

# MATHS

# **BOOKS - ZEN MATHS (KANNADA ENGLISH)**

# TRIANGLES

**Illustrative Examples** 

1. In the figure,  $PR \mid |RC$  and  $QR \mid |BD$ . Prove that  $PQ \mid |CD$ .





2. In the given figure DE||BC and CD||BF prove that  $AC^2 = AE \times AF.$ 



**3.** In the figure,  $AB \perp BC$  and  $DE \perp AC$ . Prove that  $\triangle ABC \sim \triangle AED$ .

Watch Video Solution

**4.** In the given figure P is the midpoint of BC and Q is the midpoint of AP. If BQ when produced meets AC at R, prove that  $RA = \frac{1}{3}CA.$ 

**5.** In the given figure, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm, then find the pair of parallel lines and hence their lengths.



**6.** In the  $\Delta ABC$ , altitudes AD and CE intersect each other at point P. Prove that

i]  $\Delta APE \sim \Delta CPD$ 

ii]  $AP \times PD = CP \times PE$ 

iii]  $\Delta ADB \sim \Delta CEB$ 

iv]  $AB \times CE = BC \times AD$ 

Watch Video Solution

7. In the figure  $\lfloor QPR = \lfloor UTS = 90^\circ ext{ and } PR \mid \mid TS.$  Prove that  $\Delta PQR$ - $\Delta TUS.$ 



Watch Video Solution

8. In the figure 
$$\frac{AO}{OC} = \frac{BO}{OD} = \frac{1}{2}$$
 and AB = 5 cm. Find DC

**9.** If the area of two similar triangles is in the ratio 25 : 64, find the of their corresponding sides.

**10.** D, E and F are the mid-points of sides of  $\Delta ABC$ . P, Q, R are the mid-points of sides DEF. This process of marking the mid-points and forming a new triangle is continued. How are the areas of these triangles related?



11. In areas of two similar triangles ABC and PQR are in the ratio 9: 16. If BC = 4.5 cm. Find the length of QR.

Watch Video Solution

12.  $\Delta ABC$  and  $\Delta BDE$  are two equilateral triangles and BD = DC. Find the ratio between areas of  $\Delta ABC$  and  $\Delta BDE$ .



**13.** AD is altitude of equilateral  $\triangle ABC$ . On AD as base, another equilateral triangle ADE is constructed. Prove that  $\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle ABC} = \frac{3}{4}$ .

Watch Video Solution

14. The lengths of diagonals of a rhombus are 24 cm and 32 cm.

Calculate the altitide of the rhombus.

**15.** The sides AB and AC and the perimeter  $P_1$  of  $\Delta ABC$  are respectively three times the corresponding sides DE and DF and the perimeter  $P_2$  of  $\Delta DEF$ . Are the two triangles similar? If yes, find  $\frac{ar(\Delta ABC)}{ar(\Delta DEF)}$ .

Watch Video Solution

**16.** In the rectangle WXYZ, XY + YZ = 17 cm and XZ + YW = 26.

Calculate the length and breadth of the rectangle.



**17.** An insect 8 m away from the foot of a lamp post 6 m tall, crawls towards it. After moving through a distance, its distance from the top of the lamp post is equal to the distance it has moved. How far is the insect away from the foot of the lamp post?

Watch Video Solution

**18.** In  $\Delta ABC$ , C is a point on BD such that BC:CD=1:2 and  $\triangle$ ABC is

an equilateral triangle Prove that  $AD^2 = 7AC^2$ 

Watch Video Solution

19. In  $\Delta ABC, CD \perp AB, CA = 2AD, BD = 3AD$ . Prove that  $\lfloor BCA = 90^{\circ}.$ 

**20.** In the figure,  $AB \perp BC$  and  $DE \perp AC$ . Prove that  $\triangle ABC \sim \triangle AED$ .



Watch Video Solution

**21.** In the given figure  $|BAC = 90^{\circ}$ .

Prove that :

