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India's Number 1 Education App

## MATHS

# BOOKS - DHANPAT RAI \& CO MATHS (HINGLISH) 

## PERMUTATIONS AND COMBINATIONS

## Illustration

1. If $n$ !, $3 \times n$ ! and $(n+1)$ ! are in G P, then $n!, 5 \times n$ ! and $(n+1)$ ! are in:
A. A.P.
B. G.P.
C. H.P.
D. none of these

Answer: A

## - Watch Video Solution

2. If $a_{n}=\frac{n}{(n+1)!}$ then find $\sum_{n=1}^{50} a_{n}$
A. $\frac{50!-1}{50!}$
B. $\frac{51!-1}{51!}$
C. $\frac{1}{2(n-1)!}$
D. none of these

## Answer: B

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3. If $a_{n}=n(n!)$, then $\sum_{r=1}^{100} a_{r}$ is equal to
A. 101!
B. 100!-1
C. 101!-1
D. 101!+1

## Answer: C

Watch Video Solution
4.1.1! $+2.2!+3.3!+\ldots \ldots . n . n!=$
A. $(n+1)$ !
B. $(n+1)!+1$
C. $(n+1)!-1$
D. none of these
5. Sum of the series $\sum_{r=1}^{n}\left(r^{2}+1\right) r$ !, is
A. $(n+1)$ !
B. $(n+2)!-1$
C. $n(n+1)$ !
D. none of these

## Answer:

## D Watch Video Solution

6. Find the exponent of 3 in 100 !
A. 47
B. 48
C. 49
D. 46

## Answer:

## - Watch Video Solution

7. the exponent of 15 in 100 !, is
A. 48
B. 24
C. 25
D. 23

Answer: B
8. Number of zeros in the expansion of 100 ! is
A. 22
B. 23
C. 24
D. 25

## Answer:

## - Watch Video Solution

9. The exponent of 12 in 100 ! is
A. 24
B. 46
C. 47
D. 48

Answer: D

## - Watch Video Solution

10. If $\frac{{ }^{n+2} C_{6}}{{ }^{n-2} P_{2}}=11$, then $n$ satifes the equation
A. $n^{2}+n-110=0$
B. $n^{2}+5 n-84=0$
C. $n^{2}+3 n-108=0$
D. $n^{2}+2 n=0$

## Answer: C

## - Watch Video Solution

11. If . ${ }^{n} P_{r}=720$ and $.{ }^{n} C_{r}=120$ then find the value of $r$.
A. 3
B. 5
C. 4
D. 7

## Answer: A

## - Watch Video Solution

12. The number of positive intergers satisfying the in-equality ${ }^{n+1} C_{n-2}-{ }^{n+1} C_{n-1} \leq 100$, is
A. 6
B. 8
C. 5
D. none of these

## Answer:

13. If ${ }^{15} C_{3 r}={ }^{15} C_{r+3}$, then find $r$.
A. 5
B. 4
C. 3
D. 2

## Answer: C

## - Watch Video Solution

14. If ${ }^{20} C_{r}={ }^{20} C_{r-10}$, then ${ }^{18} C_{r}$ is equal to
A. 4896
B. 816
C. 1632
D. none of these

## Answer: B

## (D) Watch Video Solution

15. If. ${ }^{n-1} C_{1}=\left(k^{2}-3\right)^{n} C_{r+1}$ then K belongs to
A. $[-\sqrt{3}, \sqrt{3}]$
B. $(-\infty,-2)$
C. $(2,-\infty)$
D. $(\sqrt{3}, 2]$

## Answer: D

- Watch Video Solution

16. For $2 \leq r \leq n,\binom{n}{r}+2\binom{n}{r-1}+\binom{n}{r-2}$ is equal to
A. $\binom{n+1}{r-1}$
B. $2\binom{n+1}{r+1}$
C. $\binom{n+2}{r}$
D. $2\binom{n+2}{r}$

## Answer: C

## Watch Video Solution

17. the value of $40 c_{31}+\sum_{r=0}^{10}\left(C_{10+r}^{40-r}\right)$ is equal to
A. ${ }^{51} C_{20}$
B. $2^{50} C_{20}$
C. $2^{45} C_{15}$
D. none of these

## Watch Video Solution

18. The value of ${ }^{50} C_{4}+\sum_{r=1}^{6}{ }^{56-r} C_{3}$, is
A. ${ }^{56} C_{4}$
B. ${ }^{56} C_{3}$
C. ${ }^{55} C_{3}$
D. ${ }^{55} C_{4}$

## Answer:

- Watch Video Solution

19. What is. ${ }^{47} C_{4}+.{ }^{51} C_{3}+\sum_{j=2}^{5} \cdot{ }^{52-j} C_{3}$ equal to ?
A. ${ }^{52} C_{4}$
B. ${ }^{52} C_{3}$
C. ${ }^{51} C_{4}$
D. ${ }^{53} C_{4}$

## Answer:

## D Watch Video Solution

20. If $n \geq r$, then
${ }^{r} C_{r}+{ }^{r+1} C_{r}+{ }^{r+2} C_{r}+\ldots . .+{ }^{n} C_{r}$ is equal to
A. ${ }^{n+1} C_{r}$
B. ${ }^{n+1} C_{r+1}$
C. ${ }^{n+2} C_{r+1}$
D. ${ }^{n+2} C_{r+2}$

## Answer: B

21. $\sum_{k=m}^{n} k C_{r}$
A. ${ }^{n+1} C_{r+1}$
B. ${ }^{n+1} C_{r+1}-{ }^{m} C_{r}$
C. ${ }^{n+1} C_{r+1}-{ }^{m} C_{r+1}$
D. ${ }^{n+1} C_{r+1}+{ }^{m} C_{r+1}$

## Answer:

## - Watch Video Solution

22. The exponent of 7 in $100 C_{50}$ is
A. 0
B. 2
C. 4
D. none of these

## - Watch Video Solution

23. In a class there are 10 boys and 8 girls. The teacher wants to select either a boy or a girl to represent the class in a function. The number of ways the teacher can make this selection.
A. 18
B. 80
C. $10^{8}$
D. $8^{10}$

## Answer: A

24. In a class there are 10 boys and 8 girls. The teacher wants to select either a boy or a girl to represent the class in a function. The number of ways the teacher can make this selection.
A. 18
B. 80
C. $8^{10}$
D. $10^{8}$

## Answer: A

## - Watch Video Solution

25. There are 3 candidates for a Classical; 5 for a Mathematical and 4 for a Natural science scholarship. In how many ways can these scholarship be awarded?
A. 12
B. 20
C. 60
D. 64

## Answer: C

## - Watch Video Solution

26. A code word of length 4 consists two distinct consonant in the English alphabet followed by two digits from 1 to 9 with repetition allowed in digits. If the number of code wards so formed ending with an even digit is $432 \times k$, then $k$ is equal to
A. 7
B. 5
C. 49
D. 35

## Answer: D

## - Watch Video Solution

27. Five persons entered the lift cabin on the ground floor of an 8 -floor building. If each of them can leave the cabin independently at any floor beginning with the first; find the total number of ways in which each of the five persons can leave the cabin:
(i) at any one of the 7 floors and
(ii) at different floors.
A. $5^{7}, 2250$
B. $7^{5}, 2520$
C. $7^{5}, 0$
D. 35,35

## Answer: B

28. The number of ways in which $n$ distinct balls can be put into three boxes, is
A. $3 n$
B. $n^{3}$
C. $3^{n}$
D. $n+3$

## Answer: C

## - Watch Video Solution

29. Find the total number of ways in which $n$ distinct objects can be put into two different boxes so that no box remains empty.
A. $2^{n}$
B. $2^{n}-1$
C. $2^{n}-2$
D. $2^{n}-3$

## Answer: C

## (D) Watch Video Solution

30. Find the total number of ways of answering 5 objective type questions, each question having 4 choices.
A. $5^{4}$
B. $4^{5}$
C. 20
D. 9

## Answer: B

31. There are 10 true-false questions in an examination. Then these questions can be answered in
A. 240
B. 20
C. 1024
D. 100

## Answer: C

## ( Watch Video Solution

32. For a set of five true/false questions, no student has written all correct answers, and no two students have given the same sequence of answers. What is the maximum number of students in the classes, for this to be possible?
A. 9
B. 32
C. 31
D. 24

## Answer: C

33. The number of ways in which one can post 4 letters in 5 letter boxes, is
A. $4^{5}$
B. $5^{4}$
C. 20
D. 9

## Answer: B

## - Watch Video Solution

34. Four die are rolled. The number of ways in which at least one die shows 3 , is
A. 625
B. 671
C. 1296
D. 1256

## Answer: B

35. A sequence is a termary sequence, if it contains digits 0,1 and 2 . The total numbre of teranryn sequences of length 9 which either begin with 210 or end with 210 , is
A. 1458
B. 1431
C. 729
D. 707

## Answer: B

## - Watch Video Solution

36. The number of ways in which five distinct objects can be put into three identical boxes so that no box remains empty is
A. $2^{n}-1$
B. $2^{n}-2$
C. $2^{n-1}-1$
D. none of these

## Answer:

## - Watch Video Solution

37. A gentleman has 6 friends to invite. In how many ways can he send invitation cards to them if he has three servants to carry the cards.
A. $3^{6}$
B. $6^{3}$
C. 18
D. none of these

## Answer: A

38. There are unlimited number of identical balls of four different colours. How many arrangements of at most 8 balls in row can be made by using them?
A. 21845
B. 87380
C. 262140
D. none of these

## Answer: B

## - Watch Video Solution

39. A rectangle with sides of lengths $(2 n-1)$ and $(2 m-1)$ units is divided into squares of unit length. The number of rectangles which can be formed with sides of odd length, is
A. $m^{2} n^{2}$
B. $m n(m+1)(n+1)$
C. $4^{m+n-1}$
D. none of these

## Answer: A

## - Watch Video Solution

40. How many 5 -letter words, with or without meaning, can be formed out of the letters of the word EQUATIONS if repetition of letters is not allowed?
A. 126
B. $5^{9}$
C. $9^{5}$
D. 15120

## Answer: D

## - Watch Video Solution

41. It is required to sent 7 men and 3 women in a row so that women occupy the even places. How many such arrangements are possible?
A. ${ }^{\wedge}(5) C_{3} \times 3!\times 7!$
B. ${ }^{\wedge}(10) C_{5} \times 5$ !
C. ${ }^{\wedge}(5) C_{3} \times 10$ !
D. none of these

## Answer: A

42. Suppose that six students, including Madhu and Puja, are having six beds arranged in a row. Further, suppose that Mudhu does not want a bed adjacent to Puja. Then the number of ways, the beds can be allotted to students is
A. 384
B. 264
C. 480
D. 600

## Answer: C

## - Watch Video Solution

43. How many different signals can be made by 5 flags from 8 flags of different colours?
A. ${ }^{\wedge}(8) C_{5}$
B. ${ }^{\wedge}(8) C_{5} \times 5$ !
C. $5^{8}$
D. $8^{5}$

## Answer: B

## - Watch Video Solution

44. How many different signals can be given using any number of flags from 6 flags of different colours?
A. 720
B. 1440
C. 1956
D. 1950

## Answer:

45. Ten different letters of an alphabet are given. Words with five letters are formed from these given letters. Determine the number4 of words which have at least one letter repeated.
A. $10^{5}$
B. 30240
C. 69760
D. none of these

## Answer:

## - Watch Video Solution

46. The number of times the digit 3 will be written when listing the integers from 1 to 1000 is: 300 (b) 269 (c) 271 (d) 302
A. 300
B. 297
C. 243
D. 273

## Answer:

## - Watch Video Solution

47. A number of 18 guests have to be seated, half on each side of a long table. Four particular guests desire to sit on one particular side and three others on the other side. Determine the number of ways in which the sitting arrangements can be made.
A. $9!\times 9!$
B. ${ }^{11} C_{5} \times 9!\times 9$ !
C. $\frac{11!}{5!} \times 9!\times 9!$
D. ${ }^{11} C_{5}$

## Answer:

## - Watch Video Solution

48. How many different words, each containing 2 vowels and 3 consonants can be formed with 5 vowels and 17 consonants?
A. ${ }^{5} C_{2} \times{ }^{17} C_{3}$
B. ${ }^{5} C_{2} \times 5$ !
C. ${ }^{17} C_{3} \times 5$ !
D. ${ }^{5} C_{2} \times{ }^{17} C_{3} \times 5$ !

Answer: D

- Watch Video Solution

49. The number of integers greater than 6,000 that can be formed, using the digits $3,5,6,7$ and 8 , without repetition, is :
A. 120
B. 72
C. 216
D. 192

## Answer: D

## (D) Watch Video Solution

50. Find the sum of all the numbers that can be formed with the digits
$2,3,4,5$ taken all at a time.
A. $(2+3+4+5) \times 3$ !
B. $(2+3+4+5)\left(\frac{10^{4}-1}{10-1}\right)$
C. $(2+3+4+5) \times 3!\times\left(\frac{10^{4}-1}{10-1}\right)$
D. $\times 3!\times\left(\frac{10^{4}-1}{10-1}\right)$

## Answer:

## - Watch Video Solution

51. The sum of all the numbers greater than 10000 formed by using digits $0,2,4,6,8$, no digit being repeated in any numbers is,
A. $\frac{20}{9}\left(10^{5}-10^{4}\right)$
B. $\frac{40}{3}\left\{4\left(10^{5}-1\right)-\left(10^{4}-1\right)\right\}$
C. $\frac{20}{9}\left\{4\left(10^{5}-1\right)-\left(10^{4}-1\right)\right\}$
D. $20 \times 4!\left(\frac{10^{5}-1}{10-1}\right)$

## Answer:

52. A debate club consists of 6 girls and 4 boys. A team of 4 members is to be selected from this club including the selection of a captain (from among these 4 members) for the team. If the team has to include at most one boy, then the number of ways of selecting the team is
A. 380
B. 320
C. 260
D. 95

## Answer: A

## - Watch Video Solution

53. There are three sections in a question paper, each containing 5 questions. A candidate has to solve any 5 questions, choosing at least
one from each section. Find the number of ways in which the candidate can choose the questions.
A. ${ }^{15} C_{5}$
B. ${ }^{3} C_{1} \times{ }^{12} C_{4}$
C. 2250
D. 2253

## Answer:

## - Watch Video Solution

54. Let $S=\{1,2,3 ; 9\} \dot{F}$ or $k=1,2,5$, let $N_{k}$ be the number of subsets of S , each containing five elements out of which exactly $k$ are odd. Then $N_{1}+N_{2}+N_{3}+N_{4}+N_{5}=$ ? 210 (b) 252 (c) 125 (d) 126
A. 210
B. 252
C. 125
D. 126

## Answer:

## - Watch Video Solution

55. On how many nights may a watch of 4 men be arranged by a security agency from a crew of 16 so that no two watches are identical.

