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## MATHS

## BOOKS - NAGEEN MATHS (HINGLISH)

## RELATIONS AND FUNCTIONS

Solved Examples

1. If $(2 x+3, y-1)=(3,5)$, then find $x$ and $y$.

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2. If $A=\{3,4\}$ and $B=\{2,3,4\}$, then evaluate $A \times B$.

0
3. If $A=\{1,2\}$ and $B=\{2,3\}$, then show that:
$A \times B \neq B \times A$

## D Watch Video Solution

4. If $A \times B=\{(a, x),(a, y),(b, x),(b, y)\}$, then find A and B

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5. A and B are two sets and $n(A \times B)=6$. If there elements of $A \times B$ are (1,2),(2,3),(3,3), then find $A \times B$ and $B \times A$.
6. If $A=\{a, b\}, B=\{2,3\}$ and $C=\{3,4\}$, then evaluate:
(i) $A \times(B \cap C)$
$(i i) A \times(B \cup C)$

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7. If $A \subseteq B$ and $C$ be any set, then prove that:
$A \times C \subseteq B \times C$

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8. If $A \subseteq B$ and $C \subseteq D$, then prove that:

$$
A \times C \subseteq B \times D
$$

9. For any A sets $A, B, C$ and $D$, prove that:
$(A \times B) \cap(C \times D)=(A \cap C) \times(B \cap D)$

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10. If $n$ elements are common in sets A and B , then prove that $n^{2}$ elements will be common in the set $A \times B$ and $B \times A$.

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11. Following relations from the set of natural number N to N are given:
$(a) R_{1}=\left\{(1,2),(4,2),(9,3),(16,4), \hat{a} €_{1}^{\prime}\right\}$
(b) $R_{2}=\left\{(3,1),(4,2),(5,3),(6,4), \hat{a} \epsilon_{\bullet}^{\prime}\right\}$

Represent them in set builder form.
12. A relation $R$ is represent from set $P$ to $Q$ in the following diagram:


Write it in Roaster and Set builder form. Write the diagram and range of the relation.

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13. If $A=\{1,2,3\}$ and $B=\{4,5,6\}$, then which of the following is a relation from set to B ? Give reason:
(i) $R_{1}=\{(1,5),(2,4),(3,5)\}$
(ii) $R_{2}=\{(4,1),(2,6),(5,1),(2,4)\}$
(iii) $R_{3}=\{(1,4),(2,5),(3,4),(2,6),(3,6)\}$
(iv) $A \times B$

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14. Let $R$ be a relation from set $Q$ to $Q$ defined as:
$R=\{(a, b): a, b \in Q$ and $a-b \in Z\}$
Prove that
(i) For each $a \in Q,(a, a) \in R$
$(i i)(a, b) \in R \Rightarrow(b, c) \in R$ where $a, b \in Q$
(iii) $(a, b) \in R,(b, c) \in R \Rightarrow(a, c) \in R$, where $a, b, c \in Q$

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15. Check whether the following relations are functions or not:

$$
R_{1}=\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}
$$

$(i i) R_{2}=\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$ $R_{3}=\{(1,3),(1,5),(2,5)\}$

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16. If $A=\{1,2,3\}$ and $B=\{2,3,4\}$, find which of the following are the functions from $A$ to $B$ ?
(i) $f=\{(1,2),(2,3),(3,4)\}$
(ii) $g=\{(1,2),(1,3),(2,3),(3,4)\}$
(iii) $h=\{(1,3),(2,4)\}$

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17. Let $R$ be a relation on the set of natural numbers $N$, defined as:
$R=\{(x, y): y=2 x, x, y \in N\}$.
Is R a function from $N \times N$ ? If yes find the domain, co-domain and range of $R$.

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18. If $f=\{(1,1),(2,3),(3,5),(4,7)\}$, is a linear function from $Z$ to $Z$, then find $f(x)$.

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19. Let $A$ be a set of two positive integers and a function $f: A \rightarrow Z^{+}$is defined as $f(n)=p$, where p is largest prime factor of $n$.
if the range of $f$ is $\{3\}$, then find $A$. Can $A$ exist uniquely?

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20. If $f(x)=x^{2}+5 x-3$, then evaluate $f(4)$
21. If $f(x)=2(1+\sin x)$, then evaluate $f\left(\frac{\pi}{2}\right)$.

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22. If $f: R \rightarrow R$ is defined as:
$f(x)=\left\{\begin{array}{l}2 x+5, x>9 \\ x^{2}-1,-9<x<9 \\ x-4,<-9\end{array}\right.$
then evaluate (i) $f(2),(i i) f(10),(i i i) f(-12)$ and $(i v) f[f(3)]$.

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23. If $f(x)=x^{3}-\frac{1}{x^{3}}$, then find the value of $f(x)+f(-x)$.
24. Let $(\mathrm{x})$ is a real function, defines as $f(x)=\frac{x-1}{x+1}$, then prove that $f(2 x)=\frac{3 f(x)+1}{f(x)+3}$.

