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India's Number 1 Education App

## PHYSICS

# BOOKS - NCERT PHYSICS (HINGLISH) 

## SYSTEM OF PARTICLES AND

## ROTATIONAL MOTION

Multiple Choice Questions Mcqs

1. For which of the following does the centre of mass lie outside the body?
A. A pencil
B. A shotput
C. A dice
D. A bangle

## Answer: D

## D Watch Video Solution

2. Which of the following points is the likely position of the centre of mass of the system
shown in Fig.

## Hollow Sphere


A. A
B. B
C. C
D. D

## Answer: C

## D Watch Video Solution

3. A particle of mass $m$ is moving in YZ-plane with a uniform velocity $v$ with its trajectory running parallel to $+v e \quad \mathrm{Y}$-axis and intersecting Z-axis at $z=a$ in figure. The change in its angular momentum about the origin as it bounces elastically form a wall at

## $y=$ constant is


A. $m v a \hat{e}_{x}$
B. $2 m v a \hat{e}_{x}$
C. $y m v \hat{e}_{x}$
D. $2 y m v \hat{e}_{x}$

Answer: B

## D Watch Video Solution

4. When a disc rotates with uniform angular velocity, which of the following is not true?
A. the sence of rotation remains same
B. the orientation of the axis of ration
remains same
C. the speed of rotation in non - zero and remains same
D. the angular acceleration is non- zero and remains same

## Answer: D

## D Watch Video Solution

5. A uniform square plate has a small piece $Q$ of an irregular shape removed and guled to the centre of the plate leaving a hole behind
in figure. The moment of inertia about the $z$ axis is then,

A. increased
B. decreased
C. the same
D. changed in unpredicted manner

Answer: B

## Watch Video Solution

6. In problem 5, the $C M$ of the plate is now in the following quadrant of $x-y$ plane.
A. I
B. II
C. III
D. IV

Answer: c

D Watch Video Solution
7. The density of a non-uniform rod of length
$1 m$ is given by $\rho(x)=a\left(1+b x^{2}\right)$
where a and b are constants and $0 \leq x \leq 1$.
The centre of mass of the rod will be at
$3(2+b)$
A. $\frac{3(2+b)}{4(3+b)}$
B. $\frac{4(2+b)}{3(3+b)}$
C. $\frac{3(3+b)}{4(2+b)}$
D. $\frac{4(3+b)}{3(2+b)}$

## - Watch Video Solution

8. A Merry -go-round, made of a ring-like plarfrom of radius $R$ and mass $M$, is revolving with angular speed $\omega$. A person of mass $M$ is standing on it. At one instant, the person jumps off the round, radially awaay from the centre of the round (as see from the round). The speed of the round after wards is
A. $2 \omega$
B. $\omega$
C. $\frac{\omega}{2}$
D. 0

## Answer: A

## D Watch Video Solution

## 9. Chosse the correct altarnatives

A. For a general rotational motion, angular
momentum L and angular velocity $\omega$ need not be parallel.
B. For a rotional motion about a fixed axis ,
angular momentum L and angular velocity oemga are always parallel.
C. For a gereral translational motion , momentum P and velocity V are always parallel.
D. For a general transational motion , acceleration a and velocity V are always parallel.

## - Watch Video Solution

10. Figure shows two identical particles 1 and

2 , each of mass $m$, moving in opposite directions with same speed $\vec{V}$ along parallel lines. At a particular instant, $\vec{r}_{1}$ and $\vec{r}_{2}$ are their respective position vectors drawn from point $A$ which is in the plane of the parallel
lines. Which of the following is the correct
statement?

A. Aguilar momentum $I_{1}$ of particle a about

$$
\mathrm{A} \text { is } I=m v\left(d_{1}\right)
$$

B. Angular momentum $I_{2}$ of particle 2
about A is $I_{2}=m v r_{2} \odot$
C. total angular momentum of the system

$$
\text { about } \mathrm{A} \text { is } I=m v\left(r_{1}+r_{2}\right) \odot
$$

D. total angular momentum of the system

$$
\text { about } \mathrm{A} \text { is } I=m v\left(d_{2}-d_{1}\right) \otimes
$$

## Answer: A,B

## D Watch Video Solution

11. The net external torque on a system of particles about an axis is zero. Which of the following are compatible with it ?
A. the forces may be acting radiaally from a point on the axis
B. the forces may be acting on the axis of rotation
C. the forces may be acting parallel to the axis of the axis of rotation
D. the torque caused by some forces may
be equal and opposite to that caused by
other forces

Answer: a,b,c,d
12. Figure shows a lamina in $x-y$ plane. Two axes $z$ and $z^{\prime}$ pass perpendicular to its plane.

A force $F$ acts in the plane of lamina at point
$P$ as shown. Which of the following statements is incorrect ?
(The point $P$ is closer to $z^{\prime}-a \xi s$ than the $z-$
axis).

