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## MATHS

## BOOKS - KC SINHA MATHS (HINGLISH)

## QUADRATIC EQUATIONS - FOR COMPETITION

## Solved Examples

1. If the roots of equation $a(b-c) x^{2}+b(c-a) x+c(a-b)=0$ be equal prove that $a, b, c$ are in H.P.

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2. If $a, b, c$ are nonzero real numbers and $a z^{2}=b z+c+i=0$ has purely imaginary roots, then prove that $a=b^{2}$.
3. If $a+b+c=0(a, b, c$ are real), then prove that equation $(b-x)^{2}-4(a-x)(c-x)=0$ has real roots and the roots will not be equal unless $a=b=c$.

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4. If $P(x)=a x^{2}+b x+c, Q(x)=-a x^{2}+d x+c$ where $a c \neq 0$ then $P(x) . Q(x)=0$ has

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5. Prove that the roots of equation $b x^{2}+(b-c) x+b-c-a=0$ are real if those of equatiion $a x^{2}+2 b x+b=0$ are imaginary and vice versa where $a, b, c \varepsilon R$.

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6. The number of integral values of 'm' less than 50 , so that the roots of the quadratic equation $m x^{2}+(2 m-1) x+(m-2)=0$ are rational are

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7. Statement (1) : If a and b are integers and roots of $x^{2}+a x+b=0$ are rational then they must be integers. Statement (2): If the coefficient of $x^{2}$ in a quadratic equation is unity then its roots must be integers

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8. If $r$ be the ratio ofthe roots of the equation $a x^{2}+b x+c=0$, show that $\frac{(r+1)^{2}}{r}=\frac{b^{2}}{a c}$

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9. If one root of equation $(l-m) x^{2}+l x+1=0$ be double of the other and if $l$ be real, show that $m \leq \frac{9}{8}$

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10. If one root of the equation $a x^{2}+b x+c=0$ is equal to the $n^{t h}$ power of the other, then $\left(a c^{n}\right)^{\frac{1}{n+1}}+\left(a^{n} c\right)^{\frac{1}{n+1}}+b$ is equal to

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11. If $\alpha, \beta$ are the roots of the equation $a x^{2}+b x+c=0$ and $S_{n}=\alpha^{n}+\beta^{n}$, show that $a S_{n+1}+b S_{n}+c S_{n-1}=0$ and hence find $S_{5}$

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12. Let $x_{1}, x_{2}$ be the roots of the equation $x^{2}-3 x+A=0$ and $x_{3}, x_{4}$ be those of equation $x^{2}-12 x+B=0$ and $x_{1}, x_{2}, x_{3}, x_{4}$ form an increasing G.P. find $A$ and $B$.

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13. Let pandq be the roots of the equation $x^{2}-2 x+A=0$ and let rands be the roots of the equation $x^{2}-18 x+B=0$. If p

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14. If $x^{2}-a x+b=0$ and $x^{2}-p x+q=0$ have a root in common then the second equation has equal roots show that $b+q=\frac{a p}{2}$

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15. If $a x^{2}+2 b x+c=0$ and $a_{1} x^{2}+2 b_{1} x+c_{1}=0$ have commonroot and $\frac{a}{a_{1}}, \frac{b}{b_{1}}, \frac{c}{c_{1}}$ are in A.P., show that are: $a x^{2}+2 b x+c=0$

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16. If $a, b, c, a_{1}, b_{1}, c_{1}$ are rational and equations $a x^{2}+2 b x+c=0$ and $a_{1} x^{2}+2 b_{1} x+c_{1}=0$ have one and only one root in common, prove that $b^{2}-a c$ and $b_{1}^{2}-a_{1} c_{1}$ must be perfect squares.

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17. Find the values of $p$ if the equations $3 x^{2}-2 x+p=0$ and $6 x^{2}-17 x+12=0$ have a common root.

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18. If the quadratic equations $x^{2}+b x+c a=0 \& x^{2}+c x+a b=0$ (where $a \neq 0$ ) have a common root. prove that the equation containing their other root is $x^{2}+a x+b c=0$

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19. If $\mathrm{p}, \mathrm{q}, \mathrm{r}, \mathrm{s}$ are real and $p r>4(q+s)$ then show that at least one of the equations $x^{2}+p x+q=0$ and $x^{2}+r x+s=0$ has real roots.

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20. If the roots of $a x^{2}+2 b x+c=0$ be possible and different then the roots of $(a+c)\left(a x^{2}+2 b x+2 c\right)=2\left(a c-b^{2}\right)\left(x^{2}+1\right) \quad$ will be impossible and vice versa

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21. If $\alpha, \beta$ are the roots of $x^{2}+p x+q=0 a d n x^{2 n}+p^{n} x^{n}+q^{n}=0 \operatorname{andilf}(\alpha / \beta),(\beta / \alpha)$ are the roots of $x^{n}+1+(x+1)^{n}=0$, the $\cap(\in N)$ a. must be an odd integer b. may be any integer c. must be an even integer d. cannot say anything

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22. Approach to solve greatest integer function of $x$ and fractional part of
$x$; (i) Let $[x]$ and $\{x\}$ represent the greatest integer and fractional part of $x$ ; respectively Solve $4\{x\}=x+[x]$

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23. If $b>a$ then show that the equation $(x-a)(x-b)-1=0$ has one root less than $a$ and other root greater than $b$.

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24. Let $-1 \leq p<1$ show that the equation $4 x^{3}-3 x-p=0$ has a unique root in the interval $\left[\frac{1}{2}, 1\right]$

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25. If $\alpha$ is a real root of the quadratic equation $a x^{2}+b x+c=0 a n d \beta$ ils a real root of $a x^{2}+b x+c=0$, then show that there is a root $\gamma$ of equation $(a / 2) x^{2}+b x+c=0$ whilch lies between aand $\beta$.

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26. If $2 \mathrm{a}+3 \mathrm{~b}+6 \mathrm{c}=0$, then show that the equation $a x^{2}+b x+c=0$ has atleast one real root between 0 to 1 .

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27. Thus $f(0)=f(1)$ and hence equation $f^{\prime}(x)=0$ has at least one root between 0 and 1. Show that equation
$(x-1)^{5}+(2 x+1)^{9}+(x+1)^{21}=0$ has exactly one real root.

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28. Find the positive solutions of the system of equations
$x^{x+y}=y^{n}$ and $y^{x+y}=x^{2 n} . y^{n}$, where $n>0$

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29. For $a \leq 0$, determine all real roots of the equation (1986, 5M)
$x^{2}-2 a|x-a|-3 a^{2}=0$

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30. Find all integers $x$ for which $(5 x-1)<(x+1)^{2}<(7 x-3)$.

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31. Show that the expression $\frac{x^{2}-3 x+4}{x^{2}+3 x+4}$ lies between $\frac{1}{7}$ and 7 for real values of $x$.

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32. For xin R which of the following cant be the value of $\frac{x^{2}+34 x-71}{x^{2}+2 x-7}$

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33. If x is real, show that the expression $\frac{4 x^{2}+36 x+9}{12 x^{2}+8 x+1}$ can have any real value.

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34. Prove that if x is real, the expression $\frac{(x-a)(x-c)}{x-b}$ is capable of assuming all values if $a>b>c$ or $a<b<c$.
35. Prove that $\left|\frac{12 x}{4 x^{2}+9}\right| \leq 1$ for all real values of x the equality being satisfied only if $|x|=\frac{3}{2}$

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36. Prove that if the equation $x^{2}+9 y^{2}-4 x+3=0$ is satisfied for real values of $x$ andy, thenx must lie between 1 and 3 and $y$ must lie between$1 / 3$ and $1 / 3$.

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37. Find the value of a which makes the expression $x^{2}-a x+1-2 a^{2}$ always positive for real values of $x$.

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38. For what real values of $k$ both the roots of equation $x^{2}+2(k-3) x+9=-0$ lie between -6 and 1 .

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39. Find all values of the parameter a for which the inequality $a .9^{x}+4(a-1) 3^{x}+a>1$ is satisfied for all real values of x

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40. The coefficient of x in the equation $x^{2}+p x+q=0$ was wrongly written as 17 in place of 13 and the roots thus found were -2 and -15 . The roots of the correct equation are (A) $15 .-2$ (B) $-3,-10$ (C) $-13,30$ (D) 4,13

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41. If the roots of the quadratic equation $a x^{2}+c x+c=0$ are in the ratio $p: q$ show that $\sqrt{\frac{p}{q}}+\sqrt{\frac{q}{p}}+\sqrt{\frac{c}{a}}=0$, where $a, c$ are real numbers, such that $a>0$

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42. Find the number of quadratic equations, which are unchanged by squaring their roots.

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43. $a, b, c$ are positive real numbers forming a G.P. ILf $a x 62+2 b x+c=0 a n d d x^{2}+2 e x+f=0$ have a common root, then prove that $d / a, e / b, f / c$ are in A.P.

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44. The equation $e^{\sin x}-e^{-\sin x}-4=0$ has (A) non real roots (B) integral roots (C) rational roots (D) real and unequal roots

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45. The roots of the equation $(q-r) x^{2}+(r-p) x+p-q=0$ are (A)
$\frac{r-p}{q-r}, 1$ (B) $\frac{p-q}{q-r}, 1$ (C) $\frac{q-r}{p-q}, 1$ (D) $\frac{r-p}{p-q}, 1$

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46. If $\alpha$ and $\beta$ are the roots equation
$a x^{2}-2 b x+c=0$, then $\alpha^{3} \beta^{3}+\alpha^{2} \beta^{3}+\alpha^{3} \beta^{2}=\quad$ (A) $\frac{c^{2}}{a^{3}}(c+2 b)$
$\frac{c^{2}}{c^{3}}(c-2 b)$ (C) $b \frac{c^{2}}{a^{3}}$ (D) none of these

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47. If $c, d$ are the roots of the equation $(x-a)(x-b)-k=0$, prove that $\mathrm{a}, \mathrm{b}$ are roots of the equation $(x-c)(x-d)+k=0$.

