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## MATHS

## BOOKS - NCERT MATHS (HINGLISH)

## STRAIGHT LINES

Short Answer Type Questions

1. Find the equation of the straight line which passes
through the point $(1-2)$ and cuts off equal intercepts from axes.
2. Find the equation of the line passing through the point $(5,2)$ and perpendicular to the line joining the points $(2,3)$ and ( $3,-1$ ).

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3. Find the angle between the lines

$$
y=(2-\sqrt{3})(x+5) \text { and } y=(2+\sqrt{3})(x-7) .
$$

4. Find the equations of the line which passes through the point $(3,4)$ and the sum of its intercepts on the axes is 14 .

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5. The points on $x+y=4$ that lie at a unit distance from the line $4 x+3 y-10=$ are

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6. Show that the tangent of an angle between the
lines $\frac{x}{a}+\frac{y}{b}=1$ and $\frac{x}{a}-\frac{y}{b}=1$ and $\frac{2 a b}{a^{2}-b^{2}}$.

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7. Find the equation of a line passing through (1, 2) and making angle of $30^{\circ}$ with $y-a \xi s$.

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8. Find the equation of the line passing through the intersection of the lines
$2 x+y=5$ and $x+3 y+8=0$ and parallel to the line $3 x+4 y=7$.
9. For what values of $a$ and $b$ the intercepts cut off $n$ the coordinate axes by the line $a x+b y+8=0$ are equal in length but opposite in signs to those cut off by the line $2 x-3 y+6=0$ on the axes.

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10. If the intercept of a line between the coordinate axes is divided by the point $(-5,4)$ in the ratio $1: 2$, then find the equation of the line.

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11. a Find equation of a straight line on which length of perpendicular from the origin is four units and the line makes an angle of $120^{\circ}$ with the positive direction of $x$-axis.

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12. Find the equations the sides of an isosceles right angled triangle the equation of whose hypotenuse is $3 x+4 y=4$ and the opposite vertex is the point (2, 2).
13. The equation of the base of an equilateral triangle is
$x+y=2$ and its vertex is $(2,-1)$. Find the length and equations of its sides.

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2. A variable line passes through a fixed point $P$. The algebraic sum of the perpendiculars drawn from the points $(2,0),(0,2)$ and $(1,1)$ on the line is zero. Find the coordinate of the point $P$.
3. Angle made with the $x$-axis by a straight line drawn through $(1,2)$ so that it intersects $x+y=4$ at a distance $\frac{\sqrt{6}}{3}$ from (1,2) is $105^{0}$ (b) $75^{0}$ (c) $60^{0}$ (d) $15^{0}$

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4. Astraight line moves so that the sum of the reciprocals of its intercepts made on axes is constant. Show that the line passes through a fixed point.
5. The equation of the straight line which passes
through the point $(-4,3)$ such that the portion of the line between the axes is divided internally be the point in the ratio $5: 3$ is (a) $9 x-20 y+96=0$

$$
9 x+20 y=24 \text { (c) } 20 x-9 y+53=0 \text { (d) none of }
$$ these

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6. Find the equations of the lines through the point of intersection of the lines
$x-y+1=0$ and $2 x-3 y+5=0$ whose distance from the point $(3,2)$ is $7 / 5$.
7. If the sum of the distances of a moving point in a plane from the axes is 1 , then find the locus of the point.

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8. $P_{1}, P_{2}$ are points on either of the two lines
$y-\sqrt{3}|x|=2$ at a distance of 5 units from the poinfÃ』f intersection. Find the coordinates of the foot of perpendiculars drawn from $P_{1}, P_{2}$ on the bisector the angle between the given lines.
9. If $p$ is the length of perpendicular from the origin on the line $\frac{x}{a}+\frac{y}{b}=1$ and $a^{2}, p^{2}$ and $b^{2}$ are in AP, the show that $a^{4}+b^{4}=0$.

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## Objective Type Questions

1. A line cutting off intercept -3 from the $Y$ - axis
and the tangent at angle to the $X$ - axis is $\frac{3}{5}$, its equation is
A. $5 y-3 x+15=0$
B. $3 y-5 x+15=0$
C. $5 y-3 x-15=0$
D. None of the above

Answer: A

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2. Slope of a line which cuts off intercepts of equal lengths on the axes is
A. -1
B. 0
C. 2
D. $\sqrt{3}$

Answer: A

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3. The equation of the straight line passing through the point $(3,2)$ and perpendicular to the line $y=x$ is
A. $x-y=5$
B. $x+y=5$
C. $x+y=1$
D. $x-y=1$

## Answer: B

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4. The equation of the line passing through the point
$(1,2)$ and perpendicular to the line $x+y+1=0$ is
A. $y-x+1=0$
B. $y-x-1=0$
C. $y-x+2=0$
D. $y-x-2=0$

