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India's Number 1 Education App

## ECONOMICS

## BOOKS = VK GLOBAL PUBLICATION ECONOMICS (HINGLISH)

## CORRELATION

## Illustrations

Ainear Correlation


Thus, for every change in variable (a) by 2 units
there is a change in variable (b) by 5 units.

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2. The following tables gives height nad weight of the students of a class. Make a scattered diagram to show if the relationship is positive or negative and if the relationship is strong or weak.

| Height (cm) | 180 | 150 | 158 | 165 | 175 | 163 | 195 | 155 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight (kg) | 65 | 54 | 55 | 65 | 60 | 54 | 63 | 50 |

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3. Calculate coefficient of correlation, given the following data :


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## 4. Calculate coefficient of correlation, between the

 age of husbands and wives.| Age of Husbama (Years) | 21 | 22 | 28 | 32 | 35 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Age of Wife (vears) | 18 | 20 | 25 | 30 | 31 |

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5. Calculate coefficient of correlation between the price and quantity supplied.

| Price | 4 | 6 | 8 | 15 | 20 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Supply (kg) | 10 | 15 | 20 | 25 | 30 |

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6. Calculated coefficient of correlation between
the price and quantity demanded.

| Prict | $\vdots$ | 10 | 15 | 20 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Deriend (kg) | $\ddots$ | 35 | $\mathbf{3 0}$ | 25 | 20 |

7. In a fancy-dress competition, two judges accorded following ranks to the 10 participants :


Calculate coefficient of rank correlation

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8. In a Poetry Recitation Competition , 10 participants were accorded following marks by two different judges, X and Y :

| $\mathbf{X}$ | 15 | 17 | 14 | 13 | 11 | 12 | 16 | 18 | 10 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 15 | 12 | 1 | 6 | 7 | $\mathbf{9}$ | $\mathbf{3}$ | $\mathbf{1 0}$ | $\mathbf{2}$ | $\mathbf{5}$ |

9. Calculate coefficient of rank correlation between the marks in Economics and Statistics, as indicated by answer books of each of the two examiners.

| Marks in Statistics | 15 | 10 | 20 | 28 | 12 | 10 | 16 | 18 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks in Economics | 16 | 14 | 10 | 12 | 11 | 15 | 18 | 12 |

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10. From the following data, compute the coefficient of correlation between $X$ and $Y$ series.

Nimbler of ltemn
Arithmente Mean
Sifuaren of Deviallonn from Mean

X-Seriea
YeSerien

| 6 | 6 |
| :---: | :---: |
| 350 | 138 |
| 19 | 94 |

138
9

Summation of product of deviations of $X$ and $Y$ series from their respective arithmetic mean =41

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11. From the following table, calculate the coefficient of correlation by Karl Pearson's method:

| X | 6 | 2 | 10 | 4 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $Y$ | 9 | 11 | - | 8 | 7 |

Arithmetic means of $X$ and $Y$ series are 6 and 8 respectively.
12. From the data given below, find the number of items $(\mathrm{N}), \mathrm{r}=0.5, \sum x y=120$, Standard Deviation of $Y\left(\sigma_{y}\right)=8, \sum x^{2}=90$ where, x and y are deviations from arithmetic mean.

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13. Find the coefficient of correlation from the following data:

| X | 10 | 12 | 18 | 16 | 15 | 19 | 18 | 17 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 30 | 35 | 45 | 44 | 42 | 48 | 47 | 46 |

14. 

$$
r=0.997, \sum x y=46, \bar{X}=4, \bar{Y}=8, \sum x^{2}=28
$$

, what will be the value of $\sum y^{2}$ ?