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25. If $\mathrm{y}=\mathrm{f}(\mathrm{x})=\frac{x+2}{x-1}, x \neq 1$, then show that $\mathrm{x}=\mathrm{f}(\mathrm{y})$.

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26. If for $x \neq 0, a f(x)+b f\left(\frac{1}{x}\right)=\frac{1}{x}-5, a \neq b$, then $\mathrm{f}(\mathrm{x})$.

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27. If $f(x)=\cot x$, then prove that :

$$
f(-x)=-f(x)
$$

28. If $f(x)=\log _{e}\left(\frac{1-x}{1+x}\right)$;
$f(a)+f(b)=f\left(\frac{a+b}{1+a b}\right)$

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29. If $\mathrm{f}(\mathrm{x})=\frac{x-1}{x+1}$, then prove that $f\{f(x)\}=-\frac{1}{x}$.

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30. If $(\mathrm{x})=x^{2}$ and $g(x)=2 x+1$ are two real valued function, then evaluate :
$(f+g)(x),(f-g)(x),(f g)(x), \frac{f}{g}(x)$

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31. Find range of $f(x)=\frac{x-3}{4-x}$.
A. R
B. $\mathrm{R}-\{1\}$
C. $R-\{-1\}$
D. None of these

## Answer: C

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32. Find the domain and range of $f(x)=\frac{1}{\sqrt{x-2}}$
33. Find the domain and range of

$$
f(x)=\frac{x}{a+x^{2}}
$$

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34. Find the domain and range of the function $f(x)=\frac{x^{2}-9}{x-3}$

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35. Find the domain and range of $f(x) \frac{1}{2-\sin 3 x}$.

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1. If $\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3} / \frac{1}{3}\right)$, then find the values of x and y.

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2. Find the values of $x$ and $y$ from each of the following
(i) $(x+y, x-2 y)-(7,1)$
(ii) $(2 x, x+3 y)=(4,5)$

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3. If $\mathrm{A}=\{2,-3\}$ and $B=\{1,3,5\}$, then find $A \times B$ and $B \times A$.
4. If $\mathrm{A}=\{1,2\}$, then find $A \times A \times A$.

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5. If $A=\{x, y, z\}$ and $\mathrm{B}=\{2,3\}$, then find $A \times B$.

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6. If $\mathrm{A}=\{1,2,3,4\}$ and $\mathrm{B}=\{x: x \in N$ and $x$, is a prime number less than 5 \}, then find $A \times B$ and $B \times A$.

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7. If $A \times B=\{(a, 3),(a, 5),(b, 3),(b, 5),(c, 3),(c, 5)\}$, then find $B \times A$.
8. Find whether the following statements are true or false. If the statement is false, then write its correct statement:
(i) If $\mathrm{P}=\{\mathrm{m}, \mathrm{n}\}$ and $\mathrm{Q}=\{\mathrm{n}, \mathrm{m}\}$,then $P \times Q=\{(m, n),(n, m)\}$.
(ii) If A and B are non-empty sets, then $A \times B$ is a non-empty set of the ordered pairs ( $\mathrm{x}, \mathrm{y}$ ) such that $x \in A$ and $y \in B$.

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9. The Cartesian product $A \times A$ has 9 elements among which are found $(1,0)$ and $(0,1)$. Find the set A and the remaining elements of $A \times A$.

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10. If $A \times B=\{(a, 2),(b, 4),(a, 6),(b, 2),(b, 6),(a, 4)\}$, then find $A$ and $B$.

## D Watch Video Solution

11. If $\mathrm{A}=\{1,2,3\}, B=\{3,4\}$ and $C=\{4,5,6\}$, then find each of the following :
(i) $A \times(B \cap C)$
$(i i)(A \times B) \cap(A \times C)$
$(i i i) A \times(B \cup C)$
$(i v)(A \times B) \cup(A \times C)$

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12. If $\mathrm{A}=\{1,2,3,4,5\}, \mathrm{B}=\{1,2,3,6,7\}$ and $\mathrm{C}\{8\}$, then find $(\mathrm{A}-\mathrm{B}) \times C$.

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13. If $\mathrm{A}=\{1,2\}$ and $\mathrm{B}=\{\mathrm{x}, \mathrm{y}\}$, then find $A x B$. Also find the number of its subsets.

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14. If $\mathrm{A}=\{-1,1\}$, then find $A \times A \times A$.

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15. If $\mathrm{A}=\{1,2,3\}$ and $\mathrm{B}=\{1,2\}$, then represent $A \times B$ graphically.

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16. If $A=\{x, y, z\}$ and $B=\{5,6\}$, then represent each of the following by arrow diagram:
$(i) A \times B \quad(i i) B \times A$
$(i i i) A \times A \quad(i v) B \times B$

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17. The set $A$ and $B$ has 3 common elements. If $n(A)=5$ and $n(B)=4$, then find $n(A \times B)$ and $x\{(A \times B) \cap(B \times A)\}$

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18. $\subseteq B$, then prove that $A \times A \subseteq(A \times B) \cap(B \times A)$.

