

MATHS

BOOKS - NAGEEN MATHS (HINGLISH)

QUADRILATERALS

Solved Examples

1. The angles of a quadrilateral are in the ratio $3\!:\!4\!:\!5\!:\!6$. Find all its angles.



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2. Three angles of a quadrilateral are in the ratio 4:6:3. If the fourth angle is 100° find the three angles of the quadrilateral.

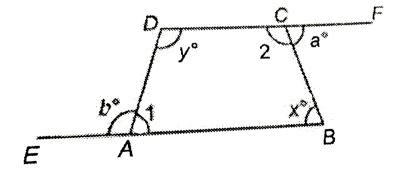
3. The angles of a quadrilateral are in the ratio 4:3:6:5. Show that it is a trapezium.



4. The side BA and DC of a quadrilateral ABCD are produced to E and F respectively. If

 $\angle BCF = a^0, \angle ABC = x^{\circ}, \angle ADC = y^{\circ} \text{ and } \angle DAE = b^{\circ},$

then find relation between a,b,x and y



$$A. x - y = a + b$$

$$B. x + y = a - b$$

$$\mathsf{C.}\,x-y=a-b$$

D.
$$x + y = a + b$$

Answer: D



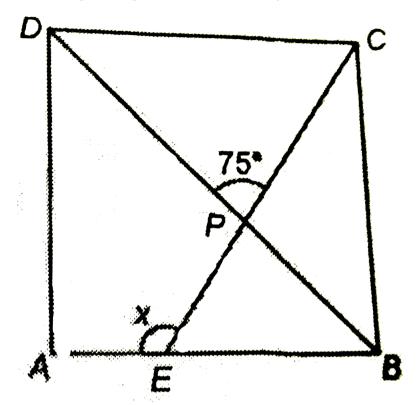
5. In a rectangle ABCD, diagonals AC and BD intersect at O. If

$$\angle OAB = 35^{\circ}$$
, find :

$$(a)\angle ABC(b)\angle ABO(c)\angle CO(d)\angle BOC)$$



6. In the given figure, ABCD is a square. Find \boldsymbol{x} .



A. 60°

B. 120°

C. 100°

D. 110°

Answer: B

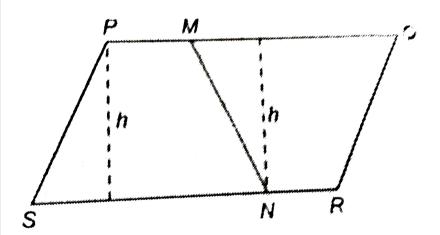


- **7.** In a quadrilateral ABCD, AO and BO are the bisectors of $\angle A$ and $\angle B$ respectively. Prove that $\angle AOB = \frac{1}{2}(\angle C + \angle D)$.
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- **8.** In a parallelogram ABCD, the bisectors of $\angle A$ and $\angle B$ intersect each other at point P. Prove that $\angle APB=90^\circ$.
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9. Find the remaining angle of a parallelogram if one of its angles is 110° .

10. PQRS is a parallelogram such that PQ is parallel to SR and SP is parallel to RQ. The length of side PQ is 20 cm. M is point between P and Q such that the length of PM is 3 cm. N is a points between points S and R. Find the length of SN such that segment MN divides the parallelogram in two regions with equal areas.



A. 15

B.17

C. 16

Answer: B

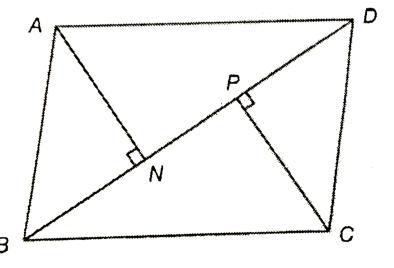


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11. In the given figure, ABCD is a parallelogram in which AN and CP are perpendiculars on diagonal BD. Prove that :

(i)
$$\Delta ADN = \Delta CBP$$

$$(ii)AN = CP$$



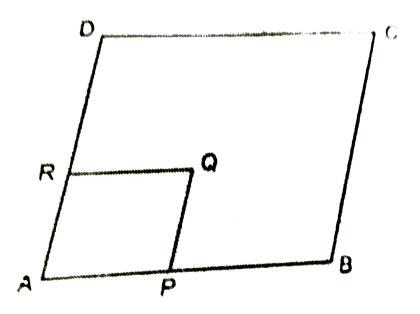
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12. In quadrilateral ABCD, AB ||CD and AD= BC, prove that /A = /B.



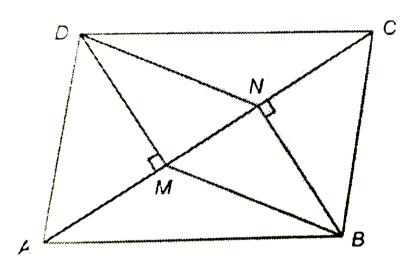
13. In the adjoining figure, $\Box ABCD$ and $\Box APQR$ are two parallelograms. Prove that :

$$\angle C = \angle Q$$
 and $\angle B = \angle R$



14. In the given figure, $\ \square$ ABCD is a parallelogram. If DM $\ \bot$ AC and

BN \perp AC, then show that $\square \, BNDM$ is a parallelogram.