a]  $\Delta AGF$  ~  $\Delta BDG$ 

b]  $\Delta AGF \sim \Delta EFC$ 

c]  $\Delta BDG \sim \Delta EFC$ 

d]  $DE^2 = BD \times EC$ 

**22.** ABC is a right angled triangle. Points D and E trisect BC. Prove that  $8AE^2 = 3AC^2 + 5AD^2$ .

23. In an equilateral triangle ABC,  $AD \perp BC$ . Prove that  $AD^2 = 3BD^2.$ 

> Watch Video Solution

Watch Video Solution

**Textual Exercises Exercise 21** 

1. Fill in the blanks using the correct word given in brackets :

All circles are ...... ( congruent , similar )



4. Two polygons of the same number of sides are similar, if

Their corresponding sides are \_\_\_\_\_



5. Two polygons of the same number of sides are similar, if

Their corresponding angles are	and
--------------------------------	-----



**6.** Give two different examples of a pair of different radii of different length:

i] Similar figures

ii] Non-similar figures.

7. State whether the following quadrilaterals are similar or not:





### **Textual Exercises Exercise 2 2**

**1.** E and F are points on the sides PQ and PR respectively of a  $\Delta PQR$ . For the following cases, state whether EF||QR.

i] PE = 3.9 cm, EQ = 3 cm, PF = 3.6 cm, and FR = 2.4 cm.

ii] PE = 4 cm, QE = 4.5 cm, PF = 8 cm, RF = 9 cm

iii] PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm, and PF = 0.36 cm.









# **4.** In the figure DE||OQ| and DF||OR. Show that EF | | QR.





**5.** In Fig A, B and C are points on OP, OQ and OR respectively such that AB || PQ and AC || PR . Show that BC || QR.





6. Prove that a line drawn through the midpoint of one side of a

triangle parallel to another side bisects the third side (using BPT).



# Watch Video Solution

7. Prove that the line joining the midpoints of any two sides of a

triangle is parallel to the third side.

8. ABCD is a trapezium in which AB || DC. Its diagonals intersect

each other at O.

Show that  $\frac{AO}{BO} = \frac{CO}{DO}$ 



9. The diagonals of a quadrilateral ABCD intersect each other at

the point O such that 
$$\frac{AO}{BO} = \frac{CO}{DO}$$
.

Show that ABCD is a trapezium.



1. If the areas of two similar triangles are equal, prove that they

#### are congruent.



Watch Video Solution

2. If the areas of two similar triangles are equal, prove that they

are congruent.





**3.** State which pairs of triangles in Fig are similar. Write the similarity criterion used by you for answering the question also write the pairs of similar triangles in the symbolic form:





4. If the areas of two similar triangles are equal, prove that they

are congruent.





**6.** In Fig , if  $\Delta ABE \angle \Delta ACD$  , show that  $\Delta ADE \text{-}\Delta ABC$ 





7. In the figure altitudes AD and CE of  $\Delta ABC$  intersect each other at the point P. Show that

1]  $\Delta AEP \sim \Delta CDP$ 

2]  $\Delta ABD \sim \Delta CBE$ 



4]  $\Delta PDC \sim \Delta BEC$ 

Watch Video Solution

**8.** E is a point on the side AD produced, of a parallelogram ABCD and BE intersects CD at F. Show that  $\Delta ABE \sim \Delta CFB$ .

Watch Video Solution

**9.** In Fig , ABC and AMP are two right triangles, right angled at B and M respectively. Prove that :





**10.** CD and GH are respectively the bisectors of  $\lfloor ACB \text{ and } \lfloor EGF \text{ such that D and H lie on sidea AB and FE of } \Delta ABC$  and  $\Delta EFG$  respectively. If  $\Delta ABC \sim \Delta FEG$ , show that. **i**]  $\frac{CD}{GH} = \frac{AC}{FG}$  ii]  $\Delta CDB \sim \Delta HGE$ 

iii]  $\Delta DCA$  ~  $\Delta HGF$ 

Watch Video Solution

11. In the figure, E is a point on side CB produced, of an isosceles triangle ABC, with AB = AC. If  $AD \perp BC$  and  $EF \perp AC$ , prove that  $\Delta ABD \sim \Delta ECF$ .