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15. Two ladies were asked to rank 10 different types of cell phone . The rank given by them are given below.

| Cell Phone | A | B | C | D | E | F | G | H | I | J |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Neclu | 1 | 5 | 3 | 9 | 5 | 2 | 7 | 10 | 8 | 4 |
| Neena | 6 | 8 | 3 | 7 | 2 | 1 | 5 | 9 | 4 | 10 |

## Calculate Spearman's rank correlation coefficient

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16. Calculate coefficient of correlation by means of
ranking method from the following data :

| $\mathbf{X}$ | 40 | 50 | 60 | 60 | 80 | 50 | 70 | 60 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{Y}$ | 80 | 120 | 160 | 170 | 130 | 200 | 210 | 130 |

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17. Calculate the coefficient of correlation using Karl Pearson's formula of the series given below:

| X | 10 | 12 | 15 | 23 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 14 | 17 | 23 | 25 | 21 |

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18. Calculate coefficient of correlation from the following data:

| X | 100 | 200 | 300 | 400 | 500 | 600 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 110 | 120 | 135 | 140 | 160 | 165 |

19. Calculate Karl Pearson's coefficient of
correlation between the values of $X$ and $Y$ for the
following data:

| $\mathbf{X}$ | 78 | 89 | 96 | 69 | 59 | 79 | 68 | 61 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 125 | 137 | 156 | 112 | 107 | 136 | 123 | 108 |

Assume 69 and 112 as the mean values for $X$ and $Y$ respectively.

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20. From the following data, compute Karl Pearson coefficient of correlation :

| X-Series | Y-Series |
| :---: | :---: |
| 7 | 7 |
| 4 | 8 |
| 28 | 76 |

Summation of product of deviation of $X$ and $Y$ series from their respective means is 46

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21. If $r=0.25, \sum x y=45, \sigma_{y}=3, \sum x^{2}=50$,
where x and y denote deviation from their respective means, find the number of items.
22. The rank of 8 same students in tests in Mathematics and Statistics were as follows :

| Rank in Mathematics | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Rank in Statistics | 4 | 2 | 1 | 6 | 8 | 3 | 5 | 7 |

Calculate the coefficient of rank correlation.

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23. Find out coefficient of rank correlation between $X$ and $Y$

| $\mathbf{X}$ | 46 | 56 | 39 | 45 | 54 | 58 | 36 | 40 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y}$ | 30 | 60 | 40 | 50 | 70 | 70 | 30 | 50 |

24. The rank correlation coefficient between marks obtained by 10 students in English and Statistics
was found to be 0.5 . Find the sum of squares of different of ranks.

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## Learning By Doing

1. Explain the relation between price and quantity
supplied through a scattered diagram

| 20 | 30 | 40 | 50 | 60 |
| :---: | :---: | :---: | :---: | :---: |
| 50 | 75 | 100 | 125 | 150 |

2. Show the relationship between $X$ and $Y$ through a scattered diagram.

| $\mathbf{X}$ | $x$ | 16 | 24 | 31 | 42 | 50 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 70 | 58 | 50 | 32 | 26 | 12 |

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## 3. Find out coefficient of correlation between the

 age of Husband and Wife, using Karl Pearson's method base on actual mean value of thefollowing series:

| Age of Husband | 20 | 23 | $27^{-}$ | 31 | 35 | 38 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Age of Wife | 18 | 20 | 24 | 30 | 32 | 34 | 36 | $\mathbf{4 2}$ |

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4. Calculate Karl Pearson's coefficient of
correlation between the age and weight of children.

| Age (Years) | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Weight (kg) | 3 | 4 | 6 | 7 | 10 |

5. Caculate coefficient of rank correlation, given the following data set:
$X$
Y
20
(i0)
11

| 72 | 65 |
| :--- | :--- |
| 26 | 35 |

$\square$ 24
51

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## Objective Type Questions

1. When two variables change in the same direction, then such a collertion is called :
A. negative
B. positive
C. no correlation

D. all of above

## Answer: B

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2. When the relation of three or more variables is
studied simultaneously, it is called :
A. siple correlation
B. partial correlation

## C. multiple correlation

D. none of above

## Answer: C

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## 3. Relation between price and demand is :