On how many of these nights would a particular person be off-duty?
A. 1820
B. 455
C. 1365
D. none of these

## Answer:

56. A box contains 2 white balls, 3 black balls and 4 red balls. The number of ways three balls be drawn from the box, if atleast one black ball is to be included in the draw is ........ .
A. 84
B. 20
C. 64
D. 104

## Answer: C

## - Watch Video Solution

57. How many diagonals are there in a polygon of n sides?
A. $\frac{n(n-1)}{2}$
B. $\frac{n(n-3)}{2}$
C. $\frac{n(n+1)}{2}$
D. none of these

## Answer: B

## (D) Watch Video Solution

58. There are 10 points in a plane, no three of which are in the same straight line, except 4 points, which are collinear.

Find the number of lines obtained from the pairs of these points,
A. 40
B. 39
C. 45
D. none of these
59. In a plane there are 37 straight lines, of which 13 pass pass through the point $B$. Besides, no three lines paseh both points $A$ and $B$ and no two are parallel, then theline passes through both points $A$ and $B$ and no number of intersection points the lines have, is
A. 533
B. 535
C. ${ }^{37} C_{2}-{ }^{24} C_{2}$
D. none of these

## Answer:

60. There are $m$ points on the line $A B$ and $n$ points on the line $A C$, excluding the point A. Triangles are formed joining these points
A. $\frac{m n}{2}(m+n-2)$
B. $\frac{m n}{2}(m+n-1)$
C. $\frac{m n}{2}(m+n)$
D. $\frac{m n}{2}(m+n+1)$

## Answer:

## - Watch Video Solution

61. Let $T_{n}$ be the number of all possible triangles formed by joining vertices of an $n$-sided regular polygon. If $T_{n+1}-T_{n}=19$ then the value of $n$, is
A. 7
B. 5
C. 10
D. 8

## Answer: B

## - Watch Video Solution

62. In how many ways five different rings can be worn in four fingers with at least one ring in each finger?
A. 120
B. 96
C. 20
D. 480

## Answer: D

63. In how many ways five different rings can be put on four fingers with at least one ring on each finger?
A. 120
B. 480
C. 240
D. 960

## Answer: D

## - Watch Video Solution

64. Let $A$ and $B$ be two finite sets having $m$ and $n$ elements respectively. Then the total number of mappings from $A$ to $B$ is
A. $n^{m}$
B. ${ }^{n} C_{m}$
C. ${ }^{n} C_{m} \times m$ !
D. $m^{n}$

## Answer:

## - Watch Video Solution

65. Two different packs of cards are shuffled together. Cards dealt equally among 4 players, each getting 13 cards. The number of ways in which a player get his cards if no two cards are from the same suit with the same denomination is
A. ${ }^{52} C_{13}$
B. $2^{13}$
C. ${ }^{52} P_{13}$
D. ${ }^{52} C_{13} \times 2^{13}$

## Answer:

## - Watch Video Solution

66. Prove that the no. of all permutations of $n$ different objects taken $r$ at a time when a particular object is to be always included in each arrangement is $r .(n-1) P_{r-1}$
A. ${ }^{n} C_{r} \times r$ !
B. ${ }^{n-1} C_{r-1} \times(r-1)$ !
C. ${ }^{n-1} C_{r-1} \times r$ !
D. ${ }^{n-1} C_{r} \times r$ !

## Answer:

67. Prove that the no. of all permutations of $n$ different objects taken $r$ at a time when a particular object is to be always included in each arrangement is $r .(n-1) P_{r-1}$
A. ${ }^{n-1} C_{r} \times(r-1)$ !
B. ${ }^{n-1} C_{r-1} \times r$ !
C. ${ }^{n-1} C_{r} \times r$ !
D. ${ }^{n} C_{r} \times r$ !

## Answer:

## - Watch Video Solution

68. Prove that the no. of permutations of $n$ different objects taken $r$ at a time in which two specified objects always occur together $2!(r-1)(n-2) P_{r-2}$

$$
\text { A. }{ }^{n-2} C_{r-2} \times r!
$$

B. ${ }^{n-2} C_{r} \times r!\times 2!$
C. ${ }^{n-2} C_{r} \quad 2 \times 2$ !
D. ${ }^{n-2} C_{r-2} \times(r-1)!\times 2$

## Answer:

## - Watch Video Solution

69. m women and n men are too be seated in a row so that no two men sit together. If $m>n$ then show that the number of wys in which they can be seated is $\frac{m!(m+1)!}{(m-n+1)!}$
A. $\frac{(m!n!)!}{(m+n)!}$
B. $\frac{m!(m+1)!}{(m-n+1)!}$
C. $\frac{m!(m+1)!}{(m+n+1)!}$
D.

## - Watch Video Solution

70. The number of ways of arranging m white and n black balls in a row
( $m>n$ ) so that no two black are placed together, is
A. ${ }^{m+1} C_{n} \times n!$
B. ${ }^{m} C_{n}$
C. ${ }^{m+1} C_{n}$
D. $m!n$ !

## Answer:

71. Five boys and five girls form a line with the boys and girls alternating. Find the number of ways of making the line.
A. $(5!)^{2}$
B. 10 !
C. $5!+5!$
D. $2(5!)^{2}$

## Answer: D

## - Watch Video Solution

72. Let n be the number of ways in which 5 boys and 5 girls can stand in a queue in such a way that all the girls stand consecutively in the queue. Let m be the number in which 5 boys and 5 girls stand in such a way that exactly four girls stand consecutively in the queue. Then the value of $\frac{m}{n}$ is
A. 4
B. 5
C. 6
D. 7

## Answer:

## - Watch Video Solution

73. The number of natural numbers belonging to (20000, 60000], whose sum of digits is even, is
A. 40000
B. 20000
C. 5000
D. 25000

## Answer:

## - Watch Video Solution

74. The number of five digit telephone numbers having at least one of their digits repeated is 90000 b .100000 c .30240 d .69760
A. 90000
B. 27216
C. 62784
D. 15120

## Answer:

75. At an election a voter may vote for nany number of candidates, not greater than the number t be eected. There are 10 candidates and 4 are to be elected. If a voter for at lest one candidates, thene the number of ways in which he can vote is (A) 5040 (B) 6210 (C) 385 (D) 1110
A. 5040
B. 6210
C. 385
D. 1110

## Answer:

## - Watch Video Solution

76. The set $S=\{1,2,3,, 12)$ is to be partitioned into three sets A, B, C of equal size. Thus, $A \cup B \cup C=S, A \cap B=B \cap C=A \cap C=\varphi$.

The numb
(4) $\frac{12!}{(4!)^{4}}$
A. $\frac{12!}{(4!)^{3}}$
B. $\frac{12!}{(3!)^{4}}$
C. $\frac{12!}{3!(4!)^{3}}$
D. $\frac{12!}{3!(3!)^{4}}$

## Answer:

## - Watch Video Solution

77. From 6 different novels and 3 different dictionaries, 4 novels and 1 dictionary are to be selected and arranged in a row on a shelf so that the dictionary is always in the middle. Then the number of such arrangements is
A. less than 500
B. at least 500 but less than 750
C. at least 750 but less than 1000
D. at least 1000

## Answer: D

## - Watch Video Solution

78. A man $X$ has 7 friends, 4 of them are ladies and 3 are men. His wife $Y$ also has 7 friends, 3 of them are ladies and 4 are men. Assume $X$ and $Y$ have no common friends. Then the total number of ways in which $X$ and $Y$ together can throw a party inviting 3 ladies and 3 men, so that 3 friends of each of $X$ and $Y$ are in the party, is :
A. 485
B. 468
C. 469
D. 484

## Answer: A

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79. How many different words can be formed with the letters of the word MISSISSIPPI?
A. $\frac{11!}{4!4!2!}$
B. $\frac{11!}{4!4!}$
C. $\frac{11!}{4!2!}$
D. none of these

Answer: A
80. How many different words can be formed by using all the letters of the word $A L L A H A B A D$ ?
A. 30
B. (9!)
C. $\frac{9!}{2!}$
D. $\frac{9!}{2!4!}$

## Answer: D

## - Watch Video Solution

81. The number of arrangements that can be made with the letters of the word 'MATHEMATICS' in which all vowels comes together, is
A. $\frac{8!\times 4!}{2!2!}$
B. $\frac{8!\times 4!}{2!2!2!}$
C. $\frac{8!}{2!2!2!}$
D. $\frac{8!}{4!2!2!}$

## Answer: B

## - Watch Video Solution

82. If all the letters of the word AGAIN be arranged as in a dictionary, what is the fiftieth word?
A. NAAGI
B. NAAIG
C. NIAAG
D. NAIAG

## Answer: B

83. If the letters of the word SACHIN are arranged in all possible ways and these words are written out as in dictionary, then the word SACHIN appears at serial number
A. 602
B. 603
C. 600
D. 601

## Answer: D

## - Watch Video Solution

84. The letters of the word COCHIN are permuted and all the permutations are arranged in an alphabetical order s in an English dictionary. The number of words that appear before the word COCHIN is
A. 360
B. 192
C. 96
D. 48

## Answer: C

## - Watch Video Solution

85. If all the words (with or without meaning) having five letters, formed using the letters of the word SMALL and arranged as in a dictionary; then the position of the word SMALL is :
A. $46^{t h}$
B. $59^{t h}$
C. $52^{\text {th }}$
D. $58^{\text {th }}$

## Answer: D

## - Watch Video Solution

86. how may four letter words can be formed using the letters of the word FAILURE so that F is included in each word?
A. ${ }^{6} C_{4} \times 4$ !
B. ${ }^{6} C_{3} \times 4$ !
C. ${ }^{6} C_{4}$
D. ${ }^{6} C_{4} \times 3$ !

## Answer: B

87. The number of five-letter words containing 3 vowels and 2 consonants that can be formed using the letters of the word 'EQUATION' so that the two consonants occur together, is
A. 720
B. 1440
C. 240
D. 480

## Answer: B

## - Watch Video Solution

88. In how many ways can 7 plus (+) and 5 minus (-) signs be arranged in a row so that no two minus ( - ) signs are together?
A. ${ }^{8} C_{5} \times 5$ !
B. ${ }^{7} C_{5} \times 5$ !
C. ${ }^{8} C_{5}$
D. 7 !

## Answer: C

## - Watch Video Solution

89. The number of ways in which four $S$ come consecutively in the word

MISSISSIPPI, is
A. 420
B. 840
C. 210
D. 630

## Answer: D

90. The number of ways in which four different letters can be put in the correspondingly five addressed envelopes so that all letters are put in the correct envelope, is
A. 6
B. 7
C. 8
D. 9

## Answer:

## - Watch Video Solution

91. If the 13 letter words (need no be meaningful) are to be formed using the letters from the word "MEDITERRANEAN" such that the first
letter is $R$ and the fourth letter is, $E$, then the total number of such words, is
A. $\frac{11!}{(2!)^{3}}$
B. 59
C. 110
D. 56

## Answer: A

## - Watch Video Solution

92. In how many ways, 20 guests and 1 host can be arranged around a circular table so that two particular guests are on either side of the host?
A. 18 !
B. $18!\times 2!$
C. $\frac{18!}{2!}$
D. 19!

## Answer: B

## - Watch Video Solution

93. There are 20 persons among whom are two brothers. The number of ways in which we can arrange them around a circle so that there is exactly one person between the two brothers, is
A. 18 !
B. $17!\times 2$ !
C. $18!\times 2$ !
D. 20 !

## Answer: C

94. There are 5 gentlemen and 4 ladies to dine at a round table. In how many ways can they as themselves so that no that ladies are together ?
A. 2880
B. 576
C. 1440
D. 480

## Answer: A

## - Watch Video Solution

95. The number of ways can seven persons sit around a table so that
all shall not have the same neighbours in any two arrangements is
A. 720
B. 360
C. 1440
D. none of these

## Answer:

## - Watch Video Solution

96. Ramesh has 6 friends. In how many ways can be invite one or more of them at a dinner ?
A. 64
B. 65
C. 63
D. $6!$

## Answer: C

## - Watch Video Solution

97. Find the total number of factors of 2160 (excluding 1 )
A. 40
B. 39
C. 41
D. 38

## Answer: B

## D Watch Video Solution

98. No of proper divisors of 7875...
A. 23
B. 24
C. 22
D. 21

## Answer: C

## - Watch Video Solution

99. The number of factors (excluding 1 and the expression itself) of the product of $a^{7} b^{4} c^{3}$ def, where $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}, \mathrm{e}$, fare all prime numbers, is
A. 1279
B. 1278
C. 1280
D. 1277

## Answer:

100. The number of even divisors of 10800 is
A. 12
B. 24
C. 36
D. 48

## Answer: D

## D Watch Video Solution

101. The number of divisors of the form $(4 n+2)$ of the integer 240 is
A. 4
B. 8
C. 10
D. 3

## Answer: A

## - Watch Video Solution

102. The number of divisors of 10800 which are divisible by 15 , is
A. 10
B. 20
C. 15
D. 30

## Answer: D

Watch Video Solution
103. If $r, s, t$ are prime numbers and $p, q$ are the positive integers such that their LCM of $p, q$ is $r^{2} t^{4} s^{2}$, then the numbers of ordered pair of $(p, q)$ is (A) 252 (B) 254 (C) 225 (D) 224
A. 252
B. 254
C. 225
D. 224

## Answer:

## - Watch Video Solution

104. The number of ways in which a pack of 52 cards be divided equally amongst four players in order, is
A. $\frac{52!}{(13!)^{4}}$
B. $\frac{52!}{(13!)^{4} 4!}$
C. $\frac{52!}{13!}$
D. $\frac{52!}{4!\times 13!}$

Answer: A

## - Watch Video Solution

105. The number of ways of dividing a pack of 52 cards into 4 equal groups is
A. $\frac{52!}{(13!)^{4}}$
B. $\frac{52!}{(13!)^{4} 4!}$
C. $\frac{52!}{(13!)^{4} \times 4}$
D. $\frac{52!}{13!\times 4}$

## Answer: B

106. (i) In how many ways can a pack of 52 cards be divided equally among four players? (ii) (ii) In how many ways can you divide these cards in four sets, three of them having 17 cards each and the four the one just one card?
A. $\frac{52!}{(17!)^{3} 3!}$
B. $\frac{52!}{(17!)^{3}}$
C. $\frac{52!}{51!(17!)^{3}}$
D. $\frac{52!}{51!}$

