



## MATHS

### BOOKS - KC SINHA MATHS (HINGLISH)

### MATRICES - FOR COMPETITION

#### Solved Examples

1. If  $A, B, C$  are three matrices such that

$$A = \begin{bmatrix} x & y & z \end{bmatrix}, B = \begin{bmatrix} a & h & g \\ h & b & f \\ g & f & c \end{bmatrix}, C = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \text{ Find } ABC.$$

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2. Find  $X$  if  $Y = [3214]$  and  $2X + Y = [10 - 32]$ .

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3. If  $A = \begin{bmatrix} 1 & -2 & 3 \\ -4 & 2 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 2 & 3 \\ 4 & 5 \\ 2 & 1 \end{bmatrix}$ , find  $AB$  and  $BA$  and show that  $AB \neq BA$

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4. If  $A = |122212221|$ , verify that  $A^2 - 4A - 5I = 0$

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5. If  $A = [10 \ -17]$ , find  $k$  such that  $A^2 - 8A + kI = O$ .

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6. If  $A = f(x) = \begin{bmatrix} \cos x & \sin x & 0 \\ -\sin x & \cos x & 0 \\ 0 & 0 & 1 \end{bmatrix}$ , then the value of  $A^{-1} =$  (A)  $f(x)$  (B)  $-f(x)$  (C)  $f(-x)$  (D)  $-f(-x)$

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7. If  $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$  then  $\lim_{n \rightarrow \infty} \frac{A^n}{n}$  is (where  $\theta \in R$ ) (A) an identity matrix (B) a zero matrix (C)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & 1 \\ -1 & -0 \end{bmatrix}$

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8. If  $A = \begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$  is a matrix of order 3 then the value of the matrix  $(I + A) - 2A^2(I - A)$ , where  $I$  is a unity matrix is equal to (A)

$$\begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \quad \text{(B)} \quad \begin{bmatrix} 1 & -1 & -1 \\ 0 & 1 & -1 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{(C)} \quad \begin{bmatrix} 1 & 1 & -1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{(D)} \quad \begin{bmatrix} 0 & 0 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

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9. If  $A$  and  $B$  are square matrices of the same order such that  $A^2 = A$ ,  $B^2 = B$ ,  $AB = BA = 0$  then (A)  $AB^2 = 0$  (B)  $(A + B)^2 = A + B$  (C)  $(A - B)^2 = A + B$  (D) none of these

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10. Let  $f(x) = \begin{bmatrix} \cos x & -\sin x & 0 \\ \sin x & \cos x & 0 \\ 0 & 0 & 1 \end{bmatrix}$ , then (A)  $(f(x))^2 = -I$  (B)  $f(x+y) = f(x), f(y)$  (C)  $f(x)^{-1} = f(-x)$  (D)  $f(x)^{-1} = f(x)$

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11. If  $D_1$  and  $D_2$  are diagonal matrices of order  $3 \times 3$  then (A)  $D_1^n$  is a diagonal matrix (B)  $D_1 D_2 = D_2 D_1$  (C)  $D_1^2 + D_2^2$  is diagonal matrix (D)  $D_1 D_2$  is a diagonal matrix

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12. For a matrix  $A$  of order  $3 \times 3$  where
- $$A = \begin{bmatrix} 1 & 4 & 5 \\ k & 8 & 8k-6 \\ 1+k^2 & 8k+4 & 2k+21 \end{bmatrix}$$
- (A) rank of  $A = 2$  or  $k = -1$  (B) rank of  $A = 1$  or  $k = -1$  (C) rank of  $A = 2$  for  $k = 2$  (D) rank of  $A = 1$  or  $k = 2$

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13. Let A and B be two matrices of the same order  $3 \times 3$  such that

$$A = \begin{bmatrix} -5 & 1 & 3 \\ 7 & 1 & -5 \\ 1 & -1 & 1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 1 & 2 \\ 3 & 2 & 1 \\ 2 & 1 & 3 \end{bmatrix} \begin{matrix} x + y + 2z = 1, \\ 3x + 2y + z = 2 \end{matrix}$$

be a system of equations in  $x, y, z$ . The value of  $AB$  and

hence solve the system of equation

$$(A) \begin{bmatrix} -5 & 1 & 5 \\ 21 & 2 & -5 \\ 2 & -1 & 3 \end{bmatrix} \quad (B) \begin{bmatrix} 4 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 4 \end{bmatrix} \quad (C) \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \quad (D) \begin{bmatrix} 2 & -5 & 1 \\ 1 & 3 & 6 \\ 0 & 0 & -0 \end{bmatrix}$$

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## Exercise

1. Given  $A = \begin{bmatrix} 1 & 2 & -3 \\ 5 & 0 & 2 \\ 1 & -1 & 1 \end{bmatrix}$  and  $b = \begin{bmatrix} 3 & -1 & 2 \\ 4 & 2 & 5 \\ 2 & 0 & 3 \end{bmatrix}$ , find the matrix C

such that  $A + C = B$ .

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2. If  $P(x) = \begin{bmatrix} \cos x & \sin x \\ -\sin x & \cos x \end{bmatrix}$ , then show that  $P(x) \cdot P(y) = P(x + y) = P(y) \cdot P(x)$ .

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3. Find the product of the following two matrices

$$\begin{bmatrix} 0 & c & -b \\ c & 0 & a \\ b & -a & 0 \end{bmatrix} \text{ and } \begin{bmatrix} a^2 & ab & ac \\ ab & b^2 & bc \\ ac & bc & c^2 \end{bmatrix}.$$

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4. If  $f(x) = x^2 - 5x + 6$ . Find  $f(A)$ , if  $A = \begin{bmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{bmatrix}$ .

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5. Let  $A = [0 - \tan(\alpha/2) \tan(\alpha/2) 0]$  and  $I$  be the identity matrix of order 2. Show that  $I + A = (I - A)[\cos \alpha - \sin \alpha \sin \alpha \cos \alpha]$ .

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6. If  $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$ , then prove that  $A^n = \begin{bmatrix} 1+2n & -4n \\ 1-2n & 1-2n \end{bmatrix}$ , where  $n$  is any positive integer.

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7. Let  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  show that  $(aI + bA)^n = a^n I + na^{n-1}bA$ , where  $I$  is the identity matrix of order 2 and  $n \in N$ .

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8. A man buys 8 dozens of mangoes, 10 dozens of apples and 4 dozens of bananas. Mangoes cost Rs. 18 per dozen, apples Rs. 9 per dozen and bananas Rs. 6 per dozen. Represent the quantities bought by a row matrix and the prices by a column matrix and hence obtain the total cost.

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9. Express the following matrix as the sum of a symmetric and skew

symmetric matrix  $\begin{bmatrix} 1 & 2 & 4 \\ 6 & 8 & 1 \\ 3 & 5 & 7 \end{bmatrix}$



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10. Solve the following system of linear equations by matrix method:

$$3x - 2y = 7, 5x + 3y = 1$$



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11. Use matrix method to solve the equations  $5x - 7y = 2$  and

$$7x - 5y = 3$$



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12. Solve the following system of linear equations by matrix method:

$$2x + 3y + 3z = 1, 2x + 2y + 3z = 2, x - 2y + 2z = 3$$



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13. Solve the following system of linear equations by matrix method:

$$x + y + z = 3, 2x - y + z = 2, x - 2y = 3z = 2$$



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14. If  $A$  is an invertible symmetric matrix the  $A^{-1}$  is

A. a diagonal matrix

B. symmetric

C. skew symmetric

D. none of these



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15. If  $A$  is a skew-symmetric matrix and  $n$  is odd positive integer, then  $A^n$  is a skew-symmetric matrix a symmetric matrix a diagonal matrix none of these



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16. Which of the following is not true? (A)  $(A')' = A$  (B)  $(A - I)(A + I) = 0$  such that  $A^2 = I$  (C)  $(AB)^n = A^n B^n$  where  $n \in \mathbb{N}$  and  $AB = BA$  (D)  $(A + B)(A - B) = A^2 - B^2$ ,  $A$  and  $B$  being square matrices of the same type



