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## PHYSICS

## BOOKS - NCERT PHYSICS (HINGLISH)

## MOTION IN A PLANE

Multiple Choice Questions
1.

The
angle
between
$A=\hat{i}+\hat{j}$ and $B=\hat{i}-\hat{j}$ is
A. $45^{\circ}$
B. $90^{\circ}$
C. $-45^{\circ}$
D. $180^{\circ}$

Answer: B

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2. Which one of the following statements is
true?
A. A scalar quantity is the one that is conserved in a process
B. A scalar quantity is the one that can
never take negative values
C. A scalar quantity is the one that does not
vary from one point to another in space

## D. A scalar quantity has the same value for

observers with different orientation of
the axes

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3. Figure shows the orientation of two vectors $\vec{u}$ and $\vec{v}$ in the (XY) plane.

If $\vec{u}=a \hat{i}+b \hat{j}$ and $\vec{v}=p \hat{i}+q \hat{j}$ which of the following is correct ?

A. a and $p$ are positive while $b$ and $q$ are negative
B. $a, p$ and $b$ are positive while $q$ is negative
C. $a, q$ and $b$ are positive while $p$ is negative
D. $a, b, p$ and $q$ are all positive

## Answer: B

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4. The component of a vector $r$ along X -axis will have maximum value if
A. $r$ is along positive $Y$-axis
B. $r$ is along positive $X$-axis
C. r makes an angle of $45^{\circ}$ with the X-axis
D. $r$ is along negative $Y$-axis

Answer: B

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5. The range of a projectile fired at an angle of
$15^{\circ}$ is 50 m . If it is fired with the same speed at an angle of $45^{\circ}$ its range will be
A. 60 m
B. 71 m
C. 100 m
D. 141 m

Answer: C
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6. Consider the quantities , pressure, power, energy impulse, gravitational potential, electrical charge , temperature, area,Out of these, the only vector quantities are .
A. impulse, pressure and area
B. impulse and area
C. area and gravitational potential
D. impulse and pressure

Answer: B
7. In a two dimensional motion, instantaneous speed $v_{0}$ is a positive constant.Then which of the following are necessarily true?
A. The average velocity is not zero at any
time
B. Average acceleration must always vanish
C. Displacements in equal time intervals are equal

# D. Equal path lengths are traversed in equal 

## intervals

## Answer: D

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8. In a two dimensional motion, instantaneous speed $v_{0}$ is a positive constant. Then which of the following are neccessarily true?
A. The acceleration of the particle is zero
B. The acceleration of the particle is bounded
C. The acceleration of the particle is necessarily in the plane of motion

D. The particle must be undergoing a

uniform circular motion

Answer: C

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9. Three vectors $\vec{A}, \vec{B}$ and $\vec{C}$ add up to
zero. Find which is false.
A. $(A \times B) \times C$ is not zero unless $\mathrm{B}, \mathrm{C}$ are
parallel
B. $(A \times B)$. $C$ is not zero unless $\mathrm{B}, \mathrm{C}$ are
parallel
C. If $\mathrm{A}, \mathrm{B}, \mathrm{C}$ define a plane, $(A \times B) \times C$ is in that plane
D.

$$
(A \times B) . C=|A||B||C| \rightarrow C^{2}=A^{2}+B^{2}
$$

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10. It is found that $|A+B|=|A|$,This necessarily implies.
A. $B=0$
B. A, B are antiparallel
C. A, B are perpendicular
D. $A$. $B \leq 0$

## Answer: A::B

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11. Two particles are projected in air with speed $v_{0}$ at angles $\theta_{1}$ and $\theta_{2}$ (both acute) to the horizontal,respectively.If the height reached by the first particle greater than that of the second, then thick the right choices
A. Angle of projection $q_{1}>q_{2}$
B. Time of flight $T_{1}>T_{2}$
C. Horizontal range $R_{1}>R_{2}$
D. Total energy $U_{1}>U_{2}$