## Answer:

## - Watch Video Solution

107. The total number of ways in which 30 mangoes can be distributed
A. ${ }^{30} C_{5}$
B. $30^{5}$
C. $5^{30}$
D. ${ }^{34} C_{4}$

## Answer: D

## - Watch Video Solution

108. The number of ways of distributing 5 identical balls in into three boxes so that no box is empty (each box being large enough to accommodate all balls), is
A. $3^{5}$
B. $5^{3}$
C. 15
D. 6

## Answer: D

## - Watch Video Solution

109. In how many ways can 20 identical toys be distributed among 4 children so that each one gets at least 3 toys?
A. ${ }^{11} C_{2}$
B. ${ }^{12} C_{3}$
C. ${ }^{11} C_{3}$
D. ${ }^{12} C_{4}$

Answer: C

- Watch Video Solution

110. The total number of non-negative integral solutions of $x_{1}+x_{2}+x_{3}+x_{4}=100$, is
A. ${ }^{100} C_{3}$
B. ${ }^{99} C_{3}$
C. ${ }^{103} C_{3}$
D. ${ }^{99} C_{4}$

## Answer: C

## (D) Watch Video Solution

111. The number of integral solutions of equation $x+y+z+t=29$,
when $x \geq 1, y \geq 2, z \geq 2,3$ and $t \geq 0$ is
A. ${ }^{26} C_{4}$
B. ${ }^{26} C_{3}$
C. ${ }^{22} C_{3}$
D. ${ }^{29} C_{3}$

## Answer:

## - Watch Video Solution

112. The number of ways in which 16 sovereigns can be distrbuted among three applicants such that each applicant does not receive less than 3 sovereigns, is
A. ${ }^{16} C_{3}$
B. ${ }^{9} C_{2}$
C. ${ }^{9} C_{3}$
D. ${ }^{10} C_{2}$

## Answer:

113. The number of points, having both co-ordinates as integers, that lie in the interior of the triangle with vertices $(0,0),(0,41)$ and $(41,0)$ is
A. 820
B. 780
C. 901
D. 861

## Answer:

## - Watch Video Solution

114. Total number of integral solutions of the system of equations $x_{1}+x_{2}+x_{3}+x_{4}+x_{5}=20$ and $x_{1}+x_{2}+x_{3}=5$ when $x_{k} \geq l 0$, is
A. 335
B. 336
C. 338
D. 340

## Answer:

## - Watch Video Solution

115. In how many ways can four persons, each throwing a die once, make a sum of 6?
A. ${ }^{9} C_{2}$
B. ${ }^{10} C_{3}$
C. ${ }^{8} C_{3}$
D. ${ }^{9} C_{3}$

## Answer:

## - Watch Video Solution

116. In how many ways can four persons each throwing a dice, once, make a sum of 13 ?
A. 220
B. 180
C. 140
D. 80

## Answer: C

117. Between two junction stations $A$ and $B$ there are 12 intermediate stations. The total numbre of ways in which a train can be made to stop at 4 of these stations so that no two of these halting stations are consecutive, is
A. ${ }^{9} C_{5}$
B. ${ }^{9} C_{4}$
C. ${ }^{10} C_{4}$
D. ${ }^{10} C_{5}$

## Answer: B

## - Watch Video Solution

118. The number of ways in which 5 letters can be placed in 5 marked envelopes, so that no letter is in the right encelope, is
A. 45
B. 44
C. 43
D. 46

## Answer: B

## - Watch Video Solution

119. Ravish writes letters to his five friends and addresses the correspondig envelopes. The total number of ways in which letters can be placed in the envelopes so that at least two of them are in the wrong envelopes, is
A. 120
B. 118
C. 119
D. 121

## Answer:

## - Watch Video Solution

## Section I Solved Mcqs

1. If $n={ }^{m} C_{2}$ the valuen of ${ }^{n} C_{2}$ is given by
A. ${ }^{m+1} C_{4}$
B. ${ }^{m-1} C_{4}$
C. ${ }^{m+2} C_{4}$
D. none of these

## Answer: D

## - Watch Video Solution

2. If $(n-1) C_{r}=\left(k^{2}-3\right) n C_{r+1}$, then k belong to
A. $(-\infty,-2]$
B. $(2, \infty]$
C. $[-\sqrt{3}, \sqrt{3}]$
D. $(\sqrt{3}, 2]$

## Answer:

## - Watch Video Solution

3. The sum $\sum_{i=0}^{m}{ }^{10} C_{i} \times{ }^{20} C_{m-i}\left(\right.$ where ${ }^{p} C_{q}=0$ if $\left.p<q\right)$
is maximum, when m is
A. 5
B. 10
C. 15
D. 20

## Answer:

## - Watch Video Solution

4. The exponent of 7 in 100 !, is
A. 14
B. 15
C. 16
D. none of these

## Answer:

- Watch Video Solution

5. The number of zeros at the end of 100 !, is
A. 24
B. 51
C. 10
D. 70

## Answer: A

## Watch Video Solution

6. The number 24 ! is divisible by
A. $6^{24}$
B. $24^{6}$
C. $12^{12}$
D. $48^{5}$

## Answer: B

7. If a and b are the greatest values of ${ }^{2 n} C_{r}$ and ${ }^{2 n-1} C_{r}$ respectively. Then,
A. $a=2 b$
B. $\mathrm{b}-2 \mathrm{a}$
C. $a=b$
D. none of these

## Answer:

- Watch Video Solution

8. The number of ways in which n distinct objects can be put into two different boxes, is
A. $n^{2}$
B. $2^{n}$
C. 2 n
D. none of these

## Answer: B

## - Watch Video Solution

9. Find the total number of ways in which $n$ distinct objects can be put into two different boxes so that no box remains empty.
A. $2^{n}-1$
B. $n^{2}-1$
C. $2^{n}-2$
D. $n^{2}-2$

## Answer:

10. The number of ways in which $n$ distinct objects can be put into two identical boxes so that no box remains empty, is
A. $2^{n}-2$
B. $2^{n}-1$
C. $2^{n-1}-1$
D. $2^{n}-1$

## Answer:

## - Watch Video Solution

11. Find the number of ways in which 8 distinct toys can be distributed among 5 children.
A. $5^{8}$
B. $8^{5}$
C. $3^{5}$
D. none of these

## Answer: A

## (D) Watch Video Solution

12. The number of 6 -digit numbers that can be formed using the three digits 0,1 and 2 , is
A. $3^{6}$
B. $2 \times 3^{5}$
C. $3^{5}$
D. none of these

## Answer: C

13. No. of different matrices that can be formed with elements
$0,1,2$ or 3 each matrix having 4 elements is
A. $3 \times 2^{4}$
B. $2 \times 4^{4}$
C. $3 \times 4^{4}$
D. none of these

## Answer:

## - Watch Video Solution

14. The number of possible outcomes in a throw of $n$ ordinary dice in which at least one of the die shows and odd number is a. $6^{n}-1 \mathrm{~b}$. $3^{n}-1 \mathrm{c} .6^{n}-3^{n}$ d. none of these
A. $6^{n}-1$
B. $3^{n}-1$
C. $6^{n}-3^{n}$
D. none of these

## Answer:

## - Watch Video Solution

15. Find the number of distinct rational numbers $x$ such that ${ }^{\circ}$
A. 15
B. 13
C. 12
D. 11

## Answer:

16. The number of signals that can be generated by using 6 differently coloured flags, when any number of them may be hoisted at a time is
A. 1956
B. 1957
C. 1958
D. 1959

## Answer:

## - Watch Video Solution

17. Find the sum of all five digit numbers ,that can be formed using the digits $1,2,3,4$ and 5 (repetition of digits not allowed)
B. 660000
C. 360000
D. 3999960

## Answer:

## - Watch Video Solution

18. The number of 6 digit numbers that can be made with the digits $0,1,2,3,4$ and 5 so that even digits occupy odd places is
A. 24
B. 36
C. 48
D. none of these
19. Seven different lecturers are to deliver lectures in seven perday. A, B and C are three oftne lectures. The number of ways in which a routine for theday canr be made such that $A$ delivers his lecture before $B$ and $B$ before C , is
A. 420
B. 120
C. 210
D. none of these

## Answer:

## - Watch Video Solution

20. The number of arrangements of the letters of the word BANANA in which the two Ns do not appear adjacently is
A. 40
B. 60
C. 80
D. 100

## Answer: A

## Watch Video Solution

21. The total number of five-digit numbers of different digits in which the digit in the middle is the largest is a. $\sum_{n=4}^{9}{ }^{\wedge} n P_{4}$ b. $33(3!)$ c. $30(3!)$ d. none of these
A. $30 \times 30$ !
B. $33 \times 3$ !
C. $\sum_{n=4}^{9}{ }^{n} C_{4} \times 4$ !
D. none of these

## Answer:

## - Watch Video Solution

22. how many different nine digit numbers can be formed from the number 223355888 by rearranging its digits so that the odd digits occupy even positions:
A. 16
B. 36
C. 60
D. 180

## Answer:

## - Watch Video Solution

23. By using the digits $0,1,2,3,4$ and 5 (repetitions not allowed) numbers are formed by using any number of digits. Find the total number of non-zero number that can be formed.
A. 1030
B. 1630
C. 1200
D. 1530

## Answer:

## - Watch Video Solution

24. The total number not more than 20 digits that are formed by usingd the digits $0,1,2,3$, and 4 is a. $5^{20}$ b. $5^{20}-1$ c. $5^{20}+1 \mathrm{~d}$. none of these
A. $5^{20}$
B. $5^{20}-1$
C. $5^{20}+1$
D. none of these

## Answer:

## (D) Watch Video Solution

25. Six boys and six girls sit along a line alternately in x ways, and along a circle (again alternatively) in $y$ ways, then
A. $x=y$
B. $y=12 x$
C. $x=10 y$
D. $x=12 y$

## Answer: D

26. The number of times the digit 3 will be writtenn when listing the integers from 1 to 1000, is
A. 269
B. 300
C. 271
D. 302

## Answer:

## - Watch Video Solution

27. Let $T_{n}$ denote the number of triangles, which can be formed using the vertices of a regular polygon of $n$ sides. It $T_{n+1}-T-n=21$, the $\cap$ equals a. 5 b. 7 c. 6 d. 4
A. 5
B. 7
C. 6
D. 4

## Answer:

## - Watch Video Solution

28. Let $A$ be the set of all positive prime intergers less than 30 . The number of different rational numbers whose numerator and denominator belong to A is
A. 90
B. 180
C. 91
D. none of these

## Answer:

## - Watch Video Solution

29. The number of ways in which a mixed double tennis game can be arranged from amongst 9 married couple if no husband \& wife plays in the same game is:
A. 756
B. 1512
C. 3024
D. none of these

## Answer:

## - Watch Video Solution

30. The number of different seven digit numbers that can be written using only three digits $1,2 \& 3$ under the condition that the digit 2 occurs exactly twice in each number.
A. ${ }^{7} P_{5} .2^{5}$
B. ${ }^{7} C_{2} .2^{5}$
C. ${ }^{7} C_{2} .5^{2}$
D. none of these

## Answer:

## - Watch Video Solution

31. The number of six digit numbers that can be formed from the digits
$1,2,3,4,5,6 \& 7$ so that digits do not repeat and terminal digits are even is:
A. 144
B. 72
C. 288
D. 720

## Answer: D

## - Watch Video Solution

32. N a certain test, there are $n$ question. In the test, $2^{n-i}$ students gave wrong answers to at least $i$ questions, where $i=1,, 2 ; n$. if the total number of wring answers given is 2047, then $n$ is equal to a .10 b . 11 c. 12 d. 13
A. 10
B. 11
C. 12
D. 13

## Answer:

## - Watch Video Solution

33. The total number of 4 digit numbers in which the digit are in descending order, is
A. ${ }^{10} C_{4} \times 4$ !
B. ${ }^{10} C_{4}$
C. $\frac{10!}{4!}$
D. none of these

## Answer: B

34. The number of words of four letters containing equal number of vowels and consonants, where repetition is allowed, is a. $105^{2} \mathrm{~b}$. $210 \times 243$ c. $105 \times 243$ d. $150 \times 21^{2}$
A. $105^{2}$
B. $210 \times 243$
C. $105 \times 243$
D. none of these

## Answer:

## - Watch Video Solution

35. The number of 6 digit numbers that can be made with the digits
$1,2,3$ and 4 and having exactly two pairs of digits, is
A. 480
B. 540
C. 1080
D. none of these

## Answer:

## - Watch Video Solution

36. Total number of 6 -digit numbers in which all the odd digits appear, is
A. $\frac{5}{2} \times 6$ !
B. 6!
C. $\frac{1}{2} \times 6$ !
D. none of these

## Answer:

37. The number of numbers divisible by 3 that can be formed by four different even digits, is
A. 18
B. 36
C. 24
D. 48

## Answer:

## (D) Watch Video Solution

38. The number of five digit even numbers that can be made with the digits, $0,1,2$ and 3 , is
B. 192
C. 768
D. 576

## Answer:

## (D) Watch Video Solution

39. Given that n is odd, number of ways in which three numbers in AP can be selected from $1,2,3, \ldots . . . ., n$, is
A. $\frac{(n-1)^{2}}{2}$
B. $\frac{(n+1)^{2}}{4}$
C. $\frac{(n+1)^{2}}{2}$
D. $\frac{(n-1)^{2}}{4}$

## Answer: D

40. The number of triangles whose vertices are a the vertices of an octagon but none of whose sides happen to come from the sides of the octagon is
A. 24
B. 52
C. 48
D. 16

## Answer:

## - Watch Video Solution

41. There are 10 points in a plane of which no three points are collinear and four points are concyclic. The number of different circles that can
be drawn through at least three points of these points is a. 116 b .120
c. 117 d . none of these
A. 116
B. 117
C. 120
D. none of these

## Answer:

## - Watch Video Solution

42. There are three coplanar parallel lines. If any $p$ points are taken on each of the lines, the maximum number of triangles with vertices on these points is a. $3 p^{2}(p-1)+1 \mathrm{~b} .3 p^{2}(p-1)$ c. $p^{2}(4 p-3) \mathrm{d}$. none of these
A. $3 n^{2}(n-1)$
B. $3 n^{2}(n-1)+1$
C. $n^{2}(4 n-3)$
D. none of these

## Answer:

## - Watch Video Solution

43. In a polygon, no three diagonals are concurrent. If the total number of points of intersection of diagonals interior to the polygon is 70 , then the number of diagonals of the polygon is a. 20 b .28 c .8 d . none of these
A. 8
B. 20
C. 28
D. none of these

## Answer:

## - Watch Video Solution

44. ABCD is a convex quadrilateral and $3,4,5$, and 6 points are marked on the sides $A B, B C, C D$, and $D A$, respectively. The number of triangles with vertices on different sides is a. 270 b. 220 c. 282 d. 342
A. 220
B. 270
C. 282
D. 342

## Answer:

45. The number of ways in which we can select four numbers from 1 to 30 so as to exclude every selection of four consecutive numbers is a.