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48. If and the equation $a x^{2}+b x+c=0$ and $x^{2}+x+1=0$ have a common root, then

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49. If $a^{2}+2 b x+c=0$ and $a_{1} x^{2}+2 b_{1} x+c_{1}=0$ have a common root and $\frac{a}{a_{1}}, \frac{b}{b_{1}}, \frac{c}{c_{1}}$ are in AP then $a_{1}, b_{1}, c_{1}$ are in (A) A.P. (B) G.P. (C) H.P. (D) none of these

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50. The expression $x^{2}+2 x y+k y^{2}+2 x+k=0$ can be resolved into two linear factors, then $k \in$

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51. Equation $(a+5) x^{2}-(2 a+1) x+(a-1)=0$ will have roots equal in magnitude but opposite in sign if $a=$
A. 1
B. -1
C. 2
D. $-\frac{1}{2}$

## Answer: null

52. Let $\mathrm{f}(\mathrm{x})$ be defined by $f(x)=x-[x], 0 \neq x \in R$, where $[\mathrm{x}]$ is the greatest integer less than or equal to $x$ then the number of solutions of $f(x)+f\left(\frac{1}{x}\right)=1$

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53. If $0<x<1000$ and $\left[\frac{x}{2}\right]+\left[\frac{x}{3}\right]+\left[\frac{x}{5}\right]=\frac{31}{30} x$, (where [.] denotes the greatest integer function then number of possible values of x.

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54. If the equations $a x+b y=1$ and $c x^{2}+d y^{2}=1$ have only one solution, prove that $\frac{a^{2}}{c}+\frac{b^{2}}{d}=1$ and $x=\frac{a}{c}, y=\frac{b}{d}$
55. If $\alpha, \beta$ are the roots of the equations $x^{2}+p x+q=0$ then one of the roots of the equation $q x^{2}-\left(p^{2}-2 q\right) x+q=0$ is (A) 0 (B) 1 (C) $\frac{\alpha}{\beta}$ (D) $\alpha \beta$

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56. Let $\alpha$ and $\beta$ be the roots of the equation $x^{2}+x+1=0$. The equation whose roots are $\alpha^{29}, \beta^{17}$ is (A) $x^{2}-x+1=0$
$x^{2}+x+1=0$ (C) $x^{2}-x-1=0$ (D) $x^{2}+x-1=0$

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57. If $x \varepsilon R$, then the number of real solutions of the equation $3^{x}+3^{-x}=\log _{10} 99$ is (A) 0 (B) 1 (C) 2 (D) more than 2

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58. Number of real roots of the equation $2^{x}=2^{x-1}+2^{x-2}=7^{x}+7^{x-1}+7^{x-2}$ is (A) 4 (B) 2 (C) 1 (D) 0

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59. If $a, b, c$ are positive rational numbers such that $a>b>c$ and the quadratic eqution $(a+b-2 c) x^{2}+(b+c-2 a) x+(c+a-2 b)=0$ has a root of the interval $(-1,0)$ then (A) $c+a<2 b$ (B) the roots of the equation are rational (C) the roots of are imaginary (D) none of these

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60. Roots of the equation $a(b-c) x^{2}+b(c-a) x+c(a-b)=0$ are real and equal, then (A) $a+b+c \neq 0$ (B) $a, b, c$ are in H.P. (C) $a, b, c$ are in H.P. (D) $a, b, c$ are in G.P.

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61. Let $f(x)=a x^{2}+b x+c, a, b, c \varepsilon R a \neq 0$ such that $f(x)>0 \forall x \varepsilon R$ also let $g(x)=f(x)+f^{\prime}(x)+f^{\prime \prime}(x)$. Then (A) $g(x)<0 \forall x \varepsilon R$ $g(x)>0 \forall x \varepsilon R$ (C) $g(x)=0$ has real roots (D) $g(x)=0$ has non real complex roots

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62. If $\alpha a n d \beta$ are the roots of $x^{2}+p x+q=0 a n d \alpha^{4}, \beta^{4}$ are the roots of $x^{2}-r x+s=0$, then the equation $x^{2}-4 q x+2 q^{2}-r=0$ has always. one positive and one negative root two positive roots two negative roots cannot say anything

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63. If $P(x)=x^{2}+a x+b$ and $Q(x)=x^{2}+a_{1} x+b_{1}, a, b, a_{1}, b_{1} \varepsilon R$ and equation $P(x) \cdot Q(x)=0$ has at most one real root, then (A)

$$
\begin{align*}
& (1+a+b)\left(1+a_{1}+b_{1}\right)>0 \quad \text { (B) } \quad(1+a+b)\left(1+a_{1}+b_{1}\right)<0  \tag{B}\\
& \frac{1+a+b}{1+a_{1}-b_{1}}>0 \text { (D) } 1+a+b>0 \tag{C}
\end{align*}
$$

64. Find product of all real values of $x$ satisfying $(5+2 \sqrt{6})^{x^{2}-3}+(5-2 \sqrt{6})^{x^{2}-3}=10$.

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65. The set of values of a for which the inequality, $x^{2}+a x+a^{2}+6 a<0$ is satisfied for all $x$ belongs $(1,2)$ lies in the interval:

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66. If the sum of the roots of the equation $a x^{2}+b x+c=0$ is equal to sum of the squares of their reciprocals, then $b c^{2}, c a^{2}, a b^{2}$ are in

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67. If the given equation $a x^{2}+b x+c=0$ and the equation $x^{2}+2 x+9=0$ have a common root, then a:b:c is (A) $1: 2: 9$ (B) $1: 2: 3$
(C) $1: 1: 1$ (D) none of these

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68. If $a, b$, andc are odd integers, then prove that roots of $a x^{2}+b x+c=0$ cannot be rational.

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69. If the equation $f(x)=a x^{2}+b x+c=0$ has no real root, then $(a+b+c) c$ is (A) $=0(\mathrm{~B})>0(\mathrm{C})<0(\mathrm{D})$ not real

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70. If $2 \mathrm{a}+3 \mathrm{~b}+6 \mathrm{c}=0$, then show that the equation $a x^{2}+b x+c=0$ has atleast one real root between 0 to 1 .

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71. If $f(x)=x$ has non real roots, then the equation $f(f(x))=x$ (A) has all real and unequal roots (B) has some real and non real roots (C) has all real and equal roots (D) has all non real roots

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72. Consider the quadratic equation $x^{2}-m x+1=0$ with two roots $\alpha$ and $\beta$ such that $\alpha+\beta=\mathrm{m}$ and $\alpha \beta=1$ The value of m for which both the roots of the equation are less than unity are (A) $]-\infty,-2]$ (B) $[-2,2]$ (C) $[2, \infty]$ (D) $]-\infty,-2] \cup[2, \infty]$

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73. Consider the quadratic equation $x^{2}-m x+1=0$ with two roots $\alpha$ and $\beta$ such that $\alpha+\beta=\mathrm{m}$ and $\alpha \beta=1$ The value of m for which both the roots of the equation are greater then unity re (A) $[2, \infty]$ (B) $]--\infty, 2]$ (C) $[-2,2]$ (D) none of these

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74. Consider the quadratic equation $x^{2}-m x+1=0$ with two roots $\alpha$ and $\beta$ such that $\alpha+\beta=\mathrm{m}$ and $\alpha \beta=1$ The values of m for which $\alpha<1$ and $\beta>1$ are (A) $[-2, \infty[$ (B) $[-2,2] \quad$ (C) $[2, \infty]$
] $-\infty,-2]$

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75. Let $\alpha, \beta$ be the roots of $x^{2}-x+p=0$ and $\gamma, \delta$ be the roots of $x^{2}-4 x+q=0 \quad$ such that $\alpha, \beta, \gamma, \delta \quad$ are in G.P. and $p \geq 2$. Ifa $b, c \varepsilon\{1,2,3,4,5\}$, let the number of equation of the form
$a x^{2}+b x+c=0$ which have real roots be $r$, then the minium value of $p$ $q \mathrm{r}=$

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76. Let $\alpha, \beta$ and $\gamma$ be the roots of equation $f(x)=0$, where $f(x)=x^{3}+x^{2}-5 x-1=0$. then the value of $|[\alpha]+[\beta]+[\gamma]|$, where $[$.$] denotes the integer function, is equal to$

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## Exercise

1. If the roots of the equation $a x^{2}+b x+c=0$ be in the ratio $m: n$, prove that $\sqrt{\frac{m}{n}}+\sqrt{\frac{n}{m}}+\frac{b}{\sqrt{a c}}=0$
2. If $\alpha, \beta$ are the roots of the equation $x^{2}-b x+c=0$ then find the equation whose roots are $\left(\alpha^{2}+\beta^{2}\right)\left(\alpha^{3}+\beta^{3}\right)$ and $\alpha^{5} \beta^{3}+\alpha^{3} \beta^{5}-2 \alpha^{4} \beta^{4}$

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3. If n and r are positive integers such that $0<r<n$ then show that the roots of the quadratic equation $n C_{r} x^{2}+2 \cdot{ }^{n} C_{r+1} x+{ }^{n} C_{r+2}=0$ are real.