15. The median AD of ΔABC is prodiced upto X such that AD= DX.

Prove that $\ \Box\ ABXC$ is a parallelogram.



16. ABCD is a parallelogram. Tow points P and Q are taken on sides AD and BC respectively such that AP $\frac{1}{3}AD$ and $CQ=\frac{1}{3}BC$. Prove that $\square AQCP$ is a parallelogram.



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17. A cyclic polygon has n sides such that each of its interior angle measures 114° . What is the measure of he angle subtended by each of its sides at the geometrical centre of the polygon?



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18. The number of diagonals of a regular polygon is 27. Then, find the measure of each of the interior angles of the polygon.

A. 120°		
B. 130°		
C. 150°		
D. 140°		
Answer: D		
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19. P is the mid-point of side AB of parallelogram ABCD. A line drawn from B parallel to PD meets CD at Q and AD produce at R. Prove that:

(i) AR = 2BC (ii) BR = 2BQ

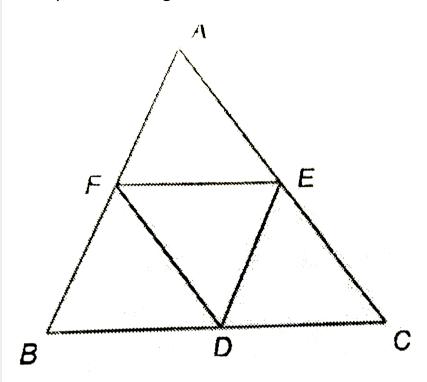


20. E and F are the mid-points of the sides AB and CD of a parallelogram ABCD. Prove that the line segment AF and CE trisects BD in three equal parts.



21. In the adjoining figure D, E and F are the mid-points of the sides BC, CA and AB of the equilateral ΔABC . Prove that ΔDEF is also

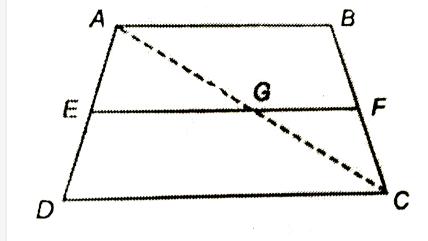
an equilateral triangle.





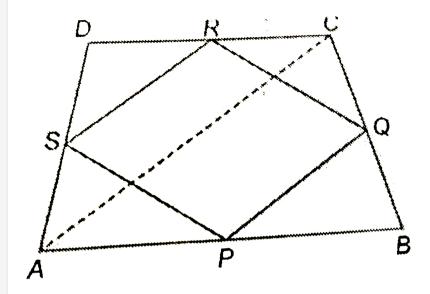
22. In the given figure. ABCD is a trapezium in which AB|| DC and E is the mid-point of AD, if EF||DC, then show that

 $EF = rac{1}{2}(AB + DC).$





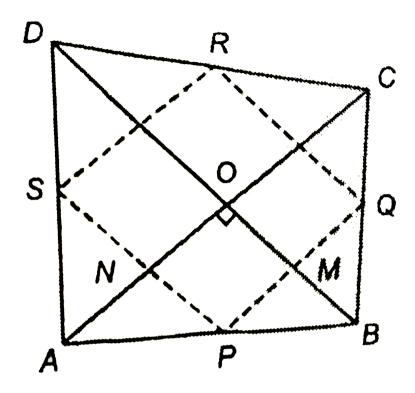
23. Prove that the figure formed by joining the mid-points of the pairs of consecutive sides of a quadrilateral is a parallelogram.





24. The diagonals of a quadrilateral ABCD are mutually perpendicular . Prove that the quadrilateral formed by joining the

mid-points of its consecutive sides is a reactangle.





25. Show that the quadrilateral formed by joining the mid-points of the consecutive sides of a rectangle is a rhombus.



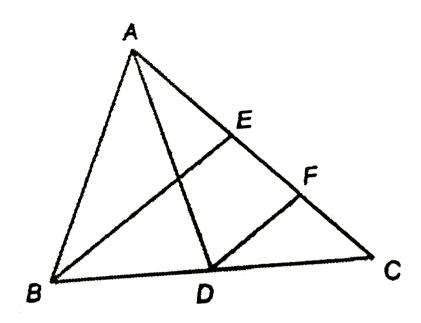
26. Show that the lines joining the mid-points of opposite sides of a quadrilateral bisect each other.



27. Prove that the line joining the mid-points of the diagonals of a trapezium is parallel to the parallel sides of trapezium and is half of their difference.



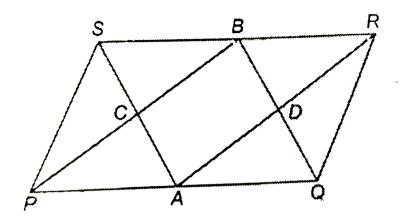
28. In the adjoining figure. AD and BE and BE are two medians of ΔANC . if DF||BE, then prove that $CG=rac{1}{4}AC$.