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19. Let $A$ be a non-empty set such that $A \times B=A \times C$. Show that $B=C$.
20. If $\operatorname{Aand} B$ are any two non-empty sets, then prove that: $A \times B=B \times A A=B$.

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## Exercise 2 B

1. If $A=\{a, b, c, d\}$ and $B=\{w, x y, z\}$, then which of the following is a relation from set $A$ to $B$ ? Given reason:
$(i) R_{1}=\{(a, w),(a, x),(a, y),(a, z)\}$
$(i i) R_{2}=\{(w, b),(z, c),(y, d)\}$
(iii) $R_{3}=\{(a, y),(b, y),(w, y),(d, y)\}$
(iv) $R_{4}=\{(b, z),(b, y),(c-z),(c, w)\}$

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2. Set $A$ has 5 eleements and set $B$ has 3 elements. Find the number of relations from set $A$ to $B$.

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3. If $A=\{a, y\}$ and $B=\{2,5\}$, then find the number of relations from set

A to B.
A. 4
B. 8
C. 16
D. 32

## Answer: C

4. If $A=\{1,2,3,4\}$ and $B=\{5,7,8,11,15\}$, are two sets and a relation $R$ from $A$ to $B$ is defined as follows:
${ }_{x} R_{y} \Leftrightarrow 2 x+3$, where $x \in A, y \in B$
(i) Express R in Roaster form.
(ii) Find the domain and range of $R$.
(iii) Find $R^{-1}$.
(iv) Represent R by arrow diagram.

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5. If $A=\{2,4,6,8\}$ and $B=\{1,3,5\}$, then find the domain and range of the relation:

$$
R\{(x, y): x \in A, y \in B \text { and } x>y\}
$$

6. If ${ }^{\prime} A=\{1,2,3,4,5,6\}$, then define a relation $R=\{(x, y): y=x-1\}$, from $A$ to $A$.

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7. A relation $R$ is shown from sets $P$ to $Q$ in the following diagram:

write this relation in Roaster form and in Set builder form. Also
find the domain, co-domain and range of the relation.
8. Write the relation $R=\left\{\left(x, x^{3}\right): x\right.$ is a prime number less than $10\}$ in roster form.

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9. $A$ is a set of first 10 natural numbers and $R$ is a relation from $A$ to $A$ defined as:
$(x, y) \in R \Leftrightarrow x+2 y=10$ when $x, y \in A$
(i)Express R in the form of a set of ordered pairs.
(ii) Find the domain and range of R.
(iii) Find $R^{-1}$.

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10. A relation $R_{1}$ is defined on the set of real numbers as follows:
$(\mathrm{a}, \mathrm{b}) \in R_{1} \Leftrightarrow 1+a b>0$, when $\mathrm{a}, \mathrm{b} \in \mathrm{R}$
(iii) $(a, b) \in R_{1}$ and $(b, c) \in R_{1} \rightarrow(a, c) \in R_{1}$ is not true when $\mathrm{a}, \mathrm{b}, \mathrm{c}, \in R$

## D Watch Video Solution

11. A relation R is defined on the set of $N_{2}$ as follows:
$R:\left\{(a, b): a, b \in N\right.$ and $\left.a=b^{2}\right\}$
Check whether the following statements are true ?
(i) For each $a \in N,(a, a) \in R$
(ii) (a,b) in R and (b,c) in R,whena, $b \in N$
(iii) $(a, b) \in R$ and $(b, c) \in R \rightarrow(a, c) \in R$, whena, $b, c \in N$

## D View Text Solution

12. If set $A=\{1,2,3,4\}$ and a relation $R$ is defined from $A$ to $A$ as
follows:
$R=\{(x, y): x>1, y=3\}$
Find the domain and range of $R$.

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13. A relation $R$ is defined from the set of integer $Z$ to $Z$ as follows:
$(x, y) \in Z \Leftrightarrow x^{2}+y^{2}=25$
(i) Express R and $R^{-1}$ as the set of ordered pairs.
(ii) Write the domain of R and $R^{-1}$.

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14. If $A=\{1,2,3,4,6\}$ and a relation $R$ on $A$ is defined as follows :
$R=\{(a, b): a, b \in A$, a divides $b\}$, then
(i) Write R in Roaster form.
(ii) Find the domain of R.
(iii) Find the range of $R$.

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Exercise 2 C

1. Let f be the subset of $Z \times Z$ defined by $f=\{(a b, a+b): a, b \in Z\}$. Is f a function from Z to Z ? Justify your answer.

