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India's Number 1 Education App

## MATHS

## BOOKS - NAGEEN MATHS (HINGLISH)

## REAL NUMBERS

Solved Examples

1. Use Euclid's division algorithm to find the HCF of
(i) 135 and 225 (ii) 196 and 38220 (iii) 867 and 255
( Watch Video Solution

# 2. Use Euclid's algorithm to find the H.C.F. of 4052 

 and 12576.
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3. Find the HCF of 55 and 210 . express it as a linear combinaton of 55 and 210, i.e. HCF of 55 and 210= $210 a+55 b$, for some $a \operatorname{andb}$

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4. Find HCF 65 and 117and express it in the form of $65 m+117 n$.
5. If the HCF of 56 and 72 is $m$ then find $x$ and $y$ such that $m=56 x+72 y$

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6. Find the largest number, which divides 246 and 1030 leaving remainder 6 in each case.
7. Find the largest number that will divide 400,437 and 542 leaving 9,12 , 15 respectively .

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8. Show that every positive even integer is of the
form $2 q$, and that every positive odd integer is of the form $2 q+1$, where $q$ is some integer.

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9. Use Euclid's division lemma to show that the square of any positive integer is either of the form
$3 m$ or $3 m+1$ for some integer $m$.[Hint: Let x be any positive integer then it is of the form $3 q, 3 q+1$ or $3 q+2$ Now square each of these and sho

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10. Use Euclids division Lemma to show that the
cube of any positive integer is either of the form
$9 m, 9 m+1$ or, $9 m+8$ for some integer $m$.

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11. Show that one and only one out of $n,(n+2)$ and ( $\mathrm{n}+4$ ) is divisble by 3 , where n is any positive interger.

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12. Show that the square of an odd positive integer is of the form $8 q+1$, for some integer $q$.

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13. Any contingent of 616 members is to march
behind an army band of 32 members in a parade.

The two groups are to march in the same number of
columns. What is the maximum number of columns in which they can march?

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14. There are 156, 208 and 260 students in group A,
$B$ and C respectively. Buses are to be hired to take
them for a field trip. Find the minimum number of buses to be hired, if the same number of students
should be accommodated in each bus and separate bus for separate group is needed.
15. A sweet seller has 420 Kaju burfis and 130 Badam burfis she wants to stack them in such a way that each stack has the same number, and they take up the least area of the tray. What is the number of burfis that can be placed in each stack for this purpose?

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16. An electronic device makes a beep after every 60 sec. Another device makes a beep after every 62 sec .

They beeped together at 10 a.m. The next time, when they would beep together at the earliest is
17. Express each of the following as a product of prime factors:
(i) 140 (i)156 (iii) 3825

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18. Find the missing numbers in the following prime
factorisation

19. Show that $5 \times 11 \times 17+17$ is a composite number.

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20. Find the HCF and LCM of the following pairs using prime factorisation method:
(i) 140 and 154 (ii) 504 and 735

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21. Find the HCF and LCM of the following by prime factorisation method:
(i) $12,18,24$ (ii) $15,25,45$

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22. Find the LCM and HCF of the 26 and 91 and verify that

HCF $\times$ LCM $=$ product of the given two numbers.

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23. The HCF of two numbers is 23 and their LCM is
24. If one number is 207 , find the other number.
25. The HCF of 2472,1284 and a third number $N$ is 12. If their LCM is $2^{3} \times 3^{2} \times 5 \times 103 \times 107$. Find the number $N$.

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25. Given that $\operatorname{HCF}(306,657)=9$. Find
$\operatorname{LCM}(306,657)$

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26. Show that $12^{n}$ cannot end with the digits 0 or 5
for any natural number $n$

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27. In a morning walk, three persons step off together and their steps measure $40 \mathrm{~cm}, 42 \mathrm{~cm}$ and

45 cm , respectively. What is the minimum distance each should walk so that each can cover thesame distance in complete steps?
28. What is the smallest number that, when divided by 35,56 and 91 leaves remainder of 7 .

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29. Find the greatest number of 5 digits exactly divisible by 35,56 and 91 .

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30. Three bells ring at intervals of 4,7 and 14 minutes. All three range at 6 am . When will they ring together again ?
31. Amar visits the recreation club after every 5days,

Akbar visit after every 24 days, while Anthony goes
there after every 9 days. If all three of them met at the club last on a Sunday, then tall me O' student, on which day of the week will all three meet again ?

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32. Five bells begins to toll together and toll respectively at intervals $6,7,8,9$ and 12 seconds. How
many times will they toll together in one hour, excluding the one at the start?