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4. If $a, b, c\left(a b c^{2}\right) x^{2}+3 a^{2} c x+b^{2} c x-6 a^{2}-a b+2 b^{2}=0$ ares rational.

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5. If $\alpha_{1}, \alpha_{2}$ be the roots of equation $x^{2}+p x+q=0$ and $\beta_{1}, \beta$ be those of equation $x^{2}+r x+s=0$ and the system of equations $\alpha_{1} y+\alpha_{2} z=0$ and $\beta_{1} y+\beta_{2} z=0$ has non trivial solution, show that $\frac{p^{2}}{r^{2}}=\frac{q}{s}$

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6. If a,b,c are the roots of the equation $x^{3}+p x^{2}+q x+r=0$ such that $c^{2}=-a b$ show that $\left(2 q-p^{2}\right)^{3} \cdot r=(p q-4 r)^{3}$.

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7. Let $\alpha+i \beta(\alpha, \beta \in R)$ be a root of the equation $x^{3}+q x+r=0, q, r \in R$. Find a real cubic equation, independent of $\alpha a n d \beta$, whose one roots is $2 \alpha$.

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8. Find the values of $k$ for which $5 x^{2}-4 x+2+k\left(4 x^{2}-2 x-1\right)=0$ has real and equal roots.

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9. Find the value of $m$ for which the equation $5 x^{2}-4 x+2+m\left(4 x^{2}-2 x-1\right)=0$ the product of the roots is 2

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10. Find the value of $m$ for which the equation $5 x^{2}-4 x+2+m\left(4 x^{2}-2 x-1\right)=0$ the sum of the rots is 6.

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11. If the sum of the rotsof the equation $p x^{2}+q x+r=0$ be equal to the sum of their squares, show that $2 p r=p q+q^{2}$
12. In copying a quadratic equation of the form $x^{2}+p x+q=0$, the coefficient of $x$ was wrongly written as -10 in place of -11 and the roots were found to be 4 and 6 . find the roots of the correct equation.

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13. Solve for $\mathrm{x}: \sqrt{11 x-6}+\sqrt{x-1}=\sqrt{4 x+5}$

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14. If $x$ and $y$ satisfy the equation $y=2[x]+3$ and $y=3[x-2]$ simultaneously, where [.] denotesthe greatest integer function, then $[x+y]$ is equal to

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15. $|x+1|-|x|+3|x-1|-2|x-2| x+2$. Solve for $x$

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16. Solve $\left|x^{2}+4 x+3\right|+2 x+5=0$.

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17. Show that the equation $(x-1)^{5}+(x+2)^{7}+(7 x-5)^{9}=10$ has exactly one root.

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18. Solve $\frac{1}{x}+\frac{1}{[2 x]}=\{x\}+\frac{1}{3}$ where [.] denotes the greatest integers function and\{.\} denotes fractional part function.
19. Solve for $x: 4^{x} 3^{x-1 / 2}=3^{x+1 / 2}-2^{2 x-1}$.

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20. the value of $x$,satisfying the equation $\log _{10}\left(98+\sqrt{x^{3}-x^{2}-12 x+36}\right)=2$ is

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21. 

Solve:
$(\log )_{(2 x+3)}\left(6 x^{2}+23+21\right)+(\log )_{(3 x+7)}\left(4 x^{2}+12 x+9\right)=4$

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22. Find all the real values of x such that $\frac{2 x-1}{2 x^{3}+3 x^{2}+x}>0$

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23. Find the value of x such that $\log _{10}\left(x^{2}-2 x-2\right) \leq 0$

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24. For real $x$, the function $(x-a)(x-b) /(x-c)$ will assume all real values provided $a>b>c \mathrm{~b}$. ${ }^{`} \mathrm{c} \mathrm{c}>\mathrm{b} d$. a

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25. If $x, a, b$ are real prove that
$4(a-x)\left(x-a+\sqrt{a^{2}+b^{2}}\right) \ngtr a^{2}+b^{2}$

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26. Prove that for real values of $x,\left(a x^{2}+3 x-4\right) /\left(3 x-4^{2}+a\right)$ may have any value provided a lies between 1 and 7 .

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27. if $\alpha, \beta, \gamma$ are roots of $2 x^{3}+x^{2}-7=0$ then find the value of $\sum_{\alpha, \beta, \gamma}\left(\frac{\alpha}{\beta}+\frac{\beta}{\gamma}\right)$

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28. The equation
$x^{3}+p x^{2}+q x+r=0$ and $x^{3}+p^{\prime} x^{2}+q^{\prime} x+r^{\prime}=0 \quad$ have two common roots, find the quadratic whose roots are these two common roots.

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29. FIND that condition that the roots of equation $a x^{3}+3 b x^{2}+3 c x+d=0$ may be in G.P.

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30. Show that one of the roots of equation $a x^{2}+b x+c=0$ may be reciprocal of one of the roots of $a_{1} x^{2}+b_{1} x+c_{1}=0$ if $\left(a a_{1}-c\right.$ $\left.c_{1}\right)^{2}=\left(b c_{1}-a b_{1}\right)\left(b_{1} c-a_{1} b\right)$

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31. If every pair from among the equations $x^{2}+p x+q r=0, x^{2}+q x+r p=0$ and $x^{2}+r x+p q=0$ has a common root, then the sum of the three common roots is

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32. If $a<b<c<d$ then show that the quadratic equation $\mu(x-a)(x-c)+\lambda(x-b)(x-d)=0$ has real roots for all real $\mu$ and $\lambda$

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33. Show that the following equation can have at most one real root $3 x^{5}-5 x^{3}+21 x+3 \sin x+4 \cos x+5=0$

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34. If $e^{\left(\cos ^{2} x+\cos ^{4}+\cos ^{x} \ldots \ldots\right) \log 3}$ satisfies the equation $t^{2}-8 t-9=0$ then the value of $\operatorname{tn} x,\left(0<x<\frac{\pi}{2}\right)$ is (A) $\sqrt{3}$ (B) $\sqrt{2}$ (C) 1 (D) $\frac{1}{\sqrt{2}}$

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35. 

$a=\cos \left(\frac{2 \pi}{7}\right)+i \sin \left(\frac{2 \pi}{7}\right), A=a+a^{2}+a^{4}$ and $B=a^{3}+a^{5}+a^{6}$, then A and B are the roots of the equation (A) $x^{2}-x+2=0$
$x^{2}-x-2=0$ (C) $x^{2}+x+2=0(\mathrm{D})$ none of these

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36. The number of real solution of $2 \sin \left(e^{x}\right)=5^{x}+5^{-x} \in[0,1]$ is (A) 0 (B) 1 (C) 2 (D) 4

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37. If $\left(x^{2}-3 x+2\right)$ is a factor of $x^{4}-p x^{2}+q=0$, then the values of $p$ and $q$ are

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38. Equation $\frac{a}{x-1}+\frac{b}{x-2}+\frac{c}{x-3}=0(a, b, c>0)$ has (A) two imaginary roots (B) one real roots in $(1,2)$ and other in $(2,3)$ (C) no real root in [1,4] (D) two real roots in (1,2)

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39. 

$4 x^{2}+2 x-1=0$ and $f(x)=4 x^{3}-3 x+1$, then $2(f(\alpha)+\alpha)$ is

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40. The number of solution of equation $|x-1|=e^{x}$ is (A) 0 (B) 1 (C) 2 (D) none of these

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41. If $p, q, r, s \in R$, then equaton
$\left(x^{2}+p x+3 q\right)\left(-x^{2}+r x+q\right)\left(-x^{2}+s x-2 q\right)=0$ has

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42. If $\alpha$ and $\beta$ are the roots of $x^{2}+p x+q=0$ and $\alpha^{4}, \beta^{4}$ are the roots of $x^{2}-r x+s=0$, then the equation $x^{2}-4 q x+2 q^{2}-r=0$ has

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43. If $a+b+c>\frac{9 c}{4}$ and quadratic equation $a x^{2}+2 b x-5 c=0$ has non-real roots, then-

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44. If $a, b, c \varepsilon R$ and $a b>0, a+2 b+4 c=0$ then equation $a x^{2}+b x+c=0$ has (A) both roots positive (B) both roots negative (C) one positive and one negative root (D) both roots imginary

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45. If $n$ is an even number and $\alpha, \beta$ are the roots of equation $x^{2}+p x+q=0 \quad$ and also of equation
$x^{2} n+p^{n} x^{n}+q^{n}=0$ and $f(x)=\frac{(1+x)^{n}}{1+x^{n}}$, then $f\left(\frac{\alpha}{\beta}\right)=\quad$ (where $\alpha^{n}+\beta^{n} \neq 0, p \neq 0$ ) (A) 0 (B) 1 (C) -1 (D) none of these

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46. If $p, q$ be non zero real numbes and $f(x) \neq 0, \in[0,2]$ and $\int_{0}^{1} f(x) \cdot\left(x^{2}+p x+q\right) d x=\int_{0}^{2} f(x) \cdot\left(x^{2}+p x+q\right) d x=0 \quad$ then equation $x^{2}+p x+q=0$ has (A) two imginary roots (B) no root in $(0,2)$ (C) one root in $(0,1)$ and other in $(1,2)$ (D) one root in $(-\infty, 0)$ and other in $(2, \infty)$

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47. The number of real roots of equation $x^{8}-x^{5}+x^{2}-x+1=0$ is (A) 2 (B) 4 (C) 6 (D) 0

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48. If $\sin \theta$ and $\cos \theta$ are the roots of the equation $a x^{2}+b x+c=0$, then (A) $(a-c)^{2}=b^{2}+c^{2}$ (B) $(a+c)^{2}=b^{2}-c^{2}$ (C) $a^{2}=b^{2}-2 a c$ (D) $a^{2}+b^{2}-2 a c=0$

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49. If $x^{2}+p x+q$ is an integer for every integral value of x then which is necessarily true? (A) $p \varepsilon I, q \not \mathcal{Z} I$ (B) $p \not \mathscr{Z} I, q \varepsilon I$ (C) $p \varepsilon I, q \varepsilon I$ (D) $p \not \mathscr{Z}, q \not Z I$

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50. If $x^{2}+a x+b$ is an integer for every integral value of x and roots of equation $x^{2}+a x+b=0$ are rational then is (A) both roots are integers
(B) one is an integer and the othe is not (C) no root is an integer (D) one root is zero and other is non zero

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51. If $0<\alpha<\frac{\pi}{4}$ equation $(x-\sin \alpha)(x-\cos \alpha)-2=0$ has (A) both roots in $(\sin \alpha, \cos \alpha)$ (B) both roots in $(\cos \alpha, \sin \alpha)$ (C) one root in $(-\infty, \cos \alpha)$ and other in $(\sin \alpha, \infty)$ (D) one root in $(-\infty, \sin \alpha)$ and other in $(\cos \alpha, \infty)$

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52. Number of roots of the equation $\sin x+\cos x=x^{2}-2 x+\sqrt{6}$ is (A) 0 (B) 2 (C) 4 (D) an odd number

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53. 