> Watch Video Solution

12. Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of  $\Delta PQR$ . Show that  $\Delta ABC \sim \Delta PQR$ .

**13.** D is a point on the side BC of a triangle ABC such that  $\lfloor ADC = \lfloor BAC \rfloor$ . Show that  $CA^2 = CB . CD$ .

Watch Video Solution

14. Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of  $\Delta PQR$ . Show that  $\Delta ABC \sim \Delta PQR$ .



**15.** A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts shadow 28 m long. Find the height of the tower.

 $\blacktriangleright$ 16. If AD and PM are median of triangles ABC and PQR respectively where  $\Delta ABC - \Delta PQR$ , prove that  $\frac{AB}{PQ} = \frac{AD}{PM}$ .

Watch Video Solution

Textual Exercises Exercise 2 4

1. Let  $\Delta ABC \sim \Delta DEF$  and their areas be , respectively ,  $64cm^2$  and  $121cm^2$  . If EF = 15.4 cm, find BC

Watch	Video	Solution	

**2.** Diagonals of a trapezium ABCD with AB  $\parallel$  DC intersect each other at the point O. If AB = 2CD, find the ratio of the areas of triangle AOB and COD.



Watch Video Solution

3. In the figure ABC and DBC are two triangles on the same base

BC. If AD intersects BC at 0, show that  $\frac{\text{Area}(\Delta ABC)}{\text{Area}(\Delta DBC)} = \frac{AO}{DO}$ .

Watch Video Solution

**4.** If the areas of two-similar triangles are equal, prove that the they are congruent.

<b>O</b> Watch Video Solution
-------------------------------

5. D,Eand F are respectively the mid - points of sides AB, BC and CA

of  $\Delta ABC$  . Find the ratio of the areas of  $\Delta DEF$  and  $\Delta ABC$ .



**6.** Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.



**7.** Prove that the area of an equilateral triangle described on one side of a square is equal of half the area of the equilateral triangle described on one of its diagonals.

Watch Video Solution

**8.** ABC and BDF are two equilateral triangles such that D is the mid -point of BC. Ratio of the areas of triangles ABC and BDF is

A. 2:1

B.1:2

C.4:1

D.1:4

Answer: C

**9.** Sides of two similar triangles are in the ratio 4 : 9 Areas of these triangles are in the ratio

A. 2:3

B.4:9

C. 81:16

D. 16:81

Answer: D

**Watch Video Solution** 

Textual Exercises Exercise 2 5

**1.** Sides of triangles are given below. Determine which of them are right triangles.

In case of a right triangle , write the length of its hypotenuse.

7cm, 24 cm, 25 cm

Watch Video Solution

2. PQR is a triangle right angled at P and M is a point on QR such

that  $PM \perp QR$ . Show that  $PM^2 = QM$ . MR.



**3.** In the figure ABD is a triangle right-angled at A and  $AC \perp BD$ .

Show that

i]  $AB^2 = BC. BD$ 



5. ABC is an isosceles triangle with AC = BC. If  $AB^2=2AC^2$ ,

prove that ABC is a right-angled triangle.



**6.** ABC is an equilateral triangle of side 2a. Find each of its altitudes.



Watch Video Solution

7. Prove that sum of the squares of the side of a rhombus is equal

to the to the sum of the squares of its diagonals.