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## Solved Example

1. Without actual performing the long division, state whether the following rational numbers will have a terminating decimal expansion or a nonterminationg repeating decimal expansion :
(i) $\frac{12}{125}$ (ii) $\frac{7}{1600}$ (iii) $\frac{11}{3125}$
2. Show that :
(i) $\frac{3}{250}$ (ii) $\frac{11}{50}$
are terminating decimals. Express each of them in decimal form without actual division (long division).

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3. Show that each of the following are nonterminating repeating decimal :
(i) $\frac{5}{12}$ (ii) $\frac{7}{75}$

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4. The decimal expansion of the rational number $\frac{43}{2^{4} \times 5^{3}}$ will terminate after how many places of decimals?

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5. Express each of the following in the simplest form
:
(i) $0 . \overline{6}$ (ii) $3 . \overline{3}$

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6. Express each of the following in the simplest form :
(i) $0 . \overline{36}$ (ii) $1 . \overline{046}$

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7. A rational number in its decimal expansion is 327.7081. What can you say about the prime factors of $q$, when this number is expressed in the from $\frac{p}{q}$ ?

Give reason.

## 8. Prove that $\sqrt{2}$ is an irrational number.

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9. Prove that $\sqrt{11}$ is irrational.

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10. Prove that for any prime positive integer $p, \sqrt{p}$ is an irrational number.Watch Video Solution
11. Show that $(2+\sqrt{3})$ is an irrational number.

## D View Text Solution

12. Prove that $5 \sqrt{7}$ is irrational.

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13. Show that the following numbers are irrational.

1
$\frac{1}{\sqrt{2}}$ (ii) $7 \sqrt{5}$

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14. A rational number in its decimal expansion is
327.7081. What can you say about the prime factors
of q , when this number is expressed in the from $\frac{p}{q}$ ?
Give reason

## - Watch Video Solution

15. Show that $12^{n}$ cannot end with the digits 0 or 5
for any natural number $n$

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## 1. Write whether every positive integer can be of the

 form $4 q+2$ where q is an integer, Justify your answer
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2. The number 525 and 3000 are both divisible only

3,5,15,25,75. What is HCF (525, 3000)? Justify your answer.
3. Can two numbers have 18 as their HCF and 380 as their LCM? Give reason.

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4. Show that the square of any positive integer cannot be of the form $6 m+2$ or $6 m+5$ for some integer $q$.

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5. Show that any positive odd integer is of the form $6 q+1$ or $6 q+3$ or $6 q+5$, where $q$ is some integer.
6. Show that the cube of a positive integer of the
form $6 q+r, q$ is an integer and $\mathrm{r}=0,1,2,3,4,5$ is also of the form $6 m+r$

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7. If n is an odd positive integer, show that $\left(n^{2}-1\right)$ is divisible by 8 .
8. Using Euclid's division algorithm, find the largest number that divides 1251, 9377 and 15628 leaving remainders 1, 2 and 3, respectively.

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9. Prove that $\sqrt{p}+\sqrt{q}$ is an irrational, where $p$ and $q$ are primes.

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10. For any positive integer $n$, prove that $n^{3}-n$ is
divisible by 6 .
11. Use Euclid division algorithm to find the HCF of 441, 567 and 693.

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## Exercise 1 A

1. Use Euclid's division algorithm , to find the H.C.F. of the following : (i) 70 and 40
(ii) 18 and 45
(iii) 56 and $88^{`}$
2. If the HCF of 408 and 1032 is expressible in the form $1032 m-408 \times 5$, find $m$.

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3. यदि 56 तथा 72 का HCF $d$ है तो $x$ व $y$ के वे मान ज्ञात कीजिए जो $d=56 x+72 y$ को संतुष्ट करते हैं। यह भी सिध्द कीजिए कि

इस प्रकार प्राप्त $x$ व $y$ अद्वितीय नहीं है।

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4. Express the H.C.F. of 18 and 24 in the form of $18 \mathrm{x}+$ $24 y$.

## - Watch Video Solution

5. Express the H.C.F. of 30 and 36 in the form of $30 x+$ $36 y$.

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6. Find the largest number that divides 1989 and 967 and leaves a remainder of 5 and 7 respectively.
7. Find the largest number that divides 189 and 249 leaving remainder 9 in each case.

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8. Find the largest number that divides 280 and 1248
leaving remainders 4 and 6 respectively.

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9. Find the greartest number that divides 699 and

572 leaving remainders 6 and5 respectively .

## - Watch Video Solution

10. Show that any positive odd integer is of the form
$4 q+1$ or $4 q+3$, where q is some integer.

## - Watch Video Solution

11. Show that any positive integer is of the form $3 q$ or, $3 q+1$ or, $3 q+2$ for some integer $q$.
12. Show that every even positive integer is of the form $6 q$ or $6 q+2$ or $6 q+4$ for some integer $q$.

