



## MATHS

### BOOKS - OBJECTIVE RD SHARMA MATHS VOL I (HINGLISH)

#### DEFINITE INTEGRALS

#### Illustration

1. The value of  $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$  is

A.  $\frac{\pi}{2} + 1$

B.  $\frac{\pi}{2} - 1$

C. -1

D. 1

**Answer: B**



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2. The value of  $I = \int_0^{\pi/2} \frac{(\sin x + \cos)^2}{\sqrt{1 + \sin 2x}} dx$  is

A. 3

B. 1

C. 2

D. 0

**Answer: C**

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3. If  $I(m, n) = \int_0^1 t^m (1 - t)^n dt$ , then the expression for  $I(m, n)$  in terms of

$I(m+1, n-1)$ , is

A.  $\frac{2^n}{m+1} - \frac{n}{m+1} I(m+1, n-1)$

B.  $\frac{n}{m+1} I(m+1, n-1)$

$$C. \frac{2^n}{m+1} - \frac{n}{m+1} I(m+1, n-1)$$

$$D. \frac{m}{n+1} I(m+1, n-1)$$

**Answer: B**



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4. If a function  $f(x) + b f\left(\frac{1}{x}\right) = \frac{1}{x} - 5$ ,  $x \neq 0$ ,  $a \neq b$ , then  $\int_1^2 f(x) dx$  equals

$$A. \frac{(\ln 2 - 5)a + \frac{13}{2}b}{a^2 - b^2}$$

$$B. \frac{(\ln 2 - 5)a + \frac{7b}{2}}{a^2 - b^2}$$

$$C. \frac{(5 - \ln 2)a + \frac{7b}{2}}{a^2 - b^2}$$

D. none of these

**Answer: B**



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5.  $\int_{\pi/4}^{3\pi/4} \frac{1}{1 + \cos x} dx =$

A. 2

B. 6

C. 5

D. 3

**Answer: A**



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6. If  $\int_0^a \frac{1}{1 + 4x^2} dx = \frac{\pi}{8}$ , then  $2a =$

A. 1

B.  $\frac{1}{2}$

C.  $-\frac{1}{2}$

D. None

**Answer: A**



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7. The solution for  $x$  of the equation

$$\int_{\sqrt{2}}^x \frac{1}{t\sqrt{t^2-1}} dt = \frac{\pi}{2}, \text{ is}$$

A.  $\frac{\sqrt{3}}{2}$

B.  $2\sqrt{2}$

C. 2

D.  $-\sqrt{2}$

**Answer: D**



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8. If  $2 \int_0^1 \tan^{-1} x dx = \int_2^1 \cot^{-1}(1-x+x^2) dx$ . Then

$\int_0^1 \tan^{-1}(1-x+x^2) dx$  is equal to

A.  $\log 2$

B.  $\frac{\pi}{2} + \log 2$

C.  $\log 4$

D.  $\frac{\pi}{2} - \log 4$

**Answer: A**

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9. Let  $\frac{d}{dx}(F(x)) = \frac{e^{\sin x}}{x}, x > 0$

If  $\int_1^4 \frac{2e^{\sin x^2}}{x} - dx = F(k) - F(1)$ , then one of the possible values of  $k$ ,  
is

A. 4

B. 8

C. 16

D. 32

**Answer: C**

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10. The value of the integral  $\int_0^{\pi/4} \frac{\sin x + \cos x}{3 + \sin 2x} dx$ , is

A.  $\log 2$

B.  $\log 3$

C.  $\frac{1}{4} \log 3$

D.  $\frac{1}{8} \log 3$

**Answer: C**

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11. If  $I_1 = \int_e^{e^2} \frac{dx}{\log x}$  and  $I_2 = \int_1^2 \frac{e^x}{x} dx$ , then

A.  $I_1 = I_2$

B.  $2I_1 = I_2$

C.  $I_1 = 2I_2$

D. none of these

**Answer: A**

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12. The value of the integral  $\int_0^{\log 5} \frac{e^x \sqrt{e^x - 1}}{e^x + 3} dx$ , is

A.  $3 + 2\pi$

B.  $4 - \pi$

C.  $2 + \pi$

D. none of these

**Answer: B**

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13. Given  $\int_1^2 e^{x^2} dx = a$ , the value of  $\int_e^{e^4} \sqrt{\log_e x} dx$ , is

A.  $e^4 - e$

B.  $e^4 - a$

C.  $2e^4 - a$

D.  $2e^4 - e - a$

Answer: D



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14. If  $\int_0^1 \frac{\sin t}{1+t} dt = \alpha$ , then the value of the integral

$\int_{4\pi-2}^{4\pi} \frac{\sin \frac{t}{2}}{4\pi + 2 - t} dt$  in terms of  $\alpha$  is given by

A.  $2\alpha$

B.  $-2\alpha$

C.  $\alpha$

D.  $-\alpha$

**Answer: D**



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15.  $\int_0^{2\pi} e^{x/2} \sin\left(\frac{x}{2} + \frac{\pi}{4}\right) dx =$

A.  $2\pi$

B.  $e^\pi$

C. 0

D.  $2\sqrt{2}$

**Answer: C**



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16. If  $I_n = \int_0^{\pi/4} \tan^n \theta d\theta$ , then  $I_8 + I_6$  equals

A.  $\frac{1}{4}$

B.  $\frac{1}{5}$

C.  $\frac{1}{6}$

D.  $\frac{1}{7}$

**Answer: D**



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17.  $\int_0^2 \frac{x^3}{(x^2 + 1)^{3/2}} dx$  is equal to

A.  $(\sqrt{2} - 1)^2$

B.  $\frac{(\sqrt{2} - 1)}{\sqrt{2}}$

C.  $\frac{\sqrt{2} - 1}{\sqrt{2}}$

D. none of these

**Answer: D**



18. The value of the integral  $I = \int_0^a \frac{x^4}{(a^2 + x^2)^4} dx$  is

A.  $\frac{1}{16a^3} \left( \frac{\pi}{4} - \frac{1}{3} \right)$

B.  $\frac{1}{16a^3} \left( \frac{\pi}{4} + \frac{1}{3} \right)$

C.  $\frac{a^3}{16} \left( \frac{\pi}{4} - \frac{1}{3} \right)$

D.  $\frac{a^3}{16} \left( \frac{\pi}{4} + \frac{1}{3} \right)$

**Answer: A**



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19. Let  $f(x) = 7 \tan^8 x + 7 \tan^6 x - 3 \tan^4 x - 3 \tan^4 x - 3 \tan^2 x$  for all  $x \in \left( -\frac{\pi}{2}, \frac{\pi}{2} \right)$ . Then the correct expression (s) is (are)

$$\int_0^{\frac{\pi}{4}} x f(x) dx = \frac{1}{12} \quad \int_0^{\frac{\pi}{4}} f(x) dx = 0 \quad \int_0^{\frac{\pi}{4}} x f(x) dx = \frac{1}{6} \quad \text{(d)}$$

$$\int_0^{\frac{\pi}{4}} f(x) dx = \frac{1}{12}$$

$$\text{A. } \int_0^{\pi/4} x f(x) dx = \frac{1}{12}$$

$$\text{B. } \int_0^{\pi/4} x f(x) dx = 0$$

$$\text{C. } \int_0^{\pi/4} x f(x) dx = \frac{1}{6}$$

$$\text{D. } \int_0^{\pi/4} f(x) dx = 1$$

**Answer: A,B**



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20. If  $\alpha = \int_0^1 e^{3x + 3 \tan^{-1} x \left( \frac{12 + 9x^2}{1 + x^2} \right)} dx$ , where  $\tan^{-1}$  takes principal values,

then the value of

$\left( \log_e |1 + \alpha| - \frac{3\pi}{4} \right)$ , is

A. 9

B. 8

C. 7

D. 6

**Answer: A**



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21. The value of  $\int_0^{\pi} |\cos x| dx$ , is

A. 1

B. 2

C. 0

D. 4

**Answer: B**



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22.  $\int_0^2 |x^2 + 2x - 3| dx$  is equal to

A. 4

B. 6

C. 3

D. 2

**Answer: A**



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23.  $\int_0^3 [x] dx$  is equal to

A. 2

B. 4

C. 3

D. 1

**Answer: C**



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24.  $\int_0^{15} [x^2] dx$  is equal to

A. 2

B.  $2 - \sqrt{2}$

C.  $2 + \sqrt{2}$

D.  $\sqrt{2}$

**Answer: B**



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25.  $\int_0^2 [x^2] dx$  is equal to

A.  $5 - \sqrt{2}$

B.  $5 - \sqrt{3} - \sqrt{2}$

C.  $5 - \sqrt{3}$



D. none of these

**Answer: B**



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26. Let  $f(x) = x - [x]$ , for every real number  $x$ , where  $[x]$  is integral part of  $x$ . Then,  $\int_{-1}^1 f(x) dx$ , is

A. 1

B. 2

C. 0

D.  $1/2$

**Answer: A**



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27. If  $\{x\}$  denotes the fractional part of  $x$ , then  $\int_0^2 \{x\} dx$  is equal to

A. 1

B. 2

C.  $\frac{1}{2}$

D. 4

**Answer: A**



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28.  $\int_0^4 \{\sqrt{x}\} dx$  is equal to, where  $\{x\}$  denotes the fraction part of  $x$ .

A.  $\frac{2}{3}$

B.  $\frac{16}{3}$

C.  $\frac{5}{3}$

D.  $\frac{7}{3}$

**Answer: D**



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29. For any real number  $x$ , the value of  $\int_0^x [x] dx$ , is

A.  $x[x]$

B.  $x[x] - [x]([x] + 1)$

C.  $x[x] - \frac{1}{2}[x]([x] + 1)$

D. none of these

**Answer: C**



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30. If  $\{x\}$  denotes the fractional part of  $x$ , then  $\int_0^x \left( \{x\} - \frac{1}{2} \right) dx$  is equal to

A.  $\frac{1}{2}\{x\}(\{x\} + 1)$

B.  $\frac{1}{2}\{x\}(\{x\} - 1)$

C.  $\{x\}(\{x\} - 1)$

D.  $\{x\}(\{x\} + 1)$

**Answer: B**



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31. The value of:  $\int_{\pi/6}^{5\pi/6} \sqrt{4 - 4\sin^2 t} dt$ , is

A. 0

B. 2

C. 1

D. none of these

**Answer: B**



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32. If for a real number  $y$ ,  $[y]$  is the greatest integer less than or equal to  $y$ ,

then the value of the integral  $\int_{\pi/2}^{3\pi/2} [2 \sin x] dx$ , is

A.  $-\pi$

B. 0

C.  $-\pi/2$

D.  $\pi/2$

**Answer: C**



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33. If  $[.]$  stands for the greatest integer function, then  $\int_1^2 [3x] dx$  is equal

to

A. 3

B. 4

C. 5

D. 6

**Answer: B**



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34. The value of the integral  $\int_0^{0.9} [x - 2[x]] dx$ , where  $[.]$  denotes the greatest integer function, is

A. 0.9

B. 0

C. 1.8

D. -0.9

**Answer: B**



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35. Let  $[.]$  denote the greatest integer function, then the value of

$$\int_0^{1.5} x[x^2] dx, \text{ is}$$

A.  $\frac{3}{2}$

B.  $\frac{3}{4}$

C.  $\frac{5}{4}$

D. 0

**Answer: B**



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36. The integral  $\int_0^{\pi} \sqrt{1 + 4\sin^2 \frac{x}{2} - 4\sin \frac{x}{2}} dx$  equals ,

