



## MATHS

### BOOKS - PEARSON IIT JEE FOUNDATION

#### PROGRESSIONS

##### Example

1. In the series,  $T_n = 2n + 5$ , find  $S_4$ .

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2. Find the 14 th term of an AP whose first term is 3 and the common difference is 2.

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3. Find the first term and the common difference of an AP, if the 3rd term is 6 and 17 th term is 34.



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4. Find the sum of the first 22 terms of an AP whose first term is 4 and the common difference is  $\frac{4}{3}$ .

A. 396

B. 390

C. 456

D. 100

**Answer: A**



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5. Divide 124 into four parts in such a way that they are in AP and the product of the first and the 4<sup>th</sup> part is 128 less than the product of the 2<sup>nd</sup> and the 3<sup>rd</sup> parts.



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6. Find the three terms in AP, whose sum is 36 and product is 960.



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7. Find the sum of natural numbers and lying between 100 and 200 which leave a remainder of 2 when divided by 5 in each case.

A. 2990

B. 2847

C. 2936

D. None of these

**Answer: A**



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**8.** Find the sum of 100 terms of the series  $1(3) + 3(5) + 5(7) + \dots$

A. 1353300

B. 1353400

C. 135200

D. 1353100

**Answer: A**



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**9.** Find the 7th term of the GP whose first term is 6 and common ratio is

$$\frac{2}{3}$$



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10. Find the common ratio of the GP whose first and last terms are 25 and  $\frac{1}{625}$  respectively and the sum of the GP is  $\frac{19531}{625}$ .

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11. Find three numbers of a GP whose sum is 26 and product is 216.

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12. If  $|x| < 1$ , then find the sum of the series  $2 + 4x + 6x^2 + 8x^3 + \dots$

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13. Find the sum of the series  $1, \frac{2}{5}, \frac{4}{25}, \frac{8}{125}, \dots \infty$ .

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14.  $S_{10}$  is the sum of first 10 terms of a GP and  $S_5$  is the sum of the first 5 terms of the same GP. If  $\frac{S_{10}}{S_5} = 244$ , then find the common ratio.

A. 3

B. 4

C. 5

D. 2

**Answer: A**



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15. The difference between two hundred-digit numbers consisting of all 1's and a hundred-digit number consisting of all 2's is equal to

A.  $\underbrace{99\dots9}_{100 \text{ times}}$

B.  $\left( \frac{\underbrace{333\dots3}_{80 \text{ times}}}{80 \text{ times}} \right)^2$

C.  $\left(\frac{333\dots3}{100 \text{ times}}\right)^2$

D.  $\underbrace{99\dots9}_{200 \text{ times}}$

**Answer:**

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16. Find the 10 th term of the HP  $\frac{3}{2}, 1, \frac{3}{4}, \frac{3}{5}, \dots$

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17. Insert three harmonic between  $\frac{1}{12}$  and  $\frac{1}{20}$ .

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18. The ratio of geometric and arithmetic mean of two real numbers is 3 : 5. Then find the ratio of their harmonic mean and geometric mean.

A. 3 : 5

B. 9 : 25

C. 9 : 5

D. 5 : 9

**Answer: A**



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### Very Short Answer Type Questions

1. Third term of the sequence whose  $n$ th term is  $2n + 5$  is \_\_\_\_.



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2. If  $a$  is the first term and  $d$  is the common difference of an AP, then the  $(n + 1)$ th term of the AP is \_\_\_\_.



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3. If the sum of three consecutive terms of an AP is  $9m$ , then the middle term is \_\_\_\_.

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4. General term of the sequence  $5, 25, 125, 625, \dots$  is \_\_\_\_.

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5. The arithmetic mean of 7 and 8 is \_\_\_\_.

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6. The arrangement of numbers  $\frac{1}{2}, \frac{-3}{4}, \frac{-5}{6}, \frac{-7}{8}, \dots$  is an example of sequence. [True/False]

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7. If  $\frac{a}{2}$  is the first term and  $d$  is the common difference of an AP, then the sum of  $n$  terms of the AP is \_\_\_\_\_.

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8. In a sequence, if  $S_n$  is the sum of  $n$  terms and  $S_{n-1}$  is the sum of  $(n - 1)$  terms, then the  $n$ th term is \_\_\_\_\_.

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9. If  $T_n = 3n + 8$ , then  $T_{n-1} =$  \_\_\_\_\_.

