



India's Number 1 Education App

## MATHS

### BOOKS - KC SINHA MATHS (HINGLISH)

### TRIGONOMETRIC FUNCTIONS - SUM AND DIFFERENCE OF ANGLES - FOR BOARDS

#### Solved Examples

1. find value of  $\cos 15^\circ$



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2.. Find the value of  $\sin 105^\circ$



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3. Find the value :  $\tan 105^0$



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4. Show that:  $\sin\left(\frac{\pi}{2} - x\right) = \cos x$



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5. Show that  $\tan 75^0 + \cot 75^0 = 4$



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6. Evaluate  $\sin\left(n\pi + (-1)^n \frac{\pi}{4}\right)$ , where n is an integer.



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7. Prove that:  $2s \in^2 \frac{3\pi}{4} + 2\frac{\cos^2 \pi}{4} + \sec^2 \frac{\pi}{3} = 10$



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$$8. 2 \sin^2 \frac{\pi}{6} + \cos ec^2 \frac{7\pi}{6} \cos^2 \frac{\pi}{3} = \frac{3}{2}$$



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9. If  $A$  and  $B$  are positive acute angles and  $\cos A = \frac{1}{7}$ ,  $\cos B = \frac{13}{14}$ ,  
then show that  $A - B = 60^\circ$ .



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10. If  $\sin A = \frac{3}{5}$ ,  $0 < A < \frac{\pi}{2}$  and  $\cos B = -\frac{12}{13}$ ,  $\pi < B < 3\frac{\pi}{2}$ , find  
that :  $\sin(A - B)$



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11. If  $\sin A = \frac{3}{5}$ ,  $0 < A < \frac{\pi}{2}$  and  $\cos B = -\frac{12}{13}$ ,  $\pi < B < 3\frac{\pi}{2}$ , find that :  $\cos(A + B)$



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12. If  $\sin A = \frac{3}{5}$ ,  $0 < A < \frac{\pi}{2}$  and  $\cos B = -\frac{12}{13}$ ,  $\pi < B < 3\frac{\pi}{2}$ , find that :  $\tan(A - B)$



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13. Show that  $\sin 70^\circ \cos 10^\circ - \cos 70^\circ \sin 10^\circ = \frac{\sqrt{3}}{2}$



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14. Prove that :  
 $\cos(45^\circ - A)\cos(45^\circ - B) - \sin(45^\circ - A)\sin(45^\circ - B) = \sin(A + B)$



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**15.** Prove that  $\tan 70 = 2 \tan 50 + \tan 20$

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**16.** Prove that:  $\cos 18^0 - \sin 18^0 = \sqrt{2} \sin 27^0$

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**17.** Prove that:  $\frac{\sin(x + y)}{\sin(x - y)} = \frac{\sin x \cdot \cos y + \cos x \cdot \sin y}{\sin x \cdot \cos y - \cos x \cdot \sin y}$

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**18.** Prove that:  $\frac{\sin(A - B)}{\cos A \in B} + \frac{\sin(B - C)}{\cos B \cos C} + \frac{\sin(C - A)}{\cos C \cos A} = 0$

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19. Show that  $\cot\left(\frac{\pi}{4} + x\right)\cot\left(\frac{\pi}{4} - x\right) = 1$



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20. Prove that:  
 $\cot x \cot 2x \cot 3x = \cot 3x \cot 2x \cot x$



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21. Prove that:  $\cos^2 2x - \cos^2 6x = \sin 4x \sin 8x$



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22. Prove that:  
 $\cos 2\theta \cos 2\phi + \cos^2(\theta + \phi) - \cos^2(\theta - \phi) = \cos(2\theta + 2\phi)$



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23.