## D Watch Video Solution

2. Examine each of the following relations given below and state in each case, giving reasons whether it is a function or not?(i)
$R=\{(2,1),(3,1),(4,2)\}$, (ii) $R=\{(2,2),(2,4),(3,3),(4,4)\}$
(iii) ${ }^{\wedge} \mathrm{R}=\{(1,2$
3. If $X=\{(1,2,3,4,5\}$ and $Y=\{1,3,5,7,9\}$, then find which of the following sets are functions from $X$ to $Y$ ?
(i) $R_{1}=\{(x, y): y=x+2, x \in X, y \in Y\}$
(ii) $R_{2}=\{(1,2),(2,1),(3,3),(4,3),(5,3)\}$
(iii) $R_{3}=\{(1,1),(1,3),(3,5),(3,7),(5,7)\}$
(iv) $R_{4}=\{(1,3),(2,5),(4,7),(5,9),(3,1)\}$

## D View Text Solution

4. Let $R$ be a relation defined on the set of natural numbers as:
$R=\{(x, y): y=3 x, y \in N\}$
Is $R$ a function from $N$ to $N$ ? If yes find its domain, co-domain and range.

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5. Express each relation in the form of ordered pair and check whether is it a function or not?
(i) $f=\{(x, y): y=3 x, x \in\{1,2,3\}, y \in\{3,6,9,12\}\}$
$($ ii) $g=\{(x, y): y>x+1, x \in\{1,2\}, y \in\{2,4,6\}\}$
(iii) $h=\{(x, y): x+y=3, x, y \in\{0,1,2,3\}\}$

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6. A function $f: R \rightarrow R$ is defined as:
$f(x)= \begin{cases}1 & x \in Q \\ -1 & x \notin Q\end{cases}$
Evaluate each of the following:
(i) $f(2), f(\pi)$
(ii) Range of $f$
$(i i i) f^{-1}(-1)$
$(i v) f^{-1}(1)$

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7. Find which of the following are the function on set $A=\{a, b, c\}$ ? Give reason.
(i) $R_{1}=\{(a, b),(b, a),(a, c)\}$
(ii) $R_{2}=\{(b, b),(c, c),(a, b)\}$

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8. A function $f: R \rightarrow R$ is defined as $f(x)=x^{2}-1$. Evaluate each of the following:
(i) $f^{-1}(-2)$
(ii) $f^{-1}(17)$
$(i i i) f^{-1}(26,50)$
$(i v) f^{-1}(0)$

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9. If $A=\{-3,-2,-1,0,1,2,3\}$ and $f: A \rightarrow Z$ is a function which of the following :
(i) Range of $f$
(ii) Pre-image of 5
(iii) Pre-image of 0

## D View Text Solution

10. 

If
$A=\{1,2,3,4\}, B=\{1,5,9,11,15,16\}$
and
$f=\{(1,5),(2,9),(3,1),(4,5),(2,11)\}$ are the following statements true?
(i) $f$ is a relation from $A$ to $B$.
(ii) $f$ is a function from $A$ to $B$

Justify your answer.

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11. If $\mathrm{A}=\{9,10,11,12,13\}$ and a function $f: A \rightarrow N$ is defined as $f(n)$ $=$ largest prime factor of n . If the range of f is B , then find B .

## - Watch Video Solution

12. If $\mathrm{A}=\{1,2\}$ and $\mathrm{B}=\{3,6\}$ and two functions $f: A \rightarrow B$ and $g: A \rightarrow B$ are defined respectively as :
$f(x)=x^{2}+2$ and $g(x)=3 x$
Find whether $f=g$

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13. Express the following functions in the form of order pairs and find their range:
(i) $f: A \rightarrow R, f(x)=x^{2}+5$, where $A=\{-2,-1,0,1\}$
$g: A \rightarrow N, g(x)=3 x$, where $A:\{x: x \in N, x<4\}$

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14. If a function $f: R \rightarrow R$ is defined as $f(x)=x^{2}+1$, then find each of the following :
(i) $\{x, f(x)=26\}$
(ii) Pre-image of 17 under $f$
(iii) Pre-image of 2 under $f$

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15. Let a function $f: R^{+} \rightarrow R$ is defined as $f(x)=\log _{e} x$, then find each of the following:
(i) Range of $f$
(ii) $f(x)=-2\}$
(iii) Is $f(x y)=f(x)+f(y)$ true?

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16. A function $F(c)$ is defined as:
$F(c)=\frac{9}{5} \cdot c+32$.
Evaluate each of the following:
(i) $\mathrm{F}(0)$
(ii) $F(28)$
(f-10)
(iv) Value of c when $\mathrm{F}(\mathrm{c})=212$

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17. If $f(x)=2 x-5$, then evaluate the following:
(i) $f(0)$
(ii) $f(7)$
(iii) $f(-3)$
18. If $f(x)=x^{2}$, then evaluate: $\frac{f(1 \cdot 2)-f(1)}{1 \cdot 2-1}$

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19. If $f(x)=x^{2}$, then evaluate : $\frac{f(x+1)-f(x-1)}{4 x}$

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20. If $f(x)=\frac{x}{x-1}$, then evaluate : $\frac{f(a / b)}{f(b / a)}$