A. positive
B. negative
C. one to one
D. no relationship

Answer: B

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4. When cofficient of correlation lies between +0.25 and +0.75 , it is called :
A. perfect degree of correlation
B. high degree of correlation
C. moderate degree of correlation
D. low degree of correlation

## 5. Cofficient of correlation lies always between :

A. 0 and +1
B. -1 and 0
C. -1 and +1
D. none of these

Answer: C

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6. Rank colleration is a superior method of analysis in case of $\qquad$
A. qualitative
B. quantitative
C. frequency
D. none of these

Answer: A

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7. Which of the following equations is correct ?

$$
\begin{aligned}
& \text { A. } r_{k}=1-\frac{6 \sum D^{2}}{N} \\
& \text { B. } r_{k}=1-\frac{6 \sum D^{2}}{N^{2}-N} \\
& \text { C. } r_{k}=1-\frac{6 \sum D^{2}}{N^{3}-N} \\
& \text { D. } r_{k}=1-\frac{6 \sum D^{2}}{N^{4}-N}
\end{aligned}
$$

## Answer: C

## - View Text Solution

8. Formula of Karl pearson's cofficient of colleration is :
A. $\frac{N \sigma_{x} \sigma_{y}}{N^{3}-N}$
B. $\frac{\sum x y}{N \sigma_{x} \sigma_{y}}$
C. $\frac{\sigma_{x} \sigma_{y}}{N^{3}-N}$
D. $\frac{\sum x y}{\sigma_{x} \sigma_{y}}$

## Answer: B

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9. Whien two variables change in a constant proportion, it is called :
A. linear correlation

B. non-linear correlation

C. partial correlation
D. none of these

## Answer: A

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## Choose Apporpiate Word And Fill In The Blank

1. Correlation is a statistical technique that measures ___________ relationship between
different variables. (quantitative/qualitative)
2. If $r=0$, two variables are
(correlated/uncorrelated)

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3. _________offers a graphic expression of the
direction and degree of correlation. (scattered diagram /Rank correlation)
4. In the step-deviation method of estimating standard deviation, deviations are taken from the (actual average/assumed average)

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Concept Based Objective Questions

1. Define correlation .
2. Define partial correlation .

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3. What is the line of best fit?

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4. Name the principal methods of calculating cofficient of correlation .

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5. What is the difference between positive and negative correlation .

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6. What is the nature of correlation of two variables, when they move in the same direction?

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7. Cofficient of correlation is between -1 and +1 . How would you express it arithmetically?
8. When is rank correlation method used ?

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Short Answer Type Questions

## 1. IMPORTANCE OR SIGNIFICANCE OF CORRELATION

2. Describe the various degrees of correlation .

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3. What are the different methods of finding correlation ?

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4. Explain the various kinds of correlation.

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5. Explain the scattered diagram method of correlation.

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6. Describe Karl Pearson's method of calculating cofficient of correlation.

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7. State the properties of correlation cofficient.
8. Describe Spearman's rank difference method.

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9. State the merits of rank correlation cofficient .

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10. What kind of relationship between $X$ and $Y$ is indicated, if the points of the scattered diagram tend to cluster about
(i) a straight line parallel to the X -axis
(ii) a straight line parallel to the Y -axis
(iii) a straight line sloping upward ,and
(iv) straight line sloping downward ?

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## Long Answer Type Questions

1. Define correlation. Give its importance in statistics .
2. What is maent by correlation ? Explain its various kinds.

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3. Discuss Karl Pearson's method of calculating cofficient of correlation. Give its merits and limitations.
4. Discuss Spearman's method of calculating cofficient of correlation. Give its merits and limitations.

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5. Explain the concept of correlation .what is the basic difference between :(i) Linear and non-linear correlation, and (ii) positive and negative correlation .
6. (i)How is Karl Pearson's cofficient of correlation difened?
(ii) What are the limits of the correlation cofficient $r ?$

If $r=+1$ in one situation and $r=-1$ in the other, what kind of relationship exists between the variables $X$ and $Y$ ?