## Answer: A::B::C

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12. A particle slides down a frictionless paraboli
$\left(y=x^{2}\right)$ track $(A-B-C)$ starting from
rest at point $A$.Point $B$ is at the vertex of parabola and point $C$ is at a height less than that of point $A$.After $C$, the particle moves
freely in air as a projectile. If the particle reaches highest point at $P$,then

A. $K E$ at $P=K E$ at $B$
B. height at $\mathrm{P}=$ height at A
C. total energy at $P=$ total energy at $A$
D. time of travel from $A$ to $B=$ time of travel
from $B$ to $P$

## Answer: C

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13. Following are four different relations about displacement, velocity and acceleration for the motion of a particle in general. Choose the incorrect one (s)

$$
\begin{aligned}
& \text { A. } v_{\mathrm{av}}=\frac{1}{2}\left[v\left(t_{1}\right)+v\left(t_{2}\right)\right] \\
& \text { В. } v_{\mathrm{av}}=\frac{r\left(t_{2}\right)-r\left(t_{1}\right)}{t_{2}-t_{1}} \\
& \text { C. } r=\frac{1}{2}\left(v\left(t_{2}\right)-v\left(t_{1}\right)\right)\left(t_{2}-t_{1}\right)
\end{aligned}
$$

D. $a_{\mathrm{av}}=\frac{v\left(t_{2}\right)-v\left(t_{1}\right)}{t_{2}-t_{1}}$

## Answer: A::C

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14. For a particle performing uniform circular motion, choose the incorrect statement from the following.
A. Magnitude of particle velocity (speed)
remains constant
B. Particle velocity remains directed perpendicular to radius vector
C. Direction of acceleration keeps changing as particle moves

D. Angular momentum is constant in

magnitude but direction keeps changing

## Answer: D

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15. For tow vectros $\vec{A}$ and $\vec{B}$
$|\vec{A}+\vec{B}|=|\vec{A}-\vec{B}|$ is always true when.
A. $|A|=|B| \neq 0$
B. $A \perp B$
C. $|A|=|B| \neq 0$ and A and B are parallel
or anti-parallel
D. when either $|A|$ or $|B|$ is zero

Answer: B::D
16. A cyclist starts form centre $O$ of a circular park of radius 1 km and moves along the path
$O P R Q O$. If he maintains constant speed of
$10 m s^{-1}$. What is his acceleration at point ( R
)in magnitude and direction ?

17. A particle is projected in air at some angle
to the horizontal, moves along parabola as
shown in figure where x and y indicate horizontal and vertical directions, respectively .

Shown in the diagram, direction of velocity and
acceleration at points $\mathrm{A}, \mathrm{B}$ and C .


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18. A ball is thrown from a roof top at angle of
$40^{\circ}$ above the horizontal. It hits the ground a
few seconds later. At what point during its
motion. Does the ball have
(a) greatest speed (b) smallest speed (c ) greatest acceleration ? Explain.

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19. A football is kicked into the air vertically
upwards. What is its (a) acceleration, and (b)
velocity at the highest point ?

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20. $\vec{A}, \vec{B}$ and $\vec{C}$ are three non-collinear, non co-planar vectors. What can you say about direction of $\vec{A} \times \overrightarrow{B \times \vec{C}})$ ?

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21. A boy travelling in an open car moving on a
levelled road with constant speed tosses a ball
vetically up in the air and catches it back.
Shetch the motion of the ball as observed by a
boy stanceing on the footpath. Give explanation to support your diagram.

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22. A boy throws a ball in air at $60^{\circ}$ to the horizontal along a road with a speed of $10 \mathrm{~m} / \mathrm{s}$
. Another boy sitting in a car passing by observes the ball. Sketch the motion of the ball as observed by the boy in the car, If car has a speed of $(18 k m / h)$. Give explanation to support your diagram.
23. In dealing with motion of projectile in air, we ignore effect of air resistance on motion.

This gives trajectory as a parabola as you have studied. What would the trajectory look like it air resistance is included . Sketch such a trajectory and explain why you have drawn it that way.