## D Watch Video Solution

21. If $f(x)=\frac{x-1}{x+1}$, then prove that:
$\frac{f(b)-f(a)}{1+f(b) \cdot f(a)}=\frac{b-a}{1+a b}$
22. If $f(x)=\frac{1}{1-x}$, then prove that : $f[f\{f(x)\}]=x$

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23. If $(x)=\tan x$, the prove that : $f(x)+f(-x)=0$

## - Watch Video Solution

24. If $f(x)=x+\frac{1}{x}$, then prove that:
$\{f(x)\}^{3}=f\left(x^{3}\right)+3 \cdot f\left(\frac{1}{x}\right)$

## D Watch Video Solution

25. If $y=f(x)=\frac{a x-b}{b x-a}$, the prove that : $x=f(y)$

## D Watch Video Solution

26. If $y(x)=\sin x+\cos ^{2} x$, then prove that:
$f(x)=f(\pi-x)$

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27. If $f(x)=\frac{1-x^{2}}{1+x^{2}}$, then prove that:
$f(\tan \theta)=\cos 2 \theta$

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28. If $f(x)=x^{2}+x+1$, then find the value of ' $x$ ' for which

$$
f(x-1)=f(x)
$$

## - Watch Video Solution

29. 

If $\quad f(x)=\log _{e} x$,
then
prove
that
$: f(x y z)=f(x)+f(y)+f(z)$

## D Watch Video Solution

30. If $f(x)=\log _{e} x$ and $g(x)=e^{x}$, then prove that:
$f(g(x)\}=g\{f(x)\}$

## - Watch Video Solution

31. If $f(x)=\sqrt{\frac{1-x}{1+x}}$, then evalaute : $f(\cos 2 \theta)$

- Watch Video Solution

32. If $f(x)=\log \frac{1+x}{1-x}$, then prove that:
$f\left(\frac{2 x}{1+x^{2}}\right)=2 f(x)$

## - Watch Video Solution

33. If $f: R \rightarrow R$ is defined as:
$f(x)=\left\{\begin{array}{lll}2 x+1 & \text { if } x>2 \\ x^{2}-1 & \text { if }-2<x<2 \\ 2 x & \text { if } x<-2\end{array}\right.$
then evaluate the following:
(i) $f(1)$
(ii) $f(5)$
(iii) $f(-3)$

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34. 

$$
f(x)=\cos (\log x)
$$

$f(x) f(y)-\frac{1}{2}\left[f\left(\frac{x}{y}\right)+f(x y)\right]=$

## - Watch Video Solution

35. If $f(x)=3 \cos x$ and $g(x)=\sin ^{2} x$, the evaluate:
$(f+g)\left(\frac{\pi}{2}\right)$

## - Watch Video Solution

36. If $f(x)=x^{2}$ and $g(x)=2 x$, then evaluate,
(i) $(f+g)(3) \quad(i i)(f-g)(2)$
(iii) $(f \cdot g)(1) \quad(i v)\left(\frac{f}{g}\right)(5)$
37. Find the domain of the following functions:
$\frac{1}{x-3}$

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2. Find the domain of the following functions:
$x+1$

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3. Find the domain of the following functions:

$$
\frac{x-2}{x+4}
$$

A. R
B. $R-\{2\}$
C. $R-\{-4\}$
D. $\mathrm{R}-\{4\}$

## Answer: C

## D Watch Video Solution

4. Find the domain of the following functions:
$\frac{1}{x^{2}-4}$

- Watch Video Solution

5. Find the domain of the following functions:
$\sqrt{x-4}$
A. $[4, \infty]$
B. $[0, \infty]$
C. $(-\infty, 4]$
D. None of these

## Answer: A

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6. Find the domain of the following functions:
$\frac{1}{\sqrt{x-6}}$

## - Watch Video Solution

7. Find the domain of the following functions:
$\frac{1}{\sqrt{4-x}}$

## - Watch Video Solution

8. Find the domain of the following functions:
$\sqrt{(x-2)(4-x)}$

## - Watch Video Solution

9. Find the domain of the following functions:
$\frac{1}{\sqrt{25-x^{2}}}$

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10. Find the domain of the following functions:
$\frac{x^{2}+5 x+30}{x^{2}-8 x+7}$
A. $R-\{1,7\}$
B. $\mathrm{R}-[1,7]$
C. R
D. $\mathrm{R}-\{1\}$

## Answer: A

## D Watch Video Solution

11. Find the domain and range of the following functions:
$\frac{x-3}{2-x}$

## - Watch Video Solution

12. Find the domain and range of the following functions:
$\frac{1}{\sqrt{x-3}}$
13. Find the domain and range of the following functions:
$\frac{x^{2}}{1+x^{2}}$