29. In the adjoining figure, PQRS is a parallelogram. A and B are the mid-points of PQ of SR respectively. If PS= BR, then prove that

quadrilateral ADBC is a reactangle.





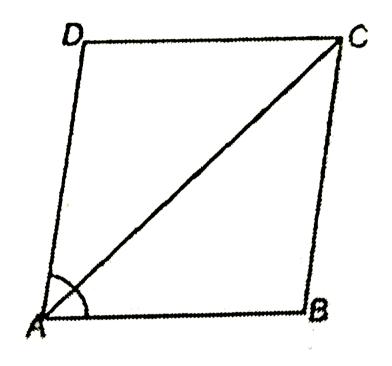
Problems From Ncert Exemplar

1. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.



2. Diagonal AC of a paraleligram ABCD bisects $\angle A$ (sec figure). Show that:

(i) it bisects $\angle C$ also (ii) ABCD is a rhombus.

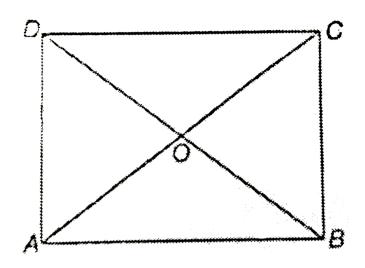




3. ABCD is a rectangle in which diagonal AC bisects $\angle A$ as well as

 $\angle C$. Show that

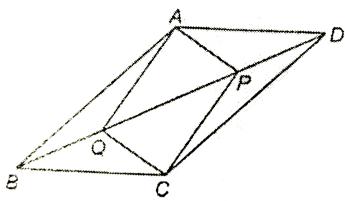
- (i) ABCD is a square
- (ii) diagonal AD bisects $\angle B$





4. In parallelogram ABCD two points P and Q are taken on diagonal BD such that DP = BQ (set figure). Show that:

 $(i)\Delta APD\cong CQB$ (ii)AP=CQ $(iii)\Delta AQB\cong \Delta CPD$ (iv)AQ=CP Itbegt (v)APCQ is a parallelogram.





5. ABCD is a rhombus and P, Q, R and S are wthe mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rectangle.

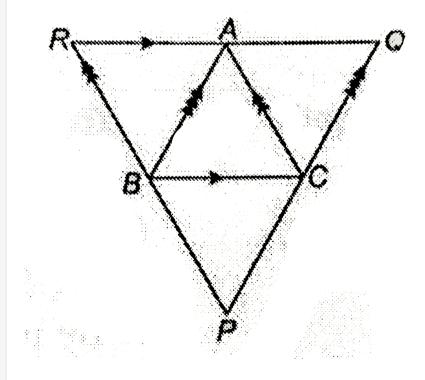


6. Show that the line segments joining the mid-points of the opposite sides of a quadrilateral bisect each other.



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7. Throuth A,B and C lines RQ, PR and QP have been drawn, respectively parallel to sides BC. CA and AB of a ΔABC as shown in the given figure. Show that $BC=\frac{1}{2}QR$.

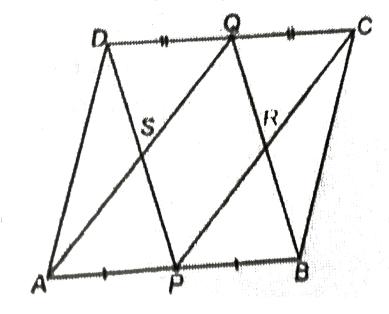


8. In the given figure, P is the mid-point of side BC of a parallelogram ABCD such that $\angle BAP = \angle DAP$. Prove that AD = 2CD.



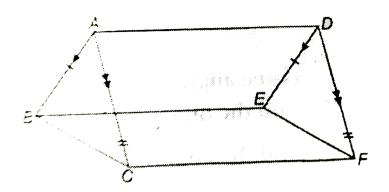
9. P and Q are the mid-point of the oposite sides AB and CD of a parallelogram ABCD. AQ interects DP at S and BQ interects CP at R.

Show that PQRS is a parallelogram.





10. In the given figure.AB||DE, AB=DE, AC||DF and AC=DF. Then which of the following is correct.



- A. BC||EF|
- B.BC = EF
- $\mathsf{C}.\,BothA$ and B
- D. None

Answer: C



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11. Prove that the quadrilateral formed by the bisectors of the angles of a parallelogram is a rectangle.

Exercise 8 A

1. The angles of a quadrilateral are 89° and 113° If the other two angles are equal, find the equal angles.



In

 $\angle A = 100^{\circ}, \angle B = 70^{\circ} \ \ ext{and} \ \ \angle C \colon \angle D = 8 \colon 11, ext{ then find } \ \ \angle D.$

quadrilateral

ABCD,

A. 100°

2.