A.  $4\sqrt{3} - 4$

B.  $4\sqrt{3} - 4 - \frac{\pi}{3}$

C.  $\pi - 4$

D.  $\frac{2\pi}{3} - 4 - 4\sqrt{3}$

**Answer: B**



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37. The value of  $\int_0^1 4x^3 \left\{ \frac{d^2}{dx^2} (1 - x^2)^5 \right\} dx$  is

A. 1

B. 2

C. 8

D. 4

**Answer: B**



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38. Let  $f: R \rightarrow R$  be a function defined by  $f(x) \begin{cases} [x], & x \leq 2 \\ 0, & x > 2 \end{cases}$  where  $[x]$  is the greatest integer less than or equal to  $x$ . If  $I = \int_{-1}^2 \frac{x f(x^2)}{2 + f(x+1)} dx$ ,

then the value, is

A.  $\frac{1}{4}$

B.  $\frac{1}{2}$

C. 8

D.  $-\frac{1}{4}$

**Answer: A**

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39. The value  $\int_1^a [x] f'(x) dx$ ,  $a > 1$ , where  $[x]$  denotes the greatest integer not exceeding  $x$ , is

A.  $a f(a) - \{f(1) + f(2) + \dots + f([a])\}$

B.  $[a] f(a) - \{f(1) + f(2) + \dots + f([a])\}$

C.  $[a]f([a]) - \{f(1) + f(2) + \dots + f(a)\}$

D.  $a f([a]) - \{f(1) + f(2) + \dots + f(a)\}$

**Answer: B**



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**40.** If  $m, n \in \mathbb{N}$ , then

$\int_0^{\pi/2} \frac{(\sin^m x)^{\frac{1}{n}}}{(\sin^m x)^{\frac{1}{n}} + (\cos^m x)^{\frac{1}{n}}} dx$  is equal to

A.  $\frac{\pi}{2}$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{2n}$

D.  $\frac{\pi}{4n}$

**Answer: B**



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41. The value of  $\int_0^{\pi/2} \log \tan x dx$ , is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{2}$

C. 0

D. none of these

**Answer: C**



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42. The value of  $\int_0^{\infty} \frac{\log x}{1+x^2} dx$ , is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{2}$

C. 0

D. none of these

**Answer: C**



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43. If  $I = \int_0^{\pi/4} \log(1 + \tan x) dx$ , then  $I =$

A.  $\frac{\pi}{8} \log_e 2$

B.  $\frac{\pi}{4} \log_e 2$

C.  $-\frac{\pi}{8} \log_e 2$

D.  $-\frac{\pi}{4} \log_e 2$

**Answer: A**



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44. The value of integral  $\int_0^1 \frac{\log(1+x)}{1+x^2} dx$ , is

A.  $\frac{\pi}{8} \log_e 2$

B.  $\frac{\pi}{4} \log_e 2$

C.  $-\frac{\pi}{8} \log_e 2$

D.  $-\frac{\pi}{4} \log_e 2$

**Answer: A**



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45. The value of the integral  $\int_0^a \frac{1}{x + \sqrt{a^2 - x^2}} dx$ , is

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{4}$

D. none of these

**Answer: C**



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46. The value of  $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$ , is

A.  $\frac{\pi}{2} \log 2$

B.  $-\frac{\pi}{2} \log 2$

C.  $\pi \log 2$

D.  $-\pi \log 2$

**Answer: B**



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47. The value of  $\int_0^{\pi/2n} \frac{1}{1 + \cos nx} dx$ , is

A. 0

B.  $\frac{\pi}{4n}$

C.  $\frac{\pi}{2n}$

D.  $\frac{\pi}{2}$

**Answer: B**



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48.  $\int_0^{\pi/2} \sin 2x \log \tan x dx$  is equal to

A.  $\pi$

B.  $\frac{\pi}{2}$

C. 0

D. 1

**Answer: C**



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49. The value of the integral  $\int_0^{\pi} \frac{1}{e^{\cos x} + 1} dx$ , is

A.  $\pi$

B. 0

C.  $2\pi$

D.  $\frac{\pi}{2}$

**Answer: D**

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50. The value of the integral  $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$ , is

A.  $\frac{\pi^2}{2}$

B.  $\frac{\pi^2}{4}$

C.  $\frac{\pi^2}{8}$

D.  $\frac{\pi^2}{16}$

**Answer: B**

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51. The integral  $\int_0^{\pi} x f(\sin x) dx$  is equal to

A.  $\frac{\pi}{2} \int_0^{\pi} f(\sin x) dx$

B.  $\frac{\pi}{4} \int_0^{\pi} (\sin x) dx$

C.  $\frac{\pi}{2} \int_0^{\pi/2} (\sin x) dx$

D.  $\frac{\pi}{2} \int_0^{\pi/2} f(\cos x) dx$

**Answer: A**



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52.  $\int_0^{\pi} [\cot x] dx$ ,  $[\cdot]$  denotes the greatest integer function, is equal to

A.  $\frac{\pi}{2}$

B. 1

C. -1

D.  $-\frac{\pi}{2}$

**Answer: B**



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**53.** The value of the integral

$$\int_{-1/2}^{1/2} \cos x \log\left(\frac{1+x}{1-x}\right) dx, \text{ is}$$

A. 0

B.  $\frac{1}{2}$

C.  $-\frac{1}{2}$

D. none of these

**Answer: A**



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54. The value of  $\int_{-1}^1 \left\{ \sqrt{1+x+x^2} - \sqrt{1-x+x^2} \right\} dx$ , is

A. 0

B. 1

C. -1

D. none of these

**Answer: A**



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55. The value of  $\frac{\left\{ \int_{-1/2}^{1/2} \cos 2x \cdot \log\left(\frac{1+x}{1-x}\right) dx \right\}}{\left\{ \int_0^{1/2} \cos 2x \cdot \log\left(\frac{1+x}{1-x}\right) dx \right\}}$  is

A. 0

B. 4

C. 2

D. 8

**Answer: A**



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56. The value of  $\int_{-2}^2 (ax^3 + bx + c) dx$  depends on

A. B

B. C

C. A

D. none of these

**Answer: B**



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57. The value of the integral

$$\int_{-1}^1 \log(x + \sqrt{x^2 + 1}) dx \text{ is}$$

A. 0

B.  $\log 2$

C.  $\log 1/2$

D. none of these

**Answer: A**



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58.  $\int_{-3\pi/2}^{-\pi/2} \left\{ (x + \pi)^3 + \cos^2(x + 3\pi) \right\} dx$ , is

A.  $\frac{\pi^4}{32}$

B.  $\frac{\pi^4}{32} + \frac{\pi}{2}$

C.  $\frac{\pi}{2}$

D.  $\frac{\pi}{4} - 1$

**Answer: C**



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59. The value of

$$I = \int_{-2}^0 \{x^3 + 3x^2 + 3x + 3 + (x + 1)\cos(x + 1)\cos(x + 1)\} dx, \text{ is}$$

A. 0

B. 3

C. 4

D. 1

**Answer: C**



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60.  $\int_{-\pi/2}^{\pi/2} \frac{1}{e^{\sin x} + 1} dx$  is equal to

A. 0

B. 1

C.  $-\frac{\pi}{2}$

D.  $\frac{\pi}{2}$

**Answer: D**



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61. The value of  $\int_{\pi/4}^{\pi/4} \frac{e^x \sec^2 x}{e^{2x} - 1} dx$ , is

A. 0

B. 2

C. E

D. none of these

**Answer: A**



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62. The value of  $\int_{-\pi/2}^{\pi/2} \frac{\cos x}{1 + e^x} dx$ , is

- A. 0
- B. -1
- C. 1
- D. none of these

**Answer: C**

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63. The value of  $\int_{-\pi/2}^{\pi/2} \frac{x^2 \cos x}{1 + e^x} dx$  is equal to

- A.  $\frac{\pi^2}{4} - 2$
- B.  $\frac{\pi^2}{4} + 2$
- C.  $\pi^2 + e^{\pi/2}$
- D. 0



**Answer: A**

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64. The value of  $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1+a^2} dx, a > 0$ , is

A.  $\pi$

B.  $\pi$

C.  $\pi/2$

D.  $2\pi$

**Answer: C**

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65. If  $I = \int_{-\pi}^{\pi} \frac{e^{\sin x}}{e^{\sin x} + e^{-\sin x}} dx$ , then I equals

A.  $\frac{\pi}{2}$

B.  $2\pi$

C.  $\pi$

D.  $\frac{\pi}{4}$

**Answer: C**



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66. The value of  $\int_{-2}^2 \frac{3x^2}{1+e^x} dx$ , is

A. 8

B. 2

C. 4

D. 0

**Answer: A**



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67. The value of  $\int_0^{2\pi} \cos^5 x dx$ , is

- A. 0
- B.  $\pi$
- C.  $2\pi$
- D.  $\pi/2$

**Answer: A**



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68. If  $\int_0^{\pi} x f(\sin x) dx = A \int_0^{\pi/2} f(\sin x) dx$ , then A is

- A.  $2\pi$
- B.  $\pi$
- C.  $\pi/4$
- D. 0

**Answer: B**



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69. The value of  $\int_0^{\pi} \cos^{11} x dx$ , is

A.  $\pi$

B.  $11\pi$

C. 0

D.  $-11\pi$

**Answer: C**



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70.  $I = \int_0^{2\pi} \frac{1}{1 + e^{\sin x}} dx$  is equal to

A.  $\pi$

B.  $2\pi$

C.  $\frac{\pi}{2}$

D. none of these

**Answer: A**



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71.  $\int_0^{2\pi} \frac{x \sin^{2n} x}{\sin^{2n} x + \cos^{2n} x} dx, n > 0$ , is equal to

A.  $\pi$

B.  $2\pi$

C.  $\pi^2$

D.  $\frac{1}{2}\pi^2$

**Answer: C**



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72. If  $[x]$  stands for the greatest integer function, the value of

$$\int_4^{10} \frac{[x^2]}{[x^2 - 28x + 196] + [x^2]} dx, \text{ is}$$

- A. 0
- B. 1
- C. 3
- D. none of these

**Answer: C**



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73. The value of  $\int_{\sqrt{\ln 2}}^{\sqrt{\ln 3}} \frac{x \sin x^2}{\sin x^2 + \sin(\ln 6 - x^2)} dx$ , is

- A.  $\frac{1}{4} \ln \frac{3}{2}$
- B.  $\frac{1}{2} \ln \frac{3}{2}$
- C.  $\ln \frac{3}{2}$

D.  $\frac{1}{6} \ln \frac{3}{2}$

**Answer: A**



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**74.** The integral

$$\int_2^4 \frac{\log x^2}{\log x^2 + \log(36 - 12x + x^2)} dx \text{ is equal to}$$

A. 1

B. 6

C. 2

D. 4

**Answer: A**



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75. The integral  $\int_{\pi/4}^{3\pi/4} \frac{1}{1 + \cos x} dx$ , is equal to

A. 4

B. -1

C. -2

D. 2

**Answer: D**

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76. If  $f(x) = \frac{e^x}{1 + e^x}$ ,  $I_1 = \int_{f(-a)}^{f(a)} xg\{x(1-x)\}dx$  and