Prove

that:

$$\cos^2 A + \cos^2 B - 2 \cos A \cos B \cos(A + B) = \sin^2(A + B)$$



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24. If  $A + B = 45^\circ$ , then the value of  $(1 + \tan A)(1 + \tan B)$  is



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25. If  $\sin \alpha \sin \beta - \cos \alpha \cos \beta + 1 = 0$ , then the value of  $1 + \cot \alpha \tan \beta$

is



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26. If  $\tan \alpha = x + 1$ ,  $\tan \beta = x - 1$ , show that  $2 \cot(\alpha - \beta) = x^2$



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27. If  $\cos(\alpha - \beta) + \cos(\beta + \gamma) + \cos(\gamma - \alpha) = -\frac{3}{2}$ , prove that:

$$\cos \alpha + \cos \beta + \cos \gamma = \sin \alpha + \sin \beta + \sin \gamma = 0$$



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28. If  $\tan \beta = \frac{n \sin \alpha \cos \alpha}{1 - n \sin^2 \alpha}$ , show that  $\tan(\alpha - \beta) = (1 - n)\tan \alpha$



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29. If  $\alpha$  and  $\beta$  are the solution of the equation  $a \sec \theta + b \tan \theta = c$ , then

$$\text{show that } \tan(\alpha + \beta) = \frac{2bc}{b^2 - c^2}$$



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30. If  $3 \tan \theta \tan \phi = 1$ . Prove that  $2 \cos(\theta + \phi) = \cos(\theta - \phi)$ .



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31.  $A + B = C$  and  $\tan A = k \tan B$ , then prove that

$$\sin(A - B) = \frac{k - 1}{k + 1} \sin C$$



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32. Find the sign of the expression  $\sin \theta + \cos \theta$  when  $\theta = 100^\circ$



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33. Find the maximum and minimum values of the expression:

$$a \cos \theta + b \sin \theta$$



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34. Find the maximum and minimum values of the expression:

$$3 \cos \theta + 5 \sin\left(\theta - \frac{\pi}{6}\right)$$



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35. Prove that  $5 \cos \theta + 3 \cos\left(\theta + \frac{\pi}{3}\right) + 3$  lies between  $-4$  and  $10$ .



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36. Express each of that as the sum or difference of cosines and sines:

$$2 \sin 3\theta \cdot \cos \theta$$



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37. Express each of the following as the sum or difference of sines and

$$\cosines: 2 \cos 7\theta \cos 3\theta$$



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38. Express each of that as the sum or difference of cosines and sines:

$$5 \sin \theta \cdot \sin 8\theta$$



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**39.** Express each of that as the sum or difference of cosines and sines:

$$\cos 75^\circ \cos 15^\circ$$



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**40.** Show that:  $s \in 50^\circ \cos 85^\circ = \frac{1 - \sqrt{2}\sin 35^\circ}{2\sqrt{2}}$



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**41.** Prove that  $\sin 20^\circ \sin 40^\circ \sin 80^\circ = \frac{\sqrt{3}}{8}$ .



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**42.** Prove that:  $2 \cos \frac{\pi}{13} \cos \frac{9\pi}{13} + \cos \frac{3\pi}{13} + \cos \frac{5\pi}{13} = 0$



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**43.** Prove that  $\sin A s \in (60^0 - A) s \in (60^0 + A) = \frac{1}{4} \sin 3A$



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**44.**  $\tan 20^\circ \tan 40^\circ \tan 80^\circ$



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**45.** Show that  $4 \sin \alpha \cdot \sin\left(\alpha + \frac{\pi}{3}\right) \sin\left(\alpha + 2\frac{\pi}{3}\right) = \sin 3\alpha$



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**46.** Prove that  $\frac{2 \cos 2A + 1}{2 \cos 2A - 1} = \tan(60^0 + A) \tan(60^0 - A)$



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47.

show

that

$$\sin A \cdot \sin(B - C) + \sin B \cdot \sin(C - A) + \sin C \cdot \sin(A - B) = 0.$$



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48. If  $\alpha + \beta + 90^\circ$ , find the maximum and minimum values of  $s \in \alpha s \in \beta$ .



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49. Express each of that as product of sines and cosines :  $\sin 4\theta + \sin 3\theta$



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50. Express each of that as product of sines and cosines :  $\sin 6\theta - \sin 2\theta$



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51. Express each of that as product of sines and cosines :  $\cos 2\theta + \cos 8\theta$

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52. Express each of that as product of sines and cosines :  $\cos 4\theta - \cos 6\theta$

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53. Prove that:  $\cos 18^\circ - \sin 18^\circ = \sqrt{2}\sin 27^\circ$

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54. Prove that :  $\frac{\sin 5\theta + \sin 3\theta}{\cos 5\theta + \cos 3\theta} = \tan 4\theta$