27378 b. 27405 c. 27399 d. none of these
A. 27378
B. 27405
C. 27399
D. none of these

## Answer:

## - Watch Video Solution

46. The number of four-digit numbers that can be made with the digits
$1,2,3,4$, and 5 in which at least two digits are identical is a. $4^{5}-5!\mathrm{b}$.
505 c. 600 d . none of these
A. $4^{5}-5$ !
B. 505
C. 600
D. none of these

## Answer:

## (D) Watch Video Solution

47. The number of 5 -digit number that can be made using the digits 1 and 2 and in which at laest one digits is different, is
A. 30
B. 31
C. 32
D. none of these

## Answer:

48. The number of ways of dividing 20 persons into 10 couples is
A. $\frac{20!}{2^{10} 10!}$
B. ${ }^{20} C_{10}$
C. $\frac{20!}{(21!)^{9}}$
D. $(20!) /\left(2^{\wedge}(10)\right.$

## Answer: A

49. The number of ways in which 10 condidates $A_{1}, A_{2}, \ldots \ldots, A_{10}$ can be ranked so that $A_{1}$ is always above $A_{2}$, is
A. 10 !
B. $\frac{10!}{2}$
C. 9!
D. none of these

## Answer:

## - Watch Video Solution

50. There are n white and n black balls marked $1,2,3, \ldots . ., \mathrm{n}$. The number of ways in which we can arrange these balls in a row so that neighbouring balls are of different colours, is
A. $n$ !
B. $(2 n)$ !
C. $2(n!)^{2}$
D. $\frac{(2 n)!}{(n!)^{2}}$

## Answer:

51. The number of ways in which we can distribute $m n$ students equally among $m$ sections is given by a. $\frac{(m n!)}{n!}$ b. $\frac{(m n)!}{(n!) 6 m}$ c. $\frac{(m n)!}{m!n!}$ d. $\left(m n^{m}\right)$
A. $\frac{(m n)!}{n!}$
B. $\frac{(m n)!}{(n!)^{m}}$
C. $\frac{(m n)!}{m!n!}$
D. $\frac{(2 n)!}{(n!)^{2}}$

## Answer:

## - Watch Video Solution

52. The total number of 6 -digit numbers in which the sum of the digits is divisible by 5 , is
A. 180000
B. 540000
C. $5 \times 10^{5}$
D. none of these

Answer: A

## - Watch Video Solution

53. The number of integers solutions for the equation $x+y+z+t=20$, where $\mathrm{x}, \mathrm{y}, \mathrm{z}$ t are all $\geq-1$, is
A. ${ }^{20} C_{4}$
B. ${ }^{23} C_{3}$
C. ${ }^{27} C_{4}$
D. ${ }^{27} C_{3}$

## Answer: D

## - Watch Video Solution

54. The number of integral solutions of $x+y+z=0$ with $x \geq-5$,
$y \geq-5, z \geq-5$ is
A. 135
B. 136
C. 455
D. 105

## Answer: B

55. The number of non-negative integral solutions of $x+y+z \leq n$, where $n \in N$ is
A. ${ }^{n+3} C_{3}$
B. ${ }^{n+4} C_{4}$
C. ${ }^{n+5} C_{5}$
D. none of these

## Answer:

## - Watch Video Solution

56. If $n$ objects are arrange in a row, then the number of ways of selecting three of these objects so that no two of them are next to each other is a. ${ }^{\wedge} n-2 C_{3} \mathrm{~b}$. ${ }^{\wedge} n-3 C_{2}$ c. ${ }^{\wedge} n-3 C_{3}$ d. none of these
A. ${ }^{n-2} C_{3}$
B. ${ }^{n-3} C_{2}$
C. ${ }^{n-3} C_{3}$
D. none of these

## Answer:

## - Watch Video Solution

57. There are three piles of identical red, blue and green balls and each pile contains at least 10 balls. The number of ways of selecting 10 balls if twice as many red balls as green balls are to be selected, is
A. 3
B. 4
C. 6
D. 8

## Answer:

58. If $n$ objects are arrange in a row, then the number of ways of selecting three of these objects so that no two of them are next to each other is a. ${ }^{\wedge} n-2 C_{3} \mathrm{~b}$. ${ }^{\wedge} n-3 C_{2}$ c. ${ }^{\wedge} n-3 C_{3}$ d. none of these
A. ${ }^{n-3} C_{3}$
B. ${ }^{n-3} C_{2}$
C. ${ }^{n-2} C_{3}$
D. none of these

## Answer:

59. Between two junction stations $A$ and $B$ there are 12 intermediate stations. The number of ways in which a train can be made to stop at 4 of these stations so that no two of these halting stations are consecutive, is
A. ${ }^{8} C_{4}$
B. ${ }^{9} C_{4}$
C. ${ }^{12} C_{4}-4$
D. none of these

## Answer:

## - Watch Video Solution

60. In how many ways can 30 marks be allotted to 8 question if each question carries at least 2 marks?
A. ${ }^{21} C_{7}$
B. ${ }^{21} C_{8}$
C. ${ }^{21} C_{9}$
D. none of these

## Answer: A

## - Watch Video Solution

61. The number of points in space, whose each co-ordinate is a negative integer such that $x+y+z+12=0$
A. 385
B. 55
C. 110
D. none of these

## Answer: B

62. If $\mathrm{x}, \mathrm{y}, \mathrm{z}$ are integers such that $x \geq 0, y \geq 1, z \geq 2$ and $\mathrm{x}+\mathrm{y}+\mathrm{z}=15$ , then the number of values of ordered triplets ( $x, y, z$ ) are
A. 91
B. 455
C. ${ }^{17} C_{15}$
D. none of these

## Answer: A

## - Watch Video Solution

63. If $a, b, c$ are three natural numbres in A.P. such that $a+b+c=21$, then possible number of odered triplet $(a, b, c)$, is
A. 15
B. 14
C. 13
D. none of these

## Answer:

## - Watch Video Solution

64. If $\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}$ are odd natural numbers such that $x+y+z+w=20$ then find the number of values of ordered quadruplet $(x, y, z, t)$.
A. 165
B. 455
C. 310
D. none of these
65. The number of ways in which a score of 11 can be made from a throw by three persons,each throwing a single die once, is
A. 45
B. 18
C. 27
D. none of these

## Answer: C

## ( Watch Video Solution

66. The sum of all the numbers of four different digits that can be made by using the digits $0,1,2$, and 3 is a. 26664 b. 39996 c. 38664 d . none of these
A. 26664
B. 39996
C. 38664
D. none of these

## Answer:

## - Watch Video Solution

67. There are 5 mangoes, 3 oranges and 4 bananas. The number of ways of selecting at least one fruit of each kind, is
A. $\frac{5!}{2!}$
B. 5!
C. 5!-4!
D. 3!

Answer: A

## - Watch Video Solution

68. There are 4 mangoes, 3 apples, 2 oranges and 1 each of 3 other varieties of fruits. The number of ways of selecting at least one fruit of each kind, is
A. 10 !
B. 9 !
C. 4 !
D. none of these

## Answer:

69. The number of divisor of 4200 , is
A. 42
B. 48
C. 54
D. none of these

## Answer: B

## - Watch Video Solution

70. The number of proper divisors of 2520 , is
A. 46
B. 52
C. 64
D. none of these

## - Watch Video Solution

71. The number of porper divisors of $2^{m} \times 6^{n} \times 15^{p}$, is
A. $(m+n+1)(n+p+1)(p+1)$
B. $(m+n+1)(n+p+1)(p+1)-2$
C. $(m+n)(n+p)-2$
D. none of these

## Answer: B

## - Watch Video Solution

72. The number of porper divisors of 1800 which are also divisible by

10 , is
A. 18
B. 34
C. 17
D. none of these

## Answer: C

73. The number of even proper divisors of 5040 , is
A. 48
B. 47
C. 46
D. none of these

## Answer: B

74. The number of odd proper divisors of 5040, is
A. 12
B. 10
C. 11
D. none of these

## Answer:

## - Watch Video Solution

75. Find the number of odd proper divisors of $3^{p} \times 6^{m} \times 21^{n}$.
A. $(m+1)(n+1)(p+1)-1$
B. $(m+n+p+1)(p+1)-1$
C. $(m+1)(n+1)(p+1)-2$
D. none of these

Answer:

## D Watch Video Solution

76. The number of divisors of the form $(4 n+2)$ of the integer 240 is
A. 4
B. 8
C. 10
D. 3

Answer: A

Watch Video Solution
77. The number of divisors of $2^{4} \cdot 3^{3} \cdot 5^{2}$, having two prime factors, is
A. 3
B. 24
C. 26
D. 60

## Answer:

## - Watch Video Solution

78. There are five balls of different colours and five boxes of colours same as those of the balls. The number of ways in which the balls, one each in a box, could be placed such that exactly one ball goes to a box of its own colour, is
A. 9
B. 24
C. 45
D. 120

## Answer:

## - Watch Video Solution

79. The number of 5 -digit numbers in which no two consecutive digits are identical, is
A. $9^{2} \times 8^{3}$
B. $9 \times 8^{4}$
C. $9^{5}$
D. none of these

## Answer: C

80. Let A be a set of $\mathrm{n}(\geq 3)$ distinct elements. The number of triplets $(x, y, z)$ of the A elements in which at least two coordinates is equal to
A. ${ }^{n} C_{3} \times 3$ !
B. $n^{3}-{ }^{n} C_{3} \times 3$ !
C. $3 n^{2}-2 n$
D. $3 n^{2}(n-1)$

## Answer:

## - Watch Video Solution

81. Find the number of ways to give 16 different things to three persons $A, B, C$ so that $B$ gets 1 more than $A$ and $C$ gets 2 more than $B$.
A. $\frac{16!}{4!5!7!}$
B. $4!5!7!$
C. $\frac{16!}{3!5!8!}$
D. none of these

## Answer: A

## - Watch Video Solution

82. If $P_{1}, P_{2}, \ldots \ldots . . P_{m+1}$ are distinct prime numbers. Then the number of factors of $P_{1}^{n} P_{2} P_{3} \ldots P_{m+1}$ is:
A. $m(n+1)$
B. $2^{n} m$
C. $(n+1) 2^{m}$
D. $n .2^{m}$

## Answer:

83. There are $m$ copies each of $n$ different books in a university library. The number of ways in which one or more than one book can be selected is
A. $m^{n}+1$
B. $(m+1)^{n}-1$
C. $(n+1)^{n}-m$
D. $m$

## Answer: B

## - Watch Video Solution

84. The number of ways in which one or more balls can be selected out of 10 white, 9 green and 7 blue balls, where balls of same color are identical, is
A. 892
B. 881
C. 891
D. 879

## Answer: D

85. The number of all three element subsets of the set $\left\{a_{1}, a_{2}, a_{3} \ldots \ldots a_{n}\right\}$ which contain $a_{3}$, is
A. ${ }^{n} C_{3}$
B. ${ }^{n-1} C_{3}$
C. ${ }^{n-1} C_{2}$
D. none of these

## Answer:

## - Watch Video Solution

86. If one quarter of all three element subsete of the set $A=\left\{a_{1}, a_{2}, a_{3}, \ldots \ldots, a_{n}\right\}$ contains the element $a_{3}$, then $\mathrm{n}=$
A. 10
B. 12
C. 14
D. none of these

## Answer:

## - Watch Video Solution

87. The sum of the divisors of $2^{5} \times 3^{4} \times 5^{2}$, is
A. $3^{2} \cdot 7^{1} \cdot 11^{2}$
B. $3^{2} \cdot 7^{1} \cdot 11^{2} \cdot 31$
C. 3.7.11.31
D. none of these

## Answer: B

## - Watch Video Solution

88. The number of words of that can be made by writing down the letters of the word $C A L C U L A T E$ such that each word starts and ends with a consonant, is
A. $\frac{5 \times 7!}{2}$
B. $\frac{3 \times 7!}{2}$
C. $2 \times 7$ !
D. none of these

Answer: A

## - Watch Video Solution

89. Find the number of ways in which $n$ different prizes can be distributed among `m(
A. $\left.n^{m}-n\right)$
B. $m^{n}$
C. $m n$
D. none of these

## Answer:

90. The total number of positive integral solutions for $(x, y, z)$ such that $x y z=24$ is
A. 36
B. 90
C. 120
D. none of these

## Answer:

## (D) Watch Video Solution

91. The total number of positive integral solutions of $a b c=30$, is
A. 30
B. 27
C. 8
D. none of these

## Answer: B

## - Watch Video Solution

92. The total numbre of intergral solutins of $a b c=24$, is
A. 36
B. 90
C. 120
D. 30

## Answer:

93. A bag contains 3 black, 4 white and 2 red balls, all the balls being different. The number of selections of at most 6 balls containing balls of all the colours, is
A. $42 \times 4$ !
B. $2^{6} \times 4$ !
C. $\left(2^{6}-1\right) 4$ !
D. none of these

## Answer:

## - Watch Video Solution

94. The number of different pairs of words (,) that can be made with the letters of the word STATICS, is
A. 828
B. 1260
C. 396
D. none of these

## Answer:

## - Watch Video Solution

95. In the decimal system of numeration the number of 6 -digit numbers in which the digit in any place is greater than the digit to the left of it, is
A. 210
B. 84
C. 126
D. none of these

## Answer:

96. There are 60 questions in a question paper. If no two students solve the same combination of questions but solve equal number of questions, then the maximum number of student who appeared in the examination, is
A. ${ }^{60} C_{29}$
B. ${ }^{60} C_{30}$
C. ${ }^{60} C_{50}$
D. none of these

## Answer:

97. nine hundred distinct $n$ digit numbers are to be formed using only the three digit $2,5,7$. the smallest value of $n$ for which is possible
A. 6
B. 7
C. 8
D. 9

## Answer:

## - Watch Video Solution

98. How many ways are there to arrange the letters in the word $G A R D E N$ with the vowels in alphabetical order?
A. 480
B. 240
C. 360
D. 120

## Answer: C

## - Watch Video Solution

99. The number of ways of distributing 8 identical balls in 3 distinct boxes so that none of the boxes is empty is
A. ${ }^{8} C_{3}$
B. 21
C. $3^{8}$
D. 5

## Answer: B

100. The number of seven digit integers, with sum of the digits equal to 10 and formed by using the digits 1,2 and 3 only, is
A. 55
B. 66
C. 77
D. 88

## Answer:

## - Watch Video Solution

101. Consider all possible permutations of the letters of the word $E N D E A N O E L$. The number of permutations containing the word ENDEA is
A. 5 !
B. $2 \times 5$ !
C. $7 \times 5$ !
D. $21 \times 5$ !