A. Torque $\tau$ caused by F about $\mathrm{z}^{-}$axis is
along $-\hat{k}$
B. Torque $\tau$ caused by F about z -axis is
along $-\hat{k}$
C. Torque $\tau$ caused by F about z -axis is
greater in magnitde to the plane containing $r$ and $F$.
D. total torque is given be $\tau=\tau+\tau^{\prime}$

Answer: b,c

## D Watch Video Solution

13. With reference to Fig. of a cube of edge a and mass m , state whether the following are true or false. (O is the centre of the cube.)

A. the moment of inertia of cube about $z$ -

$$
\text { axis is } I_{z}=I_{x}+I_{y}
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B. the moment of inertia of cube about z-

$$
\text { axis is } I_{z}=I_{z}+\frac{m a^{2}}{2}
$$

C. the moment of inertia of cube about z"-
axis is $I_{z}+\frac{m a^{2}}{2}$
D. $I_{x}=I_{y}$

Answer: a,b,d

## D Watch Video Solution

14. For which of the following does the centre of mass lie outside the body?
A. A pencil
B. A shotput
C. A dice
D. A bangle

Answer: d
( Watch Video Solution
15. Which of the following points is the likely position of the centre of mass of the system shown in Fig.

A. A
B. B
C. C
D. D

## Answer: c

## D Watch Video Solution

16. A particle of mass $m$ is moving in YZ-plane
with a uniform velocity $v$ with its trajectory
running parallel to $+v e \quad Y$-axis and
intersecting Z-axis at $z=a$ in figure. The
change in its angular momentum about the
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C. $y m v \hat{e}_{x}$
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Answer: b

## D Watch Video Solution

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A. the sence of rotation remains same
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## Answer: d

## D Watch Video Solution

18. A uniform square plate has a small piece $Q$ of an irregular shape removed and guled to the centre of the plate leaving a hole behind
in figure. The moment of inertia about the $z$ axis is then,

A. increased
B. decreased
C. the same
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Answer: b

## Watch Video Solution

19. In problem 5, the $C M$ of the plate is now in
the following quadrant of $x-y$ plane.
A. I
B. II
C. III
D. IV

Answer: c

D Watch Video Solution
20. The density of a non-uniform rod of length

1 m is given by $\rho(x)=a\left(1+b x^{2}\right)$ where, a and b are constants and $0 \leq x \leq 1$. The centre of mass of the rod will be at
$3(2+b)$
A. $\frac{3(2+b)}{4(3+b)}$
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C. $\frac{3(3+b)}{4(2+b)}$
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## - Watch Video Solution

21. A merry-go-round, made of ring-like platform of radius $R$ and mass $M$ is revolving with angular speed $\omega$. A person of mass $M$ is standing on it. At one instant, the person jumps off the round, radially away from the centre of the round (as seen from the round). The speed of the round of afterward is
A. $2 \omega$
B. $\omega$
c. $\frac{\omega}{2}$
D. 0

## Answer: a

## - Watch Video Solution

22. Chosse the correct altarnatives
A. For a general rotational motion, angular
momentum L and angular velocity $\omega$ need not be parallel.
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D. For a general transational motion , acceleration a and velocity V are always
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## - Watch Video Solution

23. Figure shows two identical particles 1 and

2 , each of mass $m$, moving in opposite directions with same speed $\vec{V}$ along parallel lines. At a particular instant, $\vec{r}_{1}$ and $\vec{r}_{2}$ are their respective position vectors drawn from point $A$ which is in the plane of the parallel
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D. total angular momentum of the system
about A is $I=m v\left(d_{2}-d_{1}\right) \otimes$

## Answer: a,b

## D Watch Video Solution

24. The net external torque on a system of particles about an axis is zero. Which of the following are compatible with it ?
A. the forces may be acting radiaally from a point on the axis
B. the forces may be acting on the axis of rotation
C. the forces may be acting parallel to the axis of the axis of rotation
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Answer: a,b,c,d
25. Figure shows a lamina in $x-y$ plane. Two axes $z$ and $z^{\prime}$ pass perpendicular to its plane.

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$P$ as shown. Which of the following statements is incorrect ?
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Answer: b,c

## D Watch Video Solution

26. With reference to Fig. of a cube of edge a and mass m , state whether the following are true or false. (O is the centre of the cube.)

A. the moment of inertia of cube about $z$ -

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\text { axis is } I_{z}=I_{x}+I_{y}
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B. the moment of inertia of cube about z-

$$
\text { axis is } I_{z}=I_{z}+\frac{m a^{2}}{2}
$$

C. the moment of inertia of cube about $z^{\prime \prime}$ -
axis is $I_{z}+\frac{m a^{2}}{2}$
D. $I_{x}=I_{y}$

Answer: a,b,d

## ( Watch Video Solution

## Very Short Answer Type Questions

1. the centre of gravity of a body on the earth coincides with its centre of mass for a small object whereas for an extended object it may not ,what is the qualitaitve meaning of small and extended in this regard ?
for which of the following two coincides ? A building, a pond , a lake ,a mountain ?