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55.  $\frac{\sin 3\theta + \sin 5\theta + \sin 7\theta + \sin 9\theta}{\cos 3\theta + \cos 5\theta + \cos 7\theta + \cos 9\theta}$



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$$56. \frac{\sin(\theta + \phi) - 2\sin\theta + \sin(\theta - \phi)}{\cos(\theta + \phi) - 2\cos\theta + \cos(\theta - \phi)} = \tan\theta$$



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$$57. \text{Prove that : } (\cos\alpha + \cos\beta)^2 + (\sin\alpha + \sin\beta)^2 = 4\cos^2\left(\frac{\alpha - \beta}{2}\right)$$



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58.

Prove

that

$$\cos\alpha + \cos\beta + \cos\gamma(\alpha + \beta + \gamma) = 4 \frac{\cos(\alpha + \beta)}{2} \frac{\cos(\beta + \gamma)}{2} \frac{\cos(\gamma + \alpha)}{2}$$



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59. If  $\cos(A + B)\sin(C - D) = \cos(A - B)\sin(C + D)$ , then show that

$$\tan A \tan B \tan C + \tan D = 0$$



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60. If  $s \int h \eta = n \sin(\theta + 2\alpha)$ , prove that  $\tan(\theta + \alpha) = \frac{1+n}{1-n} \tan \alpha$ .



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61. If  $\frac{\sin(\theta + \alpha)}{\cos(\theta - \alpha)} = \frac{1-m}{1+m}$ , prove that  $\tan\left(\frac{\pi}{4} - \theta\right) \tan\left(\frac{\pi}{4} - \alpha\right) = m$



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## Exercise

1. Find the value of :  $\cos 210^\circ$



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2. Using the formula of  $\sin(A - B) = \sin A \cos B - \cos A \sin B$  find the value of  $\sin 15^\circ$

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3. Find the value of :  $\sin 75^\circ$

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4. Find the value of :  $\tan 15^\circ$

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5. Find the value of :  $\tan 75^\circ$

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6. Find  $\tan(-330^\circ)$



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7. Find the value of :  $\cos 1395^\circ$



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8.  $\tan\left(\frac{11\pi}{12}\right)$



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9. Find the value of  $\tan \frac{13\pi}{12}$ .



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10. Prove that:  $s \in 105^\circ + \cos 105^\circ = \cos 45^\circ$



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$$11. \sin 300^\circ \cos ec 1050^\circ - \tan(-120^\circ)$$



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$$12. \sin 690^\circ \cos 930^\circ + \tan(-765^\circ) \cos ec(-1170^\circ)$$



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$$13. \text{Find the value of the : } \cos^2\left(\frac{\pi}{6}\right) + \cos ec\left(5\frac{\pi}{6}\right) + 3 \tan^2\left(\frac{\pi}{6}\right)$$



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$$14. \text{Prove that: } 2\frac{\sin \pi}{6} \sec \frac{\pi}{3} - 4\frac{\sin(5\pi)}{6} \frac{\cos \pi}{4} = 1$$



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**15.** Find the value of the :  $\sin^2\left(\frac{\pi}{6}\right) + \cos^2\left(\frac{\pi}{3}\right) - \tan^2\left(\frac{\pi}{4}\right)$



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**16.** Prove that :  $\sin 75^\circ = \frac{\sqrt{6} + \sqrt{2}}{4}$



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**17.** Find the value of :  $\tan 15^\circ$



**Watch Video Solution**

**18.** Evaluate  $\tan\left\{(-1)^n \frac{\pi}{4}\right\}$  where n is an integer



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19.  $\alpha = \frac{1}{\sqrt{10}} \cdot \sin \beta = \frac{1}{\sqrt{5}}$  (where  $\alpha, \beta$  and  $\alpha + \beta$  are positive acute angles). show that  $\alpha + \beta = \frac{\pi}{4}$



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20. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$ ,  $0 < B < \frac{\pi}{2}$ .

Find the values of that :  $\sin(A + B)$



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21. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$ ,  $0 < B < \frac{\pi}{2}$ .

Find the values of that :  $\cos(A + B)$



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22. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$ ,  $0 < B < \frac{\pi}{2}$ .

Find the values of that :  $\sin(A - B)$



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23. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$ ,  $0 < B < \frac{\pi}{2}$ .