$I_2 = \int_{f(-a)}^{-f(-a)} g\{x(1-x)\}dx$ , where  $g$  is not identify function. Then

the value of  $I_2 / I_1$ , is

A. -1

B.  $1/2$



C. 2

D. 1

**Answer: C**



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77. If  $f(x)=f(a+b-x)$ , then  $\int_a^b x f(x) dx$  is equal to

A.  $(a + b) \int_a^b f(x) dx$

B.  $\frac{1}{2}(a + b) \int_a^b f(x) dx$

C.  $(b - a) \int_a^b f(x) dx$

D.  $\frac{1}{2}(b - a) \int_a^{b-a} f(x) dx$

**Answer: B**



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78. The value of the integral  $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \sqrt{\tan x}} dx$  is

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{6}$

C.  $\frac{\pi}{12}$

D. 0

**Answer: C**



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79.  $I = \int_{\pi/5}^{3\pi/10} \frac{\sin x}{\sin x + \cos x} dx$  is equal to

A.  $(\pi)$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{4}$

D. none of these

**Answer: D**



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80. The value of the integral  $\int_3^6 \frac{\sqrt{x}}{\sqrt{9-x+\sqrt{x}}} dx$  is

A.  $\frac{1}{2}$

B.  $\frac{3}{2}$

C. 2

D. 1

**Answer: B**



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81. Evaluate  $\int_{-4}^{-5} e^{(x+5^2)} dx + 3 \int_{1/3}^{2/3} e^{9\left(x-\frac{2}{3}\right)^2} dx$

A. 1

B. 0

C. -1

D. none of these

**Answer: B**



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**82.** The value of the integral

$\int_0^{400\pi} \sqrt{1 - \cos 2x} dx$ , is  $A\sqrt{2}$ . then find the value of  $A$ .



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**83.** If  $n \in N$ , then  $\int_0^n (x[x]) dx$  is equal to

A.  $n$

B.  $n/2$

C.  $2n$

D. none of these

**Answer: B**

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84. The value of  $\int_0^{100} e^{x - [x]} dx$ , is

A.  $100e$

B.  $100(e-1)$

C.  $100(e+1)$

D. none of these

**Answer: B**

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85. The value of  $\int_0^{32\pi/3} \sqrt{1 + \cos 2x} dx$  is

A.  $\frac{44 + \sqrt{3}}{\sqrt{2}}$

B.  $\frac{44 - \sqrt{3}}{\sqrt{2}}$

C.  $\frac{22 - \sqrt{3}}{\sqrt{2}}$

D.  $\frac{22 + \sqrt{3}}{\sqrt{2}}$

**Answer: B**



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86. The value of  $\int_{[x]}^0 (-x - [x])dx$ , is

A.  $[x]$

B.  $2[x]$

C.  $(1/2)[x]$

D. none of these

**Answer: C**



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87.  $\frac{d}{dx} \int_{x^2}^{x^3} \left( \frac{1}{\log t} dt \right)$  is equal to

A.  $x^2 - x$

B.  $(x^2 - x) \log x$

C.  $\frac{x^2 - x}{\log x}$

D.  $\frac{x - 1^2}{\log x}$

**Answer: C**

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88. If  $g(x) = \int_{\sin x}^{\sin 2x} \sin^{-1}(t) dt$ , then

A.  $g' \left( \frac{\pi}{2} \right) = -2\pi$

B.  $g' \left( -\frac{\pi}{2} \right) = 2\pi$

C.  $g' \left( \frac{\pi}{2} \right) = 0$

$$D. g' \left( -\frac{\pi}{2} \right) = 0$$

**Answer: C::D**



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89. If  $\phi(x) = \int_{1/x}^{\sqrt{x}} \sin(t^2) dt$  then  $\phi'(1)$  is equal to

A.  $\sin 1$

B.  $2 \sin 1$

C.  $(3/2)\sin 1$

D. none of these

**Answer: C**



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90.  $\lim_{x \rightarrow \infty} \frac{\int_0^{2x} te^{t^2} dt}{e^{4x^2}}$  equals



A. 0

B. 2

C.  $\frac{1}{2}$

D.  $\infty$

**Answer: C**

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91. Let  $f: R \rightarrow R$  be a differentiable function having  $f(2)=6, f'(2) = \frac{1}{12}$ .

Then,  $\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{4t^3}{x-2} dt$ , equals

A. 18

B. 12

C. 36

D. 24

**Answer: A**



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92.  $\lim_{\pi/4} \frac{\int_2^{\sec^2 x} f(t) dt}{x^2 - \frac{\pi^2}{16}}$  equals

A.  $\frac{8}{\pi} f(2)$

B.  $\frac{2}{\pi} f(2)$

C.  $\frac{2}{\pi} f\left(\frac{1}{2}\right)$

D.  $4f(2)$

**Answer: A**



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93. If  $\int_{\sin x}^1 t^2 f(t) dt = 1 - \sin x$  for all  $x \in \left[0, \frac{\pi}{2}\right]$ , then  $f\left(\frac{1}{\sqrt{3}}\right) =$

A. 3

B.  $\sqrt{3}$

C.  $\frac{1}{3}$

D. none of these

**Answer: A**

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94. If  $y = \int_0^x f(t) \sin\{k(x - t)\} dt$ , then  $\frac{d^2y}{dx^2} + k^2y =$

A.  $f(x)$

B.  $k f(x)$

C.  $k^2 f(x)$

D. none of these

**Answer: B**

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95. The value of

$$\int_0^{\sin^2} \sin^{-1} \sqrt{t} dt + \int_0^{\cos^2 x} \cos^{-1} \sqrt{t} dt, \text{ is}$$

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{4}$

D. none of these

Answer: C



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96. Let  $f: (0, \infty) \in \mathbb{R}$  be given

$$f(x) = \int_{1/x}^x e^{-\left(t + \frac{1}{t}\right)} \frac{1}{t} dt, \text{ then}$$

A.  $f(x)$  is monotonically increasing on  $[1, \infty]$

B.  $f(x)$  is monotonically increasing on  $(0,1)$

C.  $f(x)$  is monotonocally decreasing on  $(0,1)$

D.  $f(2^x)$  is an odd function of  $x$  on  $\mathbb{R}$

**Answer: A::C::D**

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97. Let  $I = \int_0^1 \frac{\sin x}{\sqrt{x}} dx$  and  $J = \int_0^1 \frac{\cos x}{\sqrt{x}} dx$ .

Then , which one of the following is true?

A.  $I > \frac{2}{3}$  and  $J > 2$

B.  $I < \frac{2}{3}$  and  $J < 2$

C.  $I < \frac{2}{3}$  and  $J > 2$

D.  $I > \frac{2}{3}$  and  $J < 2$

**Answer: B**

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98. The value of the integral  $\int_0^1 e^{x^2} dx$  lies in the interval

- A. (0,1)
- B. (-1,0)
- C. (1, e)
- D. none of these

**Answer: C**



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99. The smallest interval  $[a,b]$  such that

$\int_0^1 \sqrt{1+x^4} dx \in [a, b]$  is given by

- A.  $[1/\sqrt{2}, 1]$
- B.  $[0,1]$
- C.  $[1/2, 1]$
- D.  $[3/4, 1]$

**Answer: A**



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100. If  $I = \int_0^1 \frac{1}{1+x^{\pi/2}} dx$  then

A.  $\ln 2 < 1 < \frac{\pi}{4}$

B.  $I < \ln 2$

C.  $\ln 2 > \frac{\pi}{4}$

D. none of these

**Answer: A**



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101. Let  $f(a) > 0$ , and let  $f(x)$  be a non-decreasing continuous function in

$[a, b]$ . Then,  $\frac{1}{b-a} \int_a^b f(x) dx$  has the

A. maximum value  $f(b)$  and minimum value  $f(a)$

B. maximum value  $f(b)$  and minimum value  $f(a)$

C. maximum value  $f(a)$  and minimum value  $f(b)$

D. none of these

**Answer: A**

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102. If  $I = \sum_{k=1}^{98} \int_k^{k+1} \frac{k+1}{x(x+1)} dx$ , then

A.  $I > \log_e 99$

B.  $I < \log_e 99$

C.  $I < \frac{49}{50}$

D.  $I > \frac{49}{50}$

**Answer: B::D**

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103. Let  $f: \left[\frac{1}{2}, 1\right] \in R$  (the set of all real numbers) be a positive, non-constant and differentiable function such that  $f'(x) < 2f(x)$  and  $f\left(\frac{1}{2}\right) = 1$ . Then the value of  $\int_{1/2}^1 f(x)dx$  lies in the interval

A.  $(2e-1, 2e)$

B.  $(e-1, 2e-1)$

C.  $\left(\frac{e-1}{2}, e-1\right)$

D.  $\left(0, \frac{e-1}{2}\right)$

Answer: D



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104. Let  $f'(x) = \frac{192x^3}{2 + \sin^4 \pi x}$  for all  $x \in R$  with  $f\left(\frac{1}{2}\right) = 0$ . If  $m \leq \int_{1/2}^1 f(x)dx \leq M$ , then the possible values of  $m$  and  $M$  are

A.  $m=13, M=24$

B.  $m = \frac{1}{4}, M = \frac{1}{2}$

C.  $m=-11, M=0$

D.  $m=1, M=12$

**Answer: D**



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**105.** Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a function which satisfies

$$f(x) = \int_0^x f(t) dt. \text{ Then the value of } f(\ln 5), \text{ is}$$

A. 5

B. 0

C. 1

D. -5

**Answer: B**



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106. The least value of the function

$$\phi(x) = \int_{5\pi/4}^x (3 \sin t + 4 \cos t) dt$$

on the interval  $[5\pi/4, 4\pi/3]$ , is

A.  $\sqrt{3} + \frac{3}{2}$

B.  $-2\sqrt{3} + \frac{3}{2} + \frac{1}{\sqrt{2}}$

C.  $\frac{3}{2} + \frac{1}{\sqrt{2}}$

D. none of these

Answer: B



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107.  $\lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{1}{n} e^{r/n}$  is

A.  $e+1$

B. e-1

C. 1-e

D. e

**Answer: B**



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108.  $\lim_{n \rightarrow \infty} \sum_{r=2n+1}^{3n} \frac{n}{r^2 - n^2}$  is equal to

A.  $\ln \sqrt{\frac{2}{3}}$

B.  $\ln \sqrt{\frac{3}{2}}$

C.  $\ln \frac{2}{3}$

D.  $\ln \frac{3}{2}$

**Answer: B**



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109.  $\lim_{n \rightarrow \infty} \frac{1}{2} \sum_{r=+1}^{2n} \frac{r}{\sqrt{n^2 + r^2}}$  equals

A.  $1 + \sqrt{5}$

B.  $-1 + \sqrt{5}$

C.  $-1 + \sqrt{2}$

D.  $1\sqrt{2}$

**Answer: B**

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110.  $\lim_{n \rightarrow \infty} \left\{ \frac{1}{n+1} + \frac{1}{n+2} + \frac{1}{n+3} + \dots + \frac{1}{n+n} \right\}$  is, equal to

A.  $\log_e 3$

B. 0

C.  $\log_e 2$

D. 1

Answer: C



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111.  $\lim_{n \rightarrow \infty} \left\{ \frac{n}{n^2 + 1^2} + \frac{n}{n^2 + 2^2} + \dots + \frac{n}{n^2 + n^2} \right\}$  is equal to