## - Watch Video Solution

2. Why does a solid sphere have smaller moment of inertia than a hollow cylinder of
same mass and radius, about an axis passing through their axes of symmentry?

## D Watch Video Solution

3. The variation of angular position $\theta$, of $a$ point on a rotating rigid body, with time $t$ is shown in Fig. Is the body rotating clock wise or
anti-clockwise?


## - Watch Video Solution

4. A uniform cube of mass $m$ and side a is
placed on a frictionless horizontal surface. A
vertical force $F$ is applied to the edge as
shown in Fig. Match the following (most appropriate choice) :
(a) $m g / 4<F<m g / 2$ (i) Cube will move up.
(b) $F>m g / 2$ (ii) Cube will not exhibit motion.
(c) $F>m g$ (iii) Cube will begin to rotate and slip at $A$.
(d) $F=m g / 4$ (iv) Normal reaction effectively
at $a / 3$ from A, no motion.


## D Watch Video Solution

5. A uniform sphere of mass $m$ and radius $R$ is placed on a rough horizontal surface. The spher is struck horizontally at a height $h$ from
the floor. Show that the sphere rolls without
slipping with a constant velocity, when $h=7 R / 5$.

## D Watch Video Solution

6. The vector sum of a system of non-collinear forces acting on a rigid body is given to be non-zero. If the vector sum of all torques due to the system of forces about a certain point is found to be zero, does this mean that it is necessarily zero about any arbitrary point ?
7. A wheel in uniform motion about an axis
passing through its centre and perpendicular
plus is considered to be in mechanical
(translational plus rotational ) equilibrium
because no net external force or torqure is
reqired to sustain its motion However, the
particles than constitute the wheel do experience a centripeteal the acceleration wheel being in equilibrium ?
how would you set a half wheel into unifrom motion about an axis passing throgh the
centre of mass of the wheel and perpendicular to its plane ? will ypu require external forces to sustain the motion ?

## D Watch Video Solution

8. A door is hinged at one and is free to rotate
about a vertical axis [Fig.] Does its weight
cause any torque the axis ? Given reason for
you answer.


## - Watch Video Solution

9. $(n-1)$ equal point masses each of mass $m$ are placed at the vertices of a angular $n$ -
polygon. The vacant vertex has $a$ position vector $a$ with respect to the centre of the polygon. Find the position vector of centre of mass.

## - Watch Video Solution

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for which of the following two coincides ? A building, a pond, a lake ,a mountain ?

## D Watch Video Solution

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shown in Fig. Is the body rotating clock wise or anti-clockwise ?

13. A unifrom cube of mass $m$ and side $a$ is placed on a frictionless horizontal surface .A vertical force $F$ is applied to the edge as shown in figure ,match the following (most appropriate choice )


D Watch Video Solution
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.the sphere is stuuck horizontally at a height $h$
from the floor. Match the following


## D View Text Solution

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## - Watch Video Solution

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D Watch Video Solution
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## - Watch Video Solution

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polygon. The vacant vertex has $a$ position vector $a$ with respect to the centre of the polygon. Find the position vector of centre of mass.

## D Watch Video Solution

## Long Answer Type Questions

1. Find the centre of mass of a unifrom (a) halfdisc,(b) quarter-disc.
2. Two discs of moments of inertia $I_{1}$ and $I_{2}$
about their respective axes (normal to the disc
and passing through the centre), and rotating
with angular speed $\omega_{1}$ and $\omega_{2}$ are brought into contact face to face with their axes of rotation coincident. What is the angular speed of the two-disc system?
A. Does the law of conservation of angular monentum apply to the situation? Why
B. Find the angular speed of the two disc system.
C. Calculate the loss in kinetic energy of the system in the the process.
D. Account for this loss.

## Answer:

- Watch Video Solution

3. A disc of radius $R$ is rotating with an angular speed $\omega_{0}$ about a horizontal axis. It is placed on a horizontal table. The coefficient of kinetic friction is $\mu_{k}$.
(a) What was the velocity of its centre of mass
before being brought in contact with the table
?
(b) What happens to the linear velocity of a point on its rim when placed in contact with the table?
(c ) What happens to the linear speed of the centre of mass when disc is placed in contact
with the table?
(d) Which force i sresponsible for the effects in
(b) and (c).
(e) What condition should be satisfied for rolling to begin ?
(f) Calculate the time taken for the rolling to begin.