8. In the figure given below, O is point in the interior of a triangle ABC,  $OD \perp BC$ ,  $OE \perp AC$  and  $OF \perp AB$ . Show that

(i)

$$OA^2 + OB^2 + OC^2 + OD^2 - OE^2 - OF^2 = AR^2 + BD^2 + CE^2$$

(ii)  $AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$ 





9. A ladder 10 m long reaches a window 8 m above the ground.

Find the distance of the foot of the ladder from base of the wall.



**10.** A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end . How far from the base of the pole should the stake be driven so that the wire will be taut ?

Watch Video Solution

**11.** An aeroplane leaves an airport and files due north at a speed of 1000 km per hour. At the same time, another aeroplane leaves the same airpot and flies due west at a speed of 1200 km per hour . How far apart will be the two planes after  $1\frac{1}{2}$  hours ?



**12.** Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12m , find the





14. The perpendicular from A on side BC of a  $\Delta ABC$  intersects

BC at D such that DB = 3CD. Prove that  $2AB^2 = 2AC^2 + BC^2$ .



**15.** In an equilateral triangle ABC, D is a point on BC such that

$$BD=rac{1}{3}BC$$
. Prove that  $9AD^2=7AB^2$ .

Watch Video Solution

Watch Video Solution

16. In an equilateral triangle prove that three times the square of

one side is four times the square of its altitude.

17. Tick the correct answer and justify : In  $\Delta ABC, AB=6\sqrt{3}cm, AC=12cm$  and BC=6cmThe angle B is : A.  $120^{\,\circ}$ 

 $\text{B.}\,60^{\,\circ}$ 

C.  $90^{\circ}$ 

D.  $45^{\,\circ}$ 

Answer: C

**Watch Video Solution** 

Zee Additional Questions Multiple Choice Questions

1. ABC is an isosceles triangle right-angled at C. Prove that  $AB^2=2AC^2.$ 

A.  $AB^2=2AC^2$ 

 $\mathsf{B}.\,BC^2=2AB^2$ 

 $\mathsf{C}.AC^2 = 2AB^2$ 

 $\mathsf{D}.\,AB^2 = 4AC^2$ 

#### Answer: A



2. If  $\triangle ABC$  is similar to  $\triangle DEF$  such that  $\lfloor D = 47^{\circ}$  and  $\lfloor B = 83^{\circ}, \lfloor F \text{ is}$ A.  $80^{\circ}$ B.  $60^{\circ}$ 

C.  $40^{\circ}$ 

D.  $50^{\circ}$ 

### Answer: D



### 3. In $\Delta ABC$ , $DE \mid BC$ . AD = (7x - 4) cm, AE = (5x - 2) cm, DB =

(3x + 4) cm, and EC = 3x cm. The value of x is

A. 4

B. 3

C. 5

D. 2.5

#### Answer: A

4. The lengths of the diagonals of a rhombus are 16 cm and 12 cm.

Then the length of the side of the rhombus is

A. 9 cm

B. 10 cm

C. 8 cm

D. 20 cm

Answer: B

**Watch Video Solution** 

5. If in two triangles ABC and PQR,  $\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$ , then

A.  $\Delta PQR \sim \Delta CAB$ 

В.  $\Delta PQR \sim \Delta ABC$ 

C.  $\Delta CBA \sim \Delta PQR$ 

D.  $\Delta BCA \sim \Delta PQR$ 

Answer: A

Watch Video Solution

6. If in two triangles DEF and PQR,  $\lfloor D = \lfloor Q, \text{ and } \lfloor R = \lfloor E \end{pmatrix}$  which of the following is not true?