B. 110°

C. 130°

D. 80°

Answer: B



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3. In quadrilateral ABCD, side AB is parallel to side

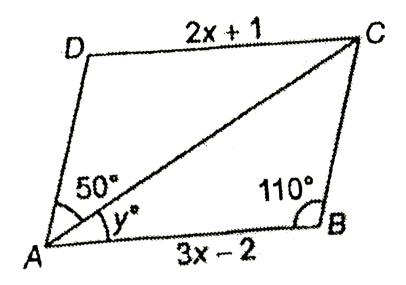
DC. $IF \angle A: \angle D = 1:2$ and $\angle C: \angle B = 4:5$.

- (i) Calculate wach angle of the quadrilateral.
- (ii) Assign special name to quadrilateral ABCD.



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4. Find the values of x and y from adjoining parallelogram.



A.
$$x=4,y=20^{\circ}$$

B.
$$x=3,y=20^\circ$$

C.
$$x=4,y=30^\circ$$

D. None

Answer: B

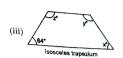


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5. Find x,y and z in each of the following figure:



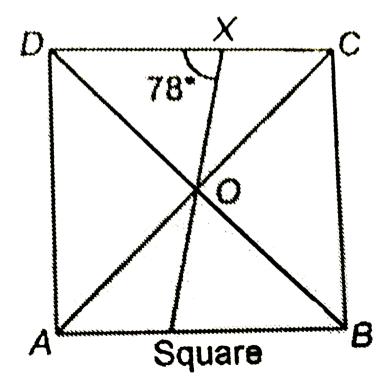






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6. In the given figure, find $(i) \angle XOD(ii) \angle XOC$



A.
$$(i)45^{\circ}$$
 $(ii)53^{\circ}$

B.
$$(i)57^{\circ}$$
 $(ii)33^{\circ}$

C.
$$(i)67^{\circ}$$
 $(ii)31^{\circ}$

D.
$$(i)37^{\circ}$$
 $(ii)23^{\circ}$

Answer: B



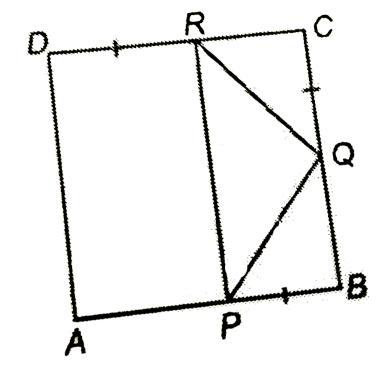
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7. In the given figure, ABCD is a square and

$$\angle PQR = 90^{\circ}$$
 . $IfPB = QC = DR, \,\, {
m prove \, that}.$

- (i) QB = RC
- (ii) PQ = QR

(iii) $\angle QPR = 45^{\circ}$





8. In a square ABCD, diagonals meet at O. P is point on BC such that

OB = BP.Show that (i)
$$\angle POC = \left(22\frac{1}{2}\right)^{\circ}$$

(ii)
$$\angle BDC = 2 \angle POC$$

(iii)
$$\angle BOP = 3 \angle COP$$

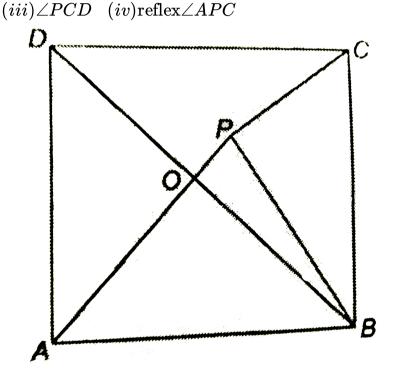


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9. The give figure shows a square ABCD and an equilayeral teiangle

APB. Calculate:

$$(1)\angle AOB$$
 $(ii)\angle BPC$



A.
$$(i)75^{\circ}$$
 $(ii)75^{\circ}$ $(ii)15^{\circ}$ $(iv)225^{\circ}$

B.
$$(i)55^{\circ}$$
 $(ii)65^{\circ}$ $(ii)35^{\circ}$ $(iv)215^{\circ}$

C.
$$(i)65^{\circ}$$
 $(ii)35^{\circ}$ $(ii)45^{\circ}$ $(iv)220^{\circ}$

D. $(i)45^{\circ}$ $(ii)65^{\circ}$ $(ii)35^{\circ}$ $(iv)125^{\circ}$

Answer: A

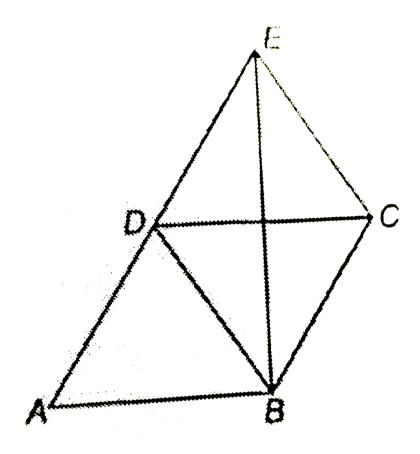


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10. In the given figure, ABCD is a rohombus with $A=67^{\circ}$. If DEC is an equilateral triangle, calculate

(i) $\angle CBE$

(ii) $\angle DBE$



A.
$$(i)25.5^{\circ}$$
 $(ii)29^{\circ}$

B.
$$(i)24.5^{\circ}$$
 $(ii)40^{\circ}$

C.
$$(i)26.5^{\circ}$$
 $(ii)30^{\circ}$

D.
$$(i)28.5^{\circ}$$
 $(ii)28^{\circ}$

Answer: C



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11. If the adjacent angles of a parallelogram are in the ratio $\frac{1}{3}$: $\frac{1}{2}$.