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17. A square matrix  $A$  is invertible iff  $\det(A)$  is equal to (A) -1 (B) 0 (C) 1 (D) none of these



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18. If A, B and C be the three square matrices such that  $A = B + C$  then  $\det A$  is necessarily equal to (A)  $\det B$  (B)  $\det C$  (C)  $\det B + \det C$  (D) none of these



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19. A square matrix A is called idempotent if (A)  $A^2 = 0$  (B)  $A^2 = I$  (C)  $A^2 = A$  (D)  $2A = I$



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20. The value of  $\det \begin{vmatrix} a & 0 & 0 & 0 \\ 2 & b & 0 & 0 \\ 4 & 6 & c & 0 \\ 6 & 8 & 10 & d \end{vmatrix}$  is (A) 0 (B)  $a+b+c+d$  (C)  $abcd$  (D) none of these



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21. If A and B are any two square matrices of the same order then

(A)  $(AB)^T = A^T B^T$

(B)  $(AB)^T = B^T A^T$

(C)  $Adj(AB) = adj(A)adj(B)$

(D)  $AB = 0 \rightarrow A = 0 \text{ or } B = 0$



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22. A square matrix A is called singular if  $\det A$  is (A) negative (B) zero

(C) positive (D) non-zero



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23. Let A be any  $m \times n$  matrix then  $A^2$  can be found only when (A)  $m < n$

(B)  $m = n$  (C)  $m > n$  (D) none of these



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24. The matrix of the transformation reflection in the line  $x + y = 0$  is (A)

$\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$



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25. Rank of a non zero matrix is always (A) 0 (B) 1 (C)  $> 1$  (D)  $> 0$



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26. The values of  $x$  for which the matrix  $\begin{bmatrix} x+a & b & c \\ a & x+b & c \\ a & b & x+c \end{bmatrix}$  is non-singular are (A)  $R - \{0\}$  (B)  $R - \{-(a+b+c)\}$  (C)  $R - \{0, -(a+b+c)\}$  (D) none of these



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27. If  $A = \begin{bmatrix} 1 & 1 & 2 \\ 5 & 2 & 6 \\ -2 & -1 & -3 \end{bmatrix}$  then A is (A) nilpotent (B) idempotent (C) symmetric (D) none of these



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28. If  $A = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$  then (A)  $A^2 = I$  (B)  $A^2 = 0$  (C)  $A^3 = 0$  (D)

none of these



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29. If A and B are square matrices of order 3 then (A)  $AB = 0 \rightarrow |A| = 0$  or  $|B| = 0$  (B)  $AB = 0 \rightarrow |A| = 0$  and  $|B| = 0$  (C)  $Adj(AB) = AdjAAdjB$  (D)  $(A + B)^{-1} = A^{-1} + B^{-1}$



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30. If A a non singular matrix an  $A^T$  denotes the transpose of A then (A)

$|AA^T| \neq |A^2|$  (B)  $|A^T A| \neq |A^T|^2$  (C)  $|A| + |A^T| \neq 0$  (D)  $|A| \neq |A^T|$



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31. If A and B are square matrices of the same order then

$(A + B)^2 = A^2 + 2AB + B^2$  implies (A)  $AB = 0$  (B)  $AB + BA = 0$  (C)

$AB = BA$  (D) none of these



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32. If  $A = \begin{bmatrix} 0 & 2 & -3 \\ -2 & 0 & -1 \\ 3 & 1 & 0 \end{bmatrix}$  then A is (A) diagonal matrix (B) symmetric

matix (C) skew symmetric matrix (D) none of these



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33. If  $A = \begin{bmatrix} 2 & -4 \\ 1 & -1 \end{bmatrix}$  the value of  $A^n$  is (A)  $\begin{bmatrix} 3^n & (-4)^n \\ 1 & (-1)^n \end{bmatrix}$  (B)  $\begin{bmatrix} 3n & -4n \\ n & n \end{bmatrix}$  (C)  $\begin{bmatrix} 2+n & 5-n \\ n & -n \end{bmatrix}$  (D) none of these



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34. For a non singular matrix A of order n the rank of A is (A) less than n (B) equal to n (C) greater than n (D) none of these



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35. Inverse of diagonal matrix is (A) a diagonal matrix (B) symmetric (C) skew symmetric (D) none of these



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36. IF  $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  then for all natural numbers n  $A^n$  is equal to (A)  $\begin{bmatrix} 1 & 0 \\ 1 & n \end{bmatrix}$  (B)  $\begin{bmatrix} n & 0 \\ 1 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 0 \\ n & 1 \end{bmatrix}$  (D) none of these



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37. Prove that the product of the matrices  $\begin{bmatrix} \cos^2 \alpha & \cos \alpha \sin \alpha \\ \cos \alpha \sin \alpha & \sin^2 \alpha \end{bmatrix}$  and  $\begin{bmatrix} \cos^2 \beta & \cos \beta \sin \beta \\ \cos \beta \sin \beta & \sin^2 \beta \end{bmatrix}$  is the null matrix when  $\alpha$  and  $\beta$  differ by an odd multiple of  $\frac{\pi}{2}$ .

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38. For an invertible square matrix of order 3 with real entries  $A^{-1} = A^2$  then  $\det A =$  (A)  $\frac{1}{3}$  (B) 3 (C) 0 (D) 1

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39. If  $\begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix} A \begin{bmatrix} -3 & 2 \\ 5 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  then  $a$  is equal to (A)  $\begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$

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40. The roots of the equation  $\det \begin{bmatrix} 1-x & 2 & 3 \\ 0 & 2-x & 0 \\ 0 & 2 & 3-x \end{bmatrix} = 0$  are (A) 1 and 2 (B) 1 and 3 (C) 2 and 3 (D) 1, 2, and 3



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41. If  $A = \begin{bmatrix} 1 & 2 & 0 \\ -1 & 1 & 2 \\ 2 & -1 & 1 \end{bmatrix}$  then  $\det(\text{Adj}(\text{Adj}A)) =$  (A) 13 (B)  $13^2$  (C)  $13^4$  (D) none of these



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42. The transformation due of reflection of  $(x, y)$  through the origin is described by the matrix (A)  $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & -1 & 0 \\ 0 & & -1 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$



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43. If  $A = [a_{ij}]_{m \times n}$  and  $B = [b_{ij}]_{n \times p}$  then  $(AB)'$  is equal to (A)  $BA'$   
(B)  $B'A$  (C)  $A'B'$  (D)  $B'A'$



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44. If  $A$  is a skew-symmetric matrix and  $n$  is odd positive integer, then  $A^n$  is a skew-symmetric matrix a symmetric matrix a diagonal matrix none of these



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45. If  $A$  is a skew-symmetric matrix and  $n$  is odd positive integer, then  $A^n$  is a skew-symmetric matrix a symmetric matrix a diagonal matrix none of these



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46. If A and B are symmetric of the same order, then (A) AB is a symmetric matrix (B) A-B is skew symmetric (C) AB-BA is symmetric matrix (D) AB+BA is a symmetric matrix



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47. If  $A = [x, y, z]$ ,  $B = \begin{bmatrix} a & h & g \\ h & b & f \\ g & f & c \end{bmatrix}$  and  $C = [x, y, z]^T$ , then ABC is

(A) not defined (B) a  $1 \times 1$  matrix (C) a  $3 \times 3$  matrix (D) none of these



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48. If for a square matrix A,  $A^2 = A$  then  $|A|$  is equal to (A)  $-3$  or  $3$  (B)  $-2$  or  $2$  (C)  $0$  or  $1$  (D) none of these



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49. For a matrix A of rank  $r$  (A)  $\text{rank}(A') < r$  (B)  $\text{rank}(A') = r$ . (C)  $\text{rank}(A') > r$  (D) none of these



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50. If  $A = \begin{bmatrix} 1 & 3 & 9 & 27 \\ 3 & 9 & 27 & 1 \\ 9 & 27 & 1 & 3 \\ 27 & 1 & 3 & 9 \end{bmatrix}$  then  $\det A =$  (A) 0 (B)  $-(80^3) \cdot 27$  (C)  $(80^3) \cdot 27$   
(D)  $81^3$



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51. If  $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$  then matrix A is (A) scalar (B) involuntary (C) idempotent (D) nilpotent