## D Watch Video Solution

14. Find the domain and range of the following functions:
$\frac{x^{2}-4}{x-2}$

## - Watch Video Solution

15. Find the domain and range of the real function
$f(x)=\sqrt{9-x^{2}}$

- Watch Video Solution

16. Find the domain and range of the following functions:
$\sqrt{2-x}$

## - Watch Video Solution

17. Find the domain and range of the following functions:
$\frac{1}{\sqrt{x}}$

## D Watch Video Solution

18. Find the domain and range of the following functions:
$\sqrt{1-x^{2}}$

- Watch Video Solution

1. If $f(x)=x$ and $g(x)=|x|$, then define the following functions:
$(i) f+g$
(ii) $f-g$
$(i i i) f \cdot g$
(iv) $\frac{f}{g}$

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2. Find the domain of $f(x)=\frac{1}{x-|x|}$, when $x \in R$

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3. Find the domain of the function $\log \left|4-x^{2}\right|$.

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4. Find the domain and range of $f(x)=-|x|$.

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5. Find the domain and range of $f(x)=|x-1|$
A. Domain $=\mathrm{R}$, Range $=[0, \infty)$
B. Domain $=(-3,3)$, Range $=[0,-\infty)$
C. Domain $=$ R , Range $=[7, \infty)$
D. None of above

## Answer: A

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1. If $f=\{(2,3),(3,4),(4,5\}$, then its inverse is:
A. $\{(3,4),(4,5),(3,2)\}$
B. $\{(3,2),(4,3),(5,4)\}$
C. $\{(2,3),(4,3),(5,4)\}$
D. None of these

## Answer: b

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2. If $\mathrm{f}(\mathrm{x})=\frac{x+1}{x-1}$, then the value of $\mathrm{f}\{\mathrm{f}(3)\}$ is:
A. 3
B. 2
C. 6
D. None of these

## Answer: a

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3. If $\mathrm{f}(\mathrm{x})=\frac{x^{2}}{1+x^{2}}$, then the value of $\mathrm{f}\{\mathrm{f}(2)\}$ is:
A. $\frac{9}{41}$
B. $\frac{25}{41}$
C. $\frac{16}{25}$
D. $\frac{16}{41}$

Answer: d
4. If $\mathrm{f}(\mathrm{x})=\mathrm{x}-\frac{1}{x}$, then the value of $\mathrm{f}(\mathrm{x})+f\left(\frac{1}{x}\right)$ is:
A. 0
B. 2 x
C. $\frac{2}{x}$
D. None of these

Answer: a

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5. If $\mathrm{f}(\mathrm{x})=\log _{e}\left(\frac{1-x}{1+x}\right)$, then $f\left(\frac{2 x}{1+x^{2}}\right)$ is equal to :
A. $[f(x)]^{2}$
B. $2 \mathrm{f}(\mathrm{x})$
C. $4 \mathrm{f}(\mathrm{x})$
D. None of these

## Answer: b

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6. The domain of $\mathrm{f}(\mathrm{x})=\frac{x^{2}}{x^{2}-3 x+2}$ is:
A. R
B. R - \{1\}
C. $\mathrm{R}-\{1,2\}$
D. $R-\{-1,-2\}$

## Answer: c

7. The range of $\mathrm{f}(\mathrm{x})=\frac{|x|}{x} x \neq 0$ is :
A. $[0,1]$
B. $[-1,1]$
C. $(-1,1)$
D. $\{-1,1\}$

## Answer: D

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8. The domain of $\mathrm{f}(\mathrm{x})=\frac{1}{\sqrt{x-3}}$ is :
A. $(-\infty, 3)$
B. $(3, \infty)$
C. $[3, \infty)$
D. None of these

## Answer: B

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9. The range of function $\mathrm{f}(\mathrm{x})=|x+2|$ is:
A. R
B. $[0, \infty[$
C. ] $-\infty, 0$ ]
D. $] 0, \infty[$

## Answer: B

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10. If $\mathrm{f}(\mathrm{x})=\frac{1}{1-x} x \neq 1$ and $\mathrm{g}(\mathrm{x})=\frac{x-1}{x}, x \neq 0$, then the value of $g[f(x)]$ is :
A. $-x$
B. $x$
C. 2 x
D. None of these

## Answer: b

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## Exercise 2 G

1. If $f(x)=\cos (\log x)$, then $f(x) f(y)-\frac{1}{2}\left[f\left(\frac{x}{y}\right)+f(x y)\right]=$
B. $f(x+y)$
C. $\frac{1}{2} \cdot f(x) f(y)$
D. None of these

## Answer: a

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2. If $f(x)=\left(a-n^{n}\right)^{1 / n}$ where $a>0$ and $n \in N$, then $f[f(x)]$
is equal to :
A. $x$
B. a
C. $x^{n}$
D. None of these

## Answer: a

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3. If $f(x)=|x+1|$ then the true statement from the following is
A. $f\left(x^{2}\right)=\{f(x)\}^{2}$
B. $f(x+y)=f(x)+f(y)$
C. $f(|x|)=|f(x)|$
D. None of these