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10. The sum of the first  $(n + 1)$  natural number is \_\_\_\_\_.

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11. For a series in geometric progression, the first term is  $a$  and the second term is  $3a$ . The common ratio of the series is \_\_\_\_\_.

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12. In a series, starting from the second term, if each term is its previous term, then the series is in \_\_\_\_\_ progression.

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13. All the multiples of 3 form a geometric progression. [True/False]

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14. If  $a$ ,  $b$  and  $c$  are in geometric progression then,  $a^2$ ,  $b^2$  and  $c^2$  are in \_\_\_\_\_ progression.

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15. If every term of a series in geometric progression is multiplied by a real number, then the resulting series also will be in geometric progression. [True/False]

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16. Geometric mean of 5, 10 and 20 is \_\_\_\_\_.

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17. Sum of the infinite terms of the GP,  $-3, -6, -12, \dots$  is 3. [True/False]

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18. The reciprocals of all the terms of a series in geometric progression form a \_\_\_\_\_ progression.

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19. The  $n$ th term of the sequence  $\frac{1}{100}, \frac{1}{10000}, \frac{1}{1000000}, \dots$  is \_\_\_\_\_.

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20. In a series,  $T_n = x^{2n-2} (x \neq 0)$ , then write the infinite series.

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21. The harmonic mean of 1, 2 and 3 is  $\frac{3}{2}$ . [True/False]

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22. If  $a, b, c$  and  $d$  are in harmonic progression, then  $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$  and  $\frac{1}{d}$  are in \_\_\_\_\_ progression.

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23. If the AM of two numbers is 9 and their HM is 4, then their GM is 6.

[True/False]

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24. If  $a, b$  and  $c$  are the arithmetic mean, geometric mean and harmonic mean of two distinct terms respectively, then  $b^2$  is equal to \_\_\_\_\_.

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25. If the sum of first  $n$  terms which are in GP is  $a(r + 1)$ , then the number of terms is \_\_\_\_\_. (Where  $a$  is the first term and  $r$  is the common

ratio)

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26. Write the first three terms of the sequence whose  $n$ th term is

$$T_n = 8 - 5n.$$

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27. Write the first three terms of the sequence whose  $n$ th term is

$$T_n = 5^{n+1}$$

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28. If three arithmetic means are inserted between 4 and 5, then the common difference is \_\_\_\_\_.

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29. If the 7 th and the 9 th terms of a GP are  $x$  and  $y$  respectively, then the common ratio of the GP is \_\_\_\_\_.

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30. In a series,  $T_n = 3 - n$ , then  $S_5 =$  \_\_\_\_\_.

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### Short Answer Type Questions

1. If the 5th term and the 14 th term of an AP are 35 and 8 respectively, then find the 20 th term of the AP.

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2. Which term of the series 21, 15, 9, ... is  $-39$  ?





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3. If the seventh term of an AP is 25 and the common difference is 4, then find the 15 th term of AP.



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4. Find the general term of AP whose sum of n terms is given by  $4n^2 + 3n$ .



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5. Find the sum of all three-digit numbers which leave a remainder 2, when divided by 6.



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6. If the ratio of the sum of first three terms of a GP to the sum of first six terms is 448 : 455, then find the common ratio.

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7. If in a GP, 5th term and the 12th term are 9 and  $\frac{1}{243}$  respectively, find the 9th term of GP.

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8. A person opens an account with ₹ 50 and starts depositing every day double the amount he has deposited on the previous day. Then find the amount he has deposited on the 10th day from the beginning.

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9. Find the sum of 5 geometric means between  $\frac{1}{3}$  and 243, by taking common ratio positive.

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10. Using progressions express the recurring decimal  $2 \cdot \overline{123}$  in the form of  $\frac{p}{q}$ , where  $p$  and  $q$  are integers.

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11. A ball is dropped from a height of 64 m and it rebounds  $\frac{3}{4}$  of the distance every time it touches the ground. Find the total distance it travels before it comes to rest.

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12. Find the sum to  $n$  terms of the series  $5 + 55 + 555 + \dots$





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13. In an HP, if the 3<sup>rd</sup> term and the 12<sup>th</sup> term are 12 and 3 respectively, then find the 15<sup>th</sup> term of the HP.



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14. If  $l$ th,  $m$ th and  $n$ th terms of an HP are  $x$ ,  $y$  and  $z$  respectively, then find the value of  $yz(m - n) + xz(n - 1) + xy(l - m)$ .