## D Watch Video Solution

4. Two cylindrical hollow drums of radii
$R$ and $2 R$, and of a commom height h , are
rotating with angular velocities $\omega$ (anticlockwise) and $\omega$ (clockwise), respectively. Their axes, fixed are parallel and in a horizontal plane separated by $(3 R+\delta)$. They are now brought in contact $(\delta \rightarrow 0)$.
(a) Show the frictional forces just after contact.
(b) Identify forces and torque external to the system just after contact.
(c) What would be the ratio of final angular velocities when friction ceases?

## 5. A uniform square plate $S($ sidec) and a

 unifrom rectangular plate $R($ sideb, $a$ ) have identical areas and mass [Fig.]Show that
(i) $I_{x R} / I_{x S}<1$,
(ii) $I_{y R} / I_{y S}>1$,
(iii)
$I_{z R} / I_{z S}>1$.


- Watch Video Solution

6. A unifrom disc of radius $R$, is resting on a table on its rim. The coefficient of friction between disc and table is $\mu$ Fig. Now the disc is pulled with a force $F$ as shown in the Fig.

What is the maximum value of $F$ for which the disc rolls without slipping ?


## - Watch Video Solution

7. Find the centre of mass of a uniform :
(a) half-disc, (b) quarter-disc.
A. $\left(\frac{4 R}{3 \pi}, \frac{3 R}{3 \pi}\right),\left(\frac{4 R}{3 \pi}, \frac{3 R}{3 \pi}\right)$
B. $\left(0, \frac{4 R}{3 \pi}\right),\left(\frac{4 R}{3 \pi}, \frac{3 R}{3 \pi}\right)$
c. $\left(0, \frac{4 R}{3 \pi}\right),\left(\frac{4 R}{3 \pi}, \frac{4 R}{3 \pi}\right)$
D. $\left(\frac{2 R}{2 \pi}, \frac{4 R}{3 \pi}\right),\left(\frac{4 R}{3 \pi}, \frac{4 R}{3 \pi}\right)$

Answer: C
8. Two discs of moments of inertia $I_{1}$ and $I_{2}$ about their respective axes (normal to the disc and passing through the centre), and rotating with angular speeds $\omega_{1}$ and $\omega_{2}$ are brought into contact face to face with their axes of rotation coincident. (a) What is the angular speed of the two-disc system? (b) Show that the kinetic energy of the combined system is less than the sum of the initial kinetic energies
of the two discs. How do you account for this
loss in energy? Take $\omega_{1} \neq \omega_{2}$
A. Does the law of conservation of angular monentum apply to the situation ? Why ?
B. Find the angular speed of the two disc
system.
C. Calculate the loss in kinetic energy of
the system in the the process.
D. Account for this loss.

## Answer:

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(a) What was the velocity of its centre of mass
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(c) What happens to the linear speed of the centre of mass when disc is placed in contact with the table?
(d) Which force i sresponsible for the effects in
(b) and (c).
(e) What condition should be satisfied for rolling to begin?
(f) Calculate the time taken for the rolling to begin.

$$
\text { A. } t=\frac{\left(R \omega_{0}\right)^{2}}{\mu_{k} g\left(1+\frac{m R^{2}}{I}\right)}
$$

$$
\begin{aligned}
& \text { B. } t=\frac{R \omega_{0}}{\mu_{k} g\left(1+\frac{m R^{2}}{I}\right)} \\
& \text { C. } t=\frac{R \omega_{0}}{\mu_{k} g\left(1+\frac{m R^{2}}{I}\right)^{\frac{1}{2}}} \\
& \text { D. } t=\frac{R \omega_{0}}{\mu_{k} g\left(1+\frac{R^{2}}{I}\right)}
\end{aligned}
$$

## Answer: B

## D Watch Video Solution

10. Two cylindrical hollow drums of radii
$R$ and $2 R$, and of a commom height h , are rotating with angular velocities $\omega$ (anti-
clockwise) and $\omega$ (clockwise), respectively. Their axes, fixed are parallel and in a horizontal plane separated by $(3 R+\delta)$. They are now brought in contact $(\delta \rightarrow 0)$.
(a) Show the frictional forces just after contact.
(b) Identify forces and torque external to the system just after contact.
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## - Watch Video Solution

11. A uniform square plate $S(s i d e c)$ and a unifrom rectangular plate $R(s i d e b, a)$ have identical areas and mass [Fig.]

Show that
(i) $\quad I_{x R} / I_{x S}<1$,
(ii) $\quad I_{y R} / I_{y S}>1$,
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( Watch Video Solution
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What is the maximum value of $F$ for which the disc rolls without slipping ?

A. $F_{\max }=3 \mu M g$
B. $F_{\text {max }}=2 \mu M g$
C. $F_{\max }=\left(\frac{1}{2}\right) \mu M g$
D. $F_{\text {max }}=4 \mu M g$

Answer: A

- Watch Video Solution