A.
$$72^{\circ}$$
, 108° , 72° , 108°

Find all the angles of parallelogram.

B.
$$70^{\circ}$$
, 110° , 70° , 110°

$$\mathsf{C.\,73}^{\circ},\,107^{\circ},\,73^{\circ},\,107^{\circ}$$

D.
$$74^\circ$$
 , 106° , 74° , 106°

Answer: A



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12. Prove that the sum of two consecutive angles of a parallelogram is $180\,^\circ$.



13. One angle of a parallelogram is 60° . Find its remaining angles.



14. One diagonal of a parallelogram biscets its one of the angles. Show tht it will also bisec the opposite angle.

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15. The opposite angles of a parallelogram are
$$(3x-2)^{\circ}$$
 and $(150-x)^{\circ}$. Find each angle of the parallelogram.

- A. 110° , 70° , 110° , 70°
- B. 111° , 69° , 111° , 69°
- C. 112° , 68° , 112° , 68°
- D. 109° , 71° , 109° , 71°

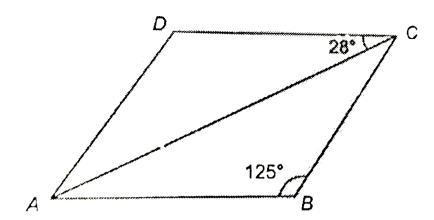
Answer: C



16. In the adjoining figure, ABCD is a parallelogram. If

$$\angle ABC = 125^{\circ}$$
,

 $\angle ACD = 28^{\circ}$, then fine $\angle DAC$.



- A. $25^{\,\circ}$
- B. 26°
- C. 27°
- D. 28°

Answer: C



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17. In a parallelogram, one angleis twice of its consecutiv angle. Find all the angles of the parallelogram.



18. In a parallelogram ABCD, AX and CY are the bisectors of $\angle A$ and $\angle C$ respectively. Prove that AX||CY.



19. In a parallelogram PQRS, PX and QY are the perpendiculars drawn from P and Q respectively so SR and SR produced. Prove that PX= QY.



20. In a parallelogram ABCD, the bisector of $\angle A$ bisects the line Bcat point X. Prove that AD = 2AB.

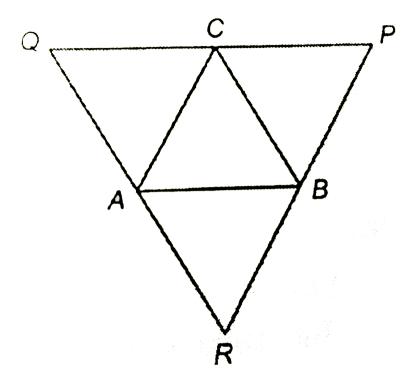


21. In a parallelogram ABCD, $\angle BCD=60^\circ$ If the bisectors AP and BP of $\angle A$ and $\angle B$ respectively, meet the side CD at point P, then prove that CP = PD.



22. In the adjoining figure, ΔPQR is formed by the sides PQ, QR and RP which are drawn parallel to sides AB,BC and CA respectively of ΔABC . Prove that

PQ + QR + RP + 2(AB + BC + CA).





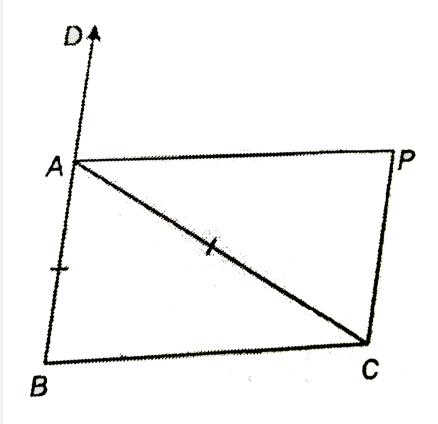
23. X and Y are the mid-points of the opposite sides AB and DC of a parallelogram ABCD. Then \Box AXCY is a ?

A. Trapezium

B. Kite

C. Rhombus
D. Parallelogram
A
Answer: D
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24. Two points X and Y lie on the diagonal BD of a parallelogram
ABCD such that DX = BT. Prove that $\ \Box\ AXCY$ is a parallelogram.
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25. In the adjoining figure, ΔABC is an isosceles triangle in which
AB = AC. Side CP is parallel to AB and AP is the bisector of exterior
angle CAD of Δ ABC. Prove that $\angle PAC = \angle BCA \ ext{and} \ \Box \ ABCP$

is a parallelogram.