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7. (i) Define Spearman's rank correlation $\left(r_{k}\right)$.
(ii) What are limits of $r_{k}$ ?
(iii) If the values of $X$ and $Y$ have been ranked and
we complete correlation between ranks of $X$ and $Y$
, will this correlation be equal to the value of $r_{k}$ ?
A.
B.
C.
D.

## Answer:

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1. Make a scattered diagram of the given below.

Does any relationship exist between the two ?

$$
\begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\mathbf{x} & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 \\
\mathbf{v} & 78 & 72 & 66 & 60 & 54 & 48 & 42 & 36 & 80 & 24 & 18 & 12
\end{array}
$$

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2. Calculate cofficient of correlation of the age of husband and wife using Karl Person's method.

| Hurband (Age) | 24 | 27 | 28 | 29 | 30 | 31 | 33 | 35 | 36 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Wife (Age) | 18 | 20 | 22 | 27 | 29 | 27 | 29 | 28 | 29 |

3. Calculate correlation of the following data using Karl Pearson's method:

| Series A | 112 | 114 | 108 | 124 | 145 | 150 | 119 | 125 | 147 | 150 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Serien B | 200 | 190 | 214 | 187 | 170 | 170 | 210 | 190 | 180 | 181 |

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4. Using assumed average in Karl Pearson's
formula, calculate cofficient of correlation, given the following data:

| X | 78 | 89 | 97 | 69 | 59 | 79 | 68 | 9 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 125 | 137 | 156 | 112 | 107 | 106 | 129 | 114 |

## 5. Find out Karl Pearson's cofficient of correlation :

Capital Units (in '000) 10
Profit Receipt
10

20 30
$30 \quad 40$
50
60
70 )
8) 9016

24 $8-5 \quad 10$ 15 $1420 \quad 20 \quad 3$

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6. Seven students of a class secured following marks in economics and history . Calculate cofficient of correlation with the help of these data:

| Economics | 66 | 90 | 89 | 55 | 58 | 44 | 42 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| History | 58 | 76 | 65 | 58 | 53 | 49 | 56 |

7. Find out rank difference of $X$ and $Y$ :

| $X$ | 80 | 78 | 75 | 75 | 58 | 67 | 60 | 59 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $Y$ | 12 | 13 | 14 | 14 | 14 | 16 | 15 | 17 |

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8. Calculate cofficient of correlation of the following data with rank difference and Karl Pearson's method:

| Economics (Marks) | 77 | 54 | 27 | 52 | 14 | 35 | 90 | 25 | 56 | 60 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Hindi (Marks) | 35 | 58 | 60 | 46 | 50 | 40 | 35 | 56 | 44 | 42 |

9. Seven students of teaching Economics in two universities are shown below. Calculate rank difference correlation.

| Teaching Methods | I | II | III | IV | V | VI | VII |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rank of'A's Students | 2 | 1 | 5 | 3 | 4 | 7 | 6 |
| Rank of 'B's Students | 1 | 3 | 2 | 4 | 7 | 5 | 6 |

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10. Give three xamples of perfect correlation. Find out rank difference cofficient of correlation with the help of the following data:

| $\mathbf{X}$ | $4 \pi$ | 33 | 40 | 9 | 16 | 65 | 26 | 15 | 57 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y}$ | 13 | 13 | 22 | 6 | 14 | 20 | 9 | 6 | 15 |

11. Calculate cofficient of correlation of the following data :

| $\mathbf{X}$ | 10 | 6 | 9 | 10 | 12 | 13 | 11 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 9 | 4 | 6 | 9 | 11 | 13 | 8 | 4 |

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12. Deviation of two series $X$ and $Y$ are shown .