A. 1

B. 0

C.  $\frac{\pi}{4}$

D.  $\frac{\pi}{2}$

Answer: C



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112.  $\lim_{n \rightarrow \infty} \left\{ \frac{1^m + 2^m + 3^m + \dots + n^m}{n^{m+1}} \right\}$  equals

A.  $\frac{1}{m+1}$

B.  $\frac{1}{m+2}$

C.  $\frac{1}{m}$

D. none of these

**Answer: A**



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113.  $\lim_{n \rightarrow \infty} \frac{(n!)^{1/n}}{n}$  equals

A.  $e$

B.  $e^{-1}$

C. 1

D. none of these

**Answer: B**



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114.  $\lim_{n \rightarrow \infty} \left\{ \frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} + \dots + \frac{1}{3n} \right\} =$

A.  $\log 2$

B.  $\log 3$

C.  $\log 5$

D. 0

**Answer: B**



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115.  $\lim_{n \rightarrow \infty} \left\{ \frac{1}{n^2} \sec^2 \frac{1}{n^2} + \frac{2}{n^2} + \sec^2 \frac{4}{n^2} + \dots + \frac{1}{n} \sec^2 1 \right\}$  equals

A.  $\frac{1}{2} \tan 1$

B.  $\tan 1$

C.  $\frac{1}{2} \operatorname{cosec} 1$

D.  $\frac{1}{2} \sec 1$



Answer: A



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116.  $\lim_{n \rightarrow \infty} \left\{ \frac{(n+1)(n+2)(n+3) \dots 3n}{n^{2n}} \right\}^{\frac{1}{n}}$  is equal to

A.  $\frac{18}{e^4}$

B.  $\frac{27}{e^2}$

C.  $\frac{9}{e^2}$

D.  $3 \log 3 - 2$

Answer: C



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117. For  $a \in R - \{-1\}$ , if

$$\lim_{n \rightarrow \infty} \frac{(1^a + 2^a + 3^a + \dots + n^a)}{(n+1)^{a-1} \{(na+1) + (na+2) + \dots + (na+n)\}} = \frac{1}{60}$$

then,  $a =$

A. 5,7

B.  $7, \frac{17}{2}$

C.  $-\frac{15}{2}, -\frac{17}{2}$

D.  $7, \frac{15}{2}$

**Answer: B**



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118. Let  $S_n = \sum_{k=1}^n \frac{n}{n^2 + nk + k^2}$  and  $T_n = \sum_{k=0}^{n-1} \frac{n}{n^2 + nk + k^2}$  for

$n = 1, 2, 3, \dots$ , then

A.  $S_n < \frac{\pi}{3\sqrt{3}}, T_n > \frac{\pi}{3\sqrt{3}}$

B.  $S_n \geq \frac{\pi}{3\sqrt{3}}, T_n < \frac{\pi}{3\sqrt{3}}$

C.  $S_n > \frac{\pi}{3\sqrt{3}}, T_n > \frac{\pi}{3\sqrt{3}}$

D.  $S_n < \frac{\pi}{3\sqrt{3}}, T_n < \frac{\pi}{3\sqrt{3}}$

**Answer: A**



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**119.** The value of  $\int_{-1}^1 x d|x|$ , is,

A. 0

B. 1

C. -1

D. 1/2

**Answer: B**



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**120.** The value of  $\int_0^x d[t]$ , is

A. x

B.  $x^2 / 2$

C.  $-x$

D.  $[x]$

**Answer: D**



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121. The value of  $\int_0^2 x d([x] - x)$ , is

A.  $1/2$

B. 1

C.  $-1$

D. 0

**Answer: B**



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122. The value of the integral  $\int_0^3 (x^2 + 1)d[x]$  is, where  $[*]$  is the greatest integer function

A. 12

B. 15

C. 17

D. 19

**Answer: C**



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## Section I - Solved Mcqs

1.  $\int_0^{10} |x(x - 1)(x - 2)|dx$  is equal to

A. 160.05

B. 1600.5

C. 16.005

D. none of these

**Answer: B**



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2. If  $\int_0^x f(t)dt = x + \int_x^1 tf(t)dt$ , then the value of  $f(1)$ , is

A.  $1/2$

B. 0

C. 1

D.  $-1/2$

**Answer: A**



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3. Let  $f$  be a positive function. Let

$$I_1 = \int_{1-k}^k x f \{ x(1-x) \} dx, I_2 = \int_{1-k}^k f \{ x(1-x) \} dx$$

where  $2k - 1 > 0$ . Then,  $\frac{I_1}{I_2}$  is

A. 2

B.  $k$

C.  $1/2$

D. 1

**Answer: C**



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4. If  $g(x) = \int_0^x \cos^4 t dt$ , then  $g(x + \pi)$  equals

A.  $g(x) + g(\pi)$

B.  $g(x) - g(\pi)$

C.  $g(x)g(\pi)$

D.  $g(x) / g(\pi)$

**Answer: A**



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5. If  $I_n = \int_0^{\pi/4} \tan^n x dx$ ,  $n \in \mathbb{N}$  then  $I_{n+2} + I_n$  equals

A.  $\frac{1}{n}$

B.  $\frac{1}{n-1}$

C.  $\frac{1}{n+1}$

D.  $\frac{1}{n+2}$

**Answer: C**



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6. If  $\Rightarrow I_n = \int_0^{\pi/4} \tan^n x dx$ , then for any positive integer,  $n$ , the value of  $(I_{n+1} - I_{n-1})$  is,

A. 1

B. 2

C.  $\pi/4$

D.  $\pi$

**Answer: A**



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7. The value of  $\int_{-1}^1 \frac{d}{dx} \left( \tan^{-1} \frac{1}{x} \right) dx$  is

A.  $\pi/2$

B.  $-\pi/4$

C.  $-\pi/2$

D. none of these

**Answer: A**



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**8.** The value of the integral

$$\int_{-1}^3 \left( \tan^{-1} \frac{x}{x^2 + 1} + \tan^{-1} \frac{x^2 + 1}{x} \right) dx \text{ is equal to}$$

A.  $\pi$

B.  $2\pi$

C.  $4\pi$

D. none of these

**Answer: B**



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9. If  $I_n = \int_1^e (\log x)^n dx$ , then  $I_n + nI_{n-1}$  is equal to

A.  $1/e$

B.  $e$

C.  $e - 1$

D. none of these

**Answer: B**



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10. If  $I_n = \int_0^1 x^n e^{-x} dx$  for  $n \in \mathbb{N}$  then  $I_n - nI_{n-1} =$

A.  $e$

B.  $1/e$

C.  $-1/e$

D. none of these

**Answer: C**

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11. The value of  $\int_{1/n}^{(an-1)/n} \frac{\sqrt{x}}{\sqrt{a-x} + \sqrt{x}} dx$ , is

A.  $\frac{a}{2}$

B.  $\frac{1}{2n}(na + 2)$

C.  $\frac{na + 2}{2n}$

D. none of these

**Answer: C**

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12. The value of the integral  $\int_0^{\pi/2} \log|\tan x \cot x| dx$  is

A.  $\pi \log 2$

B.  $-\pi \log 2$

C.  $\frac{\pi}{2} \log 2$

D. none of these

**Answer: D**



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13. If  $I_1 = \int_x^1 \frac{1}{1+t^2} dt$  and  $I_2 = \int_1^{1/x} dt$  for  $x > 0$  then,

A.  $I_1 = I_2$

B.  $I_1 > I_2$

C.  $I_2 = I_1$

D. none of these

**Answer: A**



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14. For all values of  $x$ ,  $\int_{1/e}^{\tan x} \frac{t}{1+t^2} dt + \int_{1/e}^{\tan x} \frac{dt}{t(t+t^2)}$  has the value

- A. 0
- B. 1
- C. e
- D. none of these

**Answer: B**

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15. The absolute value of  $\int_{10}^{19} \frac{\cos x}{1+x^8} dx$ , is

- A. less than  $10^{-7}$
- B. more than  $10^{-7}$
- C. less than  $10^{-8}$
- D. none of these

**Answer: A**



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16. If  $f(x)$  is an odd periodic function defined on the interval  $[-T/2, T/2]$ , where

$T$  is the period of  $f(x)$ . Then  $\phi(x) = \int_a^x f(t) dt$ , is

- A. periodic with period  $T$
- B. non-periodic
- C. periodic with period  $2T$
- D. periodic with period  $aT$

**Answer: A**



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17. If  $\int_{\pi/2}^{\theta} \sin x dx = \sin 2\theta$  then the value of  $\theta$  satisfying  $0 < \theta < \pi$ , is

A.  $3\pi/2$

B.  $\pi/6$

C.  $5\pi/6$

D.  $\pi/2$

**Answer: D**



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**18.** If  $f(x)$  is periodic function with period,  $T$ , then

A.  $\int_a^b f(x) dx = \int_a^{b+T} f(x) dx$

B.  $\int_a^b f(x) dx = \int_{a+T}^b f(x) dx$

C.  $\int_a^b f(x) dx = \int_{a+T}^{b+T} f(x) dx$

D.  $\int_a^b f(x) dx = \int_{a+T}^{b+2T} f(x) dx$



**Answer: C**



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19. If  $f(n) = \frac{1}{n} \{(n+1)(n+2)(n+3)\dots(n+n)\}^{1/n}$  then  $\lim_{n \rightarrow \infty} f(n)$

equals

A.  $e$

B.  $1/e$

C.  $2/e$

D.  $4/e$

**Answer: D**



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20. The points of extremum of  $\phi(x) = \int_1^x e^{-t^2/2} (1-t^2) dt$  are

A.  $x = 1, -1$

B.  $x = -1, 2$

C.  $x = 2, 1$

D.  $x = -2, 1$

**Answer: A**

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21.  $\int_{-2}^2 \min(x - [x], -x - [x]) dx$  equals, where  $[x]$  represents greatest integer less than or equal to  $x$ .