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15. The AM of two numbers is 40 more than GM and 64 more than HM. Find the numbers.



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1. Find the sum to  $n$  terms of the series

$$1 \cdot 2 \cdot 3 + 2 \cdot 4 \cdot 6 + 3 \cdot 6 \cdot 9 + \dots$$



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2. One side of an equilateral triangle is 36 cm. The mid-points of its sides are joined to form another triangle. Again another triangle is formed by joining the mid-points of the sides of this triangle and the process is continued indefinitely. Determine the sum of areas of all such triangles including the given triangle.



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3. Three positive numbers form a GP. If the middle number is increased by 8, the three numbers form an AP. If the last number is also increased by 64 along with the previous increase in the middle number, the resulting numbers form a GP again. Then :-



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4. Let A;G;H be the arithmetic; geometric and harmonic means of two positive no. a and b then  $A \geq G \geq H$



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5. The product of three numbers of a GP is  $\frac{64}{27}$ . If the sum of their products when taken in pairs is  $\frac{148}{27}$ , then find the numbers.



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## Level 1

1. Find  $t_5$  and  $t_6$  of the arithmetic progression  $0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \dots$

A.  $1, \frac{5}{4}$

B.  $\frac{5}{4}, 1$

C.  $1, \frac{7}{4}$

D.  $\frac{7}{4}, 1$

**Answer: A**



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2. If  $t_n = 6n + 5$ , then  $t_{n+1} = \underline{\hspace{2cm}}$ .

A.  $6n - 1$

B.  $6n + 11$

C.  $6n + 6$

D.  $6n - 5$

**Answer: B**



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3. Which term of the arithmetic progression 21, 42, 63, 84, ... is 420 ?

A. 19

B. 20

C. 21

D. 22

**Answer: B**



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4. Find the 15th term of the arithmetic progression 10, 4, -2, ...

A.  $-721 =$

B.  $-74$

C.  $-76$

D.  $-78$



**Answer: B**



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5. If the  $k$ th term of the arithmetic progression 25, 50, 75, 100, ... is 1000, then  $k$  is \_\_\_\_\_.

A. 20

B. 30

C. 40

D. 50

**Answer: C**



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6. The sum of the first 20 terms of an arithmetic progression whose first term is 5 and common difference is 4, is \_\_\_\_\_.

A. 820

B. 830

C. 850

D. 860

**Answer: D**



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7. Two arithmetic progressions have equal common differences. The first term of one of these is 3 and that of the other is 8, then the difference between their 100 th terms is \_\_\_\_\_.

A. 4

B. 5

C. 6

D. 3

**Answer: B**



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8. If  $a, b$  and  $c$  are in arithmetic progression, then  $b + c, c + a$  and  $a + b$  are in

- A. arithmetic progression
- B. geometric progression
- C. harmonic progression
- D. None of these

**Answer: A**



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9. The sum of the first 51 terms of the arithmetic progression whose 2nd term is 2 and 4th term is 8, is \_\_\_\_\_.

A. 3774

B. 3477

C. 7548

D. 7458

**Answer: A**



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**10.** Three alternate terms of an arithmetic progression are

$x + y$ ,  $x - y$  and  $2x + 3y$ , then  $x =$  \_\_\_\_\_.

A.  $-y$

B.  $-2y$

C.  $-4y$

D.  $-6y$

**Answer: D**

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11. Find the 15th term of the series 243, 81, 27, ...

A.  $\frac{1}{3^{14}}$

B.  $\frac{1}{3^8}$

C.  $\left(\frac{1}{3}\right)^9$

D.  $\left(\frac{1}{3}\right)^{10}$

**Answer: C**

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12. If  $t_8$  and  $t_3$  of a geometric progression are  $\frac{4}{9}$  and  $\frac{27}{8}$  respectively, then find  $t_{12}$  of the geometric progression.

A.  $\frac{64}{729}$

B.  $\frac{32}{243}$

C.  $\frac{729}{64}$

D.  $\frac{243}{32}$

**Answer: A**



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13. If  $t_n = 3^{n+1}$ , then  $S_6 - S_5 = \underline{\hspace{2cm}}$ .

A. 243

B. 81

C. 77

D. 27

**Answer: A**



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14. Find the sum of the first 10 terms of geometric progression  
18, 9, 4.5, ...