Calculate coefficient of correlation .

| $\mathbf{x}$ | - | 4 | -2 | +20 | -10 | 0 | +3 | 0 | -15 | -5 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{Y}$ | - | 12 | -7 | +25 | -10 | -3 | 0 | +2 | -9 | -15 |

13. In a baby competition, two judges accorded following ranks to 12 compititors. Find the coefficient of rank correlation.

| Entry | A | B | C | D | E | F | G | H | I | J | K | L |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jedge X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| Judge Y | 12 | 9 | 6 | 10 | 3 | 5 | 4 | 7 | 8 | 2 | 11 | 1 |

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14. In a Fancy - dress competition,two judges accorded the following ranks to eight participants
$\square$
Judge X
Judge Y

Calculate coefficient of rank correlation.

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15. In a beauty contest, three judges accorded following ranks to 10 participants:

| Judge I | 1 | 6 | 5 | 10 | 3 | 2 | 4 | 9 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Judge II | 3 | 5 | 8 | 4 | 7 | 10 | 2 | 1 | 6 | 9 |
| Judge III | 5 | 4 | 9 | 8 | 1 | 2 | 3 | 10 | 5 | 7 |

Find out by Spearman's Rank Difference Method which pair of judges has a common taste in respect of beauty.
16. Following data relates to age group and percentage of regular players. Calculates Karl Pearson's coefficient of correlation .

| Age Group | $20-25$ | $25-30$ | $30-35$ | $35-40$ | $40-45$ | $45-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| \% of Regular Players | 40 | 35 | 28 | 20 | 15 | 5 |

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17. From the following data, relating to playing habits in various age group of 900 students .

Calculate cor=efficient of correlation between age
group and playing habits:


| $15-16$ | $16-17$ | $17-18$ | $18-19$ | $19-20$ | $20-21$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 250 | 200 | 150 | 120 | 100 | 80 |
| 200 | 150 | 90 | 48 | 30 | 12 |

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18. Following data relates to density of population , number of deaths and population of various cities. Calculate death rate and Karl Pearson coefficient between density of population and death rate:

| Cities | P | Q | R | S | T | U |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Density of Population | 200 | 500 | 700 | 500 | 600 | 900 |
| Number of Deaths | 840 | 300 | 312 | 560 | 1,440 | 1,224 |
| Population | 42,000 | 30,000 | 24,000 | 40,000 | 90,000 | 72,000 |

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19. From the following information, determine coefficient of correlation between $X$ and $Y$ series.

|  | X-Series | Y-Series |
| :--- | :---: | :---: |
| Number of Items | 15 | 15 |
| Mean | 25 | 18 |
| SD | 3.01 | 3.03 |
| Sum of Squares of deviation from Mean | 136 | 138 |
| Sum of product of deviations of $\mathbf{X}$ and Y from their respective Means |  | 122 |

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20. From the following data, determine Karl

Pearson's coefficient of correlation between $X$ and

Y series for 15 pairs .

|  | X-Series | Y-Series |
| :--- | :---: | :---: |
| Mean | 80 | 120 |
| Sum of Squares of deviation from Arithmetic Mean | 56 | $1 \% 1 i$ |
| Sum of product of deviations of $X$ and $Y$ from their respective Means | 92 |  |

## Ncert Questions With Hints To Answers

## 1. Can $r$ lies outside the -1 and 1 range depending

 on the type of data?
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2. Does correlation imply causation ? ,No.

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3. When is rank correlation more precise than simple correlation cofficient?

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4. Does zero correlation mean independence?

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5. Can simple correlation cofficient measure any
type of relationship ?

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6. Interpret the value of $r$ as $1,-1$ and 0 .

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7. Why does rank correlation cofficient differ from

## Pearsonian correlation cofficient ?

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8. Calculate the correlation cofficient between the heights of Fathers in inches $(X)$ and their sons $(Y)$.

| $\mathbf{X}$ | 65 | 66 | 57 | 67 | 68 | 69 | 70 | 72 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 67 | 56 | 65 | 68 | 72 | 72 | 69 | 71 |

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9. Calculate the correlation cofficient between $X$
and $Y$ and comment on their relationship.


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10. Calculate the correlation cofficient beteen $X$ and Y and comment on their relationship .