## Answer: A

## - Watch Video Solution

102. Consider all possible permutations of the letters of the word ENDEANOEL. The number of permutations in which the letter E occurs in the first and last positions is
A. 5 !
B. $2 \times 5$ !
C. $7 \times 5!$
D. $21 \times 5$ !

## Answer:

103. Consider all possible permutations of the letters of the word ENDEANOEL. The number of permutations in which none of the letters $D, L$ and $N$ occurs in the last positions is
A. 5 !
B. $2 \times 5$ !
C. $7 \times 5$ !
D. $21 \times 5$ !

## Answer:

## - Watch Video Solution

104. All possible permutations of the letters of the word ENDEANOEL if

A, E, O occur only in odd positions is
A. 5 !
B. $2 \times 5$ !
C. $7 \times 5$ !
D. $21 \times 5$ !

## Answer: B

105. If ${ }^{m} C_{r}=0$ for $r>m$ then the sum $\sum_{r=0}^{m}{ }^{18} C_{r}{ }^{20} C_{m-r}$ is maximum when $\mathrm{m}=$
A. 20
B. 19
C. 10
D. 10

## Answer:

## - Watch Video Solution

106. Let $S=\{1,, 2,34\}$. The total number of unordered pairs of disjoint subsets of $S$ is equal a. 25 b. 34 c. 42 d. 41
A. 25
B. 34
C. 42
D. 41

## Answer:

107. There are two urns. Urn A has 3 distinct red balls and urn B has 9 distinct blue balls. From each urn two balls are taken out at random and then transferred to the other. The number of ways in which this can be done is (1) 36 (2) 66 (3) 108 (4) 3
A. 66
B. 108
C. 3
D. 36

## Answer:

## D Watch Video Solution

108. 2 . There are 10 points in a plane, out of these 6 arecollinear. If $N$ is the number of triangles formed byjoining these points, then(a) $\mathrm{N}>$ 190(b) $\mathrm{N}<100$ (c) $100<\mathrm{N}<140$ (d) $140<\mathrm{N}<190$
A. $100<N \leq 140$
B. $140<N \leq 190$
C. $N<190$
D. $N \leq 100$

## Answer:

## - Watch Video Solution

109. The total number of ways in which 5 balls of differert colours can be distributed among 3 persons so thai each person gets at least one ball is
A. 75
B. 150
C. 210
D. 243

## Answer: B

## D Watch Video Solution

110. There are 10 girls and 8 boys in a class room including Ms. Rani and Radha. A list of speakers consisting of 8 girls and 6 boys has to be prepared. Mr. Ravi refuses to speak if Ms. Rani is a speaker. Ms. Rani refuses to speak if Ms. Radha is a speaker. The number of ways the list can be prepared is
A. 202
B. 308
C. 567
D. 952

## Answer:

111. The number of words which can be formed out of the letters $a, b, c$, $d, e f$ taken 3 together, each word containing one vowel at least is
A. 128
B. 24
C. 72
D. 96

## Answer: D

## (D) Watch Video Solution

## Section li Assertion Reason Type

1. Statement-1: The number of zeros at the end of $100!\mathrm{ls}, 24$.

Statement-2: The exponent of prine $p$ in $n!$, is

$$
\left[\frac{n}{p}\right]+\left[\frac{n}{p^{2}}\right]+\ldots \ldots+\left[\frac{n}{p^{r}}\right]
$$

Where r is a natural number such that $P^{r} \leq n<P^{r+1}$.
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

2. In a shop there are five types of ice-creams available. A child buys six ice-creams. Statement -1: The number of different ways the child can buy the six ice-creams is ${ }^{\wedge} 10 C_{5}$. Statement -2 : The number of
different ways the child can buy the six ice-creams is equal to the number of different ways of arranging 6 As and 4 Bs in a row. (1) Statement 1 is false, Statement (2)(3) - 2(4) is true (6) Statement 1 is true, Statement $(7)(8)-2(9)(10)$ is true, Statement $(11)(12)-2(13)$ is a correct explanation for Statement 1 (15) Statement 1 is true, Statement $(16)(17)-2(18)(19)$ is true; Statement $(20)(21)-2(22)$ is not a correct explanation for Statement 1. (24) Statement 1 is true, Statement (25)(26) - 2(27) is false.
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

3. Statement-1: The expression
${ }^{40} C_{r} \times{ }^{60} C_{0}+{ }^{40} C_{r-1} \times{ }^{60} C_{1}+{ }^{40} C_{r-2} \times{ }^{60} C_{2}+\ldots . \quad$ attains its maximum volue when $r=50$

Statement-2: ${ }^{2 n} C_{r}$ is maximum when $\mathrm{r}=\mathrm{n}$.
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

4. Statement-1: The number of non-negative integral solutions of $x+y+z=40$ is ${ }^{43} C_{3}$.

Statement-2: The number of ways of distributing n identical items among $r$ persons giving zero or more items to a person is ${ }^{n+r-1} C_{r-1}$
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

5. Statement-1: The number solutions of the equations $x+y+z=15$ in the set N of all natural numbers is ${ }^{4} C_{2}$.

Statement-2: The number of ways of distributing n identical items among $r$ persons is ${ }^{n+r-1} C_{r-1}$
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

6. Consider the natural number $n=453600$.

Statement-1: The number of divisors of n is 180 .
Statement-2: The sum of the divisors of n is

$$
\left(2^{6}-1\right)\left(3^{5}-1\right)\left(5^{3}-1\right)\left(7^{2}-1\right)
$$

A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

7. Statement-1: The number $1000 C_{500}$ is not divisible by 11 .

Statement-2: The exponent of prime p in n ! is

$$
\left[\frac{n}{p}\right]+\left[\frac{n}{p^{2}}\right]+\left[\frac{n}{p^{3}}\right]+\ldots \ldots+\left[\frac{n}{p^{x}}\right] \text { where } p^{k} \leq n<p^{k+1}
$$

A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

8. Statement-1: A student is allowed to select at most n books from a collection of $(2 n+1)$ books. If the total number of ways in which he can
select at least one book is 255 , then $\mathrm{n}=3$.
$\sum_{r=1}^{n}{ }^{2 n+1} C_{r}=2^{2 n}$
A. Statement- 1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

9. Statement-1: The number of ways of distributing 10 identical balls in 4 distinct boxes such that no box is empty is ${ }^{9} C_{3}$.

Statement-2: The number of ways of choosing any 3 places from 9 different places is ${ }^{9} C_{3}$.
A. Statement-1 is True, Statement-2 is true, Statement-2 is a correct explanation for Statement-1.
B. Statement-1 is True, Statement-2 is True, Statement-2 is not a correct explanation for Statement-1.
C. Statement-1 is True, Statement-2 is False.
D. Statement-1 is False, Statement-2 is True.

## Answer:

## - Watch Video Solution

Exercise

1. The value of $\sum_{r=1}^{n} \frac{{ }^{n} P_{r}}{r!}$ is
A. $2^{n}$
B. $2^{n}-1$
C. $2^{n}-1$
D. $2^{n}+1$

## Answer: B

## D Watch Video Solution

2. If ${ }^{12} P_{r}={ }^{11} P_{6}+6\left({ }^{11} P_{5}\right)$, then $r$ is equal to
A. 6
B. 5
C. 7
D. none of these
3. If ${ }^{n-1} C_{3}+{ }^{n-1} C_{4}>{ }^{n} C_{3}$, then
A. $n \leq 4$
B. $n>5$
C. $n>7$
D. none of these

## Answer: C

- Watch Video Solution

4. ${ }^{n} C_{r}+2^{n} C_{r-1}+C_{r-2}$ is equal to
A. ${ }^{n+1} C_{r}$
B. ${ }^{n} C_{r+1}$
C. ${ }^{n-1} C_{r+1}$
D. none of these

## Answer: D

## - Watch Video Solution

5. If $\wedge 2 n+1 P_{n-1}:^{2 n-1} P_{n}=3: 5, f \in d n$.
A. 4
B. 6
C. 3
D. 8

## Answer: A

Watch Video Solution
6. If . ${ }^{35} C_{n+7}=.{ }^{35} C_{4 n-2}$ then find the value of $n$.
A. 28
B. 3,6
C. 3
D. 6

## Answer: B

## - Watch Video Solution

7. If . ${ }^{n} C_{r-1}=36, .{ }^{n} C_{r}=84$ and $.{ }^{n} C_{r+1}=126$, find n and r .
A. $n=8, r=4$
B. $n=9, r=3$
C. $n=7, r=5$
D. none of these

## Answer: B

## - Watch Video Solution

8. If $(n-1) C_{6}+(n-1) C_{7}>n C_{6}$ then
A. $n>4$
B. $n>12$
C. $n \geq 13$
D. $n>13$

## Answer: D

## - Watch Video Solution

9. Which of the following is incorrect?

$$
\text { A. }{ }^{n} C_{r}={ }^{n} C_{n-r}
$$

B. ${ }^{n} C_{r}={ }^{n-1} C_{r}+{ }^{n} C_{n-r}$
C. ${ }^{n} C_{r}={ }^{n-1} C_{r}+{ }^{n-1} C_{n-r}$
D. $r!^{n} C_{r}={ }^{n} P_{n}$

## Answer: B

## - Watch Video Solution

10. $I f^{56} P_{r+6}:{ }^{54} P_{r+3}=30800: 1$, find $r$
A. 40
B. 41
C. 42
D. none of these

Answer: B
11. $\sum_{r=0}^{m} \cdot{ }^{n+r} C_{n}$ is equal to
A. ${ }^{n+m+1} C_{n+1}$
B. ${ }^{n+m+2} C_{n}$
C. ${ }^{n+m+3} C_{n-1}$
D. none of these

## Answer: A

## - Watch Video Solution

12. Every two persons shakes hands with each other in a party and the total number of handis 66 . The number of guests in the party is
A. 11
B. 12
C. 13
D. 14

## Answer: B

## - Watch Video Solution

13. On the occasion if Deepawali festival, each student in a class sends greeting cards to other. If there are 20 students in the class, find the total number of greeting cards exchanged by the students?
A. ${ }^{20} C_{2}$
B. 2. ${ }^{20} C_{2}$
C. $2 \times{ }^{20} P_{2}$
D. none of these

## Answer: B

14.If ${ }^{\wedge}(n+2) C_{8}:{ }^{n-2} P_{4}: 57: 16$, find $n$.
A. 20
B. 19
C. 18
D. 17

## Answer: B

## - Watch Video Solution

15. Find the exponent of 3 in 100 !
A. 33
B. 44
C. 48
D. 52

## Answer: C

## - Watch Video Solution

16. Ten different letters of an alphabet are given. Words with five letters are formed from these given letters. Determine the number4 of words which have at least one letter repeated.
A. 69760
B. 30240
C. 99748
D. none of these

## Answer: A

17. If 7 points out of 12 are in the same straight line, then the number of triangles formed is
A. 19
B. 158
C. 185
D. 201

## Answer: C

## (D) Watch Video Solution

18. A polygon has 44 diagonals. The number of its sides are
A. 9
B. 10
C. 11
D. 12

## Answer: C

## Watch Video Solution

19. No. of diagonals of a polygon are 170. No. of sides in this polygon are:
A. 12
B. 17
C. 20
D. 25

## Answer: C

20. The number of all possible selections of one or more questions from 10 given questions, each question having an alternative is :
A. 310
B. $2^{10}-1$
C. $3^{10}-1$
D. $2^{10}$

## Answer: C

## - Watch Video Solution

21. The number of ways of painting the faces of a cube with six different colours is
A. 1
B. 6
C. 6!
D. none of these

## Answer: A

## - Watch Video Solution

22. A box contains 2 white balls, 3 black balls and 4 red balls. The number of ways three balls be drawn from the box, if atleast one black ball is to be included in the draw is $\qquad$
A. 129
B. 84
C. 64
D. none of these

## Answer: C

23. Find the number of different permutations of the letters of the word BANANA?
A. 720
B. 60
C. 120
D. 360

## Answer: B

## - Watch Video Solution

24. A person tries to form as many different parties as he can, out of his 20 friends. Each party should consist of the same number. How many friends should be invited at a time? In how many of these parties would the same friends be found?
A. 5
B. 10
C. 8
D. none of these

## Answer: B

## Watch Video Solution

25. Find the number of ways in which 8 different flowered can be strung to form a garland so that four particular flowers are never separated.
A. $4!.4$ !
B. $\frac{8!}{4!}$
C. 288
D. none of these

## - Watch Video Solution

26. The number of words which can be formed out of the letters $a, b, c$,
$d, e f$ taken 3 together, each word containing one vowel at least is
A. 72
B. 48
C. 96
D. none of these

## Answer: C

27. The smallest value of x satisfying the inequality ${ }^{10} C_{x-1}>2 .{ }^{10} C_{x}$ is.
A. 7
B. 10
C. 9
D. 8

## Answer: D

## - Watch Video Solution

28. The number of arrangenments which can be made using all the letters of the word $L A U G H$, if the vowels are adjacent, is
A. 10
B. 24
C. 48
D. 120

## Answer: C

## - Watch Video Solution

29. The number of ways of choosing a committee of 4 women and 5 men from 10 women and 9 men, if Mr. A refuses to serve on the committee when Ms. $B$ is a member of the committee, is
A. 20580
B. 21000
C. 21580
D. all the above

## Answer: A

30. A set contains $2 n+1$ elements. The number of subsets of this set containing more than n elements :
A. $2^{n-1}$
B. $2^{n}$
C. $2^{n+1}$
D. $2^{2 n}$

## Answer: D

## - Watch Video Solution

31. The number of ways in which any four letters cab be selected from the word 'CORGOO' is
A. 15
B. 11
C. 7
D. none of these

## Answer: C

## - Watch Video Solution

32. A five digit number divisible by 3 is to be formed using the numerals $0,1,2,3,4$ and 5 , without repetition. The total number of ways this can be done, is
A. 216
B. 240
C. 600
D. 3125
33. If 7 points out of 12 are in the same straight line, then the number of triangles formed is
A. 19
B. 158
C. 185
D. 201

