



MATHS

BOOKS - NAGEEN MATHS (HINGLISH)

CO-ORDINATE GEOMETRY

Solved Examples

1. Find the distance between the following points :

(i) (3, 4) and (5, 2)

(ii) (0, 2) and (4, -1)

(iii) (a, 2a) and (-a, -2a)

(iv) (4, -3) and (- 6, 5)



6. If the distance between the points (x, 2) and (6, 5) is 5 units, find the

value of 'x'.



8. If the distances of P(x, y) from A(5, 1) and B(-1, 5) are equal,

then,

A. 2x=3y

B. 2x = 5y

 $\mathsf{C.}\,3x=2y$



11. Prove that the points (4, 8), (7, 5), (1, -1) and (-2, 2) are the vertices

of a parallelogram.

Watch Video Solution 12. Prove that the points (2, -1), (4, 1), (2, 3) and (0, 1) are the vertices of a square. Watch Video Solution 13. Show that the points A(-3,3), B(7, -2) and C(1,1) are collinear. Watch Video Solution

14. Show that the points (9, -2), (-5, 12) and (-7, 10) lie on that circle

whose centre is the point (1, 4)

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15. In the given figure, ΔABC is an equilateral triangle of side 3 units. Find the coordinates of the other two vertices.



16. A cyclic quadrilateral is drawn such that three of its consecutive vertices are (0, 4), (0, 0) and (2, 0). Find the longest distance between any two vertices of this quadrilateral.

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17. The co-ordinates of two vertices of an equilateral triangle are (0, 0)

and (3, $\sqrt{3}$) . Find the co-ordinates of the third vertex of the triangle.

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18. What point on the X-axis is equidistant from (7, 6) and (-3, 4)?

19. Find the equation of the set of all points equidistant form the point (4, 2) and the X-axis.

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20. Find the equation of the set of points such that the sum of its distances from $(0, 3)$ and $(0, -3)$ is 8.
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21. Find the equation of the set of all points which are twice as far from (3, 2) as from (1, 1).
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22.

$$A(2,2), B(-2, -2), C(-2\sqrt{3}, 2\sqrt{3}) ext{ and } D(-4-2\sqrt{3}, 4+2\sqrt{3})$$

are the co-ordinates of 4 points. What can be said about these four points ?

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23. Find the coordinates of points on the line joining the point that is

twice as far from as from



24. Show that
$$\Delta ABC$$
, where $A(-2,0), B(2,0), C(0,2)$ and ΔPQR where $P(-4,0), Q(4,0)$ and $R(0,4)$ are similar triangles.

25. Find the co-ordinates of a point which divides the line segment joining the points (5, 1) and (-10, 11) in the ratio 2 : 3 internally.





27. Find the co-ordinates of a point which divides the line joining the

points A(3, 4) and B(-2, -1) in the ratio 3 : 2 externally.

28. Find the co-ordinates of a point which divides the line joining the points A(5, -2) and B(4, 6) in the ratio 1:2 externally.



29. Find the co-ordinates of the mid-point of the line segment joining the points A(3, -5) and B(1, 1).

A. (2, 2)

- B. (4, -4)
- C.(1, -1)
- D. (2, -2)

Answer: D



30. The co-ordinates of the end points of a diameter are (-1, 5) and (3,

-1). Find the co-ordinates of the centre and the radius of circle.

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31. The co-ordinates of the mid-point of line joining the points A and B are (2, -3). If the co-ordinates of point A are (-3, 4), then find the co-ordinates of point B.



32. Find the ratio in which X-axis divides the line segment joining the

points (8, 5) and (-3, - 7).

33. In what ratio does the point $\left(\frac{24}{11}, y\right)$ divide the line segment joining the points P(2, -2) and Q(3, 7)? Also find the value of y.

34. The co-ordinates of the vertices of ΔABC are A(3, 2), B(1, 4) and C(-1, 0). Find the length of median drawn from point A.

35. Find the co-ordinates of the points fo trisection of the line joining

the points (3,-2) and (-3, -4).

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36. If two adjacent vertices of a parallelogram are (3, 2) and (-1, 0) and the diagonals intersect at (2, -5), then find the coordinates of the other two vertices.



37. The co-ordinates of three consecutive vertices of a parallelogram are (-1,0), (3, 1) and (2, 2). Find the co-ordinates of fourth vertex of the parallelogram.

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38. Find the image of point P(3,-1) in the point A (-5, 2).



42. A line intersect the Y-axis and X-axis at he points P and Q respectively. If (2,-5) is the mid-point of PQ, then find the coordinate of P and Q.

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43. Point P (h,k) divides a line segment between the exes in the ratio 1:2 Find the lengths (intercepts) on the axes made by this segment. Also find the area of triangle formed by the line segment and the axes.

