?

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12. Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12 m , find the
distance between their tops .

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13. $D$ and $E$ are points on the sides $C A$ and $C B$ respectively of a triangle $A B C$ right angale at $C$ prove that $A E^{2}+B D^{2}=A B^{2}+D E^{2}$.

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14. The perpendicular from A on side BC of a $\triangle A B C$ intersects BC at D such that $\mathrm{DB}=3 \mathrm{CD}$. Prove that $2 A B^{2}=2 A C^{2}+B C^{2}$.

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15. In an equilateral triangle $A B C, D$ is a point on $B C$ such that $B D=\frac{1}{3} B C$. Prove that $9 A D^{2}=7 A B^{2}$.

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16. In an equilateral triangle prove that three times the square of one side is four times the square of its altitude.

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17. Tick the correct answer and justify : In
$\triangle A B C, A B=6 \sqrt{3} \mathrm{~cm}, A C=12 \mathrm{~cm}$ and $B C=6 \mathrm{~cm}$
The angle B is :
A. $120^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $45^{\circ}$

## Answer: C

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Zee Additional Questions Multiple Choice Questions

1. $A B C$ is an isosceles triangle right-angled at $C$. Prove that $A B^{2}=2 A C^{2}$.
A. $A B^{2}=2 A C^{2}$
B. $B C^{2}=2 A B^{2}$
C. $A C^{2}=2 A B^{2}$
D. $A B^{2}=4 A C^{2}$

## Answer: A

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2. If $\triangle A B C$ is similar to $\triangle D E F$ such that $\left\lfloor D=47^{\circ}\right.$ and $\left\lfloor B=83^{\circ},\lfloor F\right.$ is
A. $80^{\circ}$
B. $60^{\circ}$
C. $40^{\circ}$
D. $50^{\circ}$

## Answer: D

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3. In $\triangle A B C, D E| | B C . \mathrm{AD}=(7 \mathrm{x}-4) \mathrm{cm}, \mathrm{AE}=(5 \mathrm{x}-2) \mathrm{cm}, \mathrm{DB}=$ $(3 x+4) c m$, and $E C=3 x \mathrm{~cm}$. The value of $x$ is
A. 4
B. 3
C. 5
D. 2.5

## Answer: A

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4. The lengths of the diagonals of a rhombus are 16 cm and 12 cm .

Then the length of the side of the rhombus is
A. 9 cm
B. 10 cm
C. 8 cm
D. 20 cm

## Answer: B

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5. If in two triangles ABC and $\mathrm{PQR}, \frac{A B}{Q R}=\frac{B C}{P R}=\frac{C A}{P Q}$, then
A. $\triangle P Q R \sim \triangle C A B$
B. $\triangle P Q R \sim \triangle A B C$
C. $\triangle C B A \sim \triangle P Q R$
D. $\triangle B C A \sim \triangle P Q R$

Answer: A

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6. If in two triangles DEF and PQR, $\lfloor D=\lfloor Q$, and $\lfloor R=\lfloor E$ which of the following is not true?
A. $\frac{E F}{P R}=\frac{D F}{P Q}$
B. $\frac{D E}{P Q}=\frac{E F}{R P}$
C. $\frac{D E}{Q R}=\frac{D F}{P Q}$
D. $\frac{E F}{R P}=\frac{D E}{Q R}$

Answer: B
7. The altitude of an equilateral triangle having the length of its side 12 cm is
A. 12 cm
B. $6 \sqrt{2} \mathrm{~cm}$
C. 6 cm
D. $6 \sqrt{3} \mathrm{~cm}$

## Answer: D

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8. 

$\triangle A B C \sim \Delta P Q R$.

$$
\left\lfloor A=40^{\circ},\left\lfloor C=60^{\circ}, A B=5 \mathrm{~cm}, A C=8 \mathrm{~cm} \text { and } P Q=7.5 \mathrm{~cm}\right.\right.
$$

, the correct statement among the following is
A. $P R=12 \mathrm{~cm},\left\lfloor R=60^{\circ}\right.$
B. $Q R=12 \mathrm{~cm},\left\lfloor R=80^{\circ}\right.$
C. $P Q=12 \mathrm{~cm},\left\lfloor R=80^{\circ}\right.$
D. $Q R=12 \mathrm{~cm},\left\lfloor P=40^{\circ}\right.$

## Answer: C

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9. In $\triangle D E F,\left\lfloor D=90^{\circ}\right.$, and $D L \perp E F$, then $\frac{E L}{L F}$ is
A. $\left(\frac{D E}{D F}\right)^{2}$
B. $\frac{D E}{D F}$
C. $\left(\frac{D E}{D L}\right)^{2}$
D. $\frac{D E}{D L}$