Find the values of that :  $\cos(A - B)$



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24. If  $\sin A = \frac{1}{2}$ ,  $\cos B = \frac{\sqrt{3}}{2}$  , where  $\frac{\pi}{2} < A < \pi$  and  $0 < B < \frac{\pi}{2}$ ,

find that :  $\tan(A + B)$



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25. If  $\sin A = \frac{1}{2}$ ,  $\cos B = \frac{\sqrt{3}}{2}$  , where  $\frac{\pi}{2} < A < \pi$  and  $0 < B < \frac{\pi}{2}$ ,

find that :  $\tan(A-B)$



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**26.** if  $\sin x = \frac{3}{5}$ ,  $\cos y = -\frac{12}{13}$  where  $\frac{\pi}{2} < x < \pi$  and  $\frac{\pi}{2} < y < \pi$   
then show that  $\sin(x+y) = -\frac{56}{65}$



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**27.** Evaluate :  $\cos^2\left(\frac{\pi}{4} + x\right) - \sin^2\left(\frac{\pi}{4} - x\right)$



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**28.** Evaluate :  $\sin^2(15^\circ + A) - \sin^2(15^\circ - A)$



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**29.**  $\sin^2\left(\frac{\pi}{8} + \frac{A}{2}\right) - \sin^2\left(\frac{\pi}{8} - \frac{A}{2}\right)$  is equal to :



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30.

Prove

that:

$$\cos\left(\frac{3\pi}{2} + x\right) \cos(2\pi + x) \left\{ \cot\left(\frac{3\pi}{2} - x\right) + \cot(2\pi + x) \right\} = 1$$



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31. Prove that  $\frac{\cos(\pi + \theta)\cos(-\theta)}{\cos(\pi - \theta)\cos\left(\frac{\pi}{2} + \theta\right)} = -\cot\theta$



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32. Show that :  $\cos 70^\circ \cdot \cos 10^\circ + \sin 70^\circ \cdot \sin 10^\circ = \frac{1}{2}$



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33. Evaluate the following:  $s \in 78^\circ \cos 18^\circ - \cos 78^\circ s \in 18^\circ$



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$$34. \sin(40 + \theta) \cdot \cos(10 + \theta) - \cos(40 + \theta) \sin(10 + \theta) = \frac{1}{2}$$

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$$35. \sin(n+1)x \sin(n+2)x + \cos(n+1)x \cos(n+2)x = \cos x$$

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36. Prove that:

$$\cos\left(\frac{\pi}{4} - x\right) \cos\left(\frac{\pi}{4} - y\right) - \sin\left(\frac{\pi}{4} - x\right) \sin\left(\frac{\pi}{4} - y\right) = \sin(x + y)$$

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$$37. (\sin 3x + \sin x) \sin x + (\cos 3x - \cos x) \cos x = 0$$

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$$38. \text{ Prove that: } \frac{\tan\left(\frac{\pi}{4} + x\right)}{\tan\left(\frac{\pi}{4} - x\right)} = \left(\frac{1 + \tan x}{1 - \tan x}\right)^2$$



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$$39. \text{ Prove that: } \frac{\cos 20^0 - \sin 20^0}{\cos 20^0 + \sin 20^0} = \tan 25^0$$



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$$40. \text{ Prove that: } \cos 9^0 + \sin 9^0 = \sqrt{2}\sin 54^0$$



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$$41. \text{ Prove that: } \frac{\tan A + \tan B}{\tan A - \tan B} = \frac{\sin(A + B)}{\sin(A - B)}$$



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**42.** Prove that:  $\tan 8\theta - \tan 6\theta - \tan 2\theta = \tan 8\theta \tan 6\theta \tan 2\theta$ .



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**43.** The value of  $\tan 9^\circ + \tan 36^\circ + \tan 9^\circ \cdot \tan 36^\circ$  is equal to



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**44.** Show that

$$\tan 3x + \tan 2x + \tan x = \tan 3x + \tan 2x + \tan x$$

.