A. 2

B. 1

C. 4

D. 0

**Answer: B**



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22. The integral  $\int_0^a \frac{g(x)}{f(x) + f(a-x)} dx$  vanishes, if

- A.  $g(x)$  is odd
- B.  $f(x) = f(a-x)$
- C.  $g(x) = -g(a-x)$
- D.  $f(a-x)g = g(x)$

Answer: C



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23. If  $\frac{1}{\sqrt{a}} \int_1^a \left( \frac{3}{2} \sqrt{x} + 1 - \frac{1}{\sqrt{x}} \right) dx < 4$  then 'a' may take values :

- A. 0
- B. 4

C. 9

D. none of these

**Answer: D**



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24. The expression  $\frac{\int_0^n [x] dx}{\int_0^n \{x\} dx}$  where  $[x]$  and  $\{x\}$  are integral and fractional parts of  $x$  and  $n \in \mathbb{N}$  is equal to

A.  $\frac{1}{n-1}$

B.  $\frac{1}{n}$

C.  $n$

D.  $n-1$

**Answer: D**



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25. If  $f(x) = \text{Min} \{|x - 1|, |x|, |x + 1|\}$  then  $\int_{-1}^1 f(x) dx$  equals

- A. 1
- B. 2
- C. 0
- D. none of these

**Answer: D**



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26. The value of  $\int_0^{100} [\tan^{-1} x] dx$  is

- A. 100
- B.  $100 - \tan^{-1} 1$
- C.  $100 - \tan 1$
- D. none of these

**Answer: C**



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27.  $\int_{-1}^{10} \text{sgn}(x - [x]) dx$  equals

A. 10

B. 11

C. 9

D.  $11/2$

**Answer: B**



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28. If  $n \in \mathbb{N}$ , then  $\int_{-n}^n (-1)^{[x]} dx$  equals

A.  $2n$

B.  $n$

C.  $n^2$

D. none of these

**Answer: D**



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29. The value of  $\therefore \int_0^{[x]} \frac{2^x}{2^{[x]}} dx$  is

A.  $\log 2$

B.  $\frac{[x]}{\log 2}$

C.  $\frac{1}{2} \frac{[x]}{\log 2}$

D. none of these

**Answer: B**



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30. If  $f(x) \Rightarrow \int_{\sin \theta}^{\operatorname{cosec} \theta} f(x) dx$  equals

A.  $\sin \theta + \operatorname{cosec} \theta$

B.  $\sin^2 \theta$

C.  $\operatorname{cosec}^2 \theta$

D. none of these

Answer: D



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31. If  $f(x) = \begin{cases} e^{\cos x} \sin x & \text{for } |x| \leq 2 \\ 2 & \text{otherwise} \end{cases}$  then  $\int_{-2}^3 f(x) dx =$

A. 0

B. 1

C. 2

D. 3



Answer: C



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32. The value of the integral  $\int_{e^{-1}}^{e^2} \left| \frac{\log_e x}{x} \right| dx$  is

A.  $\frac{3}{2}$

B.  $\frac{5}{2}$

C. 3

D. 5

Answer: B



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33. Let  $g(x) = \int_0^x f(t)dt$ , where  $f$  is such that  $\frac{1}{2} \leq f(t) \leq 1$  for  $t \in [0, 1]$  and  $0 \leq f(t) \leq \frac{1}{2}$  for  $t \in [1, 2]$  then,  $g(2)$  satisfies the inequality,

A.  $-\frac{3}{2} \leq g(2) < \frac{1}{2}$

B.  $0 \leq g(2) \leq 2$

C.  $\frac{3}{2} \leq g(2) \leq \frac{5}{2}$

D.  $2 < g(2) < 4$

**Answer: B**



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34. Let  $f: (0, \infty) \in R$  and  $F(x) = \int_0^x f(t)dt$ . If  $F(x^2) = x^2(1+x)$

then  $f(4)$  equals

A.  $5/4$

B. 7

C. 4

D. 2

**Answer: C**



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35. The integral  $\int_{-1/2}^{1/2} \left\{ [x] + \epsilon \left( \frac{1+x}{1-x} \right) \right\} dx$  equals

A.  $-\frac{1}{2}$

B. 0

C. 1

D.  $2 \ln\left(\frac{1}{2}\right)$

Answer: A



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36. Let  $T > 0$  be a fixed real number. Suppose  $f$  is a continuous function such that  $f(x + T) = f(x)$  for all  $x \in R$ . If  $I = \int_0^T f(x) dx$ , then the value of  $\int_3^{3+3T} f(2x) dx$  is

A.  $\frac{3}{2}I$

B. 2I

C. 3I

D. 6I

**Answer: C**



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37. Let  $f(x) = \int_1^x \sqrt{2-t^2} dt$ . Then the real roots of the equation  $x^2 - f'(x) = 0$  are

A.  $\pm 1$

B.  $\pm \frac{1}{\sqrt{2}}$

C.  $\pm \frac{1}{2}$

D. 0 and 1

**Answer: A**



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38. If  $f\left(\frac{1}{x}\right) + x^2 f(x) = 0$ ,  $x > 0$  and  $I = \int_{1/x}^x f(t) dt$ ,  $\frac{1}{2} \leq x \leq 2x$ ,

then I is equal to

A.  $f(2) - f\left(\frac{1}{2}\right)$

B.  $f\left(\frac{1}{2}\right) - f(2)$

C. 0

D. none of these

**Answer: C**



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39. If  $\left| \int_a^b f(x) dx \right| = \int_a^b |f(x)| dx$ ,  $a < b$ , then  $f(x) = 0$  has

A. exactly one root in (a,b)

B. at least one root in (a,b)

C. no root in (a,b)

D. none of these

**Answer: C**



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**40.** Let  $f(x)$  be an odd continuous function which is periodic with period 2.

if  $g(x) = \int_0^x f(t) dt$ , then

- A.  $g(x)$  is an odd function
- B.  $g(n) = 0$  for all  $n \in \mathbb{N}$
- C.  $g(2n) = 0$  for all  $n \in \mathbb{N}$
- D.  $g(x)$  is non periodic

**Answer: C**



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41. All the values of 'a' for which  $\int_1^2 \{a^2 + (4 - 4a)x + 4x^3\} dx \leq 12$  are given by

A.  $a=3$

B.  $a \leq 4$

C.  $0 \leq a \leq 3$

D. none of these

**Answer: A**



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42. Let  $f(x)$  be a function defined by

$$f(x) = \int_0^x t(t^2 - 3t + 2) dt, 1 \leq x \leq 3.$$

Then, the range of  $f(x)$  is

A.  $[0,2]$

B.  $[-1/4,4]$

C.  $[-1/4, 2]$

D. none of these

**Answer: C**



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43. If  $\int_0^x \{t\} dt = \int_0^{\{x\}} t dt$  (where  $x > 0 \notin \mathbb{Z}$  and  $\{ \cdot \}$

represents fractional part function), then

A.  $x \in (0, 1)$

B.  $[x] = 1$

C.  $x \in (1, 6) - I$

D. none of these

**Answer: A**



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44. Let  $f(x) = \max . \{x + |x|, x - [x]\}$  , where  $[x]$  denotes the greatest integer less than or equal to  $x$ , then  $\int_{-2}^2 f(x)$  is equal to

A. 3

B. 5

C. 1

D. none of these

**Answer: B**



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45.  $\Rightarrow \int_0^{\infty} \left[ \frac{2}{e^x} \right] dx$  (where  $[*]$  denotes the greatest integer function) equals

A.  $\log_e 2$

B.  $e^2$

C. 0

D.  $2/e$

**Answer: A**



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46. If  $\Rightarrow \int_0^1 \frac{e^{-t}}{t+1} dt = a$ , then  $\int_{b-1}^b \frac{e^{-1}}{t-b-1} dt$  is equal to

A.  $ae^{-b}$

B.  $-ae^{-b}$

C.  $be^b$

D. none of these

**Answer: B**



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47. If  $\Rightarrow \int_{-1}^{-4} f(x)dx = 4$  and  $\int_2^{-4} (3 - f(x))dx = 7$ , then the value of  $\Rightarrow \int_{-2}^1 f(-x)dx$  is

A. 2

B. -3

C. 5

D. none of these

**Answer: D**



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48. For  $x \in R$  and  $a$  continuous function  $f(x)$ , let

$I_1 \int_{\sin^2 t}^{1 + \cos^2 t} x f\{x(2 - x)\}dx$  and  $I_2 \int_{\sin^2 t}^{1 + \cos^2 t} f(x(2 - x))dx$ . Then,  $\frac{I_1}{I_2} =$

A. 0

B. 1

C. 2

D. 3

**Answer: B**



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49.  $\int_1^4 \log_e [x] dx$  equals

A.  $\log_e 6$

B.  $\log_e 3$

C.  $\log_e 2$

D. none of these

**Answer: A**



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50. If  $[*]$  denotes the greatest integer function then the value of the integral  $\int_{-\pi/2}^{\pi/2} \left( \left[ \frac{x}{\pi} \right] + 0.5 \right) dx$ , is

- A.  $\pi$
- B.  $\pi/2$
- C. 0
- D.  $-\pi/2$

**Answer: C**



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51. The value of  $\int_0^{100\pi} \sum_{r=1}^{10} \tan rx dx$  is equal to

- A.  $100\pi$
- B.  $-100\pi$
- C. 1

D. none of these

**Answer: D**



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52.

If

$$I_1 = \int_0^{\pi/2} \cos(\sin x) dx, I_2 = \int_0^{\pi/2} \sin(\cos x) dx \text{ and } I_3 = \int_0^{\pi/2} \cos x dx$$

then

A.  $I_1 > I_3 > I_2$

B.  $I_3 > I_1 > I_2$

C.  $I_1 > I_2 > I_3$

D.  $I_3 > I_2 > I_1$

**Answer: A**



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53. For any  $n \in \mathbb{N}$ , the value of the integral  $\int_0^\pi \frac{\sin 2nx}{\sin x} dx$  is,

A.  $\pi$

B.  $2\pi$

C.  $-\pi$

D. none of these

**Answer: D**



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54. For any  $n \in \mathbb{N}$ ,  $\int_0^\pi \frac{\sin^2 nx}{\sin^2 x} dx$  is equal to

A.  $\pi$

B.  $n\pi$

C. 0

D. none of these

**Answer: B**



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55. For any  $n \in N$ ,  $\int_0^\pi \frac{\sin(2n+1)x}{\sin x} dx$  is equal to

A.  $\pi$

B. 0

C.  $n\pi$

D.  $(2n+1)\pi$

**Answer: A**



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56. If  $I_n \int_{-\pi}^\pi \frac{\sin nx}{(1+\pi^x)\sin x} dx$ ,  $n = 0, 1, 2, \dots$  then which one of the following is not true?



A.  $I_n = I_{n+2}$

B.  $\sum_{m=1}^{10} I_{2m+1} = 10\pi$

C.  $\sum_{m=1}^{10} I_{2m} = 0$

D.  $I_n = I_{n+1}$

**Answer: D**

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57. If  $I_n = \int_0^{\pi/4} \tan^n x dx$ , then  $\frac{1}{I_2 + I_4}, \frac{1}{I_3 + I_5}, \frac{1}{I_4 + I_6}, \dots$  form\

A. an A.P.

B. a G.P.

C. a H.P.

D. none of these

**Answer: A**



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58. Let  $f(x)$  be a function defined on  $R$  satisfyin  $f(x) = f(1 - x)$  for all

$x \in R$ . Then  $\int_{-1/2}^{1/2} f\left(x + \frac{1}{2}\right) \sin x dx$  equals

A.  $\int_{-1/2}^{1/2} f\left(x + \frac{1}{2}\right) \sin x dx$

B.  $2 \int_{-1/2}^{1/2} f\left(x + \frac{1}{2}\right) \sin x dx$

C.  $f(x) \sin dx dx$

D. none of these

Answer: D



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59. The vlaue of  $\frac{(5050) \int_0^1 (1 - x^{50})^{100} dx}{\int_0^1 (1 - x^{50})^{100} dx}$ , is

A. 5049

B. 5051

C. 5050

D. none of these

**Answer: B**



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**60.** If  $f$  and  $g$  are continuous functions on  $[0, \pi]$  satisfying  $f(x) + f(\pi - x) = 1 = g(x) + g(\pi - x)$  then  $\int_0^\pi \{f(x) + g(x)\} dx$  is equal to