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44. Find the area of the triangle, whose vertices are (2,1), (4,5) and (6,3).

B. 6

C. 9

 $\mathsf{D}.\,12$

Answer: B

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45. Find the area of triangle, whose vertices are (2,3), (7,5) and (-7,-5).

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46. Find the area of the triangle, whose vertices are (a,c+a), (a,c) and (-

a,c-a).

47. Prove that the points (6,4) (4,5) and (2,6) are collinear.

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48. If the points A (x,y), B (1,4) and C (-2,5) are collinear, then shown

that x + 3y = 13.

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49. For what value of 'k', the points (k,1), (1,-1) and (11,4) are collinear ?

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50. If a $\neq b \neq 0$, prove that the points $(a, a^2), (b, b^2), (0, 00)$ will

not be colliear.

51. If (x,y) be any point on the line segment joinijng the points (a,0)and (0,b) then prove that $\frac{x}{b} + \frac{y}{b} = 1$.

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52. If P be a point equidistant from points A (3,4) and B (5,-2) and area

of ΔPAB is 10 square units, then find the co-ordinates of point P.

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53. The area of a triangle is 5 sq. units. Two. Of its vertices are (2,1) and

(3,-2). If the third vertex is $\left(\frac{7}{2}, y\right)$, find the value of y.

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Miscellaneous Examples

1. If the point P(k-1, 2) is equidistant from the points A(3, k) and B(k, 5),

find the values of k.



4. The points A(4, 7), B(p, 3) and C(7, 3) are the vertices of a right triangle, right-angled at B. Find the value of p.



7. Find the lengths of the medians AD and BE of ΔABC whose vertices are A(7, -3), B(5, 3) and C(3, 1)



8. If the points A(-1, -4), B(b, c) and C(5, -1) are collinear

and 3b + c = 4, find the values of b and c.

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Problems Of Ncert Exemplar

1. Find the points on the X-axis which are at distance of $2\sqrt{5}$ from the

point (7,-4). How many such points are there?





 $A(3a+1,\ -3)$ and B(8a,5) in the ratio 3 : 1, then find the values of a and b.

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5. A(6, 1), B(8, 2) and C(9, 4) are three vertices of parallelogram ABCD. If E is the mid-point of DC, then find the area of ΔADE .



6. Student of a school are standing in rows and columns in their playground for a drill practice. A, B, C, D are the positions of four students as shown in the figure. Is it possible to place Jaspal in the drill in such a way that he is equidistant from eachl of the four

students A, B, C and D? If so, what should be his position?





7. Ayush starts walking from his house to office. Instead of going to the office directly, he goes to a bank first, from there to his daughter's school and then reaches the office. What is the extra distance travelled by Ayush in reaching his office ? (Assume that all distance covered are in straight lines). If the house is situated at (2, 4), bank at

(2, 4), bank at (5, 8) school at (13, 14) and office at (13, 26) and coordinates are in km.

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8. To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in figure.

Niharika runs $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags ? If Rashmi has to post a blue flag exactly halfway between the line segment joining





9. Find the ratio in which the line segment joining the points (-3, 10)

and (6, -8) is divided by (-1, 6).

10. Find the co-ordinates of the points which divide the line segment

joining A (-2, 2) and B(2, 8) into four equal parts.



11. Find the area of a rhombups if its vertices are (3, 0), (4, 5), (-1, 4)

and (-2, -1) taken in order.

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12. Find the centre of a circle passing through the points (6, -6), (3,-7)

and (3, 3).

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13. The two opposite vertices of a square are (3, 4) and (1, -1). Find the co-ordinates of the other two vertices.



14. ABCD is a rectangle formed by joining the points A(-1, -1), B(-1, 4), C(5, 4) and D(5, -1) P, Q, R and S are the mid-points of sides AB, BC, CD and DA respectively. Is the quadrilateral PQRS a square? a rectangle? or a rhombus? Justify your answer.





2. Find the distance of the following points from origin :

(i) (3, -4)

(ii) (-8, -6)

(iii) (5, 12)

(iv) (7, 24)

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3. Find the distance between the points (a, b) and (-b, a).



4. Find the distance between the points (2a, 3a) and (6a, 6a).

5. Find the distance between origin and the point (a, -b).

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6. If the distance between the points (6, 0) and (0, y) is 10 units, find the value of y.
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7. If the distance between the points (3, x) and (-2, -6) is 13 units, then find the value of x.
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8. Prove that the distance between the origin and the point (-6, -8) is

twice the distance between the points (4, 0) and (0, 3).



triangle :

(i) A(-2, 2), B(13, 11) and C(10, 14)

(ii) A(-1, -6), B(-9, -10) and C(-7, 6)



11. Prove that the following points are the vertices of an isosceles right-angled triangle :

(i)
$$A(-8, -9), B(0, -3)$$
 and $C(-6, 5)$

(ii) A(1, -1), B(-2, 2) and C(-2, -1)

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13. Prove that the poins (-4, -3), (-3, 2), (2, 3) and (1, -2)

are the vertices of a rhombus.