## Answer: C

## D Watch Video Solution

34. If $a$ denotes the number of permutations of $(x+2)$ things taken all at a time, $b$ the number of permutations of $x$ things taken 11 at a
time and $c$ the number of permutations of $x-11$ things taken all at a time such that $a=182 b c$, find the value of $x$.
A. 15
B. 12
C. 10
D. 18

## Answer: B

## D Watch Video Solution

35. There are number of seats and $m$ number of people have to be seated, then how many ways are possible to do this $(m<n)$ ?
A. ${ }^{n} P_{m}$
B. ${ }^{n} C_{m}$
C. ${ }^{n} C_{n} \times(m-1)!$
D. ${ }^{n-1} P_{m-1}$

## Answer: A

## - Watch Video Solution

36. There are 5 letters and 5 directed envelopes. The number of ways in which all the letters can be put in wrong envelope is
A. 119
B. 44
C. 59
D. 40

## Answer: B

37. The number of ways of selecting 10 balls from unlimited number of red, black, white and green balls, is
A. 286
B. 84
C. 715
D. none of these

## Answer: A

## - Watch Video Solution

38. The total number of different combinations of letters which can be made from the letters of the word MISSISSIPPI, is
A. 150
B. 148
C. 149
D. none of these

## Answer: C

## - Watch Video Solution

39. The total number of six-digit natural numbers that can be made with the digits $1,2,3,4$, if all digits are to appear in the same number at least once is a. 1560 b. 840 c. 1080 d. 480
A. 1560
B. 840
C. 1080
D. 480

Answer: A
40. The number of numbers of 7 digits whose sum of digits is even, is
A. 9000000
B. 4500000
C. 8100000
D. none of these

## Answer: B

## - Watch Video Solution

41. All possible four-digit numbers have formed using the digits $0,1,2$, 3 so that no number has repeated digits. The number of even numbers among them, is
A. 9
B. 18
C. 10
D. none of these

## Answer: C

## - Watch Video Solution

42. If the permutations of $a, b, c, d$, $e$ taken all together be written dowan in alphabetical order as in dictionary and numbered then the rank of the permutation debac, is
A. 90
B. 91
C. 92
D. 93

## Answer: D

43. The number of natural numbers smaller than $10^{4}$ of which all digits are different, is
A. 5274
B. 5265
C. 4676
D. none of these

## Answer: A

## - Watch Video Solution

44. If eight persons are to address a meeting, then the number of ways in which a specified speaker is to speak before another specified speaker, is
A. 2520
B. 20160
C. 40320
D. none of these

## Answer: B

## - Watch Video Solution

45. Find the number of proper factors of the number 38808.
A. 72
B. 70
C. 69
D. 71

## Answer: B

46. All possible products are formed from the numbers $1,2,3,4, \ldots, 200$ by selecting any two without repetition. The number of products out of the total obtained which are multiples of 5 is :
A. 5040
B. 7180
C. 8150
D. none of these

## Answer: B

## - Watch Video Solution

47. In an examination there are three multiple choice questions and each question has 4 choices. The number of ways in which a student can fail to get all answers correct is (a) 11 (b) 27 (c) 12 (d) 63
A. 11
B. 15
C. 80
D. 63

## Answer: D

## - Watch Video Solution

48. If all the words formed with the letters of the word 'RANDOM' arranged in a dictionary then the word 'RANDOM' will be placed at position no:
A. 614
B. 615
C. 613
D. 616

Answer: A

## D Watch Video Solution

49. Find the sum of all the numbers that can be formed with the digits $2,3,4,5$ taken all at a time.
A. 93324
B. 66666
C. 84844
D. none of these

Answer: A

- Watch Video Solution

50. The sum of the digits in the unit place of all numbers formed with the help of 3,4,5,6 taken all at a time is
A. 18
B. 108
C. 432
D. none of these

## Answer: B

## - Watch Video Solution

51. If the letters of the word MOTHER are written in all possible orders and these words are written out as in a dictionary, find rank of the word MOTHER.
A. 240
B. 261
C. 308
D. 309

## Answer: D

## - Watch Video Solution

52. Numbers greater than 1000 but not greater than 4000 which can be formed with the digits $0,1,2,3,4$ (repetition of digits is allowed) are a. 350 b. 375 c. 450 d. 576
A. 375
B. 374
C. 376
D. none of these
53. The number of ways in which 5 picturers can be hung from 7 picture nails on the wall is
A. $7^{5}$
B. $5^{7}$
C. 2520
D. none of these

## Answer: C

## D Watch Video Solution

54. The number of all four digit numbers which are divisible by 4 that can be formed from the digits $1,2,3,4$, and 5 , is
A. 125
B. 30
C. 95
D. none of these

## Answer: A

## - Watch Video Solution

55. The number of all five digit numbers which are divisible by 4 that can be formed from the digits $0,1,2,3,4$ (without repetition) is
A. 36
B. 30
C. 34
D. none of these

## Answer: B

## - Watch Video Solution

56. The number of ways in which $m+n(n \leq m+1)$ different things
can be arranged in a row such that no two of the n things may be together, is
A. $\frac{(m+n)!}{m!n!}$
B. $\frac{m!(m+1)!}{(m+n)!}$
C. $\frac{m!(m+1)!}{(m-n+1)!}$
D. none of these

## Answer: C

57. All possible two-factor products are formed from the numbers 1 , $2, \ldots . . ., 100$. The numbers of factors out of the total obtained which are multiple of 3 , is
A. 2211
B. 4950
C. 2739
D. none of these

## Answer: C

## - Watch Video Solution

58. $m$ men and $n$ women ae to be seated in a row so that no two women sit together. If $m>n$ then show that the number of ways $n$ which they fan be seated as $\frac{m!(m+1)!}{(m-n+1)!}$.
A. $\frac{m!n!}{(m+n)!}$
B. $\frac{m!(m+1)!}{(m-n+1)!}$
C.
D. none of these

## Answer: B

## - Watch Video Solution

59. The total number of ways in which six ' + ' and four '-' signs can be arranged in a line such that no two signs '-' occur together, is $\qquad$
A. 35
B. 15
C. 30
D. none of these

Answer: A

## D Watch Video Solution

60. If in a chess tournament each contestant plays once against each of the other and in all 45 games are played, then the number of participants, is
A. 9
B. 10
C. 15
D. none of these

## Answer: B

Watch Video Solution
61. Total number of four digit odd numbers that can be formed by using $0,1,2,3,5,7$ are
A. 216
B. 375
C. 400
D. 720

## Answer: D

## - Watch Video Solution

62. A committee of 5 is to be formed from 9 ladies and 8 men. If the committee commands a lady majority, then the number of ways this can be done is

$$
\text { A. } 2352
$$

B. 1008
C. 3360
D. 3486

## Answer: D

## - Watch Video Solution

63. The number of ordered triplets of positive integers which are solutions of the equation $x+y+z=100$.
A. 6005
B. 4851
C. 5081
D. none of these

## Answer: B

64. Find the number of straight lines that can be drawn through any two points out of 10 points, of which 7 are collinear.
A. 26
B. 21
C. 25
D. none of these

## Answer: C

## - Watch Video Solution

65. The number of ways in which 10 candidates $A_{1}, A_{2}, A_{10}$ can be ranked such that $A_{1}$ is always above $A_{10}$ is a. $5!$ b. $2(5!)$ c. 10 ! d. $\frac{1}{2}(10!)$
A. 5 !
B. 2(5!)
C. 10 !
D. none of these

## Answer: D

## - Watch Video Solution

66. In Q. 65 , the number of ways in which $A_{1}$ and $A_{2}$ are next to each other, is
A. 9 !
B. 2(9!)
C. $\frac{1}{2}(9!)$
D. none of these

## Answer: B

## - View Text Solution

67. The total number of all proper factors of 75600 , is
A. 120
B. 119
C. 118
D. none of these

## Answer: C

## - Watch Video Solution

68. The total number of ways in which 11 identical apples can be distributed among 6 children such that every student gets atleast one
apple,is
A. 252
B. 462
C. 42
D. none of these

## Answer: A

## - Watch Video Solution

69. The number of ways in which a pack of 52 cards be divided equally amongst four players in order, is
A. ${ }^{52} C_{13}$
B. ${ }^{52} C_{4}$
C. $\frac{52!}{(13!)^{4}}$
D. $\frac{52!}{(13!)^{4} 4!}$

## Answer: C

## - Watch Video Solution

70. (i) In how many ways can a pack of 52 cards be divided equally among four players? (ii) (ii) In how many ways can you divide these cards in four sets, three of them having 17 cards each and the four the one just one card?
A. $\frac{52!}{(17!)^{3}}$
B. $\frac{52!}{(17!)^{3} 3!}$
C. $\frac{51!}{(17!)^{3}}$
D. $\frac{51!}{(17!)^{3} 3!}$

## Answer: B

71. The total number of ways of dividing 15 different things into groups of 8 . , 4 and 3 respectively, is
A. $\frac{15!}{8!4!(3!)^{2}}$
B. $\frac{15!}{8!4!3!}$
C. $\frac{15!}{8!4!}$
D. none of these

## Answer: B

## - Watch Video Solution

72. There are three copies each of 4 different books. In how many ways can they be arranged in a shelf?
A. $\frac{12!}{(3!)^{4}}$
B. $\frac{12!}{(4!)^{3}}$
C. $\frac{12!}{(3!)^{4} 4!}$
D. $\frac{12!}{(4!)^{3} 3!}$

## Answer: A

## D Watch Video Solution

73. The number of ways in which 12 books can be put in three shelves with four on each shelf is a. $\frac{12!}{(4!)^{3}}$ b. $\frac{12!}{(3!)(4!)^{3}}$ c. $\frac{12!}{(3!)^{3} 4!}$ d. none of these
A. $\frac{12!}{(4!)^{3}}$
B. $\frac{12!}{(3!)(4!)^{3}}$
C. $\frac{12!}{(3!)^{3} 4!}$
D. none of these

## Answer: A

74. The total number of ways in which 12 persons can be divided into three groups of 4 persons each, is
A. $\frac{12!}{(13!)^{3} 4!}$
B. $\frac{12!}{(4!)^{3}}$
C. $\frac{12!}{(4!)^{3} 3!}$
D. $\frac{12!}{(3!)^{4}}$

## Answer: C

## - Watch Video Solution

75. The number of ways in which 12 balls can be divided between two friends, one receiving 8 and the other 4 , is
A. $\frac{12!}{8!4!}$
B. $\frac{12!12!}{8!4!}$
C. $\frac{12!}{8!4!2!}$
D. none of these

## Answer: B

## - Watch Video Solution

76. The total number of ways in which $2 n$ persons can be divided into $n$ couples is a. $\frac{2 n!}{n!n!}$ b. $\frac{2 n!}{(2!)^{3}}$ c. $\frac{2 n!}{n!(2!)^{n}}$ d. none of these
A. $\frac{2 n!}{n!n!}$
B. $\frac{2 n!}{(2!)^{n}}$
C. $\frac{2 n!}{n!(2!)^{n}}$
D. none of these

## Answer: C

77. The total number of ways of selecting six coins out of 20 one-rupee coins, 10 fifty-paisa coins, and 7 twenty-five paisa coins is a. 28 b. 56 c. - $37 C_{6}$ d. none of these
A. 28
B. 56
C. ${ }^{37} C_{6}$
D. none of these

## Answer: A

## - Watch Video Solution

78. The number of ways in which thirty five apples can be distributed among 3 boys so that each can have any number of apples, is :
B. 666
C. 333
D. none of these

## Answer: B

## - Watch Video Solution

79. A person goes in for an examination in which there are four papers with a maximum of $m$ marks from each paper. The number of ways in which one can get 2 m marks is
A. ${ }^{2 m+3} C_{3}$
B. $\frac{1}{3}(m+1)\left(2 m^{2}+4 m+1\right)$
C. $\frac{1}{3}(m+1)\left(2 m^{2}+4 m+3\right)$
D. none of these
80. If $m$ parallel lines in a plane are intersected by a family of $n$ parallel lines, the number of parallelograms that can be formed is a. $\frac{1}{4} m n(m-1)(n-1)$ b. $\frac{1}{4} m n(m-1)(n-1)$ c. $\frac{1}{4} m^{2} n^{2}$ d. none of these
A. $\frac{(m-1)(n-1)}{4}$
B. $\frac{m n}{4}$
C. $\frac{m(m-1) n(n-1)}{2}$
D. $\frac{m n(m-1)(n-1)}{4}$

## Answer: D

81. 1, 2, 3, 4 are four numbers. How many numbers can be made using all four numbers without repetition?
A. 1!
B. 3!
C. 2!
D. 4 !