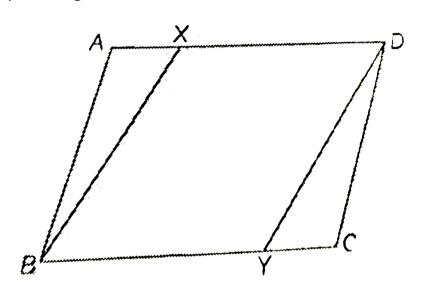




26. AB and CD are two parallel lines and a transversal 'l' intersects these lines at X and Y respectively Prove that the bisectors of interior angles from a parallelogram whose each angle is 90° .



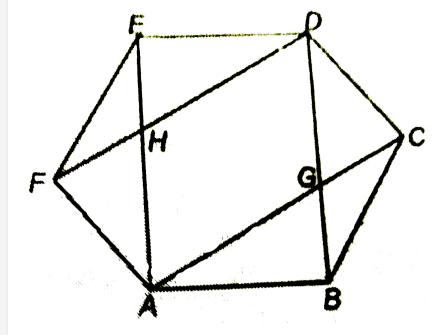
27. In the adjoining figure $\square ABCD$ is a parallelogeam. Points X and Y lie on the sides AD and BC respectively and $AX=\frac{1}{4}AD$ and $CY=\frac{1}{4}BC$. Show that $\square XBYD$ is a parallelogram.



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28. In the adjoining figure, ABCDEF is a regular hexagon. Prove that

 \square ABDE, \square ACDF and \square AGDH are parallelograms.



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29. Two triangles ΔABC and ΔDEF are given such that AB||DE,BC||EF and AB=DE,BC=EF. "Show that "AC"||"DFandAC=DE`



- **1.** The sides AB and AC are equal of an isosceles triangle ABC. D E and F are the mid-points of sides BC, CA and AB respectively. Prove that:
- (i) Line segment AD is perpedicular to line segment EF.
- (ii) Line segment AD bisects the line segment EF.
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- **2.** Show that the quadrialteral formed by joining the mid-points of the consecutive sides of a rhombus, is a rectangle.
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3. E is the mid-point of the median AD of ΔABC . Line segment BE meets AC at point F when produce, prove that $AF=rac{1}{3}AC$.

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4. Show that the quadrilateral, formed by joining the mid-points of the sides of a square is also a square.



5. Show that, in a parallelogram ABCD, the internal and external bisectors of $\angle A$ and $\angle B$ from a rectangle.



6. Prove that the quadrilateral formed by joining the mid-points of the pairs of consecutive sides of a quadrilateral is a parallelogram.



7. In $\Delta ABC, \angle B=90^{\circ}$. If P is the mid-point of side AC, then

$$PA = PB =$$

- A. AC
- B.3AC
- $C. \frac{1}{2}AC$
- D. 2AC

Answer: C



8. \square PQRS is a reactangle. If A, B and C are the mid-points of PQ,

PS and QR respectively, then prove that

$$AB + AC = \frac{1}{2}(PR + SQ).$$



9. P,Q and R are, respectively, the mid-points of sides BC,CA and AB of a triangle ABC , PR and BQ meet at $X\dot{C}R$ and PQ meet at Y . Prove that $XY=\frac{1}{4}BC$



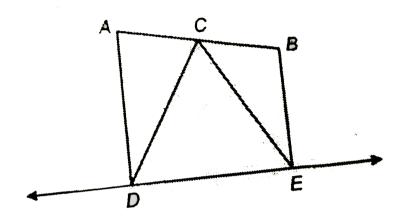
10. In ΔPQR , Pq=PR and S is the mid-point of PQ. A line drawn from S parallel to QR, intersects the line PR at T. Prove that PS = PT.



11. The points M and N divide the line seqment AB of ΔABC in three equal parts. If MP||NQ||BC and points P and Q lie on line AC, then prove that P and Q trisect the line AC.



12. In the adjoining figure, two points A and B lie on the same side of a line 'l'. C is the mid-point of AB. If AD $\perp l$ and $BE \perp l$, then prove that CD = CE.





13. AB and CD are the parallel sides of a trapeziuml. E is the midpoint of AD. A line through E and parallel to side AB meets the line BC at point F. Prove that F is the mid-point of BC.



14. Prove that a line drawn from the vertex of a triangle to its base is bisected by the line joining the mid points of the remaining two sides of the triangle.



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15. In a parallelogram ABCD, E and F are the mid-points of sides BC and AD respectively. Show that the line segment BF and ED trisect the diagonal AC.



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Revision Exercise Very Short Answer Questions

1. Three angles of aquadrilateral are respectively $100^\circ, 98^\circ, 92^\circ$.

Find the fourth angle.

Λ	50
Α.	. 11

B. 70°

C. 60°

D. 80°

Answer: B



- **2.** Find the other angles of a parallelogram if its one angle is 60°
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3. Find the angles of the parallelogram ABCD if $\angle C = \frac{2}{3} \angle D$.