Answer: B
5. Find the tangent of the angle between the lines whose intercepts n the axes are respectively $a,-b$ and $b,-a$
A. $\frac{a^{2}-b^{2}}{a b}$
B. $\frac{b^{2}-a^{2}}{2}$
c. $\frac{b^{2}-a^{2}}{2 a b}$
D. None of these

## Answer: C

6. If the line $\frac{x}{a}+\frac{y}{b}=1$ passes through the points a $(2,-3)$ and $(4,-5)$, then $(a, b)=$
A. $(1,1)$
B. $(-1,1)$
C. $(1,-1)$
D. $(-1,-1)$

## Answer: D

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7. The distance of the point of intersection of the lines
$2 x-3 y+5=0$ and $3 x+4 y=0$ from the line
$5 x-2 y=0$ is

$$
\begin{aligned}
& \text { A. } \frac{130}{17 \sqrt{129}} \\
& \text { B. } \frac{13}{7 \sqrt{29}} \\
& \text { c. } \frac{130}{7}
\end{aligned}
$$

D. None of these

Answer: A

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8. Show that the equations of eth straight lines passing through the point $(3,-2)$ and inclined at

## $60^{0}$

$\sqrt{3} x+y=1 a r e y+2=0 a n d y-\sqrt{3} x+2+3 \sqrt{3}=0$.
A. $y+2=0, \sqrt{3} x-y-2-3 \sqrt{3}=0$
B. $x-2=0, \sqrt{3} x-y+2+3 \sqrt{3}=0$
C. $\sqrt{3} x-y-2-3 \sqrt{3}=0$
D. none of above

## Answer: A

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9. Find the equations of lines passing through the point $(1,0)$ and a distance $\frac{\sqrt{3}}{2}$ from the origin.
A. $\sqrt{3} x+y-\sqrt{3}=0, \sqrt{3} x-y-\sqrt{3}=0$
B. $\sqrt{3} x+y+\sqrt{3}=0, \sqrt{3} x-y+\sqrt{3}=0$
C. $x+\sqrt{3} y-\sqrt{3}=0, x-\sqrt{3} y-\sqrt{3}=0$
D. None of the above

Answer: A

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10. The distance between the lines $y=m x+c_{1}$ and

$$
y=m x+c_{2} \text { is }
$$

A. $\frac{c_{1}-c_{2}}{\sqrt{m^{2}+1}}$
B. $\frac{\left|\left(c_{1}-c_{2}\right)\right|}{\sqrt{1+m^{2}}}$
C. $\frac{c_{2}-c_{1}}{\sqrt{1+m^{2}}}$
D. 0

## Answer: B

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11. Find coordinates of the foot of perpendicular, image and equation of perpendicular drawn from the point $(2,3)$ to the line $y=3 x-4$.
A. $\left(\frac{37}{10}, \frac{-1}{10}\right)$
B. $\left(-\frac{1}{10}, \frac{37}{10}\right)$
C. $\left(\frac{10}{37},-10\right)$
D. $\left(\frac{2}{3}, \frac{1}{3}\right)$

## Answer: B

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12. If the coordinates of the middle point of the portion of a line interceptecd between the coordinate axes is $(3,2)$, then the equation of the line will be
A. $2 x+3 y=12$
B. $3 x+2 y=12$
C. $4 x-3 y=6$
D. $5 x-2 y=10$

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13. Equation of the line passing through $(1,2)$ and parallel to the line $y=3 x-1$ is
A. $y+2=x+1$
B. $y+2=3(x+1)$
C. $y-2=3(x-1)$
D. $y-2=x-1$

Answer: C
14. Find the equations of the diagonals of the square formed by the lines $x=o, y=0, x=1$ and $y=1$.
A. $y=x, y+x=1$
B. $y=x, x+y=2$
C. $2 y=x, y+x=\frac{1}{3}$
D. $y \equiv 2 x, y+2 x=1$

Answer: A

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15. For specifying a straight line, how many geomatrical parameters should be known ?
A. 1
B. 2
C. 4
D. 3

Answer: B

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16. The point $(4,1)$ undergoes the following two successive transformations
(i) Reflection about the line $y=x$
(ii) Translation through a distance 2 units along the positive X -axis.

Then the final coordinate of the point are
A. $(4,3)$
B. $(3,4)$
C. $(1,4)$
D. $\left(\frac{7}{2}, \frac{7}{2}\right)$

Answer: B
17. A point equidistant from the line
$4 x+3 y+10=0,5 x-12 y+26=0 \quad$ and
$7 x+24 y-50=0$ is
A. $(1,-1)$
B. $(1,1)$
C. $(0,0)$
D. $(0,1)$

Answer: C

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18. A line passes through the point $(2,2)$ and is perpendicular to the line $3 x+y=3$, then its $y$ intercept is
A. $\frac{1}{3}$
B. $\frac{2}{3}$
C. 1
D. $\frac{4}{3}$

## Answer: D

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19. Find the ratio in which the line $3 x+4 y+2=0$ divides the distance between the lines
$3 x+4 y+5=0 a n d 3 x=4 y-5=0$.
A. 1:2
B. 3:7
C. 2:3
D. 2:5

Answer: B

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20. Find the coordinates of one vertex of an equilateral triangle with centroid at the origin and the opposite side $x+y-2=0$.
A. $(-1,-1)$
B. $(2,2)$
C. $(-2,-2)$
D. $(2,-2)$

Answer: C

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1. If $a, b$ and $c$ are in $A P$, then the straight line $a x+b y+c=0$ will always pass through a fixed point whose coordinates are $\qquad$

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2. Find the equation of the straight line which passes
through the point $(1-2)$ and cuts off equal intercepts from axes.