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**45.** Show that :  $\frac{1}{\tan 3A - \tan A} - \frac{1}{\cot 3A - \cot A} = \cot 2A$



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$$46. \text{ Show that: } \frac{1}{\tan 3A + \tan A} - \frac{1}{\cot 3A + \cot A} = \cot 4A$$

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$$47. \text{ Prove that: } \sin^2 6x - \sin^2 4x = \sin 2x \sin 10x$$

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$$48. \tan(\alpha + \beta)\tan(\alpha - \beta) = \frac{\sin^2 \alpha - \sin^2 \beta}{\cos^2 \alpha - \sin^2 \beta}$$

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$$49. \quad 19. \quad \text{Prove that} \\ \sin(A + B)\sin(A - B) + \sin(B + C)\sin(B - C) + \sin(C + A)\sin(C - A)$$

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50. Show that  $\tan\{(2n+1)\pi + \theta\} + \tan\{(2n+1)\pi - \theta\} = 0$



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51. If  $\tan \alpha = \frac{m}{m+1}$  and  $\tan \beta = \frac{1}{2m+1}$ , then  $\alpha + \beta$  is equal to



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52. If  $A + B = \frac{\pi}{4}$ , show that  $(\cot A - 1)(\cot B - 1) = 2$



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53. if  $8\theta = \pi$  show that  $\cos 7\theta + \cot \theta = 0$



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54. if  $\tan \alpha - \tan \beta = x$  and  $\cot \beta - \cot \alpha = y$  prove that

$$\cot(\alpha - \beta) = \frac{x + y}{xy}$$



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55. if  $\tan \alpha = 2 \tan \beta$  show that  $\frac{\sin(\alpha + \beta)}{\sin(\alpha - \beta)} = 3$



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56. If  $\cos A + s \in B = m$  and  $s \in A + \cos B = n$ , prove that

$$2 \sin(A + B) = m^2 + n^2 - 2.$$



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57.  $\tan x + \tan\left(x + \frac{\pi}{3}\right) + \tan\left(x + 2\frac{\pi}{3}\right) = 3$  prove that

$$\frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x} = 1$$



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**58.** If a right angle be divided into three parts  $\alpha$ ,  $\beta$  and  $\gamma$ , prove that

$$\cot \alpha = \frac{\tan \beta + \tan \gamma}{1 - \tan \beta \tan \gamma}.$$



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**59.** If  $\sin(\alpha + \beta) = 1$  and  $\sin(\alpha - \beta) = \frac{1}{2}$ , where  $0 \leq \alpha, \beta \leq \frac{\pi}{2}$ , then

find the values of  $\tan(\alpha + 2\beta)$  and  $\tan(2\alpha + \beta)$ .



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**60.** if  $m \cdot \tan(\theta - 30^\circ) = n \cdot \tan(\theta + 120^\circ)$ , show that

$$\cos 2\theta = \frac{m + n}{2(m - n)}.$$



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**61.** If  $\alpha + \beta = \theta$  and  $\frac{\tan \alpha}{\tan \beta} = \frac{x}{y}$ , prove that  $\sin(\alpha - \beta) = \frac{x - y}{x + y} \sin \theta$



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62. If  $\alpha, \beta$  are the roots of the equation  $a \cos \theta + b \sin \theta = c$ , then prove

$$\text{that } \cos(\alpha + \beta) = \frac{a^2 - b^2}{a^2 + b^2}.$$



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63. If  $\alpha, \beta$  are the roots of the equation  $a \cos \theta + b \sin \theta = c$ , then prove

$$\text{that } \cos(\alpha + \beta) = \frac{a^2 - b^2}{a^2 + b^2}.$$



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64. Find the maximum and minimum values of the following expressions

(i)  $a \cos \theta - b \sin \theta$  (ii)  $7 \cos \theta + 24 \sin \theta$



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**65.** Find the maximum and minimum values of the following expressions

