



MATHS

BOOKS - KC SINHA MATHS (HINGLISH)

CIRCLES - FOR BOARDS

Solved Examples

1. Find the equation of circle whose centre is $\left(\frac{1}{2}, \frac{1}{2}\right)$ and radius is $\frac{1}{\sqrt{2}}$.

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2. Find the equation of the circle whose centre is (1,2) and which passes

through the point (4,6).

3. If the equations of the two diameters of a circle are x + y = 6 and x + 2y = 4 and the radius of the circle is 10, find the equation of the circle.

4. If the line 2x - y + 1 = 0 touches the circle at the point (2, 5) and the centre of the circle lies in the line x + y - 9 = 0. Find the equation of the circle.

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5. Find the equation of the circle which passes through the origin and cuts off intercepts 6 and 8 from the positive parts of x and y axes respectively.



6. Find the equation of the circle which touches : y-axis and has centre at

(2, 3)`



9. Find the equation of a circle which touches both the axes and whose radius is 2 units

10. Find the equation of the circle which has its centre at the point (3,4) and touches the straight line 5x + 12y - 1 = 0.



11. Find the equations of the circles passing through two points on y-axis at distance 3 from the origin and having radius 5.

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12. Find the equation of a circle which passes through the point (2, 0)and whose centre is the limit of the point of intersection of eth lines 3x + 5y = 1and $(2 + c)x + 5c^2y = 1$ as $c \stackrel{\rightarrow}{1}$.

13. Find the equation of the circle with radius 5 whose centre lies on xaxis and passes through the point (2, 3).



Find the equation of the circle, if it passes through (7, 3).

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15. Find the equation of the circle passing through the points (1, -2)and(4, -3) and whose centre lies on the 3x + 4y = 7.

16. One of the diameters of the circle circumscribing the rectangle ABCD is 4y = x + y. If A and B are the points (-3, 4) and (5, 4)





17. Find the equations of circles which touch the axes and whose centres

lie on the x - 2y = 3.



18. A circle of radius 2 lies in the first quadrant and touches both the axes. Find the equation of the circle with centre at (6, 5) and touching the above circle externally.

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19. Find the equation of the circle whose radius is 5and which touches the circle $x^2 + y^2 - 2x - 4y - 20 = 0$ externally at the point (5, 5).

20. Equation of circle whose centre is (3, -1) and which cut off an intercept of length 6 unit from the line : 2x - 5y + 18 = 0 is:

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21. Find the equations of the circles touching y-axis at (0,3) and making an

intercept of 8 units on the x-axis.

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22. Find the radius of the circle which touches the axis of x at a distance 3

from the origin and cuts an intercept of length 6 on the axis of y.



23. A circle of radius 5units touches the coordinate axes in the first quadrant. If het circle makes one complete roll on $x - a\xi s$ along he positive direction of $x - a\xi s$, find its equation in new position.



$$3x^2 + 3y^2 - 8x - 10y + 3 = 0$$



27. Prove that the radi of the circles $x^2+y^2=1$, $x^2+y^2-2x-6y=6$ and $x^2+y^2-4x-12y=9$ are in arithmetic

progression.

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28. Find the coordinates of the middle point of the chord which the circle

 $x^2+y^2+4x-2y-3=0$ cuts off on the line x-y+2=0

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29. Find the area of equilateral triangle inscribed in a circle $x^2+y^2+2gx+2fy+c=0$



33. The radius of the circle passing through the vertices of the triangle formed by the lines x + y = 2, 3x - 4y = 6, x - y = 0

34. Find the equation of the circle passing through the origin and the points where the line 3x + 4y = 12 meets the axes of coordinates.

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35. Find the equation of the circle which passes through the points (1, -2), (4, -3) and whose center lies on the line 3x + 4y = 7.

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36. Show that the points (5, 5), (6, 4), (-2, 4) and (7, 1), all lie on a

circle. Find its equation, centre and radius.`

37. Find the equation of the circle which passes through the centre of the circle $x^2 + y^2 + 8x + 10y - 7 = 0$ and is concentric with the circle $2x^2 + 2y^2 - 8x - 12y - 9 = 0$



38. Find the equations of the circles touching y-axis at (0,3) and making an intercept of 8 units on the x-axis.

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39. The equation of circle which passes through (1, -1) and which touches

the line 6x + y - 18 = 0 at point (3, 0) is



40. Show that a cyclic quadrilateral is formed by the lines 5x + 3y = 9, x = 3y, 2x = y and x + 4y + 2 = 0 taken in order. Find the equation of the circumcircle.