## - Watch Video Solution

13. Show that every positive integer is either even or odd.
14. Proof that the square of any positive integer is of the form of $4 m$ or $4 m+1$ for some integer $m$.

## - Watch Video Solution

15. Show that the square of any positive integer cannot be of the form $5 m+2$ or $5 m+3$ for some integer $m$.

## - Watch Video Solution

16. Show that one and only one out of $n, n+2$ or , $n+4$ is divisible by 3 , where $n$ is any
positive integer.

## - Watch Video Solution

17. There are 576 boys and 448 girls in a school that are to be divided into equal sections of either boys or girls alone . Find the total number of sections thus formed.

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18. The length, breadth and height of a room are $8 m$
$25 \mathrm{~cm}, 6 \mathrm{~m} 75 \mathrm{~cm}$ and 4 m 50 cm respectively.

Determine,
(i) the length of the longest rod that can be placed
in this room. (Give answer in cm as whole number )
(ii) the length of the longest rod which can measure the three dimensions of the room exactly.

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19. A sweet seller has 420 kaju barfis and 130 badam
barfis. She wants to stack them in such a way that
each stack has the same number and they take up
the least area of the tray. What is the maximum number of barfis that can be placed in each sta
20. Two sets of English and social science books containing 336 and 96 respectively in a library have to be stacked in such a way that an the books are stored topic wise and the height of each stack is the same. Assuming that the books are of the same thickness, determine the number of stacks. What are the characteristics of library?

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21. In a group there are 21 childrens, 35 ladies and 49
gents. They all want to stay in same hotel. Find the
minimum number of rooms required for their stay so that in each room equal number of members stay with the condition that children, female and male stay in separate rooms.

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22. Three sets of English, Hindi and Mathematics books have to be stacked in such a way that all the books are stored topic wise and the height of each
stack is the same. The number of English books is 96, the number of Hindi books is 240 and the number of

Mathematics books is 336 . Assuming that the books
are of the same thickness, determine the number of
stacks of English, Hindi and Mathematics books.

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23. Find the HCF of 81 and 237 and express it as a linear combination of 81 and 237.

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24. Find the polynomials $u(x)$ and $v(x)$ such that

$$
\left(x^{4}-1\right) \cdot u(x)+\left(x^{7}-1\right) \cdot v(x)=(x-1)
$$

25. Six bells commence tolling together and toll at interval of $2,4,6,8,10,12$ minutes respectively. In 30 hours , how many times do they toll together ?

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26. Find the greatest number of 4 digits which is exactly divisible by 15,24 and 36 .
27. A number when divided by 143 leaves 31 as remainder. What will be the remainder, when the same number is divided by 13 ?

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28. $p$ and $q$ are two positive integers such that the least prime factor of $p$ is 3 and the least prime factor of $q$ is 5 . Find the least prime factor of $(p+q)$.

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29. Express each of the following as a product of prime factors:
(i) 96 (ii)84 (iii) 150 (iv) 240 (v) 3072 (vi)324

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## Exercise 1 B

1. 

Show
that
$7 \times 11 \times 13+13$ and $7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1+5$
are composite numbers.

## 2. Show that $5 \times 7 \times 11+11$ is a composite number

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3. Find the HCF and LCM of the following by prime factorisation method:
(i) 12 and 15 (ii) 20 and 25 (iii) 28 and 42 (iv) 336 and 56 (v) 12,15 and 21 (vi) 10,20 and 30
4. Using prime factorisation method, find the HCF and LCM of the following pairs. Hence, verify $H C F \times L C M=$ product of two numbers. (i) 96 and 120 (ii) 16 and 20 (iii) 144 and 192 (iv) 330 and 440

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5. The HCF and LCM of two numbers are 145 and 2175 respectively. If the first number is 435 , find the second number.

## 6. The HCF and LCM of two numbers are 18 and 720

 respectively. Find the product of two numbers.
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7. Is it possible to have two numbers whose HCF is 20 and LCM is 630? Give reason.

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8. Given that LCM $(252,594)=8316$. Find HCF $(252,594)$.
9. The LCM of two number is 192 and their product is 3072. Find the HCF of two numbers.

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## 10. Check whether $6^{n}$ can end with the digit 0 for any

 natural number $n$.
## - Watch Video Solution

11. Prove that there is no natural number for which
$4^{n}$ ends with the digit zero.

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12. Three pieces of timber of lengths $63 \mathrm{~m}, 42 \mathrm{~m}$ and

35m, have to be divided into planks of the same length. What is the greatest possible length of each plank?