A.
$$\angle A=\angle C=72^\circ$$
 , $\angle B=\angle D=108^\circ$

B.
$$\angle A = \angle C = 70^{\circ}$$
, $\angle B = \angle D = 110^{\circ}$

C.
$$\angle A = \angle C = 69^{\circ}$$
, $\angle B = \angle D = 111^{\circ}$

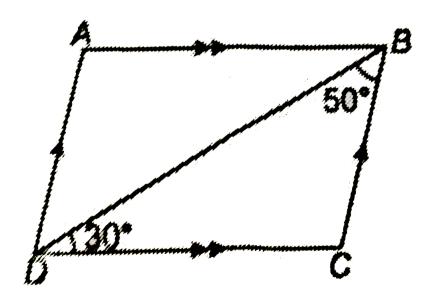
D.
$$\angle A = \angle C = 68^{\circ}$$
 , $\angle B = \angle D = 112^{\circ}$

Answer: A



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4. Find $\angle A$ of the given figure.



A.
$$\angle A=100^{\circ}$$

B.
$$\angle A = 90^{\circ}$$

C.
$$\angle A=70^{\circ}$$

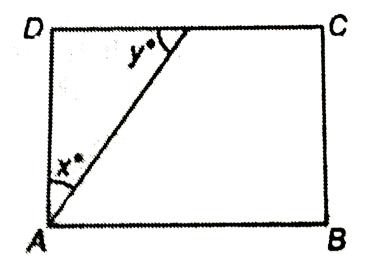
D.
$$\angle A=80^\circ$$

Answer: A



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5. In the given figure, if ABCD is a rectangle and $x\!:\!y=2\!:\!7$ find x and y.



A. 10° , 35°

B. 20° , 90°

C. 15° , 35°

D. 20° , 70°

Answer: D



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6. In a ΔABC , D, E and F are respectively the mid-points of BC, CA and AB. If the lengths of side AB, BC and CA are 7 cm, 8 cm and 9 cm respectively, find the permeter of ΔDEF .

- A. 13 cm
- $B.\,10\,\mathrm{cm}$
- $\mathsf{C.}\ 12\ \mathsf{cm}$
- D. 11 cm

Answer: C

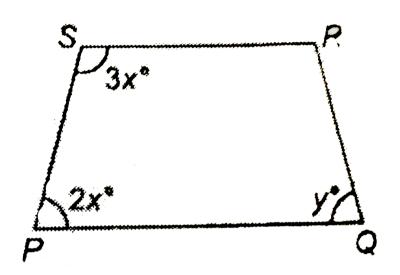


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7. If the bisectors of two adjacent angles $A\ and\ B$ of a quadrilateral ABCD intersect at a point O such that

$$\angle C + \angle D = k \angle AOB$$
, then find the value of k

8. In the given figure PQRS is an isosceles trapezium, fixd x and y.



A.
$$x=45^{\circ}~y=63^{\circ}$$

B.
$$x=50^\circ~y=58^\circ$$

C.
$$x=40^{\circ}~y=68^{\circ}$$

D.
$$x=36^{\circ}~y=72^{\circ}$$

Answer: D

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9. In a rhombus ABCD if $\angle ACB = 40^{\circ}$, then fine $\angle ADC$.



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10. The diagonals of a parallelogram ABCD intersect at O. If

$$\angle BOC = 90^{\circ} \text{ and } \angle BDC = 50^{\circ}, \text{find} \angle OAB.$$

A. $50^{\,\circ}$

B. 30°

C. 40°

D. 60°

Answer: C



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Revision Exercise Short Answer Questions

1. In an isoscles trapezium, show that the opposite angles are supplementary.



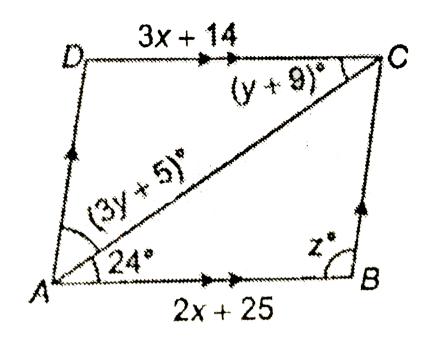
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In the given figure ABCD is a parallelogram. 2.

$$AB = (2x + 25)cm, CD = (3x + 14)cm,$$

$$egin{aligned} egin{aligned} egin{aligned} egin{aligned} B = z^o, egin{aligned} BAC = 24^\circ, egin{aligned} DAC = 3y + 5^\circ \end{aligned} ext{ and } egin{aligned} egin{aligned} DCA = y + 9^\circ, \end{aligned}$$

find the values of x, y and z.