41. Examine whether the following equation represents a circle or not :

 $3x^2 + 3y^2 + 2xy + 3x + y = 0$

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42. Examine whether the following equation represents a circle or not :

 $4x^2 + 4y^2 + 12x + 8y + 40 = 0$

43. Examine whether that equations reprsent a circle, point or no circle :

$$x^2 + y^2 - 3x + 3y + 10 = 0$$

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44. Examine whether that equations reprsent a circle, point or no circle :

$$x^2 + y^2 + 2x + 1 = 0$$

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45. Examine whether that equations reprsent a circle, point or no circle :

$$x^2 + y^2 - 1 = 0$$

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46. Find the equation of the circle when the end points of a diameter are

(5, -3) and (2, -4). Also find its centre and radius.

47. The abscissa of the two points A and B are the roots of the equation $x^2 + 2ax - b^2 = 0$ and their ordinates are the roots of the equation $x^2 + 2px - q^2 = 0$. Find the equation of the circle with AB as diameter. Also, find its radius.

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48. Find the equation of the circle passing through the origin and the points where the line 3x + 4y = 12 meets the axes of coordinates.

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49. Find the equation of the circle whose diameter is the portion of the

line 3x + 4y - 14 = 0, intercepted by the lines y = x and 11x = 4y.

50. The sides of a square are x = 1, x = 3, y = 2 and y = 4. Find the equation of the circle drawn on the diagonal of the square as its diameter.



52. Find the parametric form of the equation of the circle $x^2 + y^2 + px + py = 0.$

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53. Find the parametric equations of that circles : $2x^2 + 2y^2 - 5x - 7y - 3 = 0$



54. Find the equation of a circle whose diameters are

2x-3y+12 and x+4y-5=0 and area is 154 square units .

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55. Find the Cartesian euqaiton of that curves whose parametric equation

 $x=x+4\coslpha,y=-3+4\sinlpha$

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56. Find the Cartesian euqaiton of that curves whose parametric equation

$$x = 5 + 3\cos heta, y = 7 + 3\sin heta$$

57. Find the Cartesian euqaiton of that curves whose parametric equation

$$x = \cos heta + \sin heta + 1, y = \sin heta - \cos heta + 2$$

58. Show that equations $x = a \cos \theta + b \sin \theta$, $y = a \sin \theta - b \cos \theta$ represents a circle, wheter θ is a parameter.

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59. Show that the point (x, y) given by $x = \frac{2at}{1+t^2}andy = \left(\frac{1-t^2}{1+t^2}\right)$ lies on a circle for all real values of t such that $-1 \le t \le 1$, where a is

any given real number.













14. Find the equation of the circle passing through (0, 0) and making intercepts a and b on the coordinate axes.



17. Find the equation of the circle touching : x-axis at the origin and

having radius 10

18. Find the equation of the circle which passes through two points on

the x-axis which are at distances 4 from the origin and whose radius is 5.

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19. Find the equation of the circle with centre (2, 2) and passing through

the point (4, 5).

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20. Find the equation of image of the circle $\left(x-1
ight)^2+\left(y+2
ight)^2=5^0$ in

the x-axis.

21. Find the equation of the circle passing through the point (2, 4) and centre at the point of intersection of the lines x - y = 4 and 2x + 3y = -7.



22. I the equations of two diameters of a circles are 2x + y = 6 and 3x + 2y = 4 and the radius is 10, find the equation of the circle.

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23. Find the equation to the circle which passes through the point of intersection of 3x - 2y - 1 = 0 and 4x + y - 27 = 0 and whose centre is (2, 3)

24. Find the equation of the circle whose centre is (2, -3) and which pass through the point of intersection of 3x + 2y = 11 and 2x + 3y = 4.

25. Find the equation of the circle passing through the centre of the circle $x^2 + y^2 - 4x - 6y = 8$ and being concentric with the circle $x^2 + y^2 - 2x - 8y = 5$.

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26. Find the equaiton of the circle passing through the point of intersection of x + 3y = 0 and 2x - 7y = 0 and whose centre is the point of intersection of lines x + y + 1 = 0 and x - 2y + 4 = 0

27. Find the equation of circle whose centre is the point (1, -3) and touches the line 2x - y - 4 = 0Watch Video Solution 28. Find the equation of the circle of radius 5 whose centre lies on y-axis

and which passes through the point (3, 2).