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52. If  $A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & \cos x & \sin x \\ 0 & -\sin x & \cos x \end{bmatrix}$  then  $(Adj A)^{-1} =$  (A)  $\frac{1}{2}A$  (B)  $A$  (C)  $2A$   
(D)  $4A$



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53. Each diagonal element of a skew symmetric matrix is (A) zero (B) negative (C) positive (D) non real



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54. If  $A$  is a non singular square matrix then  $|adj. A|$  is equal to (A)  $|A|$   
(B)  $|A|^{n-2}$  (C)  $|A|^{n-1}$  (D)  $|A|^n$



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55. If  $A = \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix} \begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}^{-1} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$  then (A)

$a = b = -1$  (B)  $a = \sin 2\theta, b = \cos 2\theta$  (C)  $a = \cos 2\theta, b = \sin 2\theta$  (D)

none of these



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56. If  $A = \begin{bmatrix} \cos x & \sin x \\ -\sin x & \cos x \end{bmatrix}$  and  $A \cdot (\text{adj} A) = k \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  then the value of  $k$  is



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57. If  $I_n$  is the identity matrix of order  $n$  then  $(I_n)^{-1}$  (A) does not exist (B)  $= 0$  (C)  $= I_n$  (D)  $= nI_n$



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**58.** The number of all possible matrices of order  $3 \times 3$  with each entry 0 or 1 is: (a) 27 (b) 18 (c) 81 (d) 512



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**59.** The number of all the possible matrices of order  $2 \times 2$  with each entry 0, 1 or 2 is (A) 12 (B) 64 (C) 81 (D) none of these



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**60.** If  $A$  is an invertible matrix then  $\det(A^{-1})$  is equal to (A) 1 (B)  $\frac{1}{|A|}$  (C)  $|A|$  (D) none of these



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**61.** If  $A$  and  $B$  are two invertible matrices of same order, the  $(AB)^{-1}$  is (A)  $AB$  (B)  $BA$  (C)  $B^{-1}A^{-1}$  (D) does not exist



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62. If  $A$  and  $B$  be  $3 \times 3$  matrices the  $AB=0$  implies (A)  $A = 0$  or  $B = 0$  (B)  $A = 0$  and  $B = 0$  (C)  $|A| = 0$  or  $|B| = 0$  (D)  $|A| = 0$  and  $|B| = 0$

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63. If  $A$  and  $B$  are two matrices such that  $AB = B$  and  $BA = A$  then  $A^2 + B^2 =$  (A)  $2AB$  (B)  $2BA$  (C)  $A+B$  (D)  $AB$

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64. If  $A$  is a square matrix which of the following is not a symmetric matrix? (A)  $A - A'$  (B)  $A + A'$  (C)  $AA'$  (D)  $A + B$

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65. If  $A$  is invertible then which of the following is not true? (A)  $A^{-1} = |A|^{-1}$  (B)  $(A')^{-1} = (A^{-1})'$  (C)  $(A^2)^{-1} = (A^{-1})^2$  (D) none of these



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66. If  $A = [a_{ij}]_{m \times n}$  is a matrix of rank  $r$  then (A)  $r < \min \{m, n\}$  (B)  $r \leq \min \{m, n\}$  (C)  $r = \min \{m, n\}$  (D) none of these



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67. If  $A$  and  $B$  are symmetric matrices, then  $ABA$  is



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68.  $\cos \theta \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} + \sin \theta \begin{bmatrix} \sin \theta & -\cos \theta \\ \cos \theta & \sin \theta \end{bmatrix}$  is equal to (A)  $\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$   
(B)  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

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69. Consider the set  $A$  of all determinants of order 3 with entries 0 or 1 only. Let  $B$  be the subset of  $A$  consisting of all determinants with value 1. Let  $C$  be the subset of the set of all determinants with value  $-1$ . Then

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70. If  $A$  is an  $m \times n$  matrix such that  $AB$  and  $BA$  are both defined, then  $B$  is (A)  $m \times n$  matrix (B)  $n \times n$  matrix (C)  $m \times m$  matrix (D)  $n \times m$  matrix

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71. If  $A$  is a skew-symmetric matrix of odd order  $n$ , then  $|A| = 0$

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72. If  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  then  $A^4$  is (A)  $\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$



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73. If  $A = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{bmatrix}$  and  $a, b, c$  are non zero real numbers, then  $A^{-1}$  is

(A)  $\frac{1}{abc} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (B)  $\frac{1}{abc} \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & c & 0 \end{bmatrix}$  (C)  $\frac{1}{abc} \begin{bmatrix} a^{-1} & 0 & 0 \\ 0 & b^{-1} & 0 \\ 0 & c^{-1} & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} a^{-1} & 0 & 0 \\ 0 & b^{-1} & 0 \\ 0 & c^{-1} & 1 \end{bmatrix}$



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74. The transformation orthogonal projection on X-axis is given by the matrix (A)  $\begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$  (B)  $\begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$



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75. If  $A = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$  and  $n \in \mathbb{N}$  then  $A^n$  is equal to (A)  $2^{n-1}A$  (B)  $2^n A$  (C)  $nA$  (D) none of these



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76. If  $A = \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & 1 \end{bmatrix}$  then  $A^{50}$  is (A)  $\begin{bmatrix} 1 & 25 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 0 \\ 25 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 0 \\ 0 & 50 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 50 & 1 \end{bmatrix}$



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77. If  $\begin{bmatrix} a & b \\ c & -a \end{bmatrix}$  is a square root of the  $2 \times 2$  identity matrix then  $a, b, c$  satisfy the relation (A)  $1 - a^2 - bc = 0$  (B)  $1 - a^2 + bc = 0$  (C)  $1 + a^2 - bc = 0$  (D)  $1 + a^2 + bc = 0$



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78. Find the following system of equations is consistent,  $(a + 1)^3x + (a + 2)^3y = (a + 3)^3$   $(a + 1)x + (a + 2)y = a + 3$   $\neq 1$ , then find the value of  $a$ .



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79. Let  $A = [a_{ij}]_{n \times n}$  be a square matrix and let  $c_{ij}$  be cofactor of  $a_{ij}$  in  $A$ . If  $C = [c_{ij}]$ , then



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80. If  $F(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $G(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$ , then  $F(\alpha)G(\beta)$  is equal to (A)  $F(-\alpha)G(-\beta)$  (B)  $G(-\beta)F(-\alpha)$  (C)  $F(\alpha^{-1})G(\beta^{-1})$  (D)  $G(\beta^{-1})F(\alpha^{-1})$



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81. If  $A$  is a square matrix of order  $n \times n$  and  $\lambda$  is a scalar then  $|\lambda A|$  is (A)  $\lambda|A|$  (B)  $\lambda^n|A|$  (C)  $|\lambda||A|$  (D) none of these



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82. If neither  $\alpha$  nor  $\beta$  is a multiple of  $\frac{\pi}{2}$  and the product  $AB$  of matrices  $A = \begin{bmatrix} \cos^2 \alpha & \cos \alpha \sin \alpha \\ \cos \alpha \sin \alpha & \sin^2 \alpha \end{bmatrix}$  and  $B = \begin{bmatrix} \cos^2 \beta & \cos \beta \sin \beta \\ \cos \beta \sin \beta & \sin^2 \beta \end{bmatrix}$  is a null matrix then  $\alpha - \beta$  is (A) 0 (B) an odd multiple of  $\frac{\pi}{2}$  (C) a multiple of  $\pi$  (D) none of these



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83. If  $A$  and  $B$  are two matrices such that  $AB=A$ ,  $BA=B$ , then  $A^{25}$  is equal to (A)  $A^{-1}$  (B)  $A$  (C)  $B^{-1}$  (D)  $B$



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84. If  $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$  then  $\lim_{n \rightarrow \infty} \frac{1}{n} A^n$  is (A) an identity matrix (B)  $\begin{bmatrix} 0 & 10 \\ -1 & 0 \end{bmatrix}$  (C) a null matrix (D) none of these