## Answer: B

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10. $\Delta A B C \sim \Delta D E F$. If $\mathrm{AB}=4 \mathrm{~cm}, \mathrm{AC}=3.5 \mathrm{~cm}, \mathrm{BC}=3 \mathrm{~cm}$, and $\mathrm{EF}=6$ cm , the perimeter of $\triangle D E F$ is
A. 21 cm
B. 14 cm
C. 10.5 cm
D. 18 cm

## Answer: A

11. In the figure, if $\triangle P O Q \sim \Delta S O R$ and $P Q: R S=1: 2$, then OP
: OS is
A. 1:2
B. 2:1
C. 3:1
D. 1:3

Answer: A

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Zee Additional Questions Very Short Answer Questions

1. In $\triangle A B C$, D and E are points on AB and AC respectively, such that $D E\left|\mid B C\right.$. If $\frac{A D}{D B}=\frac{4}{13}$ and $\mathrm{AC}=20.4 \mathrm{~cm}$, find AE .

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2. In $\Delta A B C, \mathrm{D}$ and E are points on AB and AC respectively, such that $D E \| B C$. If $A D=4, A E=8, D B=x-4$, and $E C=3 x-19$, find $x$.

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3. Given $\triangle A B C \sim \triangle P Q R$. If $\frac{A B}{P Q}=\frac{1}{3}$, find $\frac{\text { Area } \triangle A B C}{\text { Area } \triangle P Q R}$.

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4. Find the perimeter of the square whose diagonal is $5 \sqrt{2} \mathrm{~cm}$.
5. $\triangle A B C \sim \Delta D E F$. If area $(\triangle A B C)=2.89 m^{2}$, area $(\triangle D E F)=2.25 m^{2}$, and $A B=1.5 \mathrm{~m}$, find $D E$.

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6. If $\triangle A B C \sim \Delta P Q R, \mathrm{AB}=7 \mathrm{~cm}, \mathrm{PQ}=12.5 \mathrm{~cm}$, and the perimeter of $\triangle A B C=70 \mathrm{~cm}$, find the perimeter of $\triangle P Q R$.

## D View Text Solution

7. A vertical stick 1 m long casts a shadow 80 cm long. At the same time a tower casts a shadow 30 m long. Determine the height of the tower.
8. In an isosceles triangle $A B C$, if $A B=A C=25 \mathrm{~cm}$ and altitude from $A$ on $B C$ is 24 cm , find $B C$.

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9. Find the length of the chord of a circle of radius 8 cm which subtends a right angle at the centre.

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10. State and prove Basic proportionality theorem

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1. Legs of a right triangle are of lengths 16 cm and 8 cm . Find the length of the side of the largest square that can be inscribed in the triangle.

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2. In the figure $\left\lfloor D=\left\lfloor E\right.\right.$ and $\frac{A D}{D B}=\frac{A E}{E C}$. Prove that BAC is an isosceles triangle.

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3. Diagonals of trapezium PQRS intersect each other at the point
$\mathrm{O}, \mathrm{PQ} \| \mathrm{RS}$, and $\mathrm{PQ}=3 \mathrm{RS}$. Find the ratio of the areas of triangles

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4. In the given figure $\mathrm{PQ} \| \mathrm{RS}$, prove that $\triangle P O Q \sim \Delta S O R$.


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5. In the triangle PQR , is a point on PR such that $Q N \perp P R$. If PN .
$\mathrm{NR}=Q N^{2}$, prove that $\left\lfloor P Q R=90^{\circ}\right.$.

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6. If in a $\triangle P Q R, X Y| | Q R, P X=22 x, X Q=3 x, P Y=x$, and $Y R=9 x$, find the value of $x$.

## D View Text Solution

7. In a rectangle $A B C D, E$ is the mid point of $A B$. If $A B=16 \mathrm{~cm}$ and $A D=6 \mathrm{~m}$, find $E D$.

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8. In the given figure, $\left\lfloor A C B=90^{\circ}\right.$ and $C D \perp A B$. Prove that $\frac{B C^{2}}{A C^{2}}=\frac{B D}{A D}$.
9. In an isosceles $\triangle A B C, A B=A C$ and $B D \perp A C$. Prove that $B D^{2}-C D^{2}=2 C D . A D$.

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10. In a quadrilateral $\mathrm{ABCD}, \quad\left\lfloor B=90^{\circ}\right.$. If
$A D^{2}=A B^{2}+B C^{2}+C D^{2}$, prove that $\left\lfloor A C D=90^{\circ}\right.$.