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13. Two tanks contain 735 litres and 504 litres of water resepectively. Find the maximum capacity of a container which can measure the water of either tank an exact number of times.
14. A circular field has a circumference of 360 km .

Three cyclists start together and can cycle 48, 60 and
72 k , a day, round the field. When will they meet again?

## D Watch Video Solution

15. Write the missing numbers in the following
factor tree :


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16. Find the greastest number of 5 digits exactly divisible by 24,15 and 36 .

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## Exercise 1 C

1. Without actual division, show that each of the following rational numbers is a terminating decimal.

Express each in the decimal form :
(i) $\frac{17}{2^{2} \times 5^{3}}$ (ii) $\frac{24}{625}$ (iii) $\frac{121}{400}$ (iv) $\frac{19}{800}$ (v) $\frac{9}{2^{4} \times 5^{2}}$
(vi) $\frac{11}{25}$
2. With out actually performing the long division, state whether the following rational numbers will have a terminating decimal expansion or a nonterminating repeating decimal expansion :
(i) $\frac{17}{8}$ (ii) $\frac{64}{455}$ (iii) $\frac{29}{343}$ (iv) $\frac{129}{2^{2} 5^{7} 7^{2}}$ (v) $\frac{6}{15}$ (vi) $\frac{27}{210}$

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3. The decimal expansion of the rational number

27
$\frac{27}{2^{2} \cdot 5^{3}}$, will terminate after how many places of decimals?
4. Express each of the following as a fraction in simplest form : (i) $0 . \overline{5}$ (ii) $1 . \overline{4}$ (iii) $0 . \overline{15}$

## D Watch Video Solution

5. What can you say about the prime factors of their denominators ? (i) 12.123456789 (ii) $12 . \overline{123456789}$

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6. State whether the given statements are true or false :
(i) The sum of two rationals is always rational.
(ii) The sum of two irrationals is always irrational.
(iii) The product of two rationals is always rational.
(iv) The product of two irrationals is always irrational.
(v) The sum of a rational and an irrational is always rational.
(vi) The product of a rational and an irrational is always irrational.

## D View Text Solution

7. Give an example of :
(i) Two rationals whose sum is rational.
(ii) Two irrationals whose sum is rational.
(iii) Two irrationals whose product is rational.

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8. Which of the following is not a rational number.
A. Square root of $4-5 \sqrt{3}$
B. Square root of 20
C. Sum of $(2+\sqrt{3})$ and its reciprocal
D. None of the above.

## Answer: C

## Revision Exercise Very Short Answer Questions

1. State Euclid Division Iemma

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2. State division algorithm to calculate HCF.

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3. Express 120 as the product of prime factors.
4. Express 75 as the product of prime factors.

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5. Find : H.C.F. $(3,5)$

- Watch Video Solution

6. Find : L.C.M. $(3,5)$

- Watch Video Solution

7. If $a$ and $b$ are relatively prime numbers, then what is their HCF?

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8. Write the H.C.F. of the smallest composite number and the smallest prime number.

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9. What is the decimal expansion of $\frac{13}{2 \times 5^{2}}$ ?
10. If $a$ and $b$ are relatively prime numbers, then what is their LCM?

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11. Give an example of two irrationals whose sum is rational.
12. Give an example of two irrational numbers whose sum is rational

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## Revision Exercise Short Answer Questions

1. Express $0 . \overline{7}$ in the simplest form.

## - Watch Video Solution

## 2. Express $1 . \overline{2}$ in the simplest form.

## 3. Prove that $2 \sqrt{3}$ is an irrational number

## D Watch Video Solution

4. Find the largest number which divides 320 and

458 leaving remainders 5 and 8 respectively.

## D Watch Video Solution

5. the smallest number which when divided by 28
and 32 leaves remainders 8 and 12 respectively
6. Find the greatest number of 3 digits which is exactly divisible by 12 and 15 .

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## Revision Exercise Long Answer Questions

1. Prove that if $x a n d y$ are odd positive integers, then $x^{2}+y^{2}$ is even but not divisible by 4.
2. If $a$ and $b$ are two odd positive integers such that $a>b$, then prove that one of the two numbers $\frac{a+b}{2}$ and $\frac{a-b}{2}$ is odd and the other is even.

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3. Prove that if a positive integer is of the form $6 q+5$, then it is of the form $3 q+2$ for some integer $q$, but not conversely.
4. Prove that the square of any positive integer is of the form $5 q, 5 q+1,5 q+4$ for some integer $q$.

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5. Show that the square of an odd positive integer is of the form $8 q+1$, for some integer $q$.