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85. If  $A = \begin{bmatrix} a & b & c \\ x & y & z \\ p & q & r \end{bmatrix}$  and  $B = \begin{bmatrix} q & -b & y \\ -p & a & -x \\ r & -c & z \end{bmatrix}$  then (A)  $|A| = |B|$  (B)  $|A| = -|B|$  (C)  $|A| = 2|B|$  (D) none of these



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86. The number of different matrices which can be formed using 12 different real numbers is (A)  $6(12)!$  (B)  $3(12)!$  (C)  $2(10)!$  (D)  $4(10)!$



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87. Which of the following is a non singular matrix? (A)  $\begin{bmatrix} 1 & a & b+c \\ 1 & b & c+a \\ 1 & c & a+b \end{bmatrix}$

(B)  $\begin{bmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{bmatrix}$  where  $\omega$  is non real and  $\omega^2 = 1$  (C)

$\begin{bmatrix} 1^2 & 2^2 & 3^2 \\ 2^2 & 3^2 & 4^2 \\ 3^2 & 4^2 & 5^2 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & 2 & -3 \\ -2 & 0 & 5 \\ 3 & -5 & 0 \end{bmatrix}$



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88. If A and B are two  $n \times n$  matrices such that  $|A| = |B|$  then (A)  $A' = A$  (B)  $A = B$  (C)  $A' = B'$  (D) none of these



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89. If  $A = [a_{ij}]$  is a scalar matrix, then trace of A is



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90. If for a matrix  $A$ ,  $A^2 + I = 0$ , where  $I$  is an identity matrix then  $A$  equals (A)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 2 \\ -1 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} -i & 0 \\ 0 & -i \end{bmatrix}$



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91. The system of linear equations  $ax + by = 0$ ,  $cx + dy = 0$  has a non trivial solution if (A)  $ad + bc = 0$  (B)  $ad - bc = 0$  (C)  $ad - bc, 0$  (D)  $ad - bc, 0$



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92. The equation  $2x + y + z = 0$ ,  $x + y + z = 1$ ,  $4x + 3y + 3z = 2$  have (A) no solution (B) only one solution (C) infinitely many solutions (D) none of these



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93. The value of  $a$  for which the system of linear equations  $ax + y + z = 0, ay + z = 0, x + y + z = 0$  possesses non-trivial solution is



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94. The system of equations  $3x + y - z = 0, 5x + 2y - 3z = 0, 15x + 6y - 9z = 5$  has (A) no solution (B) a unique solution (C) two distinct solutions (D) infinitely many solutions



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95.  $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ , then adjoint of  $A$  is equal to (A)  $\begin{bmatrix} 1 & -2 \\ -2 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 2 & 1 \\ 2 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & -2 \\ -2 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} -1 & 2 \\ 2 & -1 \end{bmatrix}$



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96. If  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ ,  $J = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$ , then  $B =$
- (A)  $I \cos \theta + J \sin \theta$  (B)  $I \cos \theta - J \sin \theta$  (C)  $I \sin \theta + J \cos \theta$  (D)  $-I \cos \theta + J \sin \theta$



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97. If  $A = [(1, 0, 0), (0, 1, 0), (1, b, -10)]$  then  $A^2$  is equal to (A) unit matrix (B) null matrix (C)  $A$  (D)  $-A$



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98. If  $A$  and  $B$  are two matrices such that  $A + B$  and  $AB$  are both defined then (A)  $A$  and  $B$  can be any matrices (B)  $A, B$  are square matrices not necessarily of same order (C)  $A, B$  are square matrices of same order (D) number of columns of  $A =$  number of rows of  $B$



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99. If A and B are symmetric matrices of order  $n$  ( $A \neq B$ ) then (A)  $A+B$  is skew symmetric (B)  $A+B$  is symmetric (C)  $A+B$  is a diagonal matrix (D)  $A+B$  is a zero matrix



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100. The number of solution of  $2x + y = 4$ ,  $x - 2y = 2$ ,  $3x + 5y = 6$  is (A) zero (B) one (C) two (D) infinitely many



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101. If  $A = \begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} -5 & 4 & 0 \\ 0 & 2 & -1 \\ 1 & -3 & 2 \end{bmatrix}$  then (A)  $AB = \begin{bmatrix} -2 \\ -1 \\ 4 \end{bmatrix}$   
 (B)  $AB = \begin{bmatrix} -2, & -1, 4 \end{bmatrix}$  (C)  $AB = \begin{bmatrix} 4, & -1, 2 \end{bmatrix}$  (D)

$$AB = \begin{bmatrix} -5 & 4 & 0 \\ 0 & 4 & -2 \\ 3 & -9 & 6 \end{bmatrix}$$



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**102.** If  $A$  and  $B$  are any  $2 \times 2$  matrices then  $\det(A + B) = 0$  implies (A)  $\det A + \det B = 0$  (B)  $\det A = 0$  or  $\det B = 0$  (C)  $AB = 0 \rightarrow |A| = 0$  and  $|B| = 0$  (D)  $AB = 0 \rightarrow A = 0$  or  $B = 0$



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**103.** From the matrix equation  $AB = AC$  we can conclude that  $B = C$  provide (A)  $A$  is singular (B)  $A$  is non singular (C)  $A$  is symmetric (D)  $A$  is square



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**104.** If each element of a  $3 \times 3$  matrix  $A$  is multiplied by 3 then the determinant of the newly formed matrix is (A)  $3 \det A$  (B)  $9 \det A$  (C)  $(\det A)^3$  (D)  $27 \det A$



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**105.** If A and B are two non-zero square matrices of the same order, such that  $AB=O$ , then (a) at least one of A and B is singular (b) both A and B are singular (c) both A and B are non-singular (d) none of these



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**106.** If A and B are two matrices such that  $AB = B$  and  $BA = A$  then  $A^2 + B^2 =$  (A)  $2AB$  (B)  $2BA$  (C)  $A+B$  (D)  $AB$



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**107.** The system of linear equations

$$x + y + z = 2$$

$$2x + y - z = 3$$

$3x + 2y + kz = 4$  has a unique solution if



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108. If  $A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  then  $A^4 =$  (A)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 1 \\ 0 & 10 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$



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109. The order of  $[x, y, z], \begin{bmatrix} a & h & g \\ h & b & f \\ g & f & c \end{bmatrix}, \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  is

(A)  $3 \times 1$

(B)  $1 \times 1$

(C)  $1 \times 3$

(D)  $3 \times 3$



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110.  $\begin{bmatrix} 1 & 3 \\ 3 & 10 \end{bmatrix}^{-1} =$  (A)  $\begin{bmatrix} 10 & 3 \\ 3 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 10 & -3 \\ -3 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 3 \\ 3 & 10 \end{bmatrix}$  (D)  $\begin{bmatrix} -1 & -3 \\ -3 & -10 \end{bmatrix}$



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111. If  $A + B = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  and  $A - 2B = \begin{bmatrix} -1 & 1 \\ 0 & -1 \end{bmatrix}$  then  $A =$  (A)  $\frac{1}{3} \begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}$  (B)  $\frac{1}{3} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}$  (D) none of these



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112. If  $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$  then  $A^2 =$  (A)  $\begin{bmatrix} 8 & -5 \\ -5 & 3 \end{bmatrix}$  (B)  $\begin{bmatrix} 8 & -5 \\ 5 & 3 \end{bmatrix}$  (C)  $\begin{bmatrix} 8 & -5 \\ -5 & -3 \end{bmatrix}$  (D)  $\begin{bmatrix} 8 & 5 \\ -5 & 3 \end{bmatrix}$



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113. The inverse of the matrix  $\begin{bmatrix} 2 & 3 \\ -4 & 7 \end{bmatrix}$  is (A)  $\begin{bmatrix} -2 & -3 \\ 4 & -7 \end{bmatrix}$  (B)  $\frac{1}{26} \begin{bmatrix} 7 & -3 \\ 4 & 2 \end{bmatrix}$  (C)  $\begin{bmatrix} 7 & 4 \\ -3 & 2 \end{bmatrix}$  (D)  $\begin{bmatrix} 7 & -3 \\ 4 & 2 \end{bmatrix}$