## Answer: D

## - Watch Video Solution

82. There were two women participating in a chess tournament. Every participant played two games with the other participants. The number of games that the men played among themselves proved to exceed by 66 number of games that the men played with eth women. The number of participants is
A. 6
B. 11
C. 13
D. none of these

## Answer: C

## - Watch Video Solution

83. The parallelogram is cut by two sets of $m$ lines parallel to its sides.

The numbers parallelogram thus formed, is
A. $\left({ }^{m} C_{2}\right)^{2}$
B. $\left({ }^{m+1} C_{2}\right)^{2}$
C. $\left({ }^{m+2} C_{2}\right)^{2}$
D. none of these

## Answer: C

## - Watch Video Solution

84. There are $n$ straight lines in a plane in which no two are parallel and no three pass through the same point. Their points of intersection are joined. Show that the number of fresh lines thus introduced is $\frac{1}{8} n(n-1)(n-2)(n-3)$
A. $\frac{n(n-1)(n-1)}{8}$
B. $\frac{n(n-1)(n-2)(n-3)}{6}$
C. $\frac{n(n-1)(n-2)(n-3)}{8}$
D. none of these

## Answer: C

85. There are 18 points in a plane such that no three of them are in the same line except five points which are collinear. The number of triangles formed by these points, is
A. 805
B. 806
C. 816
D. none of these

## Answer: B

## - Watch Video Solution

86. Given 5 different green dyes, four different blue dyes and three different red dyes, how many combinations of dyes can be chosen taking at least one green and one blue dye ?
A. 3255
B. 212
C. 3720
D. none of these

## Answer: C

## - Watch Video Solution

87. Eight chairs are numbered 1 to 8 . Two women and three men wish to occupy one chair each. First, the women choose the chairs from amongst the chairs marked 1 to 4 , and then the men select th chairs from amongst the remaining. The number of possible arrangements is a. ${ }^{\wedge} 6 C_{3} \times{ }^{4} C_{2}$ b. ${ }^{\wedge} 4 P_{2} \times{ }^{4} P_{3}$ c. ${ }^{\wedge} 4 C_{2} \times{ }^{4} P_{3}$ d. none of these
A. ${ }^{4} C_{3} \times{ }^{4} C_{2}$
B. ${ }^{4} C_{2} \times{ }^{4} P_{3}$
C. ${ }^{4} P_{2} \times{ }^{4} P_{3}$
D. none of these

## Answer: D

## - Watch Video Solution

88. A student is allowed to select at most n books from a collection of $(2 n+1)$ books. If the total number of ways in which a student selects at least one book is 63. then n equals to -
A. 6
B. 3
C. 4
D. none of these

## Answer: B

89. In a steamer there are stalls for 12 animals and there are cows, horses and calves (not less than 12 of each) ready to be shipped, the total number of ways in which the shipload can be made, is
A. $3^{12}$
B. $12^{3}$
C. ${ }^{12} P_{3}$
D. ${ }^{12} C_{3}$

## Answer: A

## - Watch Video Solution

90. The number of different numbers that can be formed by using all the digits $1,2,3,4,3,2,1$ so that odd digits always occupy the odd places IS 1) 6 2)72 3) 604 4) 18
A. 3!4!
B. 34
C. 18
D. 12

## Answer: C

## - Watch Video Solution

91. Number of ways in which RS. 18 can be distributed amongst four persons such that no body receives less than RS 4, is
A. 42
B. 24
C. 4 !
D. none of these

## Answer: D

92. A box contains 2 white balls, 3 black balls and 4 red balls. The number of ways three balls be drawn from the box, if atleast one black ball is to be included in the draw is $\qquad$
A. 74
B. 64
C. 84
D. 20

## Answer: B

## - Watch Video Solution

93. The number of ways in which four letters can be selected from the word degree, is
A. 7
B. 6
C. $\frac{6!}{3!}$
D. none of these

## Answer: A

## - Watch Video Solution

94. find the number of arrangements which can be made out of the letters of the word 'algebra', without altering the relative positions of vowels and consonants.
A. $\frac{7!}{2!}$
B. $\frac{7!}{2!5!}$
C. 4!3!
D. $\frac{4!3!}{2}$

## Answer: D

## - Watch Video Solution

95. The number of ways in which seven persons can be arranged at a round table if two particular persons may not sit together, is
A. 480
B. 120
C. 80
D. none of these

## Answer: A

- Watch Video Solution

96. The total number of ways in which 4 boys and 4 girls can form a line, with boys and girls alternating, is
A. (4!) 2
B. 8 !
C. $2(4!)^{\wedge} 2$
D. 4 !. ${ }^{5} P_{4}$

## Answer: C

## ( Watch Video Solution

97. How many different words can be formed by jumbling the letters in the word MISSISSIPPI in which no two $S$ are adjacent?
A. $8 \times{ }^{6} C_{4} \times{ }^{7} C_{4}$
B. $6 \times 7 \times{ }^{8} C_{4}$
C. $6 \times 8 \times{ }^{7} C_{4}$
D. $7 \times{ }^{6} C_{4} \times{ }^{8} C_{4}$

## Answer: D

## (D) Watch Video Solution

98. A code word consists of three letters of the English alphabet followed by two digits of the decimal system. If neither letter nor digit is repeated in any code word, then the total number of code words, is
A. 1404000
B. 16848000
C. 2808000
D. none of these
99. Find the number of words formed by permuting all the letters of the following word: EXERCISES
A. 60480
B. 30240
C. 10080
D. none of these

## Answer: B

## - Watch Video Solution

100. A father with 8 children takes 3 at a time to the Zoological

Gardens, as often as he can without taking the same 3 children
together more than once. The number of times he will go to the garden, is
A. 336
B. 112
C. 56
D. none of these

## Answer: C

## - Watch Video Solution

101. A man has 8children to take them to a zoo. He takes thre of them
at a time to the zoo as often as he can without taking the same 3 children together more than once. How many times will he have to go to the zoo? How many times a particular child will to to the zoo?
A. 56
B. 21
C. 112
D. none of these

## Answer: B

## - Watch Video Solution

102. If the letters of the word LATE be permuted and the words so performed be arranged as in a dictionary, find rank of the word LATE.
A. 12
B. 13
C. 14
D. 15

## Answer: C

103. The total number of ways of arranging the letters AAAA BBB CC D

EF in a row such that letters C are separated from one another, is
A. 2772000
B. 1386000
C. 4158000
D. none of these

## Answer: B

## - Watch Video Solution

104. The sides $A B, B C, C A$ of a triangle $A B C$ have 3,4 and 5 points.

Triangles that can be constructed by using these points as vertices, is
A. 220
B. 204
C. 205
D. 195

## Answer: C

## - Watch Video Solution

105. There are four balls of different colours and four boxes of colours, same as those of the balls. The number of ways in which the balls, one in each box, could be placed such thast a ball does not go to a box of its own colour is: (A) $\lfloor 4-1$ (B) 9 (C) $\lfloor 3+1$ (D) none of these
A. 9
B. 24
C. 12
D. none of these

## - Watch Video Solution

106. The number of all the possible selections which a student can make for answering one or more questions out of eight given questions in a paper, when each question has an altrenative, is
A. 256
B. 6560
C. 6561
D. none of these

## Answer: B

## - Watch Video Solution

107. The greatest possible number of points of intersection of 8 straight lines and 4 circles is:
A. 32
B. 64
C. 76
D. 104

## Answer: D

## - Watch Video Solution

108. A lady gives a dinner party to 5 guests to be selected from nine friends. The number of ways of forming the party of 5 , given that two of the friends will not attend the party together, is
A. 56
B. 126
C. 91
D. none of these

## Answer: C

## - Watch Video Solution

109. There are 10 lamps in a hall.Each one of them can be switched on independently.Find the number of ways in which the hall can be illuminated.
A. 102
B. 1023
C. 210
D. 10 !
110. The number of ways in which four persons be seated at a round table, so that all shall not have the same neighbours in any two arrangements,is
A. 24
B. 6
C. 3
D. 4

## Answer: C

## - Watch Video Solution

111. At an election there are five candidates and three members to be elected, and an elector may vote for any number of candidates not
greatre than the number to be elected. Then the number of ways in which an elector may vote, is
A. 25
B. 30
C. 32
D. none of these

## Answer: A

## - Watch Video Solution

112. There are $p$ copies each of $n$ different books. Find the number of ways in which a nonempty selection can be made from them.
A. $n p$
B. pn
C. $(p+1)^{n}-1$
D. $(n+1) p-1$

## Answer: C

## - Watch Video Solution

113. A library has two books each having three copies and three other books each having tow copies. In how many ways can all these books be arranged in a shelf so that copies of the same book are not separated.
A. $\frac{(a+b+c+d)!}{a!b!c!}$
B. $\frac{(a+2 b+3 c+d)!}{a!(b!)^{2}(c!)^{3}}$
C. $\frac{(a+2 b+3 c+d)!}{a!b!c!}$
D. none of these

## Answer: B

114. The total number of arrangements of the letters in the expression $a^{3} b^{2} c^{4}$ when written at full length, is
A. 1260
B. 2520
C. 610
D. none of these

## Answer: A

## - Watch Video Solution

115. The total number of selections of fruit which can be made from 3 bananas, 4 apples and 2 oranges, is
A. 39
B. 315
C. 512
D. none of these

## Answer: D

## - Watch Video Solution

116. The total number of ways of dividing mn things into $n$ equal groups, is
A. $\frac{(m n)!}{m!n!}$
B. $\frac{(m n)!}{(m!)^{m} n!}$
C. $\frac{(m n)!}{(m!)^{n} n!}$
D. none of these

## Answer: C

117. How many different words of 4 letters can be formed with the letters of the word EXAMINATION?
A. 2454
B. 2436
C. 2545
D. none of these

## Answer: A

## - Watch Video Solution

118. ${ }^{35} C_{8}+\sum_{r=1}^{1}{ }^{42-r} C_{7}+\sum_{s=1}^{5}{ }^{47-s} C_{40-s}, i s$
A. ${ }^{46} C_{7}$
B. $46 C_{8}$
C. ${ }^{47} C_{7}$
D. ${ }^{47} C_{8}$

## Answer: D

## - View Text Solution

119. ${ }^{n} C_{n-r}+3 \cdot{ }^{n} C_{n-r+1}+3 \cdot{ }^{n} C_{n-r+2}+{ }^{n} C_{n-r+3}={ }^{x} C_{r}$
A. $\mathrm{n}+1$
B. $\mathrm{n}+2$
C. n+3
D. $n+4$

## Answer: C

120. If n is even and

$$
{ }^{n} C_{0}<{ }^{n} C_{1}<{ }^{n} C_{2}<\ldots .<{ }^{n} C_{r}>{ }^{n} C_{r+1}>{ }^{n} C_{r+2}>\ldots \ldots>{ }^{n} C_{n},
$$

then, $r=$
A. $\frac{n}{2}$
B. $\frac{n-1}{2}$
C. $\frac{n-2}{2}$
D. $\frac{n+2}{2}$

## Answer: A

## D Watch Video Solution

121. Find the number of ways in which one can post 5 letters in 7letter boxes.
A. 35
B. ${ }^{7} P_{5}$
C. $7^{5}$
D. $5^{7}$

## Answer: C

## - Watch Video Solution

122. What is the total number of $2 \times 2$ matrices with each entry 0 or 1 ?
A. 8
B. 16
C. 4
D. none of these

## Answer: B

123. Three dice are rolled. Find the number of possible outcomes in which at least one dice shows 5 .
A. 215
B. 36
C. 125
D. 91

## Answer: D

## - Watch Video Solution

124. The numbers of four different digits number that can be formed from the digits of the number 12356 such that the numbers are divisible by 4 , is
A. 36
B. 48
C. 12
D. 24

## Answer: A

## - Watch Video Solution

125. If m and n are positive integers more than or equal to $2, m>n$, then (mn)! is divisible by
A. $(m!)^{n},(n!)^{m}$ and $(m+n)!$ but not by (m-n)!
B. $(m+n)!,(m-n)!,(m!)^{n}$ but $(n!)^{m}$
C. $(m!)^{n},(n!)^{m},(m+n)!$ and $(m-n)!$
D. $(m!)^{n}$ and $(n!)^{m}$ but not by $(m+n)$ and $(m-n)$ !

## Answer: C

126. Find the number of integers which lie between 1 and $10^{6}$ and which have the sum of the digits equal to 12 .
A. 8550
B. 5382
C. 6062
D. 8055

## Answer: C

## - Watch Video Solution

127. A man invites a party to $(m+n)$ friends to dinner and places $m$ at one round table and n at another. The number of ways of arranging the guests is
A. $\frac{(m+n)!}{m!n!}$
B. $\frac{(m+n)!}{(m-1)!(n-1)!}$
C. $(m-1)!(n-1)$ !
D. none of these

## Answer: D

## - Watch Video Solution

128. The number of ways of arranging $m$ positive and ' $n$ (
A. ${ }^{m+1}+P_{n}$
B. ${ }^{n+1}+P_{m}$
C. ${ }^{m+1}+C_{n}$
D. ${ }^{n+1}+C_{m}$

## Answer: C

129. Out of 10 consonants four vowels, the number of words that can be formed using six consonants and three vowels, is
A. ${ }^{10} P_{6} \times{ }^{6} P_{3}$
B. ${ }^{10} C_{6} \times{ }^{6} C_{3}$
C. ${ }^{10} C_{6} \times{ }^{4} C_{3} \times 9$ !
D. ${ }^{10} P_{6} \times{ }^{4} P_{3}$

## Answer: C

## ( Watch Video Solution

130. Four couples (husband and wife) decide to form a committee of four members. The number of different committees that can be formed in which no couple finds a place is
A. 10
B. 12
C. 14
D. 16

## Answer: D

## - Watch Video Solution

131. N a certain test, there are $n$ question. In the test, $2^{n-i}$ students gave wrong answers to at least $i$ questions, where $i=1,, 2 ; n$. if the total number of wring answers given is 2047, then $n$ is equal to a .10 b . 11 c. 12 d. 13
A. 12
B. 11
C. 10
D. none of these

## Answer: B

## - Watch Video Solution

132. The number of nine nonzero digits such that all the digits in the first four places are less than the digit in the middle and all the digits in the last four places are greater than that in the middle is a. $2(4!) \mathrm{b}$.
$3(7!) / 2$ c. $2(7!)$ d. ${ }^{\wedge} 4 P_{4} \times{ }^{4} P_{4}$
A. 48
B. 576
C. 8 !
D. none of these

## Answer: B

133. The number of ways in which 20 different pearls of two colours can be set alternately on a necklace, there being 10 pearls of each colour, is
A. $9!\times 10!$
B. $5 \times(9!)^{2}$
C. $(9!)^{2}$
D. none of these

## Answer: B

## - Watch Video Solution

134. There are n seats round a table numbered $1,2,3, \ldots, n$. The number of ways in which $m(\leq n)$ persons can take seats is
A. $(n) C_{m}$
B. ${ }^{n} C_{m} \times m$ !
C. $(m-1)$ !
D. $(m-1)!\times(n-1)$ !

## Answer: B

## - Watch Video Solution

135. A shopkeeper sells three varieties of perfumes and he has a large number of bottles of the same size of each variety in his stock. There are 5 places in a row in his showcase. The number of different ways of displaying the three varieties of perfumes in the show case, is
A. 6
B. 50
C. 150
D. none of these

## Answer: C

136. If $r>p>q$, the number of different selections of $p+q$ things taking $r$ at a time, where $p$ things are identical and $q$ other things are identical, is
A. $p+q-r$
B. $p+q-r+1$
C. $r-p-q+1$
D. none of these

## Answer: B

## - Watch Video Solution

Chapter Test

1. 7 women and 7 men are to sit round a circulartable such that there is a man on either side ofevery women. The number of seating arrangements is
A. $(7!)^{2}$
B. $(6!)^{2}$
C. $6!\times 7!$
D. $7!$

## Answer: C

## - Watch Video Solution

2. There are $(n+1)$ white and $(n+1)$ black balls, each set numbered
$1 \rightarrow n+1$. The number of ways in which the balls can be arranged in a row so that the adjacent balls are of different colors is a. $(2 n+2)$ ! b. $(2 n+2)!\times 2$ c. $(n+1)!\times 2$ d. $2\{(n+1)!\}^{2}$
A. $(2 n+2)$ !
B. $(2 n+2)!\times 2$
C. $(n+1)!\times 2$
D. $2\{(n+1)!\}^{2}$

## Answer: D

## D Watch Video Solution

3. 12 persons are to be arranged to a round table. If two particular persons among them are not to be side by side, the total number of arrangements, is
A. 9 (10!)
B. $2(10$ !)
C. $45(8!)$
D. 10 !