$f(x)=x^{3}-6 x^{2}+3(1+\pi) x+7, p>q>r$, then $\frac{\{x-f(p)\}(x-f(r)\}}{x-f(q)}$ has no value in (A) (p,q) (B) (q,r) (C) $(r, \infty)$ (D) none of these

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54. If expression $x^{2}-4 c x+b^{2}>0 f$ or allx $\varepsilon R$ and $a^{2}+c^{2}<a b$ then range of the function $\frac{x+a}{x^{2}+b x+c^{2}}$ is (A) $(0, \infty)$ (B) $(0, \infty)$ $(-\infty, \infty)$ (D) none of these

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55. If the equation $(\lambda-1) x^{2}+(\lambda+1) x+\lambda-1=0$ has real roots then $\lambda=\frac{\sin \theta}{\cos \theta} \cdot \frac{\cos 3 \theta}{\sin 3 \theta}$ for (A) only one value of $\theta$ (B) for infinitely many values of $\theta(\mathrm{C})$ for no value of $\theta(\mathrm{D})$ of only two values of $\theta$

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56. If $\alpha$ and $\beta$ are roots of equation $x^{2}+p x+q=0$ and

$$
\begin{equation*}
f(n)=\alpha^{n}+\beta^{n} \text {, then (i) } f(n+1)+p f(n)-q f(n-1)=0 \tag{ii}
\end{equation*}
$$

$f(n+1)-p f(n)+q f(n-1)=0$
(iii

$$
\begin{equation*}
f(n+1)+p f(n)+q f(n-1)=0 \tag{iv}
\end{equation*}
$$

$f(n+1)-p f(n)-q f(n-1)=0$
57. If $t_{n}$ denotes the nth term of an A.P. and $t_{p}=\frac{1}{q}, t_{q}=\frac{1}{p}$ then which one of the following is necessarily a root of the equation $(p+2 q-3 r) x^{2}+(q+2 r-3 p) x+(r+2 p-3 q)=0$ (A) $t_{p}$ (B) $t_{q}$ (C) $t_{p q}$ (D) $t_{p+q}$

## - Watch Video Solution

58. If $\alpha$ and $\beta$ ('alpha

## - Watch Video Solution

59. $\alpha$ and $\beta$ are the roots of the equation $x^{2}+p x+p^{3}=0,(p \neq 0)$. If the point $(\alpha, \beta)$ lie on the curve $x=y^{2}$ then the roots of the given equation are (A) 4,-2 (B) 4,2 (C) 1,-1 (D) 1,1
60. If $\alpha, \beta$ arethe roots of the equation $x^{2}-a x+b=0$ and $A_{n}=\alpha^{n}+\beta^{n}$ then which of the following is true? (A) $\quad A_{n+1}=a A_{n}+b A_{n-1} \quad$ (B) $A_{n+1}=b A_{n}+a A_{n-1}$
$A_{n+1}=a A_{n}-b A_{n-1}$
(D) $A_{n+1}=b A_{n} \pm a A_{n-1}$

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61. If the difference between the roots of $x^{2}+a x+b=0$ is same as that of $x^{2}+b x+a=0 a \neq b$, then:

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62. If x satisfies $|x-1|+|x-2|+|x-3| \geq 6$ then (A) $0 \leq x \leq 4$ (B) $x \leq-2$ or $x \geq 4$ (C) $x \leq 0$ or $x \geq 4$ (D) $x \geq 0$

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63. Let $a, b, c$ be nonzero real numbers such that $\int_{0}^{1}\left(1+\cos ^{8} x\right)\left(a x^{2}+b x+c\right) d x$
$=\int_{0}^{2}\left(1+\cos ^{8} x\right)\left(a x^{2}+b x+c\right) d x=0$ Then show that the equation $a x^{2}+b x+c=0$ will have one root between 0 and 1 and other root between 1 and 2.

## (D) Watch Video Solution

64. If $\alpha$ and $\beta$ are the roots of a quadratic equation such that $\alpha+\beta=2, \alpha^{4}+\beta^{4}=272$, then the quadratic equation is

## - Watch Video Solution

65. The minimum valueof $|x-3|+|x-2|+|x-5|^{\prime}$ is (A) 3 (B) 7 (C) 5 (D) 9

## - Watch Video Solution

66. Let $[x]$ denote the integral part of a real number x and $\{x\}=x-[x]$ then solution of $4\{x\}=x+[x]$ are (A) $\pm \frac{2}{3}, 0$ (B) $\pm \frac{4}{3}, 0$ (C) $0, \frac{5}{3}$ (D) $\pm 2,0$

## - Watch Video Solution

67. The roots of the equation $\left|x^{2}-x-6\right|=x+2$ are (A) $-2,1,4$ (B) $0,2,4$ (C) $0,1,4$ (D) $-2,2,4$

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68. If equation $x^{2}-(2+m) x+1\left(m^{2}-4 m+4\right)=0$ has coincident roots then (A) $m=0, m=1$ (B) $m=0, m=2$ (C) $m=\frac{2}{3}, m=6$ (D) $m=\frac{2}{3}, m=1$

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69. If $f(x)=2 x^{3}+m x^{2}-13 x+n$ and 2 and 3 are 2 roots of the equations $f(x)=0$, then values of $m$ and $n$ are

## - Watch Video Solution

70. If $y=\frac{x^{2}-3 x+1}{2 x^{2}-3 x+2}$, where x is real, the value of y lies between (A)
$-1 \leq y \leq \frac{5}{7}$ (B) $-\frac{1}{2} \leq y \leq \frac{5}{7}$ (C) $\frac{5}{7}<y<1$ (D) none of these

## - Watch Video Solution

71. If one of the roots of the equation $2 x^{2}-6 x+k=0$ is $\left(\frac{\alpha+5 i}{2}\right)$, then the values of $a$ and $k$ are

## - Watch Video Solution

72. If $f(x)$ is a continuous function and attains only rational values and $f(0)=3$, then roots of equation $f(1) x^{2}+f(3) x+f(5)=0$ as
73. If $a, b, c, d$ are unequal positive numbes, then the roots of equation $\frac{x}{x-a}+\frac{x}{x-b}+\frac{x}{x-c}+x+d=0$ are necessarily (A) all real (B) all imaginary (C) two real and two imaginary roots (D) at least two real

## Watch Video Solution

74. The number of solutions of te equation $\left|2 x^{2}-5 x+3\right|+x-1=0$ is (A) 1 (B) 2 (C) $0(D)$ infinite

## - Watch Video Solution

75. The set of value of $a$ for which both the roots of the equation $x^{2}-(2 a-1) x+a=0 \quad$ are $\quad$ positie $\quad$ is $\quad$ (A) $\left\{\frac{2-\sqrt{3}}{2}\right\}$
$\left\{\frac{2-\sqrt{3}}{2}, \frac{2+\sqrt{3}}{2}\right\}$ (C) $\left[\left(2+\frac{\sqrt{3}}{2}, \infty\right)\right.$ (D) none of these
76. If the root of the equation $(a-1)\left(x^{2}+x+1\right)^{2}=(a+1)\left(x^{4}+x^{2}+1\right)$ are real and distinct, then the value of $a \in(-\infty, 3]$ b. $(-\infty,-2) \cup(2, \infty)$ c. [ $-2,2$ ] d. $[-3, \infty)$

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77. If the product of the roots of the equation $2 x^{2}+a x+4 \sin a=0$ is 1, then roots will be imaginary, if

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78. The quadratic equation whose roots are $x$ and $y$ intercepts of the line passing through $(1,1)$ and making a triangle of area A with the axes is

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79. If $\alpha$ and $\beta$ are solutions of $\sin ^{2} x+a \sin x+b=0$ as well as that of $\cos ^{2} x+c \cos x+d=0$ then $\sin (\alpha+\beta)$ is equal to

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80. The roots $\alpha a n d \beta$ of the quadratic equation $a x^{2}+b x+c=0$ are real and of opposite sign. The roots of the equation $\alpha(x-\beta)^{2}+\beta(x-\alpha)^{2}=0$ are a. positive b. negative c. real and opposite sign d. imaginary