## Answer: d

4. If $f(x)=3 x+|x|$, then the value of $f(3 x)+f(-x)-f(x)$ is:
A. $3(x+|x|)^{2}$
B. $3(x+|x|)$
C. $(x-|x|)^{3}$
D. None of these

## Answer: B

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5. If $A=\left\{x: \frac{\pi}{6}<x<\frac{\pi}{3}\right\}$ and $f(x)=\cos x-x(1+x)$, then $f(A)$ is equal to :
A. $\left[(\pi),(6), \frac{\pi}{3}\right]$
B. $\left[\frac{-\pi}{3}, \frac{-\pi}{6}\right]$
C. $\left[\frac{1}{2}-\frac{\pi}{3}\left(1+\frac{\pi}{3}\right), \frac{\sqrt{3}}{2}-\frac{\pi}{6}\left(1+\frac{\pi}{6}\right)\right]$
D. None of these

## Answer: c

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6. If $f(x)=\frac{3 x+2}{5 x-3}$, then $f[f(x)]$ is equal to:
A. $-x$
B. $x$
C. 0
D. None of these

Answer: b
7. If $f(x)=a^{x}$, then the false statement from the following is:
A. $f(-x) \cdot f(x)=1$
B. $f(x+3)-2 f(x+2)+f(x+1)=(a-2)^{2} f(x+1)$
C. $f(x+y)=f(x) \cdot f(y)$
D. $f(x) \div f(y)=f\left(\frac{x}{y}\right)$

## Answer: b

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8. If $f(x)=10 x-7$ and $(f o g)(x)=x$, then $g(x)$ is equal to:
A. $\frac{x+7}{10}$
B. $\frac{x-7}{10}$
C. $\frac{1}{10 x-7}$
D. None of these

Answer: A

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$$
\begin{aligned}
& \text { 9. If } \quad f(x)=\cos (\log x) \\
& f\left(x^{2}\right) f\left(y^{2}\right)-\frac{1}{2}\left[f\left(\frac{x^{2}}{y^{2}}\right)+f\left(x^{2} y^{2}\right)\right] \text { has the value }
\end{aligned}
$$

A. $\frac{1}{2}$
B. -1
C. -2
D. None of these

Answer: d

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10. If $f(x)=\log \left(\frac{1+x}{1-x}\right) \operatorname{andg}(x)=\left(\frac{3 x+x^{3}}{1+3 x^{2}}\right)$, then $f(g(x))$ is equal to
A. $-f(x)$
B. $3 f(x)$
C. $[f(x)]^{2}$
D. None of these

## Answer: B

## Exercise 21

1. If $\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3}, \frac{1}{3}\right)$, find the values of x and y .

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2. If the set $A$ has 3 elements and the set $B=\{3,4,5\}$, then find the number of elements in $(A \times B)$.

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3. If $G=\{7,8\}$ and $H=\{5,4,2\}$, find $G \times \operatorname{HandH} \times G$.
4. Find whether the following statements are true or false. If the statement is false, then write its correct statement:
(i) If $\mathrm{P}=\{\mathrm{m}, \mathrm{n}\}$ and $\mathrm{Q}=\{\mathrm{n}, \mathrm{m}\}$, then $P \times Q=\{(m, n),(n, m)\}$.
(ii) If A and B are non-empty sets, then $A \times B$ is a non-empty set of the ordered pairs ( $\mathrm{x}, \mathrm{y}$ ) such that $x \in A$ and $y \in B$.

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5. If $A=\{(-1), 1)$,$\} find A \times A \times A$.

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6. If $A \times B=\{(a, x),(a, y),(b, x),(b, y)\}$. Find A and B .

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7. Let $A=\{1,2\}, B=\{1,2,3,4\}, C=\{5,6\}$ and $D=\{5,6,7,8\}$. Verify that:
(i) $A \times(B \cap C)=(A \times B) \cap(A \times C)$.
(ii) $A \times C$ is a subset of $B \times D$.

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8. Let $A=\{1,2\} \operatorname{and} B=\{3,4\}$. Write $A \times B$. How many subsets will $A \times B$ have? List them.

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9. Let $A$ and $B$ be two sets such that $n(A)=3$ and $n(B)=2 . \quad$ if $\quad(x, 1),(y, 2),(z, 1)$ are $\in A \times B$, find $A$ and $B$, where $x, y, z$ are distinct elements.

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10. The Cartesian product $A \times A$ has 9 elements among which are found $(1,0)$ and $(0,1)$. Find the set $A$ and the remaining elements of $A \times A$.

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## Exercise 22

1. Let $A=\{1,2,3 ; 14\}$. Define a relation on a set A by
$R=\{(x, y): 3 x-y=0$. where $x, y \in A\} \quad . \quad$ Depict $\quad$ this relationship using an arrow diagram. Write down its domain, codomain and range.
2. Define a relation $R$ on the set $N$ of natural numbers by $R=\{(x, y): y=x+5, \mathrm{x}$ is a natural number less than 4; $\mathrm{x}, y \in N$ \}. Depict this relationship using roster form. Write down the domain and the range.