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24. A fighter plane is flying horizontally at an altitude of 1.5 km with speed $720 \mathrm{kmh}^{-1}$. At what angle of sight (w.r.t horizontal) when the target is seen, should the pilot drop the bomb in order to attack the target?
$\left(\right.$ Takeg $\left.=10 \mathrm{~ms}^{-2}\right)$

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25. (a) Earth can be thought of as a sphere of radius 6400 km . Any object (or a person ) is performing circula motion around the axis os
earth due to earths rotation (period 1 day ).

What is acceleration o object on the surface of
th earth 9at equator ) towards its centre ?

What is its altitude $\theta$ ? How does these accelerations compare with $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$ ?
(b) Earth also moves in circular orbit around sum every year withon orbital radius of
$1.5 \times 10^{11} \mathrm{~m}$. What is the acceleration of earth
( or any object on the surface of the earth ) towards the centre of the sum ? How dies thsi acceleration comparte with $g=9.8 m s^{2}$ ?
26. Given below in Column I are the relations
between vectors a,b and c and in Column II are the orientations of $a, b$ and $c$ in the $X Y$ - plane .

Match the relation in Column I to correct
orientations in Column II.

| Column 1 | Column II |
| :---: | :---: |
| (a) $\mathbf{a}+\mathbf{b}=\mathbf{c}$ | (i) |
| (b) $\mathbf{a}-\mathbf{c}=\mathbf{b}$ | (ii) |
| (c) $\mathbf{b}-\mathbf{a}=\mathbf{c}$ | (iii) |
| (d) $\mathbf{a}+\mathbf{b}+\mathbf{c}=0$ | (iv) |

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27. If $|A|=2$ and $|B|=4$, then match the relation
in Column I with the angle $\theta$ between A and B in Column II.

|  | Column I |  | Column II |
| :---: | :---: | :---: | :---: |
| (a) | $\mathrm{A} \cdot \mathrm{B}=0$ | (i) | $\theta=0$ |
| (b) | $A \cdot B=+8$ | (ii) | $\theta=90^{\circ}$ |
| (c) | $\mathrm{A} \cdot \boldsymbol{B}=4$ | (iii) | $\theta=180^{\circ}$ |
| (d) | $A \cdot B=-8$ | (iv) | $\theta=60^{\circ}$ |

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28. If $|\vec{A}|=2$ and $|\vec{B}|=4$, then match the relations in column I with the angle $\theta$ between
$\vec{A}$ and $\vec{B}$ in column II.
Column I, Column II
(a) $|\vec{A} \times \vec{B}|=0$, (i) $\theta=30^{\circ}$
(b) $|\vec{A} \times \vec{B}|=0$, (ii) $\theta=45^{\circ}$
(c) $\vec{A} \times \vec{B} \mid=4$, (iii) $\theta=90^{\circ}$
(d) $|\vec{A} \times x \vec{B}|=4 \sqrt{2}$, (iv) $\theta=0^{\circ}$.

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29. A hill is 500 m high. Supplies are to be across the hill using a canon that can hurl packets at a speed of $125 \mathrm{~m} / \mathrm{s}$ over the hill.

The canon is located at a distance of 800 m
from the foot to hill and can be veoved on the ground at a speed of $2 \mathrm{~m} / / \mathrm{s}$, so that its distance from the hill can be adjusted. What is the shortest time inwhich a pachet can reach on the ground across the hill ? Taje $g=10 \mathrm{~m} / \mathrm{s}^{2}$.

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30. A gun can fire shells with maximum speed $v_{0}$ and the maximum horizontal range that can
be achieved is $R=\frac{v_{0}^{2}}{g}$. If a target farther away by distance $\Delta x$ (beyond R ) has to be hit with the same gun, show that it could that it could be achieved by raising the gun to a height at least $h=\Delta x\left[1+\frac{\Delta x}{R}\right]$


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31. A particle is projected in aer an angle $\beta$ to a surface which itself is inclined at an angle $\alpha$ to the horixonta (Fig. 2 (EP). 26)
(a) Find an ecxpression for range on the plane surface (distanc eon the plance from the point of projection at which particle will hit the surface). (b) Time of flight. 9c ) $\beta$ at which
range will be maximum.