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81. If $a, b, c \varepsilon\{1,2,3,4,5\}$, the number of equations of the form $a x^{2}+b x+c=0$ which have real roots is (A) 25 (B) 26 (C) 27 (D) 24

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82. The number of real solutions of the equation $-x^{2}+x-1=\sin ^{4} x$ is (A) 1 (B) 2 (C) 0 (D) 4

## - Watch Video Solution

83. The number of real solutions of the equation $(6-x)^{4}+(8-x)^{4}=16$ is (A) 1 (B) 2 (C) 4 (D) 0

## - Watch Video Solution

84. If $x, a_{1}, a_{2}, a_{3}, \ldots . a_{n} \varepsilon R$
and
$\left(x-a_{1}+a_{2}\right)^{2}+\left(x-a_{2}+a_{3}\right)^{2}+\ldots \ldots . .+\left(x-a_{n-1}+a_{n}\right)^{2} \leq 0$, then $a_{1}, a_{2}, a_{3} \ldots \ldots \ldots a_{n}$ are in (A) AP (B) GP (C) HP (D) none of these

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85. The expression $a x^{2}+2 b x+b$ has same sign as that of b for every real x , then the roots of equation $b x^{2}+(b-c) x+b-c-a=0$ are (A) real and equal (B) real and unequal (C) imaginary (D) none of these

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86. Let $\alpha+i \beta ; \alpha, \beta \in R$, be a root of the equation $x^{3}+q x+r=0 ; q, r \in R$. A real cubic equation, independent of $\alpha \& \beta$, whose one root is $2 \alpha$ is $x^{3}+q x-4=0$ (b) $x^{3}-q x+4=0$ $x^{3}+2 q x+r=0$ (d) None of these

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87. The equation $\sin x=x^{2}+x+1$ has (A) 'one real solution (B) n real solution (C) more thanone real solution (D) two positive solutons

## - Watch Video Solution

88. If $p, q, r \varepsilon R$ and the quadratic equation $p x^{2}+q x+r=0$ has no real roots, then
(A) $\quad p(p+q+r)>0$
(B) $(p+q+r)>0$
$q(p+q+r)>0$ (D) $p+q+r>0$

## - Watch Video Solution

89. If $p, q, r \varepsilon R$ and are distinct the equation $(x-p)^{5}+(x-q)^{5}+(x-r)^{5}=0$ has (A) four imaginary and one real root (B) two imaginary and three real roots (C) all the roots real (D) none of these

## - Watch Video Solution

90. Let S denotes the set of real values of 'a' for which the roots of the equation $x^{2}-a x-a^{2}=0$ exceeds 'a', then $S$ equals to

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91. 

$f(x)=x^{2}+b x+c$ and $g(x)=a f(x)+b f^{\prime}(x)+c f^{\prime \prime}(x) . I f f(x)>0 \forall$ then the sufficient condition of $g(x)$ to be $>0 \forall x \varepsilon R$ is (A) $c>0$ (B) $b>0$ (C) $b<0$ (D) $c<0$

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92. The set of values of k for which $x^{2}-k x+\sin ^{-1}(\sin 4)>0$ for all real x is

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93. Let $a, b, c$ be three distinct positive real numbers then number of real roots of $a x^{2}+2 b|x|+c=0$ is (A) 0 (B) 1 (C) 2 (D) 4

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94. The constant term of the quadratic expression $\sum_{k=2}^{n}\left(x-\frac{1}{k-1}\right)\left(x-\frac{1}{k}\right)$, as $n \rightarrow \infty$ is

## - Watch Video Solution

95. If $x^{2}+a x+b$ is an integer for every integer x then

## - Watch Video Solution

96. If $a, b$ are roots of $x^{2}+p x+q=0$ and $c, d$ are the roots $x^{2}-p x+r=0$ thena ${ }^{2}+b^{2}+c^{2}+d^{2} \quad$ equals (A) $p^{2}-q-r$
$p^{2}+q+r$ (C) $p^{2}+q^{2}-r^{2}$ (D) $2\left(p^{2}-q+r\right)$

## - Watch Video Solution

$$
\begin{aligned}
& \text { 97. If the two roots of the equation } \\
& (c-1)\left(x^{2}+x+1\right)^{2}-(c+1)\left(x^{4}+x^{2}+1\right)=0 \text { and real and distinct }
\end{aligned}
$$

and $f(x)=\frac{1-x}{1+x}$ then $f(f(x))+f\left(f\left(\frac{1}{x}\right)\right)=$ (A) $-c$ (B) $c$ (C) $2 c$
(D) none of these

## (-) Watch Video Solution

98. Te least value of $|a|$ for which $\tan \theta$ and $\cot \theta$ are the roots of the equation $x^{2}+a x+b=0$ is (A) 2 (B) 1 (C) $\frac{1}{2}$ (D) 0

## - Watch Video Solution

99. Let $\left(y^{2}-5 y+3\right)\left(x^{2}+x+1\right)<2 x$ for all $x \varepsilon R$ then the interval in which y lies is (A) $\left(\frac{5-\sqrt{5}}{2}, \frac{5+\sqrt{5}}{2}\right)$ (B) $(-\infty,-2]$
$\left[-2,-\frac{2}{3}\right]$ (D) $(1,4)$

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100. If $P(x)$ be a polynomial satisfying the identity $P\left(x^{2}\right)+2 x^{2}+10 x=2 x P(x+1)+3$, then $P(x)$ is

## - Watch Video Solution

101. Tet $\alpha, \beta$ and $\gamma$ be the roots of $f(x)=x^{3}+x^{2}-5 x-1=0$. Then $[\alpha]+[\beta]+[\gamma]$, where $\left[^{*}\right]$ greatest integer function, is equal to

## Watch Video Solution

102. Let a,b,c be positive real parameter and $a x^{2}+\frac{b}{x^{2}} \geq c, \forall x \varepsilon R$ then
(A) $c^{2} \geq 4 a b$ (B) $4 c \geq b^{2}$
(C) $4 b c \geq c^{2}$
(D) $4 a c<b^{2}$

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103. The quadratic equatin $(2 x-a)(2 x-c)+\lambda(x-2 b)(x-2 d)=0$, (where $0<4 a<4 b<c<4 d$ ) has (A) a root between 2 b and 2d for all $\lambda$ (B) as root between b nd d for all $-v e \lambda$ (C) a root between b and d for all $+v e \lambda$ ( D ) none of these
104. The set of values of c for which $x^{3}-6 x^{2}+9 x-c$ is of the form $(x-a)^{2}(x-b)(\mathrm{a}, \mathrm{b}$ is real) is given by

## - Watch Video Solution

105. The number of real roots (s) of the equation $x^{2} \tan x=1$ lying between 0 and $2 \pi$ is /are (A) 1 (B) 2 (C) 3 (D) 4

## - Watch Video Solution

106. If 1 lies between the roots of the quadratic equation $3 x^{2}-(3 \sin \theta) x-2 \cos ^{2} \theta=0$, then :
A. $-\frac{\pi}{3}<\theta<\frac{5 \pi}{3}$
B. $n \pi<\theta<2 n \pi$
C. $2 n \pi+\frac{\pi}{6}<\theta<2 n \pi+\frac{5 \pi}{6}$
D. none of these

## Answer: null

## D Watch Video Solution

107. Let $\alpha$ and $\beta$ be the real and distinct roots of the equation $a x^{2}+b x+c=|c|,(a>0)$ and $p, q$ be the real and distinct roots of the equation $a x^{2}+b x+c=0$. Then which of the following is true? (A) p and q lie between $\alpha$ and $\beta$ (B) p and q lies outside $(\alpha, \beta)$ (C) only p lies between $\alpha$ and $\beta$ (D) only q lies between ( $\alpha$ and $\beta$ )

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108. The roots of the equation $a x^{2}+b x+c=0, a \in R^{+}$, are two consecutive odd positive integers. Then

## - Watch Video Solution

109. If equation $x^{5}+10 x^{2}+x+5=0$ has one roots as alpha then (A) $[\alpha]=-3$ (where [.] denotes the greatest integer function) (B) number of roots between -2 and -1 is three (C) number of real roots is 3 (D) equation has at least one positive root

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110. The
equation
$\frac{A}{x-a_{1}}+\frac{A_{2}}{x-a_{2}}+\frac{A_{3}}{x-a_{3}}=0$ where $_{1}, A_{2}, A_{3}>0$ and $a_{1}<a_{2}<a_{3}$ has two real roots lying in the invervals. (A) $\left(a_{1}, a_{2}\right)$ and ( $a_{2}, a_{3}$ )
$\left(-\infty, a_{1}\right)$ and $\left(a_{3}, \infty\right)$
(C) $\left(A_{1}, A_{3}\right)$ and $\left(A_{2}, A_{3}\right)$
(D) none of these

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111. If both roots of the equation $x^{2}-2 a x+a^{2}-1=0$ lie between -3 and 4 and [a] denotes the integral part of a, then [a] cannot be
B. -1
C. 1
D. 4

## Answer: null

## - Watch Video Solution

112. If $\alpha$ be the number of solutons of equation $[\sin x]=|x|$, where $[x]$ denotes the integral part of $x$ and $m$ be the greatest value of $\cos \left(x^{2}+x e^{x}-[x]\right)$ in the interval $[-1,1]$, then (A) $\alpha=m$ (B) $\alpha<m$ (C) $\alpha>m$ (D) $\alpha \neq m$

## - Watch Video Solution

113. If $m$ be the number of integral solutions of equation $2 x^{2}-3 x y-9 y^{2}-11=0$ and n be the roots of $x^{3}-[x]-3=0$, then