Answer: A

## - Watch Video Solution

4. The number of committees of 5 persons consisting of at least one female number, that can be formed from 6 males and 4 females, is
A. 246
B. 252
C. 6
D. none of these

## Answer: A

5. The number of ways in which a team of 11 players can be selected from 22 players .including 2 of them and excluding 4 of them is
A. ${ }^{16} C_{11}$
B. ${ }^{16} C_{5}$
C. ${ }^{16} C_{9}$
D. ${ }^{20} C_{9}$

## Answer: C

## - Watch Video Solution

6. In a football championship, 153 matches were played. Every two teams played one match with each other. The number of teams, participating in the championship is $\qquad$
B. 18
C. 9
D. none of these

## Answer: B

## - Watch Video Solution

7. How many numbers between 5000 and 10,000 can be formed using the digits $1,2,3,4,5,6,7,8,9$, each digit appearing not more than once in each number?
A. $5 \times{ }^{8} P_{3}$
B. $5 \times{ }^{8} C_{8}$
C. $5!\times{ }^{8} P_{3}$
D. $5!\times{ }^{8} C_{3}$
8. If $x, y$ and $r$ are positive integers, then ${ }^{x} C_{r}+{ }^{x} C_{r-1}+{ }^{y} C_{1}+{ }^{x} C_{r-2}{ }^{y} C_{2}+\ldots \ldots+{ }^{y} C_{r}=$
A. $\frac{x!y!}{r!}$
B. $\frac{(x!y!)}{r!}$
C. ${ }^{x+y} C_{r}$
D. ${ }^{x y} C_{r}$

## Answer: C

9. In how many ways can 5 red and 4 white balls be drawn from a bag containing 10 red and 8 white balls
A. ${ }^{8} C_{5} \times{ }^{10} C_{4}$
B. ${ }^{10} C_{5} \times{ }^{8} C_{4}$
C. ${ }^{18} C_{9}$
D. none of these

## Answer: B

## - Watch Video Solution

10. All the letters of the word $E A M L E T$ are arranged in all possible ways. The number of such arrangements in which no two vowels are adjacent to each other is
A. 360
B. 144
C. 72
D. 54

## Answer: C

## - Watch Video Solution

11. There are 10 lamps in a hall.Each one of them can be switched on independently.Find the number of ways in which the hall can be illuminated.
A. $10^{2}$
B. 1023
C. $2^{10}$
D. 10 !

## Answer: B

12. How many 10 -digit numbers can be formed by using digits 1 and 2
A. ${ }^{10} C_{1}+{ }^{9} C_{2}$
B. $2^{10}$
C. $10^{2}$
D. 10 !

## Answer: B

## - Watch Video Solution

13. The straight lines $I_{1}, I_{2}, I_{3}$ are paralled and lie in the same plane. A total number of m point are taken on $I_{1}, n$ points on $I_{2}$, k points on $I_{3}$. The maximum number of triangles formed with vertices at these points are

$$
\text { A. }{ }^{m+n+k} C_{3}
$$

B. ${ }^{m+n+k} C_{3}-{ }^{m} C_{3}-{ }^{n} C_{3}-{ }^{k} C_{3}$
C. ${ }^{m} C_{3}+{ }^{n} C_{3}+{ }^{k} C_{3}$
D. none of these

## Answer: B

## - Watch Video Solution

14. The number of parallelograms that can be formed from a set of four parallel lines intersecting another set of three parallel lines is:
A. 6
B. 18
C. 12
D. 9
15. The number of diagonals that can be drawn by joining the vertices of an octagon is
A. 28
B. 48
C. 20
D. none of these

## Answer: C

## - Watch Video Solution

16. The sum of the digits in the unit place of all numbers formed with the help of 3,4,5,6 taken all at a time is
B. 108
C. 36
D. 18

## Answer: B

## - Watch Video Solution

17. In an examination there are three multiple choice questions and each question has 4 choices. The number of ways in which a student can fail to get all answers correct is (a) 11 (b) 27 (c) 12 (d) 63
A. 11
B. 12
C. 27
D. 63

## Answer: D

18. There are 10 points in a plane, out of these 6 are collinear. The number of triangles formed by joining these points, is
A. 100
B. 120
C. 150
D. none of these

## Answer: A

## - Watch Video Solution

19. Ramesh has 6 friends. In how many ways can be invite one or more of them at a dinner ? (A) 61 (B) 62 (C) 63 (D) 64
A. 61
B. 62
C. 63
D. 64

## Answer:

## - Watch Video Solution

20. Let $P_{m}$ stand for $m P_{m}$ then $1+P_{1}+2 P_{2}+3 P_{3}+\ldots \ldots .+n P_{n}$ is equal to
A. $(n-1$ ! $)$
B. n!
C. $(n+1)!-1$
D. none of these

## Answer:

## - Watch Video Solution

21. The number of ways four boys can be seated around a round talble in four chairs of ditterent colours, is
A. 24
B. 12
C. 23
D. 64

## Answer: A

22. We are required to form different words with the help of the word INTEGER. Let $m_{1}$ be the number of words in which I and N are never together and $m_{2}$ be the number or words which begin with and I and end with R , then $\frac{m_{1}}{m_{2}}$
A. 42
B. 30
C. 6
D. $1 / 30$

## Answer: B

## - Watch Video Solution

23. A candidate is required to answer 6 out of 10 questions, which are divide into two groups, each containing 5 questions. He is not permitted to attempt more than 4 questions from either group. The
number of different ways in which the candidate can choose 6 questions is a. 50 b. 150 c. 200 d. 250
A. 200
B. 150
C. 100
D. 50

## Answer: A

## - Watch Video Solution

24. The number of ways in which 6 men and 5 women can dine at a round table if no two women are to sit together is given by
A. $7!\times 5!$
B. $6!\times 5!$
C. 30
D. 50

## Answer: B

## D Watch Video Solution

25. A student is to answer 10 out of 13 questions in an examination such that he must choose at least 4 from the first five questions. The number of choices available to him is
A. 346
B. 140
C. 196
D. 280

## Answer: C

26. Write the number of all possible words that can be formed using the letters of the word MATHEMATICS.
A. $\frac{11!}{2!2!2!}$
B. 11!
C. ${ }^{11} C_{1}$
D. none of these

## Answer: A

## (D) Watch Video Solution

27. In a group of boys, two boys are brothers and six more boys are present in the group. In how many ways can they sit if the brothers are not to sit along with each other? $\mathrm{a} .2 \times 6$ ! b. ${ }^{\wedge} 7 P_{2} \times 6$ ! c. ${ }^{\wedge} 7 C_{2} \times 6$ !
d. none of these
B. 1410
C. 2830
D. none of these

## Answer: D

## - Watch Video Solution

28. Nishi has 5 coins, each of the different denomination. Find the number different sums of money she can form.
A. 32
B. 25
C. 31
D. none of these

## Answer: C

29. Write the number of ways in which 5 boys and 3 girls can be seated in a row so that each girl is between 2 boys.
A. 2880
B. 1880
C. 3800
D. 2800

## Answer: A

## - Watch Video Solution

30. how many different nine digit numbers can be formed from the number 223355888 by rearranging its digits so that the odd digits occupy even positions:
A. 7560
B. 180
C. 16
D. 60

## Answer: D

## - Watch Video Solution

31. The number of 4 digit even numbers that can be formed using 0,1 ,
$2,3,4,5,6$ without repetition is
A. 120
B. 300
C. 420
D. 20

## Answer: C

## - Watch Video Solution

32. The number of ways in which $n$ ties can be selected from a rack displaying $3 n$ different ties, is
A. $\frac{3 n!}{2 n!}$
B. $3 \times n$ !
C. $(3 n)$ !
D. $\frac{3!}{n!2 n!}$

## Answer: D

## - Watch Video Solution

33. There are $n$-points ( $n>2$ ) in each to two parallel lines. Every point on one line is joined to every point on the other line by a line segment drawn within the lines. The number of point (between the lines) in which these segments intersect, is
A. ${ }^{2 n} C_{2}-2 .{ }^{n} C_{1}+2$
B. ${ }^{2 n} C_{2}-2 \times{ }^{n} C_{2}$
C. ${ }^{n} C_{2} \times{ }^{n} C_{2}$
D. none of these

## Answer: C

## - Watch Video Solution

34. The maximum number of points of intersection of 8 circles is
A. 16
B. 24
C. 28
D. 56

## Answer: D

## - Watch Video Solution

35. The maximum number of points of intersection into which 4 circles and 4 straight lines intersect, is
A. 26
B. 50
C. 56
D. 72

## Answer: B

36. In a circket charmpionship there are 36 matches. The number of teams if each plays one match with other, is
A. 8
B. 9
C. 10
D. none of these

## Answer: B

## - Watch Video Solution

37. The expression

$$
{ }^{n} C_{r}+4 .{ }^{n} C_{r-1}+6 .{ }^{n} C_{r-2}+4 .{ }^{n} C_{r-3}+{ }^{n} C_{r-4}
$$

A. ${ }^{n+4} C_{r}$
B. $2 .{ }^{n+4} C_{r-1}$
C. $4 .{ }^{n} C_{r}$
D. $11 .{ }^{n} C_{r}$

## Answer: A

## - Watch Video Solution

38. The total number of numbers greater than 100 and divisible by 5 , that can be formed from the digits $3,4,5,6$ if no digit is repeated, is
A. 24
B. 48
C. 30
D. 12

## Answer: D

39. Find the number of words that can be made out of the letters of the word MOBILE when consonants always occupy odd places.
A. 20
B. 36
C. 30
D. 720

## Answer: B

## - Watch Video Solution

40. Number of numbers greater than 24000 can be formed by using digits $1,2,3,4,5$ when no digit being repeated is
B. 60
C. 84
D. 120

## Answer: C

## (D) Watch Video Solution

41. Write the number of words that can be formed out of the letters of the word COMMITTEE.
A. $\frac{9!}{(2!)^{3}}$
B. $\frac{9!}{(2!)^{2}}$
C. $\frac{9!}{2!}$
D. 9 !
42. How many different committees of 5 can be formed from 6 men and 4 women on which exact 3 men and 2 women serve?
A. 6
B. 20
C. 60
D. 120

## Answer: D

## - Watch Video Solution

43. The number of ways to rearrange the letters of the word CHEESE is
A. 120
B. 240
C. 720
D. 6

Answer: A

## - Watch Video Solution

44. If ${ }^{k+5} P_{k+1}=\frac{11(k-1)}{2} \cdot{ }^{k+3} P_{k} P_{k}$ then the values of $k$ are 7 and 11 b. 6 and 7 c. 2 and 11 d. 2 and 6
A. 7 and 11
B. 6 and 7
C. 2 and 11
D. 2 and 6

## Answer: B

45. Find the number of proper factors of the number 38808 . Also, find sum of all these divisors.
A. 70
B. 72
C. 71
D. none of these

## Answer: A

## (D) Watch Video Solution

46. In a party 15 people shake their hands with each other. How many times did the hand-shakes take place?
A. ${ }^{15} P_{2}$
B. ${ }^{15} C_{2}$
C. 15!
D. $2 \times 15$ !

## Answer: B

## D Watch Video Solution

47. The number of ways in which 5 beads of different colours can be made into a necklace is
A. 12
B. 120
C. 60
D. 24

## Answer: A

48. Find number of ways that 8 beads o different colors be strung as a necklace.
A. 2520
B. 2880
C. 5040
D. 4320

## Answer: A

## ( Watch Video Solution

49. There are $n$ points in a plane of which ' $p$ ' points are collinear. How many lines can be formed from these points
A. ${ }^{n} C_{2}-{ }^{p} C_{2}+1$
B. ${ }^{n} C_{2}-{ }^{p} C_{2}$
C. $n-{ }^{p} C_{2}$
D. ${ }^{n} C_{2}-{ }^{p} C_{2}-1$

Answer: A

## - Watch Video Solution

50. The number of 4 digit even numbers that can be formed using 0,1 ,
$2,3,4,5,6$ without repetition is
A. 120
B. 300
C. 420
D. 20

## Answer: C

51. The number of ways in which 21 objects can be grouped into three groups of 8,7 , and 6 objects,is
A. $\frac{20!}{8!+7!+6!}$
B. $\frac{21!}{8!7!}$
C. $\frac{21!}{8!7!6!}$
D. $\frac{21!}{8!+7!+6!}$

## Answer: C

## ( Watch Video Solution

52. Let $L_{1}$ and $L_{2}$ be two lines intersecting at P If $A_{1}, B_{1}, C_{1}$ are points on $L_{1}, A_{2}, B_{2}, C_{2}, D_{2}, E_{2}$ are points on $L_{2}$ and if none of these coincides with $P$, then the number of triangles formed by these 8 points is
A. 56
B. 55
C. 46
D. 45

## Answer: D

## - Watch Video Solution

53. Consider the fourteen lines in the plane given by $y=x+r, y=-x+r$, where $r \in\{0,1,2,3,4,5,6\}$. The number of squares formed by these lines whose diagonals are of length 2 , is
A. 9
B. 16
C. 25
D. 36
54. How many words can be formed out of the letters of the word, ARTICLE, so that vowels occupy even places?
A. 574
B. 36
C. 754
D. 144

## Answer: D

## - Watch Video Solution

55. The number of ways in which 9 persons can be divided into three equal groups is
A. 1680
B. 840
C. 560
D. 280

## Answer: D

## - Watch Video Solution

56. A dictionary is printed consisting of 7 lettered words only that can be made with letters of the word "CRICKET". If the words are printed in the alphabetical order, as in the ordinary dictionary, then the number of words before the word CRICKET, is
A. 530
B. 480
C. 531
D. 481

## Answer: A

## - Watch Video Solution

57. The number of times the digit 5 will be written when listing the integers from 1 to 1000, is
A. 271
B. 272
C. 300
D. none of these

## Answer: C

58. How many numbers lying between 999 and 10000 can be formed with the help of the digit $0,2,3,6,7,8$ when the digits are not to be repeated
A. 100
B. 200
C. 300
D. 400

## Answer: C

## - Watch Video Solution

59. The number of different words that can be formed from the letters of the word 'PENCIL', so that no two vowels are together, is
A. 120
B. 260
C. 240
D. 480

## Answer: C

## - Watch Video Solution

60. How many four digit numbers can be formed using digits $1,2,3,4,5$ such that at least one of the number is respeated?
A. $4^{4}-5$ !
B. $4^{5}-4$ !
C. $5^{4}-4$ !
D. $5^{4}-5$ !

## Answer: D