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11. $P$ and $Q$ are the points on sides $A B$ and $A C$ respectively of
$\triangle A B C$. If $\mathrm{AP}=3 \mathrm{~cm}, \mathrm{~PB}=6 \mathrm{~cm}, \mathrm{AQ}=5 \mathrm{~cm}$ and $\mathrm{QC}=10 \mathrm{~cm}$, show that $B C=3 P Q$.

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12. In $\Delta \mathrm{ABC}, \mathrm{AD} \perp \mathrm{BC}$ and $A D^{2}=B D \times C D$. Prove that $A B^{2}+A C^{2}=(B D+C D)^{2}$


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13. In $\Delta \mathrm{ABC}, \mathrm{DE} \| \mathrm{BC}$. If $\mathrm{AD}=5 \mathrm{~cm}, \mathrm{BD}=7 \mathrm{~cm}$ and $\mathrm{AC}=18 \mathrm{~cm}$, find the length of AE.


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14. $\triangle A B C \sim \triangle D E F$ and their areas are $64 \mathrm{~cm}^{2}$ and $100 \mathrm{~cm}^{2}$ respectively. If $E F=12 \mathrm{~cm}$ then find the measure of BC .

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15. The diagonal $B D$ of parallelogram $A B C D$ intersect $A E$ at $F$ as shown in the figure. If $E$ is any point on $B C$, then prove that $D F \times E F=F B=F A$.

## Zee Additional Questions Short Answer Type 2 Questions

1. Prove that if the area of similar triangles are equal, they are congruent.

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2. In the figure, $A B C$ is a right-angled triangle, right-angled at C. D is a midpoint of BC . Prove that $A B^{2}=4 A D^{2}-3 A C^{2}$.

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3. In Fig, $A B C$ and $D B C$ are two triangles on the same base $B C$. If

AD intersects BC ,at O , show that $\frac{\operatorname{ar}(A B C)}{\operatorname{ar}(D B C)}=\frac{A O}{D O}$


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4. In the given figure, $D E \| B C$ and $A D: D B=5: 4$. Find $\operatorname{ar}(\triangle D E F): \operatorname{ar}(\triangle C F B)$.

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5. In the given figure, $\mathrm{PA}, \mathrm{QB}$, and RC each is perpendicular to AC such that $P A=x, R C=y, Q B=z, A B=a$, and $B C=b$. Prove that $\frac{1}{x}+\frac{1}{y}=\frac{1}{z}$.

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6. A girl of height 100 cm is walking away from the base of a lamp post at a speed of $1.9 \mathrm{~m} / \mathrm{s}$. If the lamp post is 5 m above the ground, find the length of her shadow after 4 seconds.

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7. In a right-angled $\triangle A B C$ right-angled at $\mathrm{C}, \mathrm{P}$ and Q are the midpoints of BC and AC . Prove that $A P^{2}+B Q^{2}=5 P Q^{2}$.

Zee Additional Questions Long Answer Type Questions

1. Throught the mid-point $M$ of the sides of a parallelogram $A B C D$, the line $B M$ is drawn intersecting $A C$ at $L$, and $A D$ produced to $E$. Prove that $E L=2 B L$.

2. A 5 m long ladder is placed leaning towards a vertical wall such that it reaches the wall at a point 4 m high. If the foot of the ladder is moved 1.6 m towards the wall, find the distance by which the top of the ladder would slide upwards on the wall.

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3. In the figure, $O B$ is the perpendicular bisector of the line segment DE. $F A \perp O B$ and FE intersects OB at point C . Prove that $\frac{1}{O A}+\frac{1}{O B}=\frac{2}{O C}$.

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4. In triangle $A B C, A P, B Q$ and $C R$ are the medians. Prove that $3\left[A B^{2}+B C^{2}+A C^{2}\right]=4\left[A P^{2}+B Q^{2}+C R^{2}\right]$.

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5. If $A$ is the area of a right angled triangle and $b$ is one of the sides containing the right angle. Prove that the length of the altitude on the hypotenuse is $\frac{2 A b}{\sqrt{b^{4}+4 A^{2}}}$.

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6. In the given figure, $A D$ is the median of $\triangle A B C$ and $A E \perp B C$. Prove that : $b^{2}+c^{2}=2 p^{2}+\frac{1}{2} a^{2}$.

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7. In an equilateral triangle $A B C, D$ is a point of $B C$ such that $4 B D=$ $B C$. Prove that $16 A D^{2}=13 B C^{2}$.

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8. Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.

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9. In a right angled triangle, square on the hypotenuse is equal to sum of the squares on the other sides. Prove the statement.
10. State and prove pythagoras theorem .

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