## - Watch Video Solution

114. If the roots of equation $a x^{2}+b x+10=0$ are not rel and istinct where $a, b \varepsilon R$, and $m$ and $n$ are values of a and b respectively for which $5 a+b$ is minimum then the family of lines $m(4 x+2 y+3)+n(x-y-10=0$ are concurrent at (A) $(1,-1)$ (B) $\left(-\frac{1}{6},-\frac{7}{6}\right)$ (C) ( 1,1 ) (D) none of these

## - Watch Video Solution

115. If $[x]$ denotes the integral part of x and $k=\sin ^{-1}\left(\frac{1+t^{2}}{2 t}\right)>0$ then integral valueof $\alpha$ for which the equation $(x-[k])(x+\alpha)-1=0$ has integral roots is (A) $1(B) 2(C) 4$ (D) none of these

## - Watch Video Solution

116. If $[x]$ denotes the integral part of x and $m=\left[\frac{|x|}{1+x^{2}}\right], n=$ integral values of $\frac{1}{2-\sin 3 x}$ then (A) $m \neq n$ (B) $m>n$ (C) $m+n=0$ (D) $n^{m}=0$

## - Watch Video Solution

117. If 1 lies between the roots of equation $y^{\text {? }}-m y+1=0$ and $[\mathrm{x}]$ denotes the integral part of x , then $\left[\left(\frac{4|x|}{x^{2}+16}\right)\right]$ where $x \in R$ is equal to

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118. If for $x>0 f(x)=\left(a-x^{n}\right)^{\frac{1}{n}}, g(x)=x^{2}+p x+q, p, q \varepsilon R$ and equation $g(x)-x=0$ has imaginary roots, then number of real roots of equation $g(g(x))-f(f(x))=0$ is (A) 0 (B) 2 (C) 4 (D) none of these
119. Let $f(x)=x^{3}+x^{2}+10 x+7 \sin x$, then the equation $\frac{1}{y-f(1)}+\frac{2}{y-f(2)}+\frac{3}{y-f(3)}=0$ has (A) no real root (B) one real roots (C) two real roots (D) more than two real roots

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120. If $0<\alpha<\beta<\gamma<\frac{\pi}{2}$ then the equation
$\frac{1}{x-\sin \alpha}+\frac{1}{x-\sin \beta}+\frac{1}{x-\sin \gamma}=0$ has (A) imaginary roots
real and equal roots (C) real and unequal roots (D) rational roots

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121. IF $a=\frac{x^{2}-2 x+4}{x^{2}+2 x+4}$ and equation of lines $A B$ and $C D$ be $3 y=x$ and $y=3 x$ respectively, then for all real x , point $P\left(a, a^{2}\right)$ (A) lies in the acute angle between lines $A B$ and $C D$ ( $B$ ) lies in the obtuse angle between lines $A B$ and $C D(C)$ cannot be in the acute angle between lines $A B$ and $C D$ ( $D$ ) cannot lie in the obtuse angle between lines $A B$ and

## (D) Watch Video Solution

122. If $f(x)=3^{x}+4^{x}+5^{x}-6^{x}$, then $f(x)<f(3)$ for (A) only one value of $x(B)$ no value of $x(C)$ only two value of $x(D)$ infinitely many value of $x$

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123. If $\alpha_{1}, \alpha_{2}$ are the roots of equation $x^{2}-p x+1=0$ and $\beta_{1}, \beta_{2}$ be those of equation $x^{2}-q x+1=0$ and vector $\alpha_{1} \hat{i}+\beta_{1} \hat{j}$ is parallel to $\alpha_{2} \hat{i}+\beta_{2} \hat{j}$ then (A) $p= \pm q$ (B) $p= \pm 2 q$ (C) $p=2 q$ (D) none of these

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124. If $\alpha_{1}, \alpha_{2}$ be the roots of the equation $x^{2}-p x+1=0$ and $\beta_{1}, \beta_{2}$ be those of equatiion
$x^{2}-q x+1=0$ and $p^{2}=q^{2}, \vec{u}=\alpha_{1} \hat{i}+\alpha_{2} \hat{j}$, and $\vec{v}=\beta_{1} \hat{i}+\beta_{2} \hat{j}$
then which one is necessarily
$\vec{u} \| \vec{v}$ or $\vec{u} \| \vec{w}$ (D) none of these

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125. If $a, b, c, d \varepsilon R$ and $f(x)=a x^{3}+b x^{2}-c x+d$ has local extrema at two points of opposite signs and $a b>0$ then roots of equation $a x^{2}+b x+c=0$ (A) are necessarily negative (B) have necessarily negative real parts (C) have necessarily positive real parts (D) are necessarily positive

## (D) Watch Video Solution

126. Let $f(x)=A x^{2}+B x+c$, where $A, B, C$ are real numbers. Prove that if $f(x)$ is an integer whenever $x$ is an integer, then the numbers
$2 A, A+B$, and $C$ are all integer. Conversely, prove that if the number $2 A, A+B$, and $C$ are all integers, then $f(x)$ is an integer whenever $x$ is integer.
127. Let $f(x)=A x^{2}+B x+c$, where $A, B, C$ are real numbers. Prove that if $f(x)$ is an integer whenever $x$ is an integer, then the numbers $2 A, A+B$, and $C$ are all integer. Conversely, prove that if the number $2 A, A+B$, and $C$ are all integers, then $f(x)$ is an integer whenever $x$ is integer.

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128. If $a(p+q)^{2}+2 b p q+c=0$ and $q(p+r)^{2}+2 b p r+c=0$ then (A)
$q r=p^{2}+\frac{c}{a}$
(B) $\quad q r=p^{2}-\frac{c}{a}$
(C) $\quad q+r=2 \frac{a+b}{a}$
$q+r=-2 \frac{a+b}{a}$

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129. If $\alpha$ and $\beta(\alpha<\beta)$ are the roots of the equation $x^{2}+b x+a=0$, wherea $<0<b$, then (A) $\alpha>0(B) \alpha<0$ (C) $\beta<0$
(D) $\beta<|\alpha|$

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130. Let $\alpha a n d \beta$ be the roots of $x^{2}-x+p=0 a n d \gamma a n d \delta$ be the root of $x^{2}-4 x+q=0$. If $\alpha, \beta, a n d \gamma, \delta$ are in G.P., then the integral values of pandq, respectively, are $-2,-32$ b. $-2,3$ c. $-6,3$ d. $-6,-32$

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131. If $2 a+3 b+6 c=0$, then prove that at least one root of the equation $a x^{2}+b x+c=0$ lies in the interval $(0,1)$.

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132. if $\alpha, \beta$ be roots of $x^{2}-3 x+a=0$ and $\gamma, \delta$ are roots of $x^{2}-12 x+b=0$ and $\alpha, \beta, \gamma, \delta$ (in order) form a increasing GP then find the value of $a \& b$
133. If the difference of the roots of the equation $x^{2}+k x+7=0$ is 6 , then possible values of $k$ are $k$ are (A) 4 (B)-4 (C) 8 D$)-8$

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134. If x real and $y=\frac{x^{2}-x+3}{x+2}$, then (A) $y \geq 1$ (B) $y \geq 11$ $y \leq-11$ (D) $-11<y<1$

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135. All soutions o the equations
$x^{2}+y^{2}-8 x-8 y=20$ and $x y+4 x+4 y=40$ satisfy the following
equation (s) (A) $x+y=10$
(B) $|x+y|=10$
(C) $|x-y|=10$
$x+y=-10$
136. Let $f(x)=\frac{3}{x-2}+\frac{4}{x-3}+\frac{5}{x-4}$. Then $f(x)=0$ has (A) exactly one real root in (2,3) (B) exactly one real root in (3,4) (C) at least one real root in ( 2,3 ) (D) none of these

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137. Let $f(x)=a x^{3}+b x^{2}+x+d$ has local extrema at $x=\alpha$ and $\beta$ such that $\alpha \beta<0$ and $f(\alpha) . f(\beta)>0$. Then the equation $f(x)=0$ (A) has 3 distinct real roots ( B ) has only one real which is positive o a. $f(\alpha)<0$ (C) has only one real root, which is negative $a . f(\beta)>0$ (D) has 3 equal roots

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138. If every pair from among the equations $x^{2}+p x+q r=0, x^{2}+q x+r p=0$ and $x^{2}+r x+p q=0$ has a common root, then the sum of the three common roots is
139. If each pair of the following equations
$x^{2}+p x+q r=0, x^{2}+q x+p r=0$ and $x^{2}+r x+p q=0 \quad$ has common root, then the product of the three common roots is (A) $2 p q r$ (B) $p q r$ (C) $-p q r$ (D) none of these

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140. If $a+b+2 c=0, c \neq 0$, then equation $a x^{2}+b x+c=0$ has (A) at least one root in $(0,1)(B)$ at least one root in $(0,2)(C)$ at least on root in $(-1,1)(D)$ none of these

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141. If al the roots oif $z^{3}+a z^{2}+b z+c=0$ are of unit modulus, then
(A) $|a| \leq 3$ (B) $|b| \leq 3$ (C) $|c|=1$ (D) none of these
142. If the product of the roots of the equatiin $2 x^{2}+a x+4 \sin a=0$ is 1, then the roots will be imaginary if (A) $a \varepsilon R$ (B) $a \varepsilon\left\{\frac{-7 \pi}{6}, \frac{\pi}{6}\right\}$ $a \varepsilon\left\{\frac{\pi}{6}, \frac{5 \pi}{6}\right\}(\mathrm{D})$ none of these

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143. If p and q are odd integers, then the equation $x^{2}+2 p x+2 q=0$ (A) has no integral root (B) has no rational root (C) has no irrational root (D) has no imaginary root