A.  $\pi$

B.  $2\pi$

C.  $\frac{\pi}{2}$

D.  $\frac{3\pi}{2}$

**Answer: A**

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**61.** If  $f(x)$  and  $g(x)$  are two continuous functions defined on  $[-a, a]$  then the

the value of  $\int_{-a}^a \{f(x)f(-x)\}\{g(x) - g(-x)\}dx$  is,

A.  $2a$

B.  $f(a)g(a)$

C.  $a$

D. none of these

**Answer: D**

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**62.** Let  $f(x)$  be a continuous function defined on  $[0, a]$  such that

$f(a-x) = f(x)$  for all  $x \in [0, a]$ . If  $\int_0^{a/2} f(x)dx = \alpha$ , then

$\int_0^a f(x) dx$  is equal to

- A.  $\alpha$
- B.  $2\alpha$
- C. 0
- D. none of these

**Answer: B**



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63. The value of the integral  $\int_0^{a/2} \sin 2nx \cot x dx$ , where  $n$  is a positive integer, is

- A.  $\frac{\pi}{2}$
- B.  $-\pi$
- C.  $\pi$
- D. none of these

**Answer: A**



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64. The value of the integral  $\Rightarrow \int_1^{e^6} \left[ \frac{\log x}{3} \right] dx$ , where  $[*]$  denotes the greatest integral function, is

A. 0

B.  $e^{6-e^3}$

C.  $e^6 + e^3$

D.  $e^3 - e^6$

**Answer: B**



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65. For any natural number  $n$ , the value of  $\Rightarrow \int_0^{n^2} [\sqrt{x}] dx$ , is

A.  $\frac{n(n+1)(4n+1)}{6}$

B.  $\frac{n(n-1)(4n+1)}{6}$

C.  $\frac{n(n-1)(4n-1)}{6}$

D. none of these

**Answer: B**

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66. The value of the integral  $\int_a^{a+\pi/2} (|\sin x| + |\cos x|) dx$  is

A.  $a\pi$

B.  $2a\pi$

C.  $\frac{a\pi}{2}$

D. independent of  $a$

**Answer: D**

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67. If  $\Rightarrow I_n = \int_a^{a+\pi/2} \frac{\cos^2 nx}{\sin x} dx$ , then  $I_2 - I_1, I_3 - I_2, I_4 - I_3$  are in

A. G.P.

B. A.P.

C. H.P.

D. none of these

**Answer: C**



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68. Let  $f(x)$  be a polynomial of degree 2 satisfying

$f(0) = 1, f(1) = -2$  and  $f''(0) = 6$ , then  $\int_{-1}^2 f(x)$  is equal to

A. 6

B. 2



C. 9

D. none of these

**Answer: C**



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69. The value of  $\int_{-2}^2 \frac{\sin^2 x}{\left[\frac{x}{\pi}\right] + \frac{1}{2}} dx$  where  $[*]$  denotes the greatest integer function, is

A. 1

B. 2

C.  $4 - \sin 4$

D. none of these

**Answer: B**



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70. If  $\int_0^x f(t)dt = x + \int_x^1 tf(t)dt$ , then the value of  $f(1)$ , is

A.  $1/2$

B. 0

C. 1

D.  $-1/2$

**Answer: A**



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71. If  $f(x) = \int_0^{\sin x} \cos^{-1} t dt + \int_0^{\cos x} \sin^{-1} t dt$ ,  $0 < x < \frac{\pi}{2}$  then

$f(\pi/4)$  is equal to

A.  $\frac{\pi}{\sqrt{2}}$

B.  $1 + \frac{\pi}{2\sqrt{2}}$

C. 1

D. none of these

**Answer: B**

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72. Let  $f(x)$  be a continuous function such that

$$\int_n^{n+1} f(x) dx = n^3, n \in \mathbb{Z}. \text{ Then the value of the integral } \int_{-3}^3 f(x) dx,$$

is

A. 9

B.  $-27$

C.  $-9$

D. none of these

**Answer: B**

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73. Let  $f(x) = \frac{e^x + 1}{e^{-x} - 1}$  and  $\int_0^1 x^3 \frac{e^x + 1}{e^x - 1} dx = \alpha$  then,  $\int_{-1}^1 \int t^3 f(t) dt$

is equal to

A. 0

B.  $\alpha$

C.  $2\alpha$

D. none of these

**Answer: C**



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74. If  $\int_0^1 x e^{x^2} dx = \alpha \int_0^1 e^{x^2} dx$ , then

A.  $\alpha \in (0, 1)$

B.  $(1, 2)$

C.  $(-\infty, 0)$

D.  $(0, \infty)$

**Answer: A**

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75. If  $I = \int_0^1 (1 + e^{-x^2}) dx$  then, s

A.  $I = \in (1, 2)$

B.  $I \in (0, 1)$

C.  $I \in \left(1 + \frac{1}{e}, 2\right]$

D. none of these

**Answer: C**

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76. If  $I = \int_0^1 \frac{x}{8 + x^3} dx$  then the smallest interval is which I less is

A.  $(0, 1/8)$

B. (0,1/9)

C. (0,1/10)

D. (0,1/7)

**Answer: B**



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77. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a continuous function given by

$$f(x + y) = f(x) + f(y) \text{ for all } x, y \in \mathbb{R}.$$

If  $\int_0^2 f(x) dx = \alpha$ , then  $\int_2^4 f(x) dx$  is equal to

A.  $2\alpha$

B.  $\alpha$

C. 0

D. none of these

**Answer: C**



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78. Let  $f$  be an integrable function defined on  $[0, a]$  if

$$I_1 = \int_{\pi/2}^{\pi} \cos \theta f(\sin \theta \cos^2 \theta) d\theta \quad \text{and} \quad I_2 = \int_0^{\pi/2} \sin 2\theta f(\sin \theta \cos^2 \theta) d\theta$$

then

A.  $I_1 = I_2$

B.  $I_1 = -I_2$

C.  $I_1 = 2I_2$

D.  $I_1 = 2I_2$

**Answer: A**



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79.  $\lim_{x \rightarrow 0} \frac{2 \int_0^{\cos x} \cos^{-1} t dt}{2x - \sin 2x}$  is equal to

A. 0

B.  $1/2$

C.  $-1/2$

D.  $2/3$

**Answer: C**



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80. If  $I_1 = \int_1^{\sin \theta} \frac{x}{1+x^2} dx$  and  $I_2 = \int_1^{\operatorname{cosec} \theta} \frac{1}{x(x^2+1)} dx$  then the value of

$$\begin{vmatrix} I_1 & I_1^2 & I_2 \\ e^{I_1+I_2} & I_2^2 & -1 \\ 1 & I_1^2 + I_2^2 & -1 \end{vmatrix}, \text{ is}$$

A.  $\sin \theta$

B.  $\operatorname{cosec} \theta$

C. 0

D. 1

**Answer: C**





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81. If  $f(x) = \int_1^x \frac{\log t}{1+t} dt$  then  $f(x) + f\left(\frac{1}{x}\right)$  is equal to

- A.  $(\log_e x)^2$
- B.  $\frac{2}{3} \log_e x$
- C.  $\frac{1}{2} \log_e x$
- D.  $\frac{1}{2} (\log_e x)^2$

Answer: D



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82. Let  $F(x) = f(x) + f\left(\frac{1}{x}\right)$ , where  $f(x) = \int_1^x \frac{\log t}{1+t} dt$ . Then  $F(e)$  equals

- A. 1
- B. 2

C.  $1/2$

D. 0

**Answer: C**



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83. If  $\int_0^x \frac{bt \cos 4t - a \sin 4t}{t^2} dt = \frac{a \sin 4x}{x}$  for all  $x \neq 0$ , then  $a$  and  $b$  are given by

A.  $a = \frac{1}{4}, b = 1$

B.  $a = 2, b = 2$

C.  $a = -1, b = 4$

D.  $a = 2, b = 4$

**Answer: A**



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84. Let  $f: R \in R$  be given by

$$f(x) = \begin{cases} |x - [x]| & \text{when } [x] \text{ is odd} \\ |x - [x] - 1| & \text{when } [x] \text{ is even} \end{cases} \quad \text{where } [*] \text{ denotes the greatest}$$

integer function, then  $\int_{-2}^4 f(x) dx$  is equal to

A.  $\frac{5}{2}$

B.  $\frac{3}{2}$

C. 5

D. 3

Answer: D



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85. If  $f(x) = \sin x + \cos x$  and  $g(x) = \begin{cases} \frac{|x|}{x} & , x \neq 0 \\ 2 & , x = 0 \end{cases}$  then the value

of  $\int_{-\pi/4}^{2\pi} g(x) f(x) dx$  is equal to

A.  $3\pi/4$

B.  $\pi/4$

C.  $\pi$

D. none of these

**Answer: B**



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86. If  $x \in \left[ (4n + 1)\frac{\pi}{2}, (4n + 3)\frac{\pi}{2} \right]$  and  $n \in N$ , then the value of

$\int_0^x [\cos t] dt$ , is

A.  $(2n - 1)\frac{\pi}{2} - x$

B.  $(2n - 1)\frac{\pi}{\pi} / (2) - x$

C.  $(2n + 1)\frac{\pi}{2} - x$

D.  $(2n + 1)\frac{\pi}{2} + x$

**Answer: C**



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87. If  $f: R \in R$  is continuous and differentiable function such that

$$\int_{-1}^x f(t)dt + f'''(3) \int_x^1 dt = \int_1^x t^3 dt - f'(1) \int_0^x t^2 dt + f'(2) \int_x^3 r dt,$$

then the value of  $f'(4)$ , is

A.  $48 - 8f'(1) + f'(2)$

B.  $48 - 8f'(1) - f''(2)$

C.  $48 + 8f'(1) - f'(2)$

D. none of these

**Answer: B**



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88. Let  $I_1 = \int_0^1 \frac{e^x}{1+x} dx$  and  $I_2 = \int_0^1 \frac{x^2}{e^{x^3}(2-x^3)} dx$ .

Then,  $\frac{I_1}{I_2}$  is equal to

A.  $\frac{3}{e}$

B.  $\frac{e}{3}$

C.  $3e$

D.  $\frac{1}{3e}$

**Answer: C**



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89. Let  $f(x) = \begin{cases} 1 - |x|, & |x| \leq 1 \\ 0, & |x| > 1 \end{cases}$  and,  $g(x) = f(x-1) + f(x+1)$  for all  $x \in \mathbb{R}$ .

Then, the value of  $\int_{-3}^3 g(x) dx$ , is

A. 2

B. 3

C. 4

D. 5

**Answer: A**



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90.