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114. the order of the single matrix obtained from

$$\begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix} \left\{ \begin{bmatrix} -1 & 0 & 2 \\ 2 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 0 & 1 & 23 \\ 1 & 0 & 21 \end{bmatrix} \right\} \text{ is (A) } 2 \times 3 \text{ (B) } 2 \times 2 \text{ (C) } 3 \times 2 \text{ (D) } 3 \times 3$$



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115. The inverse of the matrix  $\begin{bmatrix} 1 & 0 & 0 \\ a & 1 & 0 \\ b & c & 1 \end{bmatrix}$  is (A)  $\begin{bmatrix} 1 & 0 & 0 \\ -a & 1 & 0 \\ b & c & 1 \end{bmatrix}$  (B)

$\begin{bmatrix} 1 & 0 & 0 \\ -a & 1 & 0 \\ ac & b & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & -a & ac-b \\ -0 & 1 & -c \\ 0 & 0 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 & 0 \\ -a & 1 & 0 \\ ac-b & -c & 1 \end{bmatrix}$



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116. If the matrix A is both symmetric and skew symmetric, then (A) A is a diagonal matrix (B) A is a zero matrix (C) A is a square matrix (D) None of these



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117. If  $A$  is a non singular matrix of order 3 then  $|adj(adjA)|$  equals (A)  $|A|^4$  (B)  $|A|^6$  (C)  $|A|^3$  (D) none of these



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118. If  $A = \begin{bmatrix} 4 & -5 & -2 \\ 5 & -4 & 2 \\ 2 & 2 & 8 \end{bmatrix}$ , then  $A(adjA)$  equals (A)  $\begin{bmatrix} 36 & -36 & 18 \\ 36 & 36 & -18 \\ 18 & -18 & 9 \end{bmatrix}$  (B)  $\begin{bmatrix} -36 & 36 & 18 \\ -36 & 36 & -18 \\ -18 & 18 & 9 \end{bmatrix}$  (C)  $\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & -0 & 0 \end{bmatrix}$  (D) none of these



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119. If  $A = \begin{bmatrix} 1 & 2 \\ 4 & 1 \end{bmatrix}$ , then  $A^{-1} =$  (A)  $\begin{bmatrix} -1 & -2 \\ 4 & 1 \end{bmatrix}$  (B)  $\frac{1}{7} \begin{bmatrix} 1 & 2 \\ -4 & -1 \end{bmatrix}$  (C)  $\frac{1}{7} \begin{bmatrix} -1 & -2 \\ 4 & 1 \end{bmatrix}$  (D)  $\frac{1}{9} \begin{bmatrix} 1 & 2 \\ 4 & 1 \end{bmatrix}$



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120. Value of  $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$  is (A)  $(a-b)(b-c)(c-a)$  (B)

$(a^2 - b^2)(b^2 - c^2)(c^2 - a^2)$  (C)  $(a-b+c)(b-c+a)(c+a-b)$  (D)

none of these



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121.  $\begin{bmatrix} 7 & 1 & 2 \\ 9 & 2 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 3 \\ 5 \end{bmatrix} + 2 \begin{bmatrix} 4 \\ 2 \end{bmatrix} =$  (A)  $\begin{bmatrix} 43 \\ 44 \end{bmatrix}$  (B)  $\begin{bmatrix} 43 \\ 45 \end{bmatrix}$  (C)  $\begin{bmatrix} 45 \\ 44 \end{bmatrix}$  (D) none

of these



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122. Multiple inverse of the matrix  $\begin{bmatrix} 2 & 1 \\ 7 & 4 \end{bmatrix}$  is (A)  $\begin{bmatrix} 4 & -1 \\ 7 & -2 \end{bmatrix}$  (B)

$\begin{bmatrix} -4 & -1 \\ 7 & -2 \end{bmatrix}$  (C)  $\begin{bmatrix} 4 & -1 \\ 7 & 2 \end{bmatrix}$  (D)  $\begin{bmatrix} 4 & -1 \\ -7 & -2 \end{bmatrix}$



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123. If  $f(x) = x^2 + 4x - 5$  and  $A = \begin{bmatrix} 1 & 2 \\ 4 & -3 \end{bmatrix}$  then  $f(A) =$  (A)  $\begin{bmatrix} 0 & -4 \\ 8 & 8 \end{bmatrix}$  (B)  $\begin{bmatrix} 0 & -4 \\ 8 & 8 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 8 & 4 \\ 8 & 0 \end{bmatrix}$



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124. The inverse of the matrix  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$  is (A)  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$  (B)  $\begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} \frac{1}{2} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{2} \end{bmatrix}$



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125. If  $A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & a & 1 \end{bmatrix}$   $A^{-1} = \begin{bmatrix} \frac{1}{2} & \frac{-1}{2} & \frac{1}{2} \\ -4 & 3 & c \\ \frac{5}{2} & \frac{-3}{2} & \frac{1}{2} \end{bmatrix}$ , then



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126. If  $A = \begin{bmatrix} 0 & -1 & 2 \\ 1 & 0 & 3 \\ -2 & -3 & 0 \end{bmatrix}$ , then  $A + 2A^t$  equals (A)  $A$  (B)  $-A^t$  (C)  $A^t$  (D)  $2A^2$



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127. The adjoint of the matrix  $\begin{bmatrix} 2 & 5 \\ 3 & 1 \end{bmatrix}$  is (A)  $\begin{bmatrix} 2 & 5 \\ 3 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & -5 \\ -3 & 2 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & -3 \\ -5 & 2 \end{bmatrix}$  (D)  $\begin{bmatrix} -1 & 3 \\ 5 & -2 \end{bmatrix}$



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128. If  $A$  is a square matrix then  $A - A'$  is a

A. diagonal matrix

B. skew symmetric matrix

C. symmetric matrix

D. none of these

**Answer: A**



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**129.** If  $A = \begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$  then  $9A^{-1}$  is equal to (A)  $A'$  (B)  $2A$  (C)  $\frac{1}{2}A$  (D)  $A$



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**130.** The matrix  $X$  in the equation  $AX = B$ , such that  $A = \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$  is given by (A)  $\begin{bmatrix} 1 & 0 \\ -3 & 1 \end{bmatrix}$  (B)  $[(1, -4), (0, 1)]$  (C)  $\begin{bmatrix} 1 & -3 \\ 0 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & -1 \\ -3 & 1 \end{bmatrix}$



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**131.** If  $\begin{bmatrix} 1 & a & 2 \\ 1 & 2 & 5 \\ 2 & 1 & 1 \end{bmatrix}$  is non invertible then  $a =$  (A) 2 (B) 1 (C) 0 (D) -1



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132. If  $A = \begin{bmatrix} -a^2 & ab & ac \\ ab & -b^2 & bc \\ ac & bc & -c^2 \end{bmatrix}$  then  $\det A$  is equal to (A)  $4abc$  (B)  $4a^2b^2c^2$  (C)  $-4abc$  (D)  $-4a^2b^2c^2$



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133. If  $A = \begin{bmatrix} 1 & \tan\left(\frac{\theta}{2}\right) \\ -\tan\left(\frac{\theta}{2}\right) & 1 \end{bmatrix}$  and  $AB = I$ , then  $B =$  (A)  $\left\{ \cos^2\left(\frac{\theta}{2}\right) \right\} A$  (B)  $\left\{ \cos^2\left(\frac{\theta}{2}\right) \right\} A'$  (C)  $\left\{ \cos^2\left(\frac{\theta}{2}\right) \right\} I$  (D) none of these



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134. If  $A = \begin{bmatrix} -1 & 0 & 0 & 1 \\ -1 & 1 & 0 & 2 \\ -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$ , then  $A(adjA)$  equals (A)  $\begin{bmatrix} 1 & 5 & 0 & 2 \\ 5 & 1 & 7 & 1 \\ -1 & 0 & 1 & 0 \\ 0 & 0 & 5 & 0 \end{bmatrix}$

(B) zero matrix (C) a scalar quantity (D) identity matrix



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135. If  $A = \begin{bmatrix} 0 & 5 \\ 0 & 0 \end{bmatrix}$  and  $f(x) = 1 + x + x^2 + \dots + x^{16}$ , then  $f(A) =$  (A)  $\begin{bmatrix} 1 & 5 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 5 \\ 0 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 5 \\ 0 & 0 \end{bmatrix}$  (D)  $\begin{bmatrix} 0 & 5 \\ 1 & 1 \end{bmatrix}$



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136. If  $A$  is a non singular square matrix of order 3 then  $|adj(A^3)|$  equals (A)  $|A|^8$  (B)  $|A|^6$  (C)  $|A|^9$  (D)  $|A|^{12}$



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137. If  $A$  is a square matrix of order  $n \times n$  and  $k$  is a scalar, then  $adj(kA)$  is equal to (1)  $kadjA$  (2)  $k^n adjA$  (3)  $k^{n-1} adjA$  (4)  $k^{n+1} adjA$



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138. If  $A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$  then show that  $A^{-1} = A^1$ .