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144. Let $f(x)$ be a quadratic expression which is positive for all real x and $g(x)=f(x)+f^{\prime}(x)+f^{\prime \prime}(x)$.A quadratic expression $f(x)$ has same sign as that coefficient of $x^{2}$ for all real $x$ if and only if the roots of the corresponding equation $f(x)=0$ are imaginary. For function $f(x)$ and $g(x)$ which of the following is true (A) $f(x) g(x)>0$ for all
real x (B) $f(x) g(x)<0$ for all real x (C) $f(x) g(x)=0$ for some real x (D) $f(x) g(x)=0$ for all real x

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145. Let $f(x)$ be a quadratic expression which is positive for all real x and $g(x)=f(x)+f^{\prime}(x)+f^{\prime \prime}(x)$.A quadratic expression $f(x)$ has same sign as that coefficient of $x^{2}$ for all real $x$ if and only if the roots of the corresponding equation $f(x)=0$ are imaginary.Which of the following holds true? (A) $g(0) g(1)<0$ (B) $g(0) g(-1)<0$ (C) $g(0) f(1) f(2)>0$ (D) $f(0) f(1) f(2)<0$

## - Watch Video Solution

146. Let $f(x)$ be a quadratic expression which is positive for all real x and $g(x)=f(x)+f^{\prime}(x)+f^{\prime \prime}(x)$. A quadratic expression $f(x)$ has same sign as that coefficient of $x^{2}$ for all real $x$ if and only if the roots of the corresponding equation $f(x)=0$ are imaginary.lf
$F(x)=\int_{a}^{x^{3}} g(t) d t, \operatorname{the} F(x)$ is (A) an incresing function in R (B) an increasing function only in $[0, \infty$ ) (C) a decreasing function $R$ (D) a decreasing function only in $[0, \infty)$

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147. Let $\alpha+\iota \beta, \alpha, \beta \varepsilon R$ be a root of $x^{3}+q x+r=0$ If $\gamma$ be a real root of equation $x^{3}+q x+r=0$ then $\gamma(\mathrm{A})-2 \alpha$ (B) $\alpha$ (C) $2 \alpha$ (D) $-\alpha$

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148. Let $\alpha+i \beta(\alpha, \beta \in R)$ be a root of the equation $x^{3}+q x+r=0, q, r \in R$. Find a real cubic equation, independent of $\alpha a n d \beta$, whose one roots is $2 \alpha$.

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149. Number of real roots of equation $f(x)=0$ is (A) 0 (B) 1 (C) 2 (D) none of these

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150. If $\alpha$ is root of equation $f(x)=0$ then the value of $\left(\alpha+\frac{1}{\alpha}\right)^{2}+\left(\alpha^{2}+\frac{1}{\alpha^{2}}\right)^{2}+\left(\alpha^{3}+\frac{1}{\alpha^{3}}\right)+\ldots \ldots \ldots+\left(\alpha^{6}+\frac{1}{\alpha^{6}}\right)^{2}$ is (A) 18 (B) $54(\mathrm{C}) 6(\mathrm{D}) 12$

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151. Range of vlaues of $f(x)$ is (A) $\left(-\infty, \frac{3}{4}\right]$ (B) $\left[\frac{3}{4}, \infty\right)$ (C) $\left[\frac{1}{3}, 3\right]$ none of these

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152. The set of all value of a for which one root of equation $x^{2}-a x+1=0$ is less than unity and other greater than unity (A) $(-\infty, 2)$ (B) $(2, \infty)$ (C) $(1, \infty)$ (D) none of these

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153. The set of all values of a for which both roots of equation $x^{2}-a x+1=0$ are less than unity is (A) $(-\infty,-2)(\mathrm{B})(-2, \infty)$
$(-2,3)$ (D) $(-\infty,-1)$

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154. The set of all values of a for which both roots of equation $x^{2}-2 a x+a^{2}-1=0$ lies between -2 and 4 is (A) $(-1,2)$ (B) $(1,3)$ (C) $(-1,3)$ (D) none of these

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155. If $a, b, c$ are rational then roots of equation $a b c^{2} x^{2}+3 a^{2} c x+b^{2} c x-6 a^{2}-a b+2 b^{2}=0 \quad$ are (A) irrational rational (C) imaginary (D) irrational if $a^{2}<b$

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156. If n and r are positive integers such that $0<r<n$ then roots of the equation ${ }^{\wedge} n C_{r} x^{2}+2 \cdot{ }^{n} C_{r+1} x+{ }^{n} C_{r+2}=0 \quad$ are necessarily (A) imaginary (B) real and equal (C) real and unequal (D) real but may be equal or unequal

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157. If $a x^{3}+b x^{2}+c x+d$ has local extremum at two points of opposite signs then roots of equation $a x^{2}+b x+c=0$ are necessarily (A) rational (B) real and unequal (C) real and equal (D) imaginary
158. If $\alpha$ and $\beta$ are the roots of the equation $a x^{2}+b x+c=0$ then $a x^{2}+b x+c=a(x-\alpha)(x-\beta)$.Also if a quadratic equation $f(x)=0$ has both roots between $m$ and $n$ then $f(m)$ and $f(n)$ must have same sign. It is given that all the quadratic equations are of form $a x^{2}-b x+c=0 a, b, c \varepsilon N$ have two distict real roots between 0 and 1 .The least value of a for which such a quadratic equation exists is (A) 3 (B) 4 (C) 5 (D) 6

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159. If $\alpha$ and $\beta$ are the roots of the equation $a x^{2}+b x+c=0$ then $a x^{2}+b x+c=a(x-\alpha)(x-\beta)$.Also if a quadratic equation $f(x)=0$ has both roots between $m$ and $n$ then $f(m)$ and $f(n)$ must have same sign. It is given that all the quadratic equations are of form $a x^{2}-b x+c=0 a, b, c \varepsilon N$ have two distict real roots between 0 and 1 .The least value of $b$ for which such a quadratic equation exists is (A) 3 (B) 4 (C) 5 (D) 6
160. If $\alpha$ and $\beta$ are the roots of the equation $a x^{2}+b x+c=0$ then $a x^{2}+b x+c=a(x-\alpha)(x-\beta)$.Also if a quadratic equation $f(x)=0$ has both roots between $m$ and $n$ then $f(m)$ and $f(n)$ must have same sign. It is given that all the quadratic equations are of form $a x^{2}-b x+c=0 a, b, c \varepsilon N$ have two distict real roots between 0 and 1 . The least value of $c$ for which such a quadratic equation exists is (A) 1 1 (B) 2 (C) 3 (D) 4

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161. The number of real root (s) of the equation $x^{2} \tan x=1$ lying between 0 and $2 \pi$ is /are.

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162. Find the number of quadratic equations, which are unchanged by squaring their roots.

## (D) Watch Video Solution

163. If $x$ and $y$ satisfy the equation $y=2[x]+3$ and $y=3[x-2]$ simultaneously, where [.] denotesthe greatest integer function, then $[x+y]$ is equal to

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164. If $(\sqrt{2+\sqrt{3}})^{x}+(\sqrt{2-\sqrt{3}})^{x}=2^{x}$, then $\mathrm{x}=$

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165. Given that $\alpha, \gamma$ are roots of the equation $A x^{2}-4 x+1=0, \operatorname{and} \beta, \delta$ the roots of the equation of $B x^{2}-6 x+1=0$, such that $\alpha, \beta, \gamma$, and $\delta$ are in H.P., then a. $A=3 \mathrm{~b}$. $A=4 B=2$ d. $B=8$
166. Let $\alpha$ be the root of the equation $a x^{2}+b x+c=0$ and $\beta$ be the root of the equation $a x^{2}-b x-c=0$ where $\alpha<\beta$ Assertion (A): Equation $a x^{2}+2 b x+2 c=0$ has exactly one root between $\alpha$ and $\beta$, Reason $(\mathrm{R})$ : A continuous function $f(x)$ vanishes odd number of times between a and b if $f(a)$ and $f(b)$ have opposite signs. (A) Both A and R are true and $R$ is the correct explanation of $A(B)$ Both $A$ and $R$ are true $R$ is not te correct explanation of $A$ (C) $A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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167. Let $f(x)=a x^{3}+b x^{2}+c x+d=0$ have extremum of two different points of opposite signsAssertion (A): Equation $a x^{2}+b x+c=0$ has distinct real roots., Reason (R): A differentiable function $f(x)$ has extremum only at points where $f^{\prime}(x)=0(\mathrm{~A})$ Both A and R are true and $R$ is the correct explanation of $A(B)$ Both $A$ and $R$ are true $R$ is not the
correct explanation of $A(C) A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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168. Assertion (A): Equation $\quad(x-p)(x-q)-r=0 \quad$ where $p, q, r \varepsilon R$ and $0<p<q<r$ has roots in $(p, q)$, Reason(R): A polynomial equation $f(x)=0$ has odd number of roots between $a$ and $b(a<b)$ if $f(a)$ and $f(b)$ have opposite signs (A) Both A and R are true and $R$ is the correct explanation of $A(B)$ Both $A$ and $R$ are true $R$ is not the correct explanation of $A$ (C) A is true but $R$ is false. (D) $A$ is false but R is true.