A.  $9 \frac{(2^{10} - 1)}{2^8}$

B.  $9 \frac{(2^{10} - 1)}{2^{10}}$

C.  $36 \left( \frac{2^{10} - 1}{2^8} \right)$

D.  $8 \frac{(2^{10} - 1)}{2^8}$

**Answer: A**



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15. If the 3rd, 7th and 11th terms of a geometric progression are  $p$ ,  $q$  and  $r$  respectively, then the relation among  $p$ ,  $q$  and  $r$  is \_\_\_\_.

A.  $p^2 = qr$

B.  $r^2 = qp$

C.  $q^2 = p^2 r^2$

D.  $q^2 = pr$

**Answer: D**



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16. Evaluate  $\sum (3 + 2^r)$ , where  $r = 1, 2, 3, \dots, 10$ .

A. 2051

B. 2049

C. 2076

D. 1052

**Answer: C**



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17. Find the sum of the series  $\frac{27}{8} + \frac{9}{4} + \frac{3}{2} + \dots \infty$



A.  $\frac{81}{8}$

B.  $\frac{27}{8}$

C.  $\frac{81}{16}$

D.  $\frac{9}{8}$

**Answer: A**



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**18.** If  $3x - 4$ ,  $x + 4$  and  $5x + 8$  are the three positive consecutive terms of a geometric progression, then find the terms.

A. 2, 8, 32

B. 2, 10, 50

C. 2, 6, 18

D. 12, 6, 3

**Answer: C**

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19. Find the geometric mean of the first twenty five powers of twenty five.

A.  $5^{13}$

B.  $5^{19}$

C.  $5^{24}$

D.  $5^{26}$

**Answer: D**

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20. Find the sum of 3 geometric means between  $\frac{1}{3}$  and  $\frac{1}{48}$  ( $r > 0$ ).

A.  $\frac{1}{4}$

B.  $\frac{5}{24}$

C.  $\frac{7}{24}$

D.  $\frac{1}{3}$

**Answer: C**



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**21.** If the second and the seventh terms of a Harmonic Progression are

$\frac{1}{5}$  and  $\frac{1}{25}$ , then find the series.

A.  $1, \frac{1}{5}, \frac{1}{9}, \dots$

B.  $\frac{1}{2}, \frac{1}{5}, \frac{1}{8}, \dots$

C.  $\frac{1}{7}, \frac{1}{5}, \frac{1}{3}, \dots$

D.  $\frac{1}{3}, \frac{1}{5}, \frac{1}{7}, \dots$

**Answer: A**



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22. The 10th term of harmonic progression  $\frac{1}{5}, \frac{4}{19}, \frac{2}{9}, \frac{4}{17}, \dots$  is \_\_\_\_\_.

A.  $\frac{11}{4}$

B.  $\frac{13}{4}$

C.  $\frac{4}{13}$

D.  $\frac{4}{11}$

**Answer: D**



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23. If the ratio of the arithmetic mean and the geometric mean of two positive numbers is 3:2, then find the ratio of the geometric mean and the harmonic mean of the numbers.

A. 2:3

B. 9:4

C. 3:2

D. 4:9

**Answer: C**



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24. If  $A$ ,  $G$  and  $H$  are AM, GM and HM of any two given positive numbers, then find the relation between  $A$ ,  $G$  and  $H$ .

A.  $A^2 = GH$

B.  $G^2 = AH$

C.  $H^2 = AG$

D.  $G^3 = A^2H$

**Answer: B**



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25. Find the least value of  $n$  for which the sum  $1 + 2 + 2^2 + \dots$  to  $n$  terms is greater than 3000.

A. 8

B. 10

C. 12

D. 15

**Answer: C**



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26. Find the HM of  $\frac{1}{7}$  and  $\frac{1}{12}$ .