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3. Find the equation of the lines through the point (3,
2) which make an angle of 450 with the line $x-2 y=3$

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4. The points $(3,4)$ and $(2,-6)$ are situated on the
$. . . . . . . . . ~ O f ~ t h e ~ l i n e ~ 3 x-4 y-8 \equiv 0$

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5. A point moves so that square of its distance from
the point $(3,-2)$ is numerically equal to its distance
from the line $5 x-12 y=3$. The equation of its locus
is

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6. Find the locus of the mid-point of the portion of the
line $x \cos \alpha+y \sin \alpha=p$ which is intercepted between the axes.

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1. If the vertices of a triangle have rational coordinates, then prove that the triangle cannot be equilateral.

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2. The points $\mathrm{A}(-2,1), \mathrm{B}(0,5)$ and $\mathrm{C}(-1,2)$ are collinear.

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3. Equation of the line passing through the point $\left(a \cos ^{3} \theta, a \sin ^{3} \theta\right)$ and perpendicular to the line $x \sec \theta+y \cos e c \theta=a$ is $x \cos \theta-y \sin \theta=a \cos 2 \theta$.
4. The line $5 x+4 y=0$ passes through the point of intersection of straight lines (1) $x+2 y-10=0,2 x+y=-5$

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5. The vertex of an equilateral triangle is $(2,3)$ and the equation of the opposite side is $x+y=2$. Then, the other two sides are $y-3=(2 \pm \sqrt{3})(x-2)$.
6. The equation of the line joining the point $(3,5)$ to the point of intersection of the lines $4 x+y-1=0$ and $7 x-3 y-35=0$ is equidistant from the points $(0,0)$ and $(8,34)$.

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7. If the line $\left(\frac{x}{a}\right)+\left(\frac{y}{b}\right)=1$ moves in such a way that $\left(\frac{1}{a^{2}}\right)+\left(\frac{1}{b^{2}}\right)=\left(\frac{1}{c^{2}}\right)$, where $c$ is a constant, prove that the foot of the perpendicular from the origin on the straight line describes the circle $x^{2}+y^{2}=c^{2}$.
8. 

$a x+2 y+1=0, b x+3 y+1=0 a n d c x+4 y+1=0$
are concurrent, then $a, b, c$ are in a. A.P. b. G.P. c. H.P. d.
none of these

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9. Line joining the points $(3,-4)$ and $(-2,6)$ is perpendicular to the line joining the points $(-3,6)$ and $(9,-18)$.

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## 1. Match the following

| Column I | Column II |
| :---: | :---: |
| (i) The coordinates of the points $P$ and $Q$ on the line $x+5 y=13$ which are at a distance of 2 units from the line $12 x-5 y+26=0$ are | (a) $(3,1),(-7,11)$ |
| (ii) The coordinates of the point on the line $x+y=4$, which are at a unit distance from the line $4 x+3 y-10=0$ are | (b) $\left(-\frac{1}{3}, \frac{11}{3}\right),\left(\frac{4}{3}, \frac{7}{3}\right)$ |
| (iii) The coordinates of the point on the line joining $A(-2,5)$ and $B(3,1)$ such that $A P=P Q=Q B$ are | (c) $\left(1, \frac{12}{5}\right),\left(-3, \frac{16}{5}\right)$ |

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2. The value of the $\lambda$ if the lines

$$
(2+3 y+4)+\lambda(6 x-y+12)=0 \text { are }
$$

(i) parallel to $Y$ axis is
(ii) perpendicular to $7 x+y-4=0$ is
(iii) passes through $(1,2)$ is
(iv) parallel to $X$-axis is

## Column II

(a) $\lambda=-\frac{3}{4}$
(b) $\lambda=-\frac{1}{3}$
(c) $\lambda=-\frac{17}{41}$
(d) $\quad \lambda=3$

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3. The equation of the line through the intersection of
the lines $2 x-3 y=0$ and $4 x-5 y=2$ and

|  | Column 1 |  | Column II |
| :---: | :---: | :---: | :---: |
| U |  | (a) | $2 x-y=4$ |
| (1) | :ertentivar to the line $x+2 y+1=0$ | (b) | $x+y-5=0$ |
| (ii) | Sersie is the lme $2 x-4 t+5=0$ is | (c) | $x-y-1=0$ |
| n | Eucil inctined to the axes is | (d) | $3 x-4 y-1=0$ |

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