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169. Assertion (A): Equation $(x-a)(x-b)-2=0, a<b$ has one root less than a and other root greater than b., Reason (R): A polynomial equation $f^{\prime}(x)=0$ has even number of roots between $a$ and $b$ if $f(a)$ and $f(b)$ have opposite signs. (A) Both A and R are true and R is the
correct explanation of $A(B)$ Both $A$ and $R$ are true $R$ is not the correct explanation of $A(C) A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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170. Assertion (A): For $0<a<b<c$ equation $(x-a)(x-b)-c=0$ has no roots in ( $a, b$ ), Reason (R):For a continuous function $f(x)$ equation $f^{\prime}(x)=0$ has at least one root between a and b if $f(a)$ and $f(b)$ are equal. (A) Both A and R are true and R is the correct explanation of $A(B)$ Both $A$ and $R$ are true $R$ is not the correct explanation of $A$ (C) $A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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171. Assertion (A): For $\alpha<\beta$ equation $(x-\cos \alpha)(x-\cos \beta)-2=0$ has one root less than $\cos \beta$ and other greater than $\cos \alpha$., Reason (R): Quadratic expressionax $x^{2}+b x+c$ has sign opposite to that of a between the roots $\alpha$ and $\beta$ of equation $a x^{2}+b x+c=0$ if $\alpha<\beta$ (A) Both $A$ and $R$ are true and $R$ is the correct explanation of $A(B)$ Both $A$ and
$R$ are true $R$ is not te correct explanation of $A(C) A$ is true but $R$ is false.
(D) A is false but R is true.

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172. LET the equation $a x^{2}+b x+c=0$ has no real roots Assertion (A): $c(a+b+c)>0$, Reason (R): A quadratic expression $a x^{2}+b x+c$ has signs same as that of al for all real x if the roots of the corresponding equation $a x^{2}+b x+c=0$ are imaginary. (A) Both A and R are true and $R$ is the correct explanation of $A$ (B) Both $A$ and $R$ are true $R$ is not te correct explanation of $A$ (C) $A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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173. Assertion (A): Quadratic equation $f(x)=0$ has real and distinct roots. Reason ( R ): quadratic equation $\mathrm{f}(\mathrm{x})=0$ has even number of roots between p and $q(p<q)$ if $f(p)$ and $f(q)$ have same sign. (A) Both A and $R$ are true and $R$ is the correct explanation of $A(B)$ Both $A$ and $R$ are true
$R$ is not the correct explanation of $A$ (C) $A$ is true but $R$ is false. (D) $A$ is false but $R$ is true.

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174. Let $a, b, c$ be real. If $a x^{2}+b x+c=0$ has two real roots $\alpha a n d \beta$, where $\alpha\langle-1 \operatorname{and} \beta\rangle 1$, then show that $1+\frac{c}{a}+\left|\frac{b}{a}\right|<0$

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175. The real numbers $x_{1}, x_{2}, x_{3}$ satisfying the equation $x^{3}-x^{2}+b x+\gamma=0$ ar ein A.P. Find the intervals in which $\beta a n d \gamma$ lie.

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176. The sum of all the real roots of the equation $|x-2|^{2}+|x-2|-2=0$ is
177. The equation $\sqrt{x+1}-\sqrt{x-1}=\sqrt{4 x-1}$ has (1997C, 2 M ) no solution (b) one solution two solution (d) more than two solution

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178. Let $S$ be a square of nit area. Consider any quadrilateral, which has none vertex on each side of $S$. If $a, b$, candd denote the lengths of the sides of het quadrilateral, prove that $2 \leq a^{2}+b^{2}+c^{2}+x^{2} \leq 4$.

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179. Let $f(x)=A x^{2}+B x+c$, where $A, B, C$ are real numbers. Prove that if $f(x)$ is an integer whenever $x$ is an integer, then the numbers $2 A, A+B$, and $C$ are all integer. Conversely, prove that if the number $2 A, A+B$, and $C$ are all integers, then $f(x)$ is an integer whenever $x$ is integer.
180. A triangle $P Q R, \angle R=90^{\circ}$ and $\tan \left(\frac{P}{2}\right)$ and $\tan \left(\frac{Q}{2}\right)$ roots of the $a x^{2}+b x+c=0$ then prove that $a+b=c$

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181. If roots of the equation $x^{2}-2 a x+a^{2}+a-3=0$ are real and less than 3 then $a) a<2$ b) $2 \leq a \leq 3$ c) $3 l 3 a \leq 4$ d) $a>4$

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182. If $\alpha$ and $\beta$ ('alpha

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183. If $b>a$, then the equation $(x-a)(x-b)-1=0$ has (2000,1M) both roots in $(a, b)$ both roots in $(-\infty, a)$ both roots in $(b,+\infty)$ one
root in $(-\infty, a)$ and the other in $(b, \infty)$

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184. For the equation $3 x^{2}+p x+3=0, p>0$, if one of the root is square of the other, then $p$ is equal to $\frac{1}{3}$ (b) 1 (c) 3 (d) $\frac{2}{3}$

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185. If $\alpha, \beta$ are the roots of $a x^{2}+b x+c=0,(a \neq 0)$ and $\alpha+\delta, \beta+\delta$ are the roots of $A x^{2}+B x+C=0,(A \neq 0)$ for some constant $\delta$ then prove that $(2000,4 \mathrm{M}) \frac{b^{2}-4 a c}{a^{2}}=\frac{B^{2}-4 A C}{A^{2}}$

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186. Let $\alpha a n d \beta$ be the roots of $x^{2}-x+p=0 a n d \gamma a n d \delta$ be the root of $x^{2}-4 x+q=0$. If $\alpha, \beta, a n d \gamma, \delta$ are in G.P., then the integral values of pandq, respectively, are $-2,-32$ b. $-2,3$ c. $-6,3$ d. $-6,-32$
187. Let $-1 \leq p \leq 1$. Show that the equation $4 x^{3}-3 x-p=0$ has a unique root in the interval $[1 / 2,1]$ and identify it.

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188. Let $a, b, c$ be real numbers with $a \neq 0$ andlet $\alpha, \beta$ be the roots of the equation $a x^{2}+b x+c=0$. Express the roots of $a^{3} x^{2}+a b c x+c^{3}=0$ in terms of $\alpha, \beta$.

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189. The number of solution of $\log _{4}(x-1)=\log _{2}(x-3)$ is (A) 3 (B) 5
(C) 2 (D) 0

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190. Let $f(x)=\left(1+b^{2}\right) x^{2}+2 b x+1$ and let $m(b)$ the minimum value of $f(x)$. As $b$ varies, the range of $m(b)$ is $[0,1]$ (b) $\left(0, \frac{1}{2}\right]\left[\frac{1}{2}, 1\right]$ $(0,1]$

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191. The set of all real numbers $x$ for which $x^{2}-|x+2|+x>0$ is $(-\infty,-2)$ b. $(-\infty,-\sqrt{2}) \cup(\sqrt{2}, \infty)$ c. $(-\infty,-1) \cup(1, \infty)$ d. $(\sqrt{2}, \infty)$

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192. If $x^{2}+(a-b) x=(1-a-b)=0$. wherea, $b \in R$, then find the values of $a$ for which equation has unequal real roots for all values of $b$.

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193. If $f(x)=x^{2}+2 b x+2 c^{2}$ and $g(x)=-x^{2}-2 c x+b^{2}$ such that $\min f(x)>\max g(x)$, then the relation between $a$ and $c$ is (1) Non real value of $b$ and $c(2) 0<c b s q r 2(3)|c|<|b| \sqrt{2}(4)|c|>|b| \sqrt{2}$

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194. For all $x, \mathrm{x}^{\wedge} 2+2 \mathrm{ax}+10-3 \mathrm{a}>0^{\prime}$, then the interval in which a lies is

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195. If one root is square of the other root of the equation $x^{2}+p x+q=0$, then the relation between $p a n d q$ is $(2004,1 \mathrm{M})$ $p^{3}-(3 p-1) q+q^{2}=0 \quad p^{3}-q(3 p+1)+q^{2}=0$ $p^{3}+q(3 p-1)+q^{2}=0 p^{3}+q(3 p+1)+q^{2}=0$

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196. If $\alpha, \beta$ are the roots of $a x^{2}+b x+c=0,(a \neq 0)$ and $\alpha+\delta, \beta+\delta$ are the roots of $A x^{2}+B x+C=0,(A \neq 0)$ for some constant $\delta$ then prove that $(2000,4 \mathrm{M}) \frac{b^{2}-4 a c}{a^{2}}=\frac{B^{2}-4 A C}{A^{2}}$

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197. If $a, b, c$, are the sides of a triangle $A B C$ such that $x^{2}-2(a+b+c) x+3 \lambda(a b+b c+c a)=0$ has real roots, then (2006, 3м) $\lambda<\frac{4}{3}$ (b) $\lambda>\frac{5}{3} \lambda\left(\frac{4}{3}, \frac{5}{3}\right)$ (d) $\lambda\left(\frac{1}{3}, \frac{5}{3}\right)$

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198. If $x^{2}-10 a x-11 b=0$ have roots cand $\cdots x^{2}-10 c x-11 d=0$ have roots $a a n d b$, then find $a+b+c+d(2006,6 \mathrm{M})$

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199. Let $\alpha, \beta$ be the roots of the equation $x^{2}-p x+r=0 a n d \alpha / 2,2 \beta$ be the roots of the equation $x^{2}-q x+r=0$. Then the value of $r$ is $\frac{2}{9}(p-q)(2 q-p) \quad$ b. $\quad \frac{2}{9}(q-p)(2 q-p) \quad$ c. $\quad \frac{2}{9}(q-2 p)(2 q-p) \quad$ d. $\frac{2}{9}(2 p-q)(2 q-p)$

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200. The smallest value of $k$ for which both the roots of the equation $x^{2}-8 k x+16\left(k^{2}-k+1\right)=0$ are real, distinct and have values at least 4, is.

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