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139. If  $A = [(1, 0), (2, 0)]$  and  $B = \begin{bmatrix} 0 & 0 \\ 1 & 12 \end{bmatrix}$  then= (A)  $AB = 0, BA = 0$  (B)  $AB = 0, BA \neq 0$  (C)  $AB \neq 0, BA = 0$  (D)  $AB \neq 0, BA \neq 0$ )



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140. The value of  $a$  for which system of equation ,  
 $a^3x + (a + 1)^3y + (a + 2)^3z = 0, ax + (a + 1)y + (a + 2)z = 0, x + y +$   
 has a non-zero solution is:



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141. If  $I_3$  is the identity matrix of order 3 then  $I_3^{-1}$  is (A) 0 (B)  $3I_3$  (C)  $I_3$  (D) does not exist



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**142.** If the matrix  $AB=0$  then (A)  $A = 0$  or  $B = 0$  (B)  $A = 0$  and  $B = 0$   
(C) It is not necessary that either  $A=0$  or  $B=0$  (D)  $A \neq 0, B \neq 0$



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**143.** The matrix  $\begin{bmatrix} 0 & 5 & -7 & -5 \\ 0 & 1 & 1 & 7 \\ -5 & 0 & 1 & 1 \\ 7 & -1 & 1 & 0 \end{bmatrix}$  is (a) a skew-symmetric matrix (b) a symmetric matrix (c) a diagonal matrix (d) an upper triangular matrix



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**144.** A square matrix  $A = [a_{ij}]$  in which  $a_{ij} = 0$  for  $i \neq j$  and  $[a]_{ij} = k$  (constant) for  $i=j$  is called a (A) unit matrix (B) scalar matrix (C) null matrix  
(D) diagonal matrix



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145. If  $A = \begin{bmatrix} 2 & 2 \\ -3 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$  then  $(B^{-1}A^{-1})^{-1} =$  (A)  $\begin{bmatrix} 2 & -2 \\ 2 & 3 \end{bmatrix}$  (B)  $\begin{bmatrix} 3 & -2 \\ 2 & 3 \end{bmatrix}$  (C)  $\frac{1}{10} \begin{bmatrix} 2 & 2 \\ -2 & 3 \end{bmatrix}$  (D)  $\frac{1}{10} \begin{bmatrix} 3 & -2 \\ -2 & 2 \end{bmatrix}$



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146. If  $A = [023 - 4]$  and  $kA = [03a2b24]$ , then the values of  $k, a, b$ , are respectively (a) -6, -12, -18 (b) -6, 4, 9 (c) -6, -4, -9 (d) -6, 12, 18



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147. If  $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$ , then  $A^n =$  (A)  $\begin{bmatrix} 1 & 2n \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 2 & n \\ 0 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 2n \\ 0 & -1 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & n \\ 0 & 1 \end{bmatrix}$



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**148.** For the matrix  $A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 2 & 1 \\ 2 & 1 & 0 \end{bmatrix}$  which of the following is correct? (A)

$A^3 + 3A^2 - I = 0$  (B)  $A^3 - 3A^2 - I = 0$  (C)  $A^3 + 2A^2 - I = 0$  (D)

$A^3 - A^2 - I = 0$



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**149.** If  $A^2 - A + I = 0$ , then the inverse of A is: (A)  $A + I$  (B)  $A$  (C)

$A - I$  (D)  $I - A$



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**150.** If  $\begin{bmatrix} 2+x & 3 & 4 \\ 1 & -1 & 2 \\ x & 1 & -5 \end{bmatrix}$  is a singular matrix then x is (A)  $\frac{13}{25}$  (B)  $-\frac{25}{13}$

(C)  $\frac{5}{13}$  (D)  $\frac{25}{13}$



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151. If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ a & b & -1 \end{bmatrix}$  then  $A^2$  is equal to (A) null matrix (B) unit matrix (C)  $-A$  (D)  $A$



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152. If  $A = \begin{bmatrix} 1 & 2 \\ 3 & -5 \end{bmatrix}$  then  $A^{-1}$  is

A.  $\begin{bmatrix} -5 & -2 \\ -3 & 1 \end{bmatrix}$

B.  $\begin{bmatrix} \frac{5}{11} & \frac{2}{11} \\ \frac{3}{11} & -\frac{1}{11} \end{bmatrix}$

C.  $\begin{bmatrix} -\frac{5}{11} & -\frac{2}{11} \\ -\frac{3}{11} & -\frac{1}{11} \end{bmatrix}$

D.  $\begin{bmatrix} 5 & 2 \\ 3 & -1 \end{bmatrix}$



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153. If A and B are two square matrices of the same order then  $(A - B)^2$  is (A)  $A^2 - AB - BA + B^2$  (B)  $A^2 - 2AB + B^2$  (C)  $A^2 - 2BA + B^2$  (D)  $A^2 - B^2$

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154. If  $A = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}$  and  $I$  is the unit matrix of order 2, then  $A^2$  is equal to (A)  $4A - 3I$  (B)  $3A - 4I$  (C)  $A - I$  (D)  $A + I$

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155. If  $P = \begin{bmatrix} i & 0 & -i \\ 0 & -i & i \\ -i & i & 0 \end{bmatrix}$  and  $Q = \begin{bmatrix} -i & i \\ 0 & 0 \\ i & -i \end{bmatrix}$  then  $PQ$  is equal to  
(A)  $\begin{bmatrix} -2 & 2 \\ 1 & -1 \\ 1 & -1 \end{bmatrix}$  (B)  $\begin{bmatrix} 2 & -2 \\ -1 & -1 \\ -1 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 2 & 2 \\ -1 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

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156. Let  $R$  be a square matrix of order greater than 1 such that  $R$  is lower triangular. Further suppose that none of the diagonal elements of the square matrix  $R$  vanishes. Then (A)  $R$  must be non singular (B)  $R^{-1}$  does

not exist (C)  $R^{-1}$  is an upper triangular matrix (D)  $R^{-1}$  is a lower triangular matrix



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157. If  $A^{-1} = \begin{bmatrix} 1 & -1 & 0 \\ 0 & -2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$  then (A) A is non-singular (B) A is skew

symmetric (C)  $|A| = 2$  (D)  $Adj A = \begin{bmatrix} \frac{1}{2} & -\frac{1}{2} & 0 \\ 0 & -1 & \frac{1}{2} \\ 0 & 0 & -\frac{1}{2} \end{bmatrix}$



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158. If  $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$  then (A)  $A^{-1} = \frac{1}{5}(A - 4I_3)$  (B)

$A^2 - 4A - 5I_3 = 0$  (C)  $A^2$  is invertible (D)  $A^3$  is non invertible



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**159.** Which of the following is a triangular matrix? (A) a scalar matrix (B) a lower triangular matrix (C) an upper triangular matrix (D) a diagonal matrix



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**160.** If  $A$  and  $B$  are square matrices of the same order such that  $AB=BA$ , then (A)  $(A - B)(A + B) = A^2 - B^2$  (B)  $(A + B)^2 = A^2 + 2AB + B^2$  (C)  $(A + B)^3 = A^3A^2B + 3AB^2 + B^3$  (D)  $(AB)^2 = A^2B^2$



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**161.** The homogeneous system  $AX=0$  of  $n$  linear equation in  $n$  variables has (A) a unique solutions if  $|A| \neq 0$  (B) infinitely many solution if  $|A| = 0$  (C) no solution (D) none of these



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**162.** The homogeneous system  $AX=0$  of  $n$  linear equations in  $n$  variables has

- (A) a unique solution if  $|A| \neq 0$  (B) infinitely many solutions if  $|A| = 0$  (C) no solution (D) none of these



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**163.** Let  $A, B, C$  be  $2 \times 2$  matrices with entries from the set of real numbers.