A. 
$$\frac{EF}{PR} = \frac{DF}{PQ}$$
  
B.  $\frac{DE}{PQ} = \frac{EF}{RP}$   
C.  $\frac{DE}{QR} = \frac{DF}{PQ}$   
D.  $\frac{EF}{RP} = \frac{DE}{QR}$ 

#### Answer: B

7. The altitude of an equilateral triangle having the length of its

side 12 cm is

A. 12 cm

B.  $6\sqrt{2}$  cm

C. 6 cm

D.  $6\sqrt{3}$ cm

Answer: D



8. 
$$\Delta ABC \sim \Delta PQR$$
. If

 $\lfloor A=40^{\circ}, \lfloor C=60^{\circ}, AB=5cm, AC=8cm ext{ and } PQ=7.5cm$ 

, the correct statement among the following is

A. 
$$PR=12cm, \lfloor R=60^{\circ}$$

B. 
$$QR=12cm,$$
  $\lfloor R=80^{\circ}$ 

C. 
$$PQ=12cm,\,|R=80^\circ$$

D. 
$$QR=12cm,$$
  $|P=40^{\circ}$ 

#### Answer: C

**9.** In 
$$\Delta DEF, \lfloor D=90^\circ, ext{ and } DL\perp EF, ext{then } rac{EL}{LF}$$
 is

A. 
$$\left(\frac{DE}{DF}\right)^2$$
  
B.  $\frac{DE}{DF}$   
C.  $\left(\frac{DE}{DL}\right)^2$ 

D.  $\frac{DE}{DL}$ 

#### Answer: B

# Watch Video Solution

**10.**  $\Delta ABC \sim \Delta DEF$ . If AB = 4 cm, AC = 3.5 cm, BC = 3 cm, and EF = 6

cm, the perimeter of  $\Delta DEF$  is

A. 21 cm

B. 14 cm

C. 10.5 cm

D. 18 cm

Answer: A



11. In the figure, if  $\Delta POQ$  ~ $\Delta SOR \,\, {
m and} \,\, PQ$  : RS=1 : 2, then OP

#### : OS is

A. 1:2

B. 2:1

C.3:1

D.1:3

#### Answer: A

Watch Video Solution

Zee Additional Questions Very Short Answer Questions

**1.** In  $\triangle ABC$ , D and E are points on AB and AC respectively, such that  $DE \mid BC$ . If  $\frac{AD}{DB} = \frac{4}{13}$  and AC = 20.4 cm, find AE.

# Watch Video Solution

**2.** In  $\Delta ABC$ , D and E are points on AB and AC respectively, such

that DE || BC. If AD = 4, AE = 8, DB = x - 4, and EC = 3x - 19, find x.

Watch Video Solution

**3.** Given 
$$\triangle ABC \sim \triangle PQR$$
. If  $\frac{AB}{PQ} = \frac{1}{3}$ , find  $\frac{\text{Area } \triangle ABC}{\text{Area } \triangle PQR}$ .

Watch Video Solution

**4.** Find the perimeter of the square whose diagonal is  $5\sqrt{2}$  cm.



5.  $\Delta ABC$  -  $\Delta DEF$ . If area  $(\Delta ABC) = 2.89m^2$ , area

 $(\Delta DEF)=2.25m^2$ , and AB = 1.5 m, find DE.

Watch Video Solution

6. If  $\Delta ABC \sim \Delta PQR$ , AB = 7 cm, PQ = 12.5 cm, and the perimeter

of  $\Delta ABC = 70cm$ , find the perimeter of  $\Delta PQR$ .

View Text Solution

7. A vertical stick 1 m long casts a shadow 80 cm long. At the same

time a tower casts a shadow 30 m long. Determine the height of

the tower.

8. In an isosceles triangle ABC, if AB = AC = 25 cm and altitude

from A on BC is 24 cm, find BC.



9. Find the length of the chord of a circle of radius 8 cm which

subtends a right angle at the centre.



10. State and prove Basic proportionality theorem

Watch Video Solution

Zee Additional Questions Short Answer Type 1 Questions

**1.** Legs of a right triangle are of lengths 16 cm and 8 cm. Find the length of the side of the largest square that can be inscribed in the triangle.



**3.** Diagonals of trapezium PQRS intersect each other at the point O, PQ||RS, and PQ = 3RS. Find the ratio of the areas of triangles POQ and ROS.