14. Show that the following points are the vertices of a rectangle :

- (i) A(4,2), B(0, -4), C(-3, -2), D(1,4)
- (ii) A(1, -1), B(-2, 2), C(4, 8), D(7, 5)

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15. Show that the points A(2, 1), B(0, 3), C(-2, 1) and D(0, -1)

are the vertices of a square.

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16. Show that the points (1, 1), (2, 3) and (5, 9) are collinear.

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17. Show that the points (0, 0), (5, 3) and (10, 6) are collinear.



18. Show that the points (-3, 2), (2, -3) and (1, $2\sqrt{3}$) lie on the

circumference of that circle, whose centre is origin.

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19. If the point (x, y) is equidistant from the points (a+b, b-a) and (a-b,

a+b), then prove that bx=ay.

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20. If (1, 1) and (1, 8) are the opposite vertices of a square, then find

the co-oridnates of remaining two vertices.



1. Find the co-ordinates of a point which divides the line joining the

points (5, 3) and (10, 8) in the ratio 2 : 3 internally.

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2. Find the co-ordinates of a point which divides the line joining the

points (-1, 2) and (3, 5) in the ratio 3 : 5 internally.

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3. Find the co-ordinates of a point which divides the line joining the

points (2, -1) and (3, 3) in the ratio 2 : 1 internally.

4. Find the co-ordinates of a point which divides the line segment joining the points (1, -3) and (2, -2) in the ratio 3 : 2 externally.

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5. Find the co-ordinates of a point which divides the line segment joining the points (3, 0) and (0, 2) in the ratio 2 : 1 externally.

- A. (3, 4)
- B. (-3, 4)
- C.(3, -4)
- D.(-3, -4)



6. If a point A lies on the line segment joining the points P(6, 0) and Q(0, 8) such that AP: AQ = 2:3, find the co-ordinates of point A.



points (a, b) and (-b, a).



10. Find the co-ordinates of the mid-point of the line joining the following points :

(i) (2, 4) and (6, 2)

(ii) (0, 2) and (2, -4)

(iii) (a + b, a - b) and (b - a, a + b)

(iv) (3, -5) and (-1, 3)

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11. The co-ordinates of the end points of a diameter of a circle are (3,

-2) and (-3, 6). Find the co-ordinates of the centre and radius.

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12. The co-ordinates of the vertices of a ΔABC are A(1,0), B(3,6) and C(3,2). Find the length of its medians.

13. The co-ordinates of three consecutive vertices of a parallelogram

are (2, 0), (4, 1) and (6, 4). Find the co-ordinates of its 4th vertex.

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14. Find the co-ordinates of the points of trisection of the line segment joining the points (2, 5) and (6, -2).



15. Find the co-ordinates of the points fo trisection of the line segment joining the points (-2, 0) and (4, 0).

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16. Find the ratio in which the join of points (3, -1) and (8, 9) is divided

by the line y-x+2=0.

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17. The line segment joining the points (3, -4) and (1, 2) is trisected at the points P and Q. If the co-ordinates of P and Q are (p, -2) and $\left(\frac{5}{3}, q\right)$ respectively, find the values of p and q.

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18. Two circles C(0, r) and C'(0', r') touch externally at P(3, 1). If the coordinates of O and O' are (1, p) and (q, -2) repectively. Their areas are in the ratio 4 : 9. Find the value of $p^2 + q^2$.

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1. Find the area of that triangle whose vertices are (2, 3), (-3, 4) and (7, 5).



4. Find the area of that triangle whose vertices are $(at_1^2, 2at_1), (at_2^2, 2at_2)$ and $(at_3^2, 2at_3)$.



5. Find the area of that triagle whose vertices are (b + c, a), (b - c, a) and (a, -a).

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6. Prove that the following points are collinear :

7. (i) If the points (1, 4), (3, -2) and (k, 1)B(3k, 2k + 3) and C(5k - 1, 5k) are collinear, fine the value of k. (ii) If the points A(k + 1, 2k), B(3k, 2k + 3), B(3k, 2k + 3) and C(5k - 1, 5k) are collinear, then show that x + y =2.

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8. If the points A (x, y), (-1, 3) and (5, -3) ar collinear, then

show that x + y = 2.



9. Find the area of the triangle formed by joining the mid-points of

the sides of the triangle whose vertices are

(0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.