Define operations  $\cdot$  as follows  $A \cdot B = \frac{1}{2}(AB + BA)$  then (A)

$A \cdot I = A$  (B)  $A \cdot A = A^2$  (C)  $A \cdot B = B \cdot A$  (D)

$A \cdot (B + C) = A \cdot B + A \cdot C$

A.  $A \cdot B = B \cdot A$

B.  $A \cdot A = A^2$

C.  $A \cdot (B + C) = A \cdot B + A \cdot C$

D.  $A \cdot I = A$

**Answer: A, B, C, D**



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164. If  $A = \begin{bmatrix} 0 & \sin \alpha & \sin \alpha \sin \beta \\ -\sin \alpha & 0 & \cos \alpha \cos \beta \\ -\sin \alpha \sin \beta & -\cos \alpha \cos \beta & 0 \end{bmatrix}$  then (A)  $|A|$  is

independent of  $\alpha$  and  $\beta$  (B)  $A^{-1}$  depends only on  $\beta$  (C)  $A^{-1}$  does not exist (D) none of these



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165. Let  $A = \begin{bmatrix} 1 & \sin \theta & 1 \\ -\sin \theta & 1 & \sin \theta \\ -1 & -\sin \theta & 1 \end{bmatrix}$ , where  $0 \leq \theta < 2\pi$  then (A)

$|A| = 0$  (B)  $|A| \in [2, 4]$  (C)  $|A| \in (0, \infty)$  (D)  $|A| \in (2, \infty)$



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166. If  $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  then (A)  $A^{-n} = \begin{bmatrix} 1 & 0 \\ -n & 1 \end{bmatrix}, n \in \mathbb{N}$  (B)

$\lim_{n \rightarrow \infty} \frac{1}{n^2} A^{-n} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$  (C)  $\lim_{n \rightarrow \infty} \frac{1}{n} A^{-n} = \begin{bmatrix} 0 & 0 \\ -1 & 0 \end{bmatrix}$  (D) none of

these



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**167.** If A and B are symmetric matrices of the same order then (A) A-B is skew symmetric (B) A+B is symmetric (C) AB-BA is skew symmetric (D) AB+BA is symmetric



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**168.** If A and B are two matrices such that  $AB=BA$ , then for every  $n \in \mathbb{N}$  (A)  $(AB)^n = A^n B^n$  (B)  $A^n B = B A^n$  (C)  $(A^{2n} - B^{2n}) = (A^n - B^n)(A^n + B^n)$  (D)  $(A + B)^n = {}^n C_0 A^n + {}^n C_1 A^{n-1} B + {}^n C_n B^n$



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**169.** Which of the following is a symmetric matrix? (A) a null matrix (B) a triangular matrix (C) an identity matrix (D) a diagonal matrix



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**170.** If  $A$  and  $B$  are square matrices of the same order then  $(A + B)^2 = A^2 + 2AB + B^2$  implies (A) both  $AB$  and  $BA$  are defined (B)  $(AB)^t = B^t A^t$  (C)  $(AB)^{-1} = B^{-1} A^{-1}$  if  $|A| \neq 0$  (D)  $AB = BA$



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**171.** If  $A$  is an invertible matrix of order  $n \times n$ , ( $n \geq 2$ ), then (A)  $A$  is symmetric (B)  $\text{adj} A$  is invertible (C)  $\text{Adj}(\text{Adj} A) = |A|^{n-2} A$  (D) none of these



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**172.** If  $A$  is an invertible matrix then which of the following are true?

A.  $A \neq 0$

B.  $|A| \neq 0$

C.  $\text{adj} A \neq 0$

D.  $A^{-1} = |A|adjA$

**Answer:**  $(A, B, C)$



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**173.** If  $A$  and  $B$  are invertible matrices of the same order then (A)

$Adj(AB) = (adjB)(adjA)$  (B)  $(A + B)^{-1} = A^{-1} + B^{-1}$  (C)

$(AB)^{-1} = B^{-1}A^{-1}$  (D) none of these



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**174.** The system  $x + y + z = 6$ ,  $x + 2y + 3z = 10$ ,  $x + 2y + \lambda z = \gamma$  of simultaneous equations has (A) a unique solutions if  $\lambda \neq 3$  (B) no solution if  $\lambda = 3$ ,  $\gamma \neq 10$  (C) infinitely many solutions if  $\lambda = 3$ ,  $\gamma = 10$  (D) none of these



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**175.** A square matrix A is said to be orthogonal if  $A^T A = I$  If A is a square matrix of order n and k is a scalar, then  $|kA| = K^n |A|$ . Also  $|A^T| = |A|$  and for any two square matrix A and B of same order  $|AB| = |A||B|$  On the basis of above information answer the following question: If

$$A = \begin{bmatrix} p & q & r \\ q & r & p \\ r & p & q \end{bmatrix} \quad \text{be an orthogonal matrix and}$$

$pqr = 1$ , then  $p^3 + q^3 + r^3$  may be equal to (A) 2 (B) 1 (C) 3 (D) -1



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**176.** A square matrix A is said to be orthogonal if  $A^T A = I$  If A is a square matrix of order n and k is a scalar, then  $|kA| = K^n |A|$  Also  $|A^T| = |A|$  and for any two square matrix A d B of same order  $|AB| = |A| |B|$  On the basis of above information answer the following question: IF A is a  $3 \times 3$  orthogonal matrix such that  $|A| = 1$ , then  $|A - I| =$  (A) 1 (B) -1 (C) 0 (D) none of these



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**177.** A square matrix  $A$  is said to be orthogonal if  $A^T A = I$ . If  $A$  is a square matrix of order  $n$  and  $k$  is a scalar, then  $|kA| = K^n |A|$ . Also  $|A^T| = |A|$  and for any two square matrix  $A$  and  $B$  of same order  $|AB| = |A| |B|$ . On the basis of above information answer the following question: If  $A$  is an orthogonal matrix then (A)  $A^T$  is an orthogonal matrix but  $A^{-1}$  is not an orthogonal matrix (B)  $A^T$  is not an orthogonal matrix but  $A^{-1}$  is an orthogonal matrix (C) Neither  $A^T$  nor  $A^{-1}$  is an orthogonal matrix (D) Both  $A^T$  and  $A^{-1}$  are orthogonal matrices.



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**178.** A square matrix  $A$  is said to be orthogonal if  $A^T A = I$ . If  $A$  is a square matrix of order  $n$  and  $k$  is a scalar, then  $|kA| = K^n |A|$ . Also  $|A^T| = |A|$  and for any two square matrix  $A$  and  $B$  of same order  $|AB| = |A| |B|$ . On the basis of above information answer the following question: If

$A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$  and  $P$  is an orthogonal matrix and

$B = PAP^T$ ,  $P^T B^{2009} P =$  (A)  $\begin{bmatrix} 1 & 2009 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 2009 \\ 2009 & 1 \end{bmatrix}$  (C)

$\begin{bmatrix} 1 & 0 \\ 2009 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$



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**179.** If  $A$  is a square matrix of any order then  $|A - xI| = 0$  is called the characteristic equation of matrix  $A$  and every square matrix satisfies its

characteristic equation. For example if  $A = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix}$ , Then

$$[(A - xI)], = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix} - \begin{bmatrix} x & 0 \\ 0 & x \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1 & 5-x \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1 & 5-x \end{bmatrix}$$

Characteristic equation of matrix  $A$  is

$$\begin{vmatrix} 1-x & 2 \\ 1 & 5-x \end{vmatrix} = 0 \text{ or } (1-x)(5-x) - 2 = 0 \text{ or } x^2 - 6x + 3 = 0.$$

Matrix  $A$  will satisfy this equation i.e.  $A^2 - 6A + 3I = 0$  then  $A^{-1}$  can be determined by multiplying both sides of this equation let