If

 $f(x)$ 

$$= \frac{x-1}{x+1}, f^2(x) = f(f(x)), \dots, \dots, f^{k+1}(x) = f(f^k(x))$$

,  $k=1,2,3,\dots$  and  $g(x) = f^{1998}(x)$  then  $\int_{1/e}^1 g(x) dx$  is equal to

A. 0

B. 1

C. -1

D. e

**Answer: C**
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91. If  $f: R \rightarrow R$  be such that

$$f(x) = \sqrt{\sin(\cos x)} + \ln(-2 \cos^2 x + 3 \cos x - 1), \quad \text{then}$$

$\int_{x_1}^{x_2} \left[ \cos x - \frac{1}{2} \right] dx$  is equal to, where  $x_1, x_2 \in D$  and  $[.]$  denotes the

greatest integer function,

A. 0

B.  $\frac{1}{2}(x_2 - x_1)$

C.  $x_1 - x_2$

D.  $\frac{1}{2}(x_1 - x_2)$

**Answer: A**



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92. If  $\int_e^x tf(t)dt = \sin x - x \cos x - \frac{x^2}{2}$  for all  $x \in \mathbb{R} - \{0\}$ , then the value of  $f\left(\frac{\pi}{6}\right)$  will be equal to

A. 0

B. 1

C.  $-\frac{1}{2}$

D. none of these

**Answer: C**





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93. If  $f(x) = \int_0^x \{f(t)\}^{-1} dt$ , and  $\int_0^1 \{f(t)\}^{-1} dt = \sqrt{2}$ , then  $f(x) =$

A.  $\sqrt{2x}$

B.  $\sqrt{2 \log_e x}$

C.  $\sqrt{3x - 1}$

D. none of these

Answer: A



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94. If  $f(x)$  is differentiable and  $\int_0^{t^2} x f(x) dx = \frac{2}{5} t^5$ , then  $ff\left(\frac{4}{25}\right)$  equals

A.  $2/5$

B.  $-5/2$

C. 1

D.  $5/2$

**Answer: A**



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95. The value of  $\int_{-2}^3 |1 - x^2| dx$  is

A.  $\frac{1}{3}$

B.  $\frac{14}{3}$

C.  $\frac{7}{3}$

D.  $(28)/(3)$

**Answer: D**



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96.  $\int_0^{\pi} x f(\sin x) dx$  is equal to

A.  $\pi \int_0^{\pi} f(\cos x) dx$

B.  $\pi \int_0^{\pi} f(\sin x) dx$

C.  $\frac{\pi}{2} \int_0^{\pi/2} f(\sin x) dx$

D.  $\pi \int_0^{\pi/2} f(\cos x) dx$

**Answer: D**



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97. If  $f(x) \frac{e^x}{1+e^x}$ ,  $I_1 = \int_{f(-a)}^{f(a)} xg\{x(1-x)\}dx$  and  $I_2 = \int_{f(-a)}^{f(a)} g\{x(1-x)\}dx$ , then the value of  $\frac{I_2}{I_1}$  is

A. 1

B. -3

C. -1

D. 2

**Answer: D**



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98.  $\int_{-2}^2 |[x]| dx =$

A. 1

B. 2

C. 3

D. 4

**Answer: D**



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99. The value

$$\int_{-2}^2 (-2) \left\{ p \ln\left(\frac{1+x}{1-x}\right) + q \ln\left(\frac{1-x}{1+x}\right) - 2 + r \right\} dx$$

depends on the value of

- A. p
- B. q
- C. r
- D. p and q

**Answer: C**

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100.  $7 \left( \int_0^1 \frac{x^4(1-x)^4 dx}{1+x^2} + \pi \right)$  is equal to

- A.  $\frac{22}{7} - \pi$
- B.  $\frac{2}{105}$

C. 0

D.  $\frac{71}{15} - \frac{3\pi}{2}$

**Answer: A**



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101. The value of  $\lim_{x \rightarrow 0} \frac{1}{x^3} \int_0^x \frac{\ln(1+t)}{t^4+4} dt$  is

A. 0

B. 1/12

C. 1/24

D. 1/24

**Answer: B**



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102. Let  $f$  be the function defined on  $[-\pi, \pi]$  given by  $f(0) = 9$  and

$$f(x) = \frac{\sin\left(\frac{9x}{2}\right)}{\sin\left(\frac{x}{2}\right)} \text{ for } x \neq 0. \text{ The value of } \frac{2}{\pi} \int_{-\pi}^{\pi} f(x) dx \text{ is (asked as}$$

Match the following question)

A. 0

B. 2

C. 4

D. 6

**Answer: C**



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103. Let  $f$  be a real-valued function defined on the interval  $(-1, 1)$  such that

$$e^{-x} f(x) 2 + \int_0^x \sqrt{t^4 + 1} dt \text{ for all } x \in (-1, 1) \text{ and let } f^{-1} \text{ be the}$$

inverse function of  $f$ . Then,  $(f^{-1})'(2)$  is equal to

A. 1

B.  $1/3$

C.  $1/2$

D.  $1/e$

**Answer: B**



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**104.** For any real number  $x$ , let  $[x]$  denote the largest integer less than or equal to  $x$ . Let  $f$  be a real valued, function defined on the interval  $[-10,10]$  by

$$f(x) = \begin{cases} x - [x], & \text{if } [x] \text{ is odd} \\ 1 + [x] - x, & \text{if } [x] \text{ is even} \end{cases}$$

Then the value of  $\frac{\pi^2}{10} \int_{-10}^{10} f(x) \cos \pi x dx$ , is

A. 3

B. 4

C. 6



**Answer: B****Watch Video Solution**

**105.** Let  $f$  be a real-valued function defined on the interval  $(0, \infty)$  by  $f(x) = \ln x + \int_0^x \sqrt{1 + \sin t} dt$ . Then which of the following statement(s) is(are) true?

- A.  $f''(x)$  exists for all  $(x \in (0, \infty))$
- B.  $f'(x)$  exists for all  $x \in (0, \infty)$  and  $f'(x)$  is continuous on  $(0, \infty)$  but not differentiable on  $(0, \infty)$
- C. there exists  $\alpha > 1$  such that  $|f'(x)| < f(x)$  for all  $x \in (\alpha, \infty)$
- D. there exists  $\beta > 0$  such that  $|f'(x)| + f'(x) \leq \beta$  for all  $x \in (0, \infty)$

**Answer: C**

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106. Let  $p(x)$  be a function defined on  $\mathbb{R}$  such that  $p'(x)=p'$  for all  $x \in [0, 1]$ ,  $p(0) = 1$  and  $p(1)=41$ . Then,  $\int_0^1 p(x)dx$  equals

A. 41

B. 42

C.  $\sqrt{41}$

D. 21

**Answer: D**

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107. If  $\int_a^b \{f(x) - 3x\}dx = a^2 - b^2$ , then the value of  $f\left(\frac{\pi}{6}\right)$ , is

A.  $\frac{\pi}{6}$

B.  $\frac{2\pi}{3}$

C.  $\frac{\pi}{2}$

D.  $\frac{\pi}{2}$

**Answer: A**

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108. The value of  $\frac{\pi^2}{\ln 3} \int_{7/6}^{5/6} \sec(\pi x) dx$  is

A.  $\frac{2\pi}{3}$

B.  $\frac{\pi}{2}$

C.  $\pi$

D.  $\frac{4\pi}{3}$

**Answer: C**

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109. The value of the integral

$$\int_{-\pi/2}^{\pi/2} \left\{ x^2 + \log\left(\frac{\pi+x}{\pi-x}\right) \right\} \cos x dx \text{ is}$$

A. 0

B.  $\frac{\pi^2}{2} - 4$

C.  $\frac{\pi^2}{2} - 6$

D.  $\frac{\pi^2}{2}$

Answer: B



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110. Let  $f: (0, 1) \rightarrow (0, 1)$  be a differentiable function such that  $f(x) \neq 0$

for all  $x \in (0, 1)$  and  $f\left(\frac{1}{2}\right) = \frac{\sqrt{3}}{2}$ . Suppose for all  $x$ ,

$$\lim_{x \rightarrow x} \frac{\int_0^1 \sqrt{1(f(s))^2} dx \int_0^x \sqrt{1(f(s))^2} ds}{f(t) - f(x)} = f(x)$$

Then, the value of  $f\left(\frac{1}{4}\right)$  belongs to

A.  $\{(\sqrt{7}, \sqrt{15})\}$

B.  $\left\{\frac{\sqrt{7}}{2}, \frac{\sqrt{15}}{2}\right\}$

C.  $\left\{\frac{\sqrt{7}}{3}, \frac{\sqrt{15}}{3}\right\}$

D.  $\left\{\frac{\sqrt{7}}{4}, \frac{\sqrt{15}}{4}\right\}$

**Answer: D**



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111. The value of the integral  $\int_0^2 \frac{\log(x^2 + 2)}{(x + 2)^2} dx$  is

A.  $\frac{\sqrt{2}}{3} \tan^{-1} \sqrt{2} + \frac{5}{12} \log 2 - \frac{1}{4} \log 3$

B.  $\frac{\sqrt{2}}{3} \tan^{-1} \sqrt{2} - \frac{5}{12} \log 2 - \frac{1}{12} \log 3$

C.  $\frac{\sqrt{2}}{3} \tan^{-1} \sqrt{2} + \frac{5}{12} \log 2 + \frac{1}{4} \log 3$

D.  $\frac{\sqrt{2}}{3} \tan^{-1} \sqrt{2} - \frac{5}{12} \log 2 + \frac{1}{12} \log 3$

**Answer: D**



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112. The integral  $\int_{\pi/4}^{\pi/2} (2 \operatorname{cosec} x)^{17} dx$  is equal to

A.  $\int_0^{\log(1+\sqrt{2})} 2(e^u + e^{-u})^{16} du$

B.  $\int_0^{\log(1+\sqrt{2})} (e^u + e^{-u})^{17} du$

C.  $\int_0^{\log(1+\sqrt{2})} (e^u - e^{-u})^{17} du$

D.  $\int_0^{\log(1+\sqrt{2})} 2(e^u - e^{-u})^{16} du$

**Answer: A**

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113. Let  $f: [0, 2] \in \mathbb{R}$  be a function which is continuous on  $[0, 2]$  and is differentiable on  $(0, 2)$  with  $f(0)=1$ . Let  $F(x) = \int_0^{x^2} f(\sqrt{t}) dt$  for  $x \in [0, 2]$

If  $F'(x)=f'(x)$  for all  $x$  in  $(0,2)$ , then  $F(2)$  equals

A.  $e^2 - 1$

B.  $e^4 - 1$

C.  $e - 1$

D.  $e^4$

**Answer: B**



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114. Given that for each  $a \in (0, 1)$   $\lim_{h \rightarrow 0^+} \int_h^{1-h} t^{-a}(1-t)^{a-1} dt$  exists. If this limit be  $g(a)$ , then the value  $g\left(\frac{1}{2}\right)$ , is

A.  $\pi$

B.  $2\pi$

C.  $\frac{\pi}{2}$

D.  $\frac{\pi}{4}$

**Answer: A**



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115. Given that for each  $a \in (0, 1)$   $\lim_{h \rightarrow 0} \int_h^{-h} t^{-a}(1-t)^{a-1} dt$  exists and is equal to  $g(a)$ . If  $g(a)$  is differentiable in  $(0, 1)$ , then the value of  $g'(1/2)$ , is

A.  $\pi/2$

B.  $\pi$

C.  $-\pi/2$

D. 0

**Answer: D**



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116. The options (s) with the values of a and L that satisfy the following equation is (are)

$$\frac{\int_0^{4\pi} e^t (\sin^6 at + \cos^4 at) dt}{\int_0^\pi e^t (\sin^6 at + \cos^4 at) dt} = L?$$

A.  $a = 2, L = \frac{e^{4\pi} - 1}{e^\pi - 1}$

B.  $a = 2, L = \frac{e^{4\pi} + 1}{e^\pi + 1}$

C.  $a = 4, L = \frac{e^{4\pi} - 1}{e^\pi - 1}$

D.  $a = 4, L = \frac{e^{4\pi} + 1}{e^\pi + 1}$

Answer: A:C



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117. Let  $f: R \rightarrow R$  be a continuous odd function, which vanishes exactly at one point and  $f(1) = \frac{1}{2}$ . Suppose that  $F(x) = \int_{-1}^x f(t) dt$  for all  $x \in [-1, 2]$  and  $G(x) = \int_{-1}^x t|f(f(t))| dt$  for all  $x \in [-1, 2]$ . If  $\lim_{x \rightarrow x} \frac{F(x)}{G(x)} = \frac{1}{14}$ , then the value of  $f\left(\frac{1}{2}\right)$ , is

A. 7

B. 8

C. 9

D. 6

**Answer: A**



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**118.** Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a thrice differentiable function. Suppose that  $F(1)=0, F(3)=-4$  and  $F'(x) < 0$  for all  $x$  in  $(1/2, 3)$ . Let  $f(x) = xF(x)$  or all  $x$  in  $\mathbb{R}$ . If  $\int_1^3 x^2 F'(x) dx = -12$  and  $\int_1^3 F''(x) dx = 40$ , then which of the following is (are) correct?