A.  $\frac{1}{19}$

B.  $\frac{2}{19}$

C.  $\frac{3}{19}$

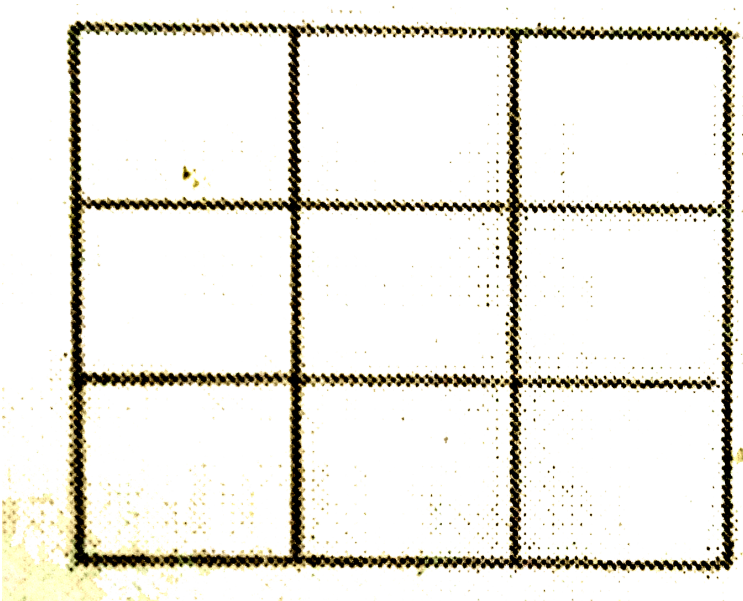
D.  $\frac{4}{19}$

Answer: B



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27. Number of rectangles in the following figure is \_\_\_\_.



- A. 9
- B. 10
- C. 24
- D. 36

**Answer: D**



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28. In a series, if  $t_n = \frac{n^2 - 1}{n + 1}$ , then  $S_6 - S_3 = \underline{\hspace{2cm}}$ .

A. 3

B. 12

C. 22

D. 25

**Answer: B**



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29. Find the number of terms to be added in the series  $27, 9, 3, \dots$  so that the sum is  $\frac{1093}{27}$ .



A. 6

B. 7

C. 8

D. 9

**Answer: B**



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**30.** Find the value of  $p(p > 0)$  if  $\frac{15}{4} + p$ ,  $\frac{5}{2} + 2p$  and  $2 + p$  are the three consecutive terms of a geometric progression.

A.  $\frac{3}{4}$

B.  $\frac{1}{4}$

C.  $\frac{5}{3}$

D.  $\frac{1}{2}$

**Answer: B**

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Level 2

1. If  $\frac{1}{b+c}$ ,  $\frac{1}{c+a}$  and  $\frac{1}{a+b}$  are in AP, then  $a^2$ ,  $b^2$  and  $c^2$  are in

- A. geometric progression
- B. arithmetic progression
- C. harmonic progression
- D. None of these

**Answer: B**

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2. Among the following, which term belongs to the arithmetic progression  $-5, 2, 9, \dots$  ?

A. 342

B. 343

C. 344

D. 345

**Answer: D**



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3. Five distinct positive integers are in arithmetic progressions with a positive common difference. If their sum is 10020, then find the smaller possible value of the last term.

A. 2002

B. 2004

C. 2006

D. 2007

**Answer: C**



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4. In a right triangle, the lengths of the sides are in arithmetic progression. If the lengths of the sides of the triangle are integers, which of the following could be the length of the shortest side ?

A. 2125

B. 1700

C. 1275

D. 1150

**Answer: C**



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5. If  $S_1 = 3, 7, 11, 15, \dots$  upto 125 terms and  $S_2 = 4, 7, 10, 13, 16, \dots$  upto 125 terms the how many terms are there in  $S_1$  that are there in  $S_2$  ?

A. 29

B. 30

C. 31

D. 32

**Answer: C**



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6. The first term and the  $m$ th term of a geometric progression are  $a$  and  $n$  respectively and its  $n$ th term is  $m$ . Then its  $(m + 1 - n)$ th term is \_\_\_\_.

A.  $\frac{ma}{n}$

B.  $\frac{na}{m}$

C.  $mna$

D.  $\frac{mn}{a}$

**Answer: B**



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7. The sum of the terms of an infinite geometric progression is 3 and the sum of the squares of the terms is 81. Find the first term of the series.

A. 5

B.  $\frac{27}{5}$

C.  $\frac{31}{6}$

D.  $\frac{19}{3}$

**Answer: B**



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8. If  $\log_{\sqrt{2}} x + \log_{\sqrt{\sqrt{2}}} x + \log_{\sqrt{\sqrt{\sqrt{2}}}} x + \dots$  upto 7 terms = 1016, the find the value of x.

- A. 4
- B. 16
- C. 64
- D. 2

**Answer: B**



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9. For which of the following values of x is  $8^{1 + \sin x + \sin^2 x + \sin^3 x + \dots + \infty} = 64$ ?