(i)  $a \cos \theta - b \sin \theta$  (ii)  $7 \cos \theta + 24 \sin \theta$



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**66.** Express each of the products into sums or difference of sines and

cosines :  $2 \cos 3\theta \cdot \sin 2\theta$



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**67.** Express each of the products into sums or difference of sines and

cosines :  $2 \sin 5\theta \cdot \cos 3\theta$



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**68.** Express each of the products into sums or difference of sines and

cosines :  $\cos 9\theta \cdot \cos 4\theta$





69. Express each of the products into sums or difference of sines and cosines :  $\sin 75^0 \cdot \cos 15^0$



70. Prove that  $\sin 25^0 \cos 115^0 = \frac{1}{2} (\sin 40^0 - 1)$



71. Prove that:  $\sin 20^0 \sin 40^0 \sin 60^0 \sin 80^0 = \frac{3}{16}$



72. Prove that:  $\cos 20^0 \cos 40^0 \cos 80^0 = \frac{1}{8}$



73. Prove that :  $\tan 20^\circ \tan 40^\circ \tan 60^\circ \tan 80^\circ = 3$



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74. Prove that:  $\cos 10^\circ \cos 30^\circ \cos 50^\circ \cos 70^\circ = \frac{3}{16}$



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75.  $\tan 20^\circ \tan 30^\circ \tan 40^\circ \tan 80^\circ = 1$



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76. Prove that:  $2 \cos \theta \cos \left( \frac{\pi}{3} + \theta \right) \cos \left( \frac{\pi}{3} - \theta \right) = \cos 3\theta$



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77. Prove that  $\frac{5x}{2} \cos 2x \cos \frac{x}{2} \cos 3x \cos \frac{9x}{2} = s \in 5x$   
 $s \in \frac{5x}{2}$ .



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78. Show that:

$$s \in (B - C)\cos(A - D) + \sin(C - A)\cos(B - D) + \sin(A - B)\cos(C - D)$$



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79. If  $\alpha + \beta = 90^0$ , show that the maximum value of  $\cos \alpha \cdot \cos \beta$  is  $\frac{1}{2}$ .



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80. Prove that  $\tan \theta \cdot \tan(60 - \theta) \cdot \tan(60 + \theta) = \tan 3\theta$  and hence find the value of  $\tan 5^0 \cdot \tan 55^0 \cdot \tan 65^0 \cdot \tan 75^0$



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81. If  $\cos \alpha = \frac{1}{\sqrt{2}}$ ,  $\sin \beta = \frac{1}{\sqrt{3}}$ , show that  
 $\tan\left(\frac{\alpha + \beta}{2}\right)\cot\left(\frac{\alpha - \beta}{2}\right) = 5 + 2\sqrt{6}$  or  $5 - 2\sqrt{6}$



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82. Express each of that as product of sines and cosines :  $\cos 9\theta^0 + \cos 3\theta$



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83. Express each of that as product of sines and cosines :  $\sin 2\theta + \sin 4\theta$



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84. Express each of that as product of sines and cosines :  $\cos 12\theta - \cos 4\theta$



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**85.** Express each of that as product of sines and cosines :  $\sin 9\theta + \sin 5\theta$

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**86.** Prove that:  $s \in 65^0 + \cos 65^0 = \sqrt{2}\cos 20^0$

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**87.** Prove that:  $s \in 47^0 + \cos 77^0 = \cos 17^0$

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**88.** Prove that :  $\frac{\cos 7x + \cos 5x}{\sin 7x - \sin 5x} = \cot x$

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**89.** Prove that :  $\frac{\cos 9x - \cos 5x}{\sin 17x - \sin 3x} = \frac{-\sin 2x}{\cos 10x}$



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90. Prove that :  $\frac{\sin x + \sin 3x}{\cos x + \cos 3x} = \tan 2x$



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91. Prove that :  $\frac{\cos 10^0 - \sin 10^0}{\cos 10^0 + \sin 10^0} = \tan 35^0$



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92. Prove that:  $\cos 80^0 + \cos 40^0 - \cos 20^0 = 0$



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93. prove that  $\sin 10^0 + \sin 20^0 + \sin 40^0 + \sin 50^0 = \sin 70^0 + \sin 80^0$



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**94.** Prove that:  $\cos 20^\circ + \cos 100^\circ + \cos 140^\circ = -0$



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**95.**  $\frac{\cos \pi}{5} + \frac{\cos(2\pi)}{5} + \frac{\cos(6\pi)}{5} + \frac{\cos(7\pi)}{5} = 0$



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**96.** Prove that : $\cos\left(\frac{\pi}{12}\right) - \sin\left(\frac{\pi}{12}\right) = \frac{1}{\sqrt{2}}$



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**97.**  $\sin\left(\frac{5\pi}{18}\right) - \cos\left(\frac{4\pi}{9}\right) = \sqrt{3} \sin\left(\frac{\pi}{9}\right)$