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & -2 & 4 \end{bmatrix} \text{ On the basis of above information answer the}$$

following questions: If  $6A^{-1} = A^2 + aA + bI$ , then  $(a, b)$  is (A)

(-6, 11) (B) (-11, 6) (C) (11, 6) (D) (6, 11)

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**180.** If A is a square matrix of any order then  $|A - xI| = 0$  is called the characteristic equation of matrix A and every square matrix satisfies its

characteristic equation. For example if  $A = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix}$ , Then

$$[(A - xI)], = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix} - \begin{bmatrix} x & 0 \\ 0 & x \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1-0 & 5-x \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1 & 5-x \end{bmatrix}$$

Characteristic equation of matrix A is

$$\begin{vmatrix} 1-x & 2 \\ 1 & 5-x \end{vmatrix} = 0 \text{ or } (1-x)(5-x)(0-2) = 0 \text{ or } x^2 - 6x + 3 = 0$$

Matrix A will satisfy this equation ie.  $A^2 - 6A + 3I = 0$   $A^{-1}$  can be determined by multiplying both sides of this equation let

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & -2 & 4 \end{bmatrix} \text{ On the basis for above information answer the}$$

following questions: Sum of elements of  $A^{-1}$  is (A) 2 (B) -2 (C) 6 (D) none of these



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**181.** If A is a square matrix of any order then  $|A - xI| = 0$  is called the characteristic equation of matrix A and every square matrix satisfies its

characteristic equation. For example if  $A = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix}$ , Then

$$[(A - xI)], = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix} - \begin{bmatrix} x & 0 \\ 0 & x \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1-0 & 5-u \end{bmatrix} = \begin{bmatrix} 1-x & 2 \\ 1 & 5-x \end{bmatrix}$$

Characteristic equation of matrix A is

$$\begin{vmatrix} 1-x & 2 \\ 1 & 5-x \end{vmatrix} = 0 \text{ or } (1-x)(5-x) - 2 = 0 \text{ or } x^2 - 6x + 3 = 0$$

Matrix A will satisfy this equation ie.  $A^2 - 6A + 3I = 0$   $A^{-1}$  can be determined by multiplying both sides of this equation let

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & -2 & 4 \end{bmatrix} \text{ ON the basis fo above information answer the}$$

following questions:  $|A^{-1}| =$  (A) 6 (B)  $\frac{1}{6}$  (C) 12 (D) none of these



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182. If the matrix  $\begin{bmatrix} 1 & 3 & \lambda + 2 \\ 2 & 4 & 8 \\ 3 & 5 & 10 \end{bmatrix}$  is singular then find  $\lambda$



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183. If  $A = \begin{bmatrix} 1 & 3 \\ 3 & 4 \end{bmatrix}$  and  $A^2 - xA - I = 0$  then find x.



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**184.** For a  $3 \times 3$  matrix A if  $|A| = 4$ , then find  $|Adj A|$



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**185.** Assertion:  $|M| = 0$ , Reason: Determinant of a skew symmetric matrix is 0. (A) Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not the correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**186.** Assertion:  $|AA^T| = 0$ , Reason : A is a skew symmetric matrix (A) Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not the correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**187.** Assertion :  $A^{-1}$  exists, Reason:  $|A| = 0$  (A) Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not the correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**188.** Assertion:  $|Adj A| = -1$ , Reason : If A is a non singular square matrix of order n then  $|adj A| = |A|^{n-1}$  (A) Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not the correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**189.** Assertion:  $adj A$  is a non singular matrix., Reason: A is a non singular matrix. (A) Both A and R are true and R is the correct explanation of A (B)

Both A and R are true R is not te correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**190.** Assertion: If  $|A^2| = 25$  then  $A = \pm \frac{1}{5}$ , Reason:  $|AB| = |A||B|$  (A)

Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not te correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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**191.** Statement 1: The system of equations has unique solution for

$\lambda = -5$ , Reason: The determinant  $\begin{vmatrix} 3 & -1 & 4 \\ 1 & 2 & -3 \\ 6 & 5 & \lambda \end{vmatrix} \neq 0$  or  $\lambda \neq -5$  (A)

Both A and R are true and R is the correct explanation of A (B) Both A and R are true R is not te correct explanation of A (C) A is true but R is false. (D) A is false but R is true.



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192. If  $M$  is a  $3 \times 3$  matrix, where  $\det M = 1$  and  $MM^T = I$ , where  $I$  is an identity matrix, prove that  $\det (M - I) = 0$ .



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193. If

$$P = \begin{bmatrix} \frac{\sqrt{3}}{2} & \frac{1}{20} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix}, A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \text{ and } Q = PAP^T, \text{ then } P^T Q^{2005} P \text{ is:}$$

(A)  $\begin{bmatrix} 1 & 2005 \\ 0 & 1 \end{bmatrix}$  (B)  $\begin{bmatrix} 1 & 2005 \\ 2005 & 1 \end{bmatrix}$  (C)  $\begin{bmatrix} 1 & 0 \\ 2005 & 1 \end{bmatrix}$  (D)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$



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194. If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{bmatrix}$ ,  $6A^{-1} = A^2 + cA + dI$ , then  $(c, d) =$



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195. Let  $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{bmatrix}$ , if  $U_1, U_2$  and  $U_3$  are column matrices

satisfying

$$AU_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, AU_2 = \begin{bmatrix} 2 \\ 3 \\ 0 \end{bmatrix} \text{ and } AU_3 = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix} \text{ and } U \text{ is a } 3 \times 3 \text{ matrix}$$

when columns are  $U_1, U_2, U_3$  now answer the following question: The value of  $|U|$  is (A) 3 (B) -3 (C)  $\frac{3}{2}$  (D) 2



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196. Let  $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{bmatrix}$ , if  $U_1, U_2$  and  $U_3$  are column matrices

satisfying

$$AU_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, AU_2 = \begin{bmatrix} 2 \\ 3 \\ 0 \end{bmatrix} \text{ and } AU_3 = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix} \text{ and } U \text{ is a } 3 \times 3 \text{ matrix}$$

when columns are  $U_1, U_2, U_3$  now answer the following question: The sum of elements of  $U^{-1}$  is: (A) -1 (B) 0 (C) 1 (D) 3



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197. Let  $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{bmatrix}$ , if  $U_1, U_2$  and  $U_3$  are column matrices

satisfying  $AU_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ ,  $AU_2 = \begin{bmatrix} 2 \\ 3 \\ 0 \end{bmatrix}$  and  $AU_3 = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$  and  $U$  is a  $3 \times 3$

matrix when columns are  $U_1, U_2, U_3$  now answer the following question:

The value of determinant  $\begin{bmatrix} 3 & 2 & 0 \end{bmatrix} I \begin{bmatrix} 3 \\ 2 \\ 0 \end{bmatrix}$  is (A) 5 (B)  $\frac{5}{2}$  (C) 4 (D)  $\frac{3}{2}$



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198. Consider the system of equations

$x - 2y + 3z = -1$ ,  $-x + y - 2z = k$ ,  $x - 3y + 4z = 1$  Assertion:

The system of equations has no solution for  $k \neq 3$  and Reason: The

determinant  $\begin{vmatrix} 1 & 3 & -1 \\ -1 & -2 & k \\ 1 & 4 & 1 \end{vmatrix} \neq 0$ , for  $k \neq 3$  (A) Both A and R are true

and R is the correct explanation of A (B) Both A and R are true R is not the

correct explanation of A (C) A is true but R is false. (D) A is false but R is

true.



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**199.** Let  $A$  be the set of all  $3 \times 3$  symmetric matrices all of whose entries are either 0 or 1. Five of these entries are 1 and four of them are 0. The number of matrices in  $A$  is



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**200.** Let  $A$  be the set of all  $3 \times 3$  symmetric matrices all of whose entries are either 0 or 1. Five of these entries are 1 and four of them are 0. The number of matrices in  $A$  is



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**201.** Let  $A$  be the set of all  $3 \times 3$  symmetric matrices all of whose entries are either 0 or 1. Five of these entries are 1 and four of them are 0. The number of matrices in  $A$  is



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