- A.  $60^\circ$
- B.  $135^\circ$
- C.  $45^\circ$

D.  $30^\circ$

**Answer: D**



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**10.** Find the sum of all the multiples of 6 between 200 and 1100.

A. 96750

B. 95760

C. 97560

D. 97650

**Answer: D**



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11. If the  $k$ th term of a HP is  $\lambda p$  and the  $\lambda$ th term is  $k p$  and  $k \neq \lambda$ , then the  $p$ th term is \_\_\_\_\_.

A.  $k^2 \lambda$

B.  $k^2 p$

C.  $p^2 k$

D.  $\lambda k$

**Answer: D**



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12. If six harmonic means are inserted between 3 and  $\frac{6}{23}$ , then the fourth harmonic mean is

A.  $\frac{6}{11}$

B.  $\frac{6}{17}$

C.  $\frac{3}{7}$

D.  $\frac{3}{10}$

**Answer: C**



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13. If  $a, b$  and  $c$  are positive numbers in arithmetic progression and  $a^2, b^2$  and  $c^2$  are in geometric progression, then  $a^3, b^3$  and  $c^3$  are in

(A) arithmetic progression.

(B) geometric progression.

(C) harmonic progression.

A. (A) and (B) only

B. only (C)

C. (A), (B) and (C)

D. only (B)

**Answer: C**



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14. The arithmetic mean  $A$  of two positive numbers is 8. The harmonic mean  $H$  and the geometric mean  $G$  of the numbers satisfy the relation  $4H + G^2 = 90$ . Then one of two numbers is \_\_\_\_\_.

- A. 6
- B. 8
- C. 12
- D. 14

**Answer: A**



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15. The infinite sum  $\sum_{n=1}^{\infty} \left( \frac{5^n + 3^n}{5^n} \right)$  is equal to

- A.  $\frac{3}{2}$

B.  $\frac{3}{5}$

C.  $\frac{2}{3}$

D. None of these

**Answer: D**



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16. (i) If  $x = 3 + \frac{3}{y} + \frac{3}{y^2} + \frac{3}{y^3} + \dots + \infty$ , then, show that  $y = \frac{x}{x-3}$ .

(Where  $|y| < 1$ ). The following are the steps involved in solving the above problem. Arrange them in sequential order.

(A)  $xy - 3y = x$

(B)  $x = 3 \left( \frac{1}{1 - \frac{1}{y}} \right)$

(C)  $y(x - 3) = x$

(D)  $x = 3 \left( \frac{y}{y - 1} \right)$

A. BDCA

B. BDAC

C. CABD

D. ACBD

**Answer: B**



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17. Find the harmonic mean of 5 and 3.

The following are the steps involved in solving the above problem. Arrange them in sequential order.

(A)  $HM = \frac{2 \times 5 \times 3}{5 + 3}$

(B) We know that the harmonic mean of  $a, b$  is  $\frac{2ab}{a + b}$ .

(C) Here,  $a = 5$  and  $b = 3$ .

(D)  $HM = \frac{30}{8} = \frac{15}{4}$

A. BCDA

B. BCAD

C. ABCD

D. BADC

**Answer: B**



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**Level 3**

1. The numbers  $h_1, h_2, h_3, h_4, \dots, h_{10}$  are in harmonic progression and  $a_1, a_2, \dots, a_{10}$  are in arithmetic progression. If  $a_1 = h_1 = 3$  and  $a_7 = h_7 = 39$ , then the value of  $a_4 \times h_4$  is

A.  $\frac{13}{49}$

B.  $\frac{182}{3}$

C.  $\frac{7}{13}$

D. 117

**Answer: D**



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2. Find the value of

$$\left(1 + \frac{1}{2}\right) \left(1 + \frac{1}{4}\right) \left(1 + \frac{1}{16}\right) \left(1 + \frac{1}{156}\right) \dots \infty.$$

A. 1

B. 2

C.  $\frac{1}{3}$

D.  $\frac{1}{4}$

**Answer: B**



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3. The ratio of the sum of  $n$  terms of two arithmetic progressions is given by  $(2n + 3) : (5n - 7)$ . Find the ratio of their  $n$ th terms.