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29. Find the equation of the circle whose radius is 5 and centre lies on the

positive side of x-axis at a distance 5 from the origin.



30. Find the equation of the circle which passes through the points (-1, 2) and (3, -2) and whose centre lies on the line x - 2y = 0.





32. Find the equation of the circle which passes through the points

(2, -2), and (3,4) and whose centre lies on the line x + y = 2.



33. Find the equation of the circle passing through the points (4, 1) and

(6, 5) and whose centre is on the line 4x + y = 16.

34. Find the equation of the circle which touches the axis of y at a distance 4 from the origin and cuts off an intercept of length 6 on the axis of x.

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35. Does the point
$$(-2.5, 3.5)$$
 lie inside, outside or on the circle
 $x^2 + y^2 = 25$?

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36. Find the centre and radius of the circles $x^2 + y^2 - 8x + 10y - 12 = 0$

37. Find the centre and the radius of the circle $x^2 + y^2 + 8x + 10y - 8 = 0.$





42. Find the centre and radius of each of that circles : $x^2 + y^2 - 2x + 4y = 8$



43. Find the centre and radius of each of that circles : $x^2 + y^2 - 4x + 6y = 5$

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44. Find the centre and radius of the circles : $x^2 + y^2 - 8x - 12y - 48 = 0$

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45. Find the centre and radius of the circles : $x^2 + y^2 - ax - by = 0$



 $x^2+y^2+6x-2y-1=0$ and $x^2+y^2-12x+4y=1$ are collinear





53. Find the equation of the circles passing through the three points : (0, 0), (5, 0) and (3, 3)

54. Find the equation of the circles passing through the three points : (1, 0), (0, 1) and (-1, 0)

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55. Find the equation of the circles passing through the three points :

(1, -2), (5, 4) and (10, 5)

56. Find the equation of the circles passing through the three points : (1, 2), (3, -4) and (5, -6)



57. Find the equation of the circle circumscribing the triangle formed by

the straight lines x + y = 6, 2x + y = 4 and x + 2y = 5.

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58. Find the equation of the circle which is concentric with the circle $x^2 + y^2 - 4x + 6y - 3 = 0$ and the double of its area.

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59. Find the equation of the circle concentric with the circle $2x^2 + 2y^2 - 6x + 8y + 1 = 0$ and of double its area.



60. Find the equation. of the circle concentric with the $x^2 + y^2 + 4x - 8y - 6 = 0$ and having radius double of its radius.

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61. Find the equation of the circle concentric with the circle $x^2 + y^2 - 4x - 6y - 9 = 0$ and passing through the point (-4, -5)

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62. Find the equation of the circle passing through the points (1, -1)and centre at the intersection of the lines x - y = 4 and 2x + 3y = -7

63. The line 5x - y = 3 is a tangent to a circle at the point (2, 7) and its

centre is on the line x + 2y = 19. Find the equation of the circle.

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64. If the line 4x - 3y = -12 is tangent at point (-3, 0) and the line 3x + 4y = 16 is tangent at the point (4, 1) to a circle then equation of circle

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65. Find the equation of the circle circumscribing the quadrilateral

formed by the straight lines

x - y = 0, 3x + 2y = 5, x - y = 10 and 2x + 3y = 0

66. Find the equation of the circle passing through the points (0, -1) and (2, 0) and whose centre lies on the line 3x + y = 5



67. Find the equaiton of the circle passing through the points (2, -3) and (3, -2) and whose centre lies on the line 2x - 3y = 8.

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68. Determine whether the equation represent a circle or not : $3x^2 - 3y^2 + 4x - 6y + 10$ =0`

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69. Determine whether the equation represent a circle or not : $5x^2 + 5y^2 + 2xy + 4x - y + 2 = 0$

70. Determine whether the equation represent a circle or not : $5x^2 + 5y^2 + 4x - 8y - 16 = 0$

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71. Determine whether the equation represent a circle or not : $x^2 + y^2 + 6x - 8y + 50 = 0$

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72. Determine whether the equation represent a circle, a point or no

 $\mathsf{circle}: x^2 + y^2 + x - y = 0$

73. Determine whether the equation represent a circle, a point or no $\operatorname{circle}: x^2+y^2-6x-8y+25=0$



74. Determine whether the equation represent a circle, a point or no ${
m circle}: x^2+y^2+2x+10y+26=0$

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75. Determine whether the equation represent a circle, a point or no circle : $2x^2 + 2y^2 - 24x + 8y + 120 = 0$