11. A(4, 3), B(6, 5) and C(5, -2) are the vertices of a ΔABC , if P is a point on BC such that BP: PC = 2:3. Find the co-ordinates of P and then prove then ar $(\Delta ABP): ar(\Delta ACP) = 2:3$.

12. The vertices of a $\Delta ABCareA(4, 6)$, B(1, 5) and C(7, 2). A line is drawn to intersect side AB and AC at D and E respectively, such that $\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$. Calculate the area of ΔADE and compare it with the area of ΔABC .

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13. The area of a triangle is 5 units. Two of its certices are (2, 1) and (3, -2). The vhird vertex lies on y = x + 3. Find the coordinates of the third vertex of the triangle.

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14. The perpendicular bisector of the line segment joining the points A(1, 5) and B(4, 6) cuts the y-axis at which point?

1. Find the values of y of which the distance between the points A(3, -1) and B(11, y) is 10 units.

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2. Find the relation between x and y such that the point P (x,y) is equidistant from the points A(1, 4) and B(-1, 2).

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3. Find the point on Y-axis which is equidistant from the points

$$(-5, 2)$$
 and $(9, -2)$.

4. Find the co-ordinates of the point equidistant from three given points A(5, 1), B(-3, -7) and C(7, -1).



5. Show that the points $(a,a), (-a, -a) \, ext{ and } \left(-\sqrt{3}a, \sqrt{3}a
ight)$ are

the vertices of an equilateral triangle. Find its area.

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6. Show that the points (1,1), (-1,5), (7,9) and (9,5) taken in

that order, are the vertices of a rectangle.



7. Show that the points A(3, 5), B(6, 0)mC(1, -3) and D(-2, 2)

are the vertices of a square ABCD.



8. If A(2, -1), B(3, 4), C(-2, 3) and D(-3, -2) be four points in a plane show the ABCD is a rhombus but not a square. Find the area of the rhombus.

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9. Find the co-ordinates of a point P on the line segment joining A(1,2) and B(6,7) such that $AP = \frac{2}{5}AB$.

10. Point P divides the line segment joining the points A(2, 1) and B(5, -8) such that $\frac{AP}{AB} = \frac{1}{3}$. If P lies on the line 2x - y + k =0, find the value of k.

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11. Find the ratio in which the point P (11,y) divides the line segment

joining the points A(15, 5) and B(9, 20). Also find the value of y.



12. Two vertices of a $\triangle ABC$ are given by A(6, 4) and B(-2, 2) and its centroid is G (3,4). Find the co-ordinates of the vertex C of $\triangle ABC$.

13. The base QR of an equilateral triangle PQR lies on X-axis. The coordinates of the point Q are (-4,0) and origin is the mid-point of the base. Find the co-ordinates of the points P and R.



14. The mid-point P of the line segment joining the points A(-10, 4) and B(-22, 0) lies on the line segment joining the points C(-9, -4) and D(-4, y). Find the ratio in which P divides CD. Also, find the value of y.

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15. Find the value of k so that the area of the triangle with vertices (1, -1), (-4, 2k) and (-k, -5) is 24 square units.



16. If A(4, -6), B(3, -2) and C(5, 2) are the vertices of a ΔABC and AD is its median, prove that the median AD divides ΔABC into two triangles of equal areas.



18. If the area of $\triangle ABC$ with vertices A(x, y), B(1, 2) and C(2, 1)

is 6 square units, then prove that x + y = 15 or x + y + 9=0.

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Revision Exercise Very Short Answer Questions

1. Find the value of a so that the point (3,a) lies on the line represented by 2x-3y=5



4. Find the distance between the points (0, -3) and (3, 0)

5. In what ratio does the Y-axis divide the join of (-4, 2) and (8, 3)?



8. Two vertices of ΔABC are $A(\,-\,1,\,4)$ and B(5,2) and its centroid is

 $(0,\;-3)$. Find the co-ordinates of point C .



1. If A(-2,4), B(0,0) and C(4,2) are the vertices of ΔABC , find the length of the median through A .





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4. Find the area of the triangle whose vertices are (3,8), (-4,2) and (5,

-1).

5. Show that the points $A(\,-1,\,-4)$, B(3,3) , C(3,4) and

D(-1, -3) are the vertices of a rhombus.



6. If D(3,-2) , E(-3,1) and F(4,-3) are the mid-points of the sides BC, CA and AB respectively of ΔABC , find the co-ordinates of point A , B and C .



7. If the point P (-1,2) divides the line segment joining A (2,5) and B

in the ratio 3:4, find the co-ordinate of B .

8. Prove that the points (a, 0), (0, b) and (1, 1) are collinear if, $\frac{1}{a} + \frac{1}{b} = 1$.



9. If A (1,2) , B(-2, 3) and C(-3,-4) be the vertices of ΔABC . Verify that

median BE divides it into two triangles of equal areas.