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32. A particle falling vertically from a height hits a plane surface inclined to horizontal at an ange $\theta$ with speed $v_{0}$ and rebounds elastically
(Fig. 2 (RP). 28). Find the distance aling the plane where it will hit second time.


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33. A girl riding a bicycle with a speed of $5 \mathrm{~m} / \mathrm{s}$ to wards Noth direction, observes rain falling vertically down. If she increases her speed to
$10 \mathrm{~m} / \mathrm{s}$, rain appeard to meet her at $45^{\circ}$ to the vertical. What is the speed ot the rain ? In what direction does rain fall as observed by a ground based observer ?

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34. A river is flowing due east with a speed $3 m / s$ (Fig. 2 (EP) . 31 ).

(a) If
swimmer starts swimming due north, what will be his resultant velocity (magnitude and direction) ? (b) If he wants to start from point
(A) on South bank and reach opposite point (B)
on North bank,
(i) Which direction should he swim? (ii) What will be his resultant speed ? (c ) From two
differenrent casses as mentioned in (a) and 9b)
above, in which casse will he reach opposite bank in shorter time ?

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35. A cricket fielder can throw the cricket ball with a speed $v_{0}$. If he throws the ball while running with speed (u) at angle $\theta$ to the horizontal, find
(b) what will be time of flight?
(c) what is the distance (horizontal range)
form the point of projection at which the ball will land?
(d) find $\theta$ at which he should throw the ball that would maxmise the horizontal range range as found in (c ).
(e) how does $\theta$ for maximum range change if $u>v_{0}, u=v_{0}, \underline{t} v_{0}$ ?
(f) how does $\theta$ in (e) compare with that for $\mathrm{u}=0$ (i.e., $45^{\wedge}$ @) ?
36. Motion in two dimensions, in a plane can be studied by expressing position, velocity and acceleration as vectors in cartesian
coordinates $A=A_{x} \hat{i}+A_{y} \hat{j}$, where $\hat{i}$ and $\hat{j}$ are unit vector along $x$ and $y$-directions, respectively and $A_{x}$ and $A_{y}$ are corresponding
components of A. Motion can also be studied
by expressing vectors in circular polar coordinates as $A=A_{r} \hat{r}+A_{\theta} \hat{\theta}$, where
$\hat{r}=\frac{r}{r}=\cos \theta \hat{i}+\sin \theta \hat{j}$
$\hat{\theta}=-\sin \theta \hat{i}+\cos \theta \hat{j}$ are unit vectors along direction in which $r$ and $\theta$ are increasing.
(a) Express $\hat{i}$ and $\hat{j}$ in terms of $\hat{r}$ and $\hat{\theta}$.
(b) Show that both $\hat{r}$ and $\hat{\theta}$ are unit vectors and are perpendicular to each other.
(c) Show that $\frac{d}{d t}(\hat{r})=\omega \hat{\theta}$, where $\omega=\frac{d \theta}{d t}$ and $\frac{d}{d t}(\hat{\theta})=-\theta \hat{r}$.
(d) For a particle moving along a spiral given
by $r=a \theta \hat{r}$, where $\mathrm{a}=1$ (unit), find dimensions of $a$.
(e) Find velocity and acceleration in polar
vector representation for particle moving
along spiral described in (d) above.


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37. A man wants to reach from $A$ to the opposite corner of the square $C$. The sides of
the square are 100 m . A central square of $50 m \times 50 m$ is filled with sand. Outside this square, he can walk at a speed $1 \mathrm{~m} / \mathrm{s}$. In the central square , he can walk only at a speed of $v$ $\mathrm{m} / \mathrm{s}(v<1)$. What is smallest value of v for which he can reach faster via a straight path
through the sand than any path in the square

## outside the sand ?