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76. Find the equation of the circle when the end points of a diameter of the circle are : (3, 4) and (-3, -4)



77. Find the equation of the circle when the end points of a diameter of

the circle are : (-2, 3) and (3, -5)

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78. Find the equation of the circle when the end points of a diameter of

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the circle are : (0, 0) and (2, -4)
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79. Find the equation of the circle when the end points of a diameter of

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the circle are : (-2, -3) and (-3, 5)
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80. Find the equation of the circle when the end points of a diameter of the circle are : (p,q) and (r,s)
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81. Find the equation of the circle when the end points of a diameter of

the circle are : (2, 3) and (-1, -3)

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82. Find the equation of the circle when the end points of a diameter of

the circle are : (3, 2) and (2, 5)



83. Find the equation of the circle, the end points of whose diameter are

(2, -3) and (-2, 4). Find its centre and radius.



84. Find the equaiton of the circle drawn on the intercept between the

axes made by the line 3x + 4y = 12 as a diameter.

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85. Find the equaiton of the circle drawn on the intercept between the

axes made by the line 3x + 4y = 12 as a diameter.

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86. Show that equation of the circle passing through the origin and cutting intercepts a and b on the coordinate axes is $x^2 + y^2 - ax - by = 0$

87. Find the equation of the circle the end points of whose diameter are the centres of the circle : $x^2 + y^2 + 6x - 14y = 1$ and $x^2 + y^2 - 4x + 10y = 2.$

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88. The abscissae of two points A and B are the roots of the equaiton $x^2 + 2x - a^2 = 0$ and the ordinats are the roots of the equaiton $y^2 + 4y - b^2 = 0$. Find the equation of the circle with AB as its diameter. Also find the coordinates of the centre and the length of the radius of the circle.

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89. If (4, 1) be an end of a diameter of the circle $x^2 + y^2 - 2x + 6y - 15 = 0$, find the coordinates of the other end of the diameter.

90. The sides of a rectangle are given by the equations x=-2, x = 4, y=-2 and y=-5. Find the equation of the circle drawn on the diagonal of this rectangle as its diameter.



91. Find the equaiton of the circle drawn on a diagonal of the rectangle as

its diameter whose sides are : x = 5, x = 8, y = 4, y = 7

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92. The sides of a square are x = 6, x = 9, y = 3 and y = 6. Find the

equation of a circle drawn on the diagonal of the square as its diameter.

93. Find the equation of the circle circumscribing the rectangle whose

sides are : x = 4, x = -5, y = 5, y = -3

94. Find the equation of the circle circumscribing the rectangle whose

sides are : x = 6, x = -3, y = 3, y = -1

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95. Find the equation of the circle circumscribing the rectangle whose

sides are : x - 3y = 4, 3x + y = 22, x - 3y = 14, 3x + y = 62

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96. Find the parametric equation of the circles : $x^2 + y^2 = 9$



100. Find the Cartesian equation of the curves whose parametric equation are : $x=5\cos heta,\,y=5\sin heta$



101. Find the Cartesian equation of the curves whose parametric equation

 $\mathsf{are}: x = a + c \cos \alpha, y = b + c \sin \alpha$

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102. Find the Cartesian equation of the curves whose parametric equation

 $\operatorname{are}: x = 3\cos\alpha, y = 3\sin\alpha$



103. Find the Cartesian equation of the curves whose parametric equation

are :
$$x = 1 + 3\cos{ heta}, y = 2 - 3\sin{ heta}$$

104. Find the Cartesian equation of the curves whose parametric

equation are : $x = \cos heta + \sin heta, y = \sin heta - \cos heta$

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105. Find the Cartesian equation of the curves whose parametric equation

are :
$$x=rac{20t}{4+t^2}, y=rac{5ig(4-t^2ig)}{4+t^2}$$

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106. Prove that : $x \cos \theta + y \sin \theta = a$ and $x \sin \theta - y \cos \theta = b$ are the

parametric equations of a circle for all heta satisfying $0 \leq heta < 2\pi$

107. Show that : $x = a \cos \theta - b \sin \theta$ and $y = a \sin \theta + b \cos \theta$, represent a circle where θ is the parameter.



108. Show that the point (x,y) , where $x=5\cos heta, y=-3+5\sin heta,$

lies on a circle for all values of `theta

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109. Show that the point (x, y), where $x = a + r \cos \theta$, $y = b + r \sin \theta$,

lies on a circle for all values of θ .