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**98.** Prove that:  $\cos\left(\frac{3\pi}{4} + x\right) - \cos\left(\frac{3\pi}{4} - x\right) = \sqrt{2} \sin x$



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99. Prove that:  $\cos\left(\frac{\pi}{4} + x\right) + \cos\left(\frac{\pi}{4} - x\right) = \sqrt{2} \cos x$



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100. Prove that

$$\cos \alpha + \cos \beta + \cos \gamma (\alpha + \beta + \gamma) = 4 \frac{\cos(\alpha + \beta)}{2} \frac{\cos(\beta + \gamma)}{2} \frac{\cos(\gamma + \alpha)}{2}$$



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101. Prove that :  $\frac{\sin x - \sin y}{\cos x + \cos y} = \tan\left(\frac{x - y}{2}\right)$



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102. Prove that :  $\frac{\sin x + \sin y}{\cos x + \cos y} = \tan\left(\frac{x + y}{2}\right)$



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103. Prove that :  $\frac{\sin x + \sin y}{\sin x - \sin y} = \tan\left(\frac{x+y}{2}\right) \cdot \cot\left(\frac{x-y}{2}\right)$



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104. Prove that:  $s \in 3x + s \in 2x \quad s \in x = 4 \quad s \in x \cos \frac{x}{2} \cos \frac{3x}{2}$



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105. show that  $\sin x + \sin 3x + \sin 5x + \sin 7x = 4 \sin 4x \cos 2x \cos x$ .



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106. Prove that :  $\frac{\sin \theta + \sin 3\theta + \sin 5\theta}{\cos \theta + \cos 3\theta + \cos 5\theta} = \tan 3\theta$



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$$107. \text{ Prove that : } \frac{\cos 4\theta + \cos 3\theta + \cos 2\theta}{\sin 4\theta + \sin 3\theta + \sin 2\theta} = \cot 3\theta$$



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$$108. \text{ Prove that : } \frac{\sin \theta + 2 \sin 3\theta + \sin 5\theta}{\sin 3\theta + 2 \sin 5\theta + \sin 7\theta} = \frac{\sin 3\theta}{\sin 5\theta}$$



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$$109. \frac{\cos 3\theta + 2 \cos 5\theta + \cos 7\theta}{\cos \theta + 2 \cos 3\theta + \cos 5\theta} = \cos 2\theta - \sin 2\theta \tan 3\theta.$$



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$$110. \text{ Prove that : } \frac{\sin 5\theta - 2 \sin 3\theta + \sin \theta}{\cos 5\theta - \cos \theta} = \tan \theta$$



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111. If  $\cos ec A + \sec A = \cos ec B + \sec B$ , prove that

$$\tan A \tan B = \frac{\cot(A + B)}{2}$$



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112. Prove that:

$$(\cos \alpha - \cos \beta)^2 + (\sin \alpha - \sin \beta)^2 = 4 \sin^2 \left( \frac{\alpha - \beta}{2} \right)$$



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113. Prove that :

$$\sin \alpha + \sin \beta + \sin \gamma - \sin(\alpha + \beta + \gamma) = 4 \sin\left(\frac{\alpha + \beta}{2}\right) \cdot \sin\left(\frac{\beta + \gamma}{2}\right) \cdot \sin\left(\frac{\alpha + \gamma}{2}\right)$$



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114.  $\frac{\cos(A - B)}{\cos(A + B)} + \frac{\cos(C + D)}{\cos(C - D)} = 0 \Rightarrow \tan A \tan B \tan C \tan D =$



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**115.** If  $\sin 2A = \lambda \sin 2B$  prove that  $\left( \frac{\tan(A + B)}{\tan(A - B)} \right) = \frac{\lambda + 1}{\lambda - 1}$



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**116.** If  $\cos(\alpha + \beta)\sin(\gamma + \delta) = \cos(\alpha - \beta).\sin(\gamma - \delta)$ , prove that :  
 $\cot \alpha. \cot \beta. \cot \alpha = \cot \delta$ .



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**117.** If  $y \sin \phi = x \sin(2\theta + \phi)$  show that  
 $(x + y)\cot(\theta + \phi) = (y - x)\cot \theta$ .



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