A.
$$x=15, y=11, z=100^\circ$$

B.
$$x = 11, y = 15, z = 106^{\circ}$$

C.
$$x=10,y=12,z=80^\circ$$

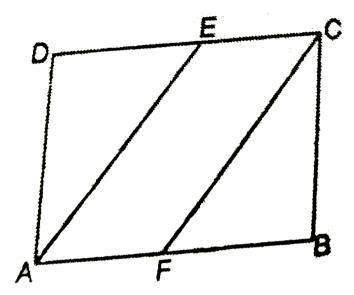
D. None

Answer: B



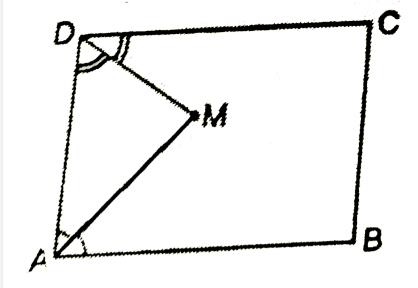
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3. ABCD is a parallelogram and AE and CF bisect $\angle A$ and $\angle C$ respectively. Prove that AE||FC.





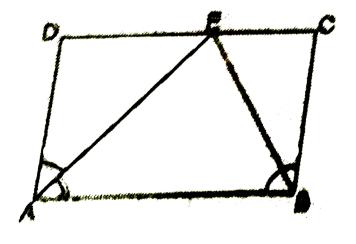
4. In the given figure, AM bisects angle A and DM bisects angle D of parallelogram ABCD. Prove that $\angle AMD=90^{\circ}$.





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5. In the given figure ABCD is a parallelogram. Prove that AB = 2BC.



6. E and F are points on diagonal AC of a parallelogram ABCD such that AE=CF. Show that BFDE is a parallelogram.

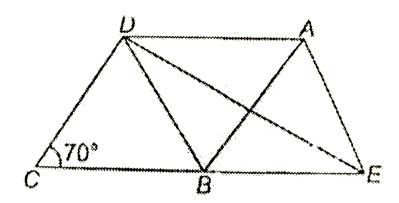


7. In a quadrilateral ABCD, AB= AD and CB = CD, prove that AC is perpendicular bisector of BD.



8. In the adjoining figure, ABCD is a rhombus and ABE is an equilateral triangle. If $\angle BCD = 70^{\circ}$, find

 $(a)\angle ADE$ $(b)\angle BDE$ $(c)\angle BED$



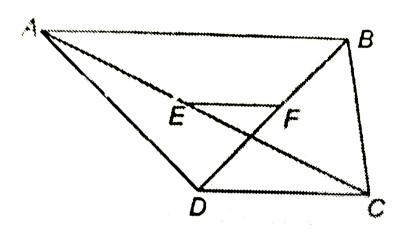
- A. $(a)20^{\circ}(b)40^{\circ}(c)30^{\circ}$
- B. $(a)25^{\circ}(b)30^{\circ}(c)35^{\circ}$
- C. $(a)30^{\circ}(b)45^{\circ}(c)15^{\circ}$
- D. $(a)40^{\circ}(b)30^{\circ}(c)20^{\circ}$

Answer: B



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9. In a trapezium ABCD, if E and F be the mid-points of diagonal AC and BD respectively. Prove that $EF=rac{1}{2}(AB-CD)$.



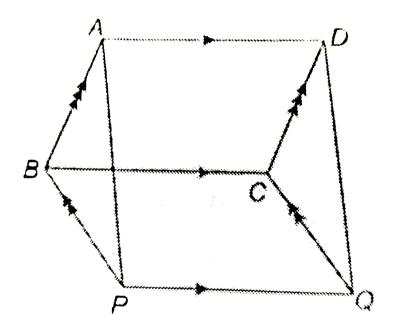


10. In a quadrilateral ABCD the linesegment bisecting $\angle C$ and $\angle D$ meet at E. Prove that $\angle A + \angle B = 2 \angle CED$.



1. In the adjoining figure, ABCD and PBCQ are paralelograms. Prove that

$$\Delta ABP\cong \Delta DCQ$$



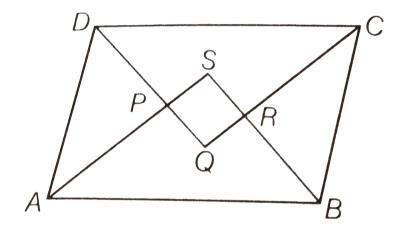


2. A transverals cuts two parallel lines at A and B. The two interior angles at A are bisected and so are the two interior angles at B, the

four bisectors from a quadrilateral ACBD, prove that ABCD is parallelogram.

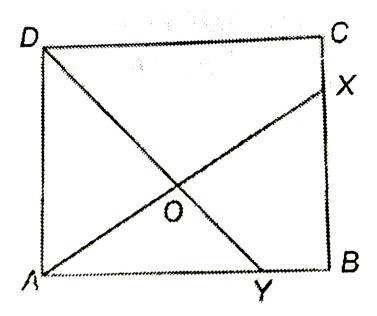


3. Prove that the quadrilateral formed by the bisectors of the angles of a parallelogram is a rectangle.





4. In a square ABCD, A is joined to a point X on BC and D is joined to a point Y on AB. If AX = DY, prove that AX is perpendicular to DY.





5. ABCD is a rhombus. RABS is a straight line such that RA = AB = BS. Prove that RD and SC when produced meet at right angles.