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3. $A=\{1,2,3,5\}$ and $B=\{4,6,9\} A$ relation $R$ is defined from $A$ to $B$ by
$R=\{(x, y)$ : the difference between $x \& y$ is odd $\}$. Writer $R$ in roster form.

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4. The figure shows a relationship between the sets P and Q .

Write this relation :
(i) in set-builder from
(ii) Roaster from. What is its domain and range?


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5. Let $A=\{1,2,3,4,6\}$. Let R be the relation on A defined by $\{(a \dot{b}): a, b \in A$, is exactly divisible by $a\}$.(i) Write R in roster form(ii) Find the domain of $R$ (iii) Find the range of $R$.

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6. Determine the domain and range of the relation $R$ defined by
$R=\{(x, x+5): x \in\{0,1,2,3,4,5\}\}$.

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7. Write the relation $R=\left\{\left(x, x^{3}\right): x\right.$ is a prime number less than $10\}$ in roster form.

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8. Let $A=\{x, y, z\}$ and $B=\{1,2\}$. Find the number of relations from $A$ to $B$.
9. Let R be the relation on Z defined by $R=\{(a, b): a, b \in Z, a b$ is an integer\}.Find the domain and range of $R$.

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## Exercise 23

1. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.
(i) $\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}$
(ii) $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$
(iii) $\{(1,3),(1,5),(2,5)\}$

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2. Find the domain and range of the following real functions:(i) $f(x)=-|x|$ (ii) $f(x)=\sqrt{9-x^{2}}$

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3. A function f is defined by $f(x)=2 x \quad 5$. Write down the values of (i) $f(0)$, (ii) $f(7)$, (iii) $f(3)$.

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4. The function $t$ which maps temperature in degree Celsius into temperature in degree Fahrenheit is defined by $t(C)=\frac{9 C}{5}+32$ . Find (i) t (0) (ii) $\mathrm{t}(28)$ (iii) $t(10)$ (iv) The value of C , when $t(C)=212$.
5. Find the rage of each of the following functions.
$f(x)=2 \quad 3 x, \quad x \in R, x \quad>\quad 0$
$f(x)=x^{2}+2, \mathrm{x}$ is a real number. (iii) $f(x)=x, \mathrm{x}$ is a real number.

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## Miscellaneous Exercise

1. The relation $f$ is defined by $f(x)=\left\{x^{2}, 0 \leq x \leq 33 x, 3 \leq x \leq 10\right.$ The relating g is defined by $g(x)=\left\{x^{2}, 0 \leq x \leq 33 x, 2 \leq x \leq 10\right.$ Show that f is a function and g is not a function.
2. If $f(x)=x^{2}$, find $\frac{f(1.1)-f(1)}{(1.1-1)}$

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3. Find the domain of the function $f(x)=\frac{x^{2}+2 x+1}{x^{2}-8 x+12}$

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4. Find the domain and the range of the real function $f$ defined by

$$
f(x)=\sqrt{(x-1)}
$$

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5. Find the domain and the range of the real function/defined by
$f(x)=|x-1|$

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6. Let $f=\left\{\left(x, \frac{x^{2}}{1+x^{2}}\right): x \in R\right\}$ be a function from R into R . Determine the rage of $f$.

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7. Let $\mathrm{f}, \mathrm{g}: \mathrm{R} \rightarrow \mathrm{R}$ be defined, respectively by $f(x)=x+1$, $g(x)=2 x 3$. Find $f+g$, fgand $\frac{f}{g}$.

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8. Let $f=\{(1,1),(2,3),(0,1),(1,3)\}$ be a function from $Z$ to $Z$ defined by $f(x)=a x+b$, for some integers $\mathrm{a}, \mathrm{b}$. Determine $\mathrm{a}, \mathrm{b}$.
9. Let $R$ be $a$ relation from $N$ to $N$ defined by $R=\left\{(a, b): a \dot{b} \in N\right.$ and $\left.a=b^{2}\right)$. Are the following true?(i) $(a, a) \in R, f$ or alla $\in N($ ii $) \quad(a, b) \in R, \operatorname{implies}(b, a) \in R($ iii $)$ ` $(a$,

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10. 

$f=\{(1,5),(2,9),(3,1),(4,5),(2,11)\}$ are the following statements true ?
(i) $f$ is a relation from $A$ to $B$.
(ii) f is a function from A to B

Justify your answer.

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11. Let f be the subset of $Z \times Z$ defined by $f=\{(a b, a+b): a, b \in Z\}$. Is f a function from Z to Z ? Justify your answer.

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12. Let $A=\{9,10,11,12,13\}$ and let $f: A \rightarrow N$ be defined by $\mathrm{f}(\mathrm{n})$
$=$ the highest prime factor of $n$. Find the range of $f$.

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