S

5. In the triangle PQR, is a point on PR such that  $QN\perp PR$ . If PN.

NR =  $QN^2$ , prove that  $\lfloor PQR = 90^\circ.$ 

Watch Video Solution

6. If in a  $\Delta PQR, XY \mid |QR, PX = 22x, XQ = 3x, PY = x$ ,

and YR = 9x, find the value of x.



Watch Video Solution

**8.** In the given figure,  $\lfloor ACB = 90^{\circ} \text{ and } CD \perp AB$ . Prove that





**11.** P and Q are the points on sides AB and AC respectively of  $\Delta ABC$ . If AP = 3 cm, PB = 6 cm, AQ = 5 cm and QC = 10 cm, show that BC = 3 PQ.

12. In  $\Delta$  ABC , AD  $\perp$  BC and  $AD^2 = BD imes CD$ . Prove that  $AB^2 + AC^2$ =  $(BD + CD)^2$ 





**13.** In  $\Delta$  ABC , DE || BC . If AD= 5 cm , BD = 7 cm and AC = 18 cm , find the length of AE.



**14.**  $\Delta ABC \sim \Delta DEF$  and their areas are  $64cm^2$  and  $100cm^2$ respectively. If EF = 12cm then find the measure of BC.

Watch Video Solution

15. The diagonal BD of parallelogram ABCD intersect AE at F as shown in the figure. If E is any point on BC, then prove that  $DF \times EF = FB = FA$ .



Zee Additional Questions Short Answer Type 2 Questions

**1.** Prove that if the area of similar triangles are equal, they are

congruent.

**Watch Video Solution** 

2. In the figure, ABC is a right-angled triangle, right-angled at C. D

is a midpoint of BC. Prove that  $AB^2 = 4AD^2 - 3AC^2$ .





5. In the given figure, PA, QB, and RC each is perpendicular to AC such that PA = x, RC = y, QB = z, AB = a, and BC = b. Prove that  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$ .

Watch Video Solution

**6.** A girl of height 100 cm is walking away from the base of a lamp post at a speed of 1.9 m/s. If the lamp post is 5 m above the ground, find the length of her shadow after 4 seconds.

Watch Video Solution

7. In a right-angled  $\Delta ABC$  right-angled at C, P and Q are the midpoints of BC and AC. Prove that  $AP^2 + BQ^2 = 5PQ^2$ .

## Zee Additional Questions Long Answer Type Questions

**1.** Throught the mid-point M of the sides of a parallelogram ABCD, the line BM is drawn intersecting AC at L, and AD produced to E. Prove that EL = 2BL.





**2.** A 5 m long ladder is placed leaning towards a vertical wall such that it reaches the wall at a point 4 m high. If the foot of the ladder is moved 1.6 m towards the wall, find the distance by which the top of the ladder would slide upwards on the wall.

# Watch Video Solution

**3.** In the figure, OB is the perpendicular bisector of the line segment DE.  $FA \perp OB$  and FE intersects OB at point C. Prove that  $\frac{1}{OA} + \frac{1}{OB} = \frac{2}{OC}$ .

**4.** In triangle ABC, AP, BQ and CR are the medians. Prove that  $3[AB^2 + BC^2 + AC^2] = 4[AP^2 + BQ^2 + CR^2].$ 

Watch Video Solution

5. If A is the area of a right angled triangle and b is one of the sides containing the right angle. Prove that the length of the altitude on the hypotenuse is  $\frac{2Ab}{\sqrt{b^4 + 4A^2}}$ .

# Watch Video Solution

6. In the given figure, AD is the median of  $\Delta ABC$  and  $AE\perp BC.$  Prove that  $:b^2+c^2=2p^2+rac{1}{2}a^2.$ 





9. In a right angled triangle, square on the hypotenuse is equal to

sum of the squares on the other sides. Prove the statement.



10. State and prove pythagoras theorem .