A.  $(4n + 5) : (10n' + 2)$

B.  $(4n + 1) : (10n' - 12)$

C.  $(4n - 1) : (10n' + 8)$

D.  $(4n - 5) : (10n' - 2)$

**Answer: B**



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4. There are  $n$  arithmetic means (where  $n \in \mathbb{N}$ ) between 11 and 53 such that each of them is an integer. How many distinct arithmetic progressions are possible from the above data ?

A. 7

B. 8

C. 14

D. 16

**Answer: C**



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5. If  $x = \frac{1}{\sqrt{2}} + \frac{1}{2} + \frac{1}{2\sqrt{2}} + \dots + \infty$ , then find the value of  $x + \frac{1}{x}$ .

A.  $\sqrt{2}$

B.  $2\sqrt{2}$

C.  $3\sqrt{2}$

D.  $4\sqrt{2}$

**Answer: B**

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6. In a GP of 6 terms, the first and last terms are  $\frac{x^3}{y^2}$  and  $\frac{y^3}{x^2}$  respectively.

Find the ratio of 3rd and 4th terms of that GP.

A.  $x^2 : 1$

B.  $y^2 : x$

C.  $y : x$

D.  $x : y$

**Answer: D**



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7. If  $x = 3 + \frac{3}{y} + \frac{3}{y^2} + \frac{3}{y^3} + \dots + \infty$ , then  $y =$  \_\_\_\_\_.

A.  $\frac{x}{3}$

B.  $\frac{x}{x - 3}$

C.  $\frac{1 - x}{3}$

D.  $1 - \frac{3}{x}$

**Answer: B**



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8. Find the sum of  $\frac{0.3}{0.5} + \frac{0.33}{0.55} + \frac{0.333}{0.555} + \dots$  to 15 terms.

A. 10

B. 9

C. 3

D. 5

**Answer: B**



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9. In a GP, if the fourth term is the square of the second term, then the relation between the first term and common ratio is \_\_\_\_.

A.  $a = r$

B.  $a = 2r$

C.  $2a = r$

D.  $r^2 = a$

**Answer: A**



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10. For which of the following values of  $x$  is

$$(0^\circ < x < 90^\circ) 16^{1 + \cos x + \cos^2 x + \cos^3 x + \dots \infty} = 256 ?$$

A.  $30^\circ$

B.  $45^\circ$

C.  $60^\circ$

D.  $15^\circ$

**Answer: C**



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11. If  $t_2$  and  $t_3$  of a GP are  $p$  and  $q$ , respectively, then  $t_5 = \underline{\hspace{2cm}}$ .

A.  $p\left(\frac{q}{p}\right)^3$

B.  $p\left(\frac{q}{p}\right)^2$

C.  $\frac{p^2}{q^3}$

D.  $p^2q^2$

**Answer: A**



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12. If  $a, b, c, d$  are in GP, then  $(b + c)^2 = \underline{\hspace{2cm}}$ .

A.  $(b + d)(a + d)$

B.  $(a + d)(c + d)$

C.  $(a + b)(c + d)$

D.  $(a + c)(b + d)$

**Answer: C**



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13.  $a, b, c$  are in GP. If  $a$  is the first term and  $c$  is the common ratio, then  $b =$  \_\_\_\_\_.

A. 1

B.  $\frac{1}{a}$

C.  $\frac{1}{c}$

D. None of these

**Answer: A**



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14. In a GP of 7 terms, the last term is  $\frac{64}{81}$  and the common ratio is  $\frac{2}{3}$ .

Find the 3rd term.

A. 4

B. 9

C. 8

D. 12

**Answer: A**



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15. An AP starts with a positive fraction and every alternate term is an integer. If the sum of the first 11 terms is 33, then find the fourth term.

A. 2

B. 3

C. 5

D. 6

**Answer: A**



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16. If the sum of 16 terms of an AP is 1624 and the first term is 500 times the common difference, then find the common difference.

A. 5

B.  $\frac{1}{2}$

C.  $\frac{1}{5}$

D. 2

**Answer: C**



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17. Find the sum of the series

$$1 + (1 + 2) + (1 + 2 + 3) + (1 + 2 + 3 + 4) + \dots + (1 + 2 + 3 + \dots + 20)$$

.

A. 1470

B. 1540



C. 1610

D. 1370

**Answer: B**



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18. Evaluate  $\sum 2^i$ , where  $i = 2, 3, 4, \dots, 10$ .

A. 2044

B. 2048

C. 1024

D. 1022

**Answer: A**



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