A.  $9f'(3) + f'(1) - 32 = 0$

B.  $\int_1^3 f(x) dx = 12$

C.  $9f'(3) - f'(1) + 32 = 0$

$$D. \int_1^3 f(x) dx = -12$$

**Answer: C::D**

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**119.** Let  $f: (0, \infty) \rightarrow \mathbb{R}$  be continuous function such that

$F(x) = \int_0^x t f(t) dt$ . If  $F(x^2) = x^4 + x^5$ , then  $\sum_{r=1}^{12} f(r^2)$  is equal to

A. 216

B. 219

C. 222

D. 225

**Answer: B**

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120. If  $f: [0, 1] \rightarrow [0, \infty)$  is differentiable function with decreasing first derivative such that  $f(0)=0$  and  $f'(x) > 0$ , then

A.  $\int_0^1 \frac{1}{f^2(x) + 1} dx > \frac{f(1)}{f'(1)}$

B.  $\int_0^1 \frac{1}{f^2(x) + 1} dx < \frac{f(1)}{f'(1)}$

C.  $\int_0^1 \frac{1}{f^2(x) + 1} dx < \frac{\tan^{-1}(f(1))}{f'(1)}$

D.  $\int_0^1 \frac{1}{f^2(x) + 1} dx = \frac{f(1)}{f'(1)}$

Answer: C



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121. If  $f(x)$  is differentiable function and  $f(x) = x^2 + \int_0^x e^{-t}(x-t)dt$ , then  $f'(x)$  equals to

A.  $\frac{-2}{3}$

B.  $\frac{2}{3}$

C.  $\frac{1}{3}$

D.  $-\frac{1}{3}$

**Answer: B**



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**122.** If  $f(x)$  is a continuous function such that  $f(x) > 0$  for all  $x > 0$  and  $(f(x))^{2020} = 1 + \int_0^x f(t) dt$ , then the value of  $\{f(2020)\}^{2019}$  is equal to

A. 2019

B. 2020

C. 2021

D. 2018

**Answer: B**



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123. If a function  $y=f(x)$  such that  $f'(x)$  is continuous function and satisfies

$$(f(x))^2 = k + \int_0^x \left[ \{f(t)\}^2 + \{f'(t)\}^2 \right] dt, k \in \mathbb{R}^+, \text{ then}$$

- A.  $f(x)$  is an increasing function for all  $x \in \mathbb{R}$
- B.  $f(x)$  is a bounded function
- C.  $f(x)$  is neither even nor odd function
- D. If  $k=100$ , then  $f(0)=10$ .

Answer: A::C



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124. The maximum value of  $f(x) = \int_0^1 t \sin(x + \pi t) dt$  is

- A.  $\frac{1}{\pi} \sqrt{\pi^2 + 4}$
- B.  $\frac{1}{\pi^2} \sqrt{\pi^2 + 4}$
- C.  $\sqrt{\pi^2 + 4}$

D.  $\frac{1}{2\pi^2} \sqrt{\pi^2 + 4}$

**Answer: B**

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125. If  $I_n = \int_0^\pi e^x \sin^n x \, dx$  then  $\frac{I_3}{I_1}$  is equal to

A.  $\frac{3}{5}$

B.  $\frac{1}{5}$

C. 1

D.  $\frac{2}{5}$

**Answer: A**

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126. If  $k = \int_0^1 \frac{e^t}{1+t} dt$ , then  $\int_0^1 e^t \log_e(1+t) dt$  is equal to

A.  $k$

B.  $2k$

C.  $e \ln 2 - k$

D. none of these

**Answer: C**



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127. If  $k \in N$  and  $I_k = \int_{-2k\pi}^{2k\pi} |\sin x| [\sin x] dx$ , where  $[\cdot]$  denotes the greatest integer function, then  $\int_{k=1}^{100} I_k$  equal to

A. -10100

B. -40400

C. -20200

D. none of these

**Answer: C**





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128. The value of

$$\int_{-1}^1 \frac{(\log x + \sqrt{1+x^2})}{x + \log(x + \sqrt{1+x^2})} f(x) dx - \int_{-1}^1 \frac{\log(x\sqrt{1+x^2})}{x + \log(x + \log\sqrt{1+x^2})} f(x) dx$$

A. 0

B.  $2 \int_0^1 \frac{\log(x + \sqrt{1+x^2})}{x + \log(x + \sqrt{1+x^2})} \{f(x) - f(-x)\} dx$

C.  $2f(x)$

D. none of these

Answer: A



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129. If  $\int_0^1 \alpha e^{\beta x^2} \sin(x+k) dx = 0$  for some  $\alpha, \beta \in R, \alpha \neq 0$ , then the value of  $k$  can belong to the interval

A.  $\left[ \frac{\pi}{3}, \frac{5\pi}{12} \right]$

B.  $\left[ \frac{\pi}{3}, \frac{\pi}{2} \right]$

C.  $\left[ \frac{3\pi}{4}, \frac{5\pi}{6} \right]$

D.  $\left[ -\frac{\pi}{2}, -\frac{\pi}{3} \right]$

**Answer: C**



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130.  $\int_0^{[x]/3} \frac{8^x}{2^{[3x]}} dx$  where  $[.]$  denotes the greatest integer function, is equal to

A.  $\frac{[x]}{\ln 2}$

B.  $\frac{[x]}{\ln 2}$

C.  $\frac{2[x]}{\ln 2}$

D.  $\frac{[x]}{\ln 8}$

**Answer: D**



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131. Let  $f(x) = \ln \left[ \cos|x| + \frac{1}{2} \right]$  where  $[.]$  denotes the greatest integer function, then  $\int_{x_1}^{x_2} \lim_{n \rightarrow \infty} \left( \frac{\{f(x)\}^n}{x^2 + \tan^2 x} \right) dx$  is equal to, where  $x_1, x_2 \in \left[ \frac{-\pi}{6}, \frac{\pi}{6} \right]$

A. 1

B. 2

C. -1

D. 0

**Answer: D**



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132.  $\lim_{x \rightarrow 0} \left( \frac{\int_0^x x e^{t^2} dt}{1 + x - e^x} \right)$  is equal to

A. 1

B. -1

C. 2

D. -2

**Answer: D**



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133. If  $\int_{2x^2}^{x^3} (\ln x) f(t) dt = x^2 - 2x + 5$ , then  $f(8) =$

A.  $\frac{1}{\ln 2}$

B.  $\frac{1}{2\ln 2}$

C.  $\frac{1}{3\ln 2}$

D.  $\frac{1}{4\ln 2}$

**Answer: B**



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134.  $\lim_{x \rightarrow 0} \frac{\int_{-x}^x f(t) dt}{\int_0^{2x} f(t+4) dt}$  is equal to

A.  $f(0)$

B. 0

C.  $\frac{f(4)}{f(0)}$

D.  $\frac{f(0)}{f(4)}$

**Answer: D**



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135. If  $f(x+f(y))=f(x)+y$  for all  $x, y \in R$  and  $f(0)=1$ , then  $\int_0^{10} f(10-x)dx$  is equal to

A. 1

B. 10

C.  $\int_0^1 f(x)dx$

D.  $10 \int_0^1 f(x)dx$

**Answer: D**



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136. If  $\alpha, \beta (\beta > \alpha)$  are the roots of  $f(x) = -ax^2 + bx + c = 0$  and  $f(x)$  is an even function, then

$\int_{\alpha}^{\beta} \frac{e^{f\left(\frac{f(x)}{x-\alpha}\right)}}{e^{f\left(\frac{f(x)}{x-a}\right)} + e^{f\left(\frac{f(x)}{x-b}\right)}} dx$  is equal to

A.  $\left| \frac{b}{a} \right|$

B.  $\left| \frac{b}{2a} \right|$

C.  $\frac{\sqrt{b^2 - 4ac}}{|2a|}$

D. none of these

**Answer: C**



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**137.** The value of the constant  $a > 0$  such that

$$\int_0^a [\tan^{-1} \sqrt{x}] dx = \int_0^a [\cot^{-1} \sqrt{x}] dx, \text{ where } [.] \text{ denotes the greatest}$$

integer function, is

A.  $\frac{2(3 + \cos 4)}{1 - \cos 4}$

B.  $\frac{2(3 - \cos 4)}{1 + \cos 4}$

C.  $\frac{2(3 - \cos 4)}{1 - \cos 4}$

D.  $\frac{2(3 + \cos 4)}{1 + \cos 4}$

**Answer: A**

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**138.** If  $f(x)$  is a continuous function in  $[0, \pi]$  such that  $f(0)=f(\pi)=0$ , then the value of

$\int_0^{\pi/2} \{f(2x) - f'(2x)\} \sin x \cos x dx$  is equal to

- A.  $\pi$
- B.  $2\pi$
- C.  $3\pi$
- D. 0

**Answer: D**

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**139.** Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be continuous function such that  $f(x)=f(2x)$  for all  $x \in \mathbb{R}$ . If  $f(1)=3$ , then the value of  $\int_{-1}^1 f(f(x)) dx$ , is



A.  $3f(0)$

B. 0

C.  $3f(3)$

D. 6

**Answer: D**



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**140.** The value of

$$\int_0^{\pi/4} (\tan^n x + \tan^{n-2} x) d\left(x - \frac{[x]}{1!} + \frac{[x]^2}{2!} - \frac{[x]^3}{3!} + \dots\right)$$

where  $[x]$  is greatest function, is

A.  $\frac{1}{n}$

B.  $\frac{1}{n+2}$

C.  $\frac{1}{n-1}$

D.  $\frac{1}{n-2}$

**Answer: C**



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**141.** The value of the definite integral

$$\int_{t+2\pi}^{t+5\pi/2} \{\sin^{-1}(\cos x) + \cos^{-1}(\cos x)\} dx \text{ is equal to}$$

A.  $\frac{\pi^2}{2}$

B.  $\frac{\pi^2}{8}$

C.  $\frac{\pi^2}{4}$

D. none of these

**Answer: C**



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**142.** If  $f(x)$  is an integrable function on  $\left[\frac{\pi}{6}, \frac{\pi}{3}\right]$  and

$$I_1 = \int_{\pi/6}^{\pi/3} \sec^2 \theta f(2 \sin 2\theta) d\theta \quad \text{and} \quad I_2 = \int_{\pi/6}^{\pi/3} \operatorname{cosec}^2 \theta f(2 \sin 2\theta) d\theta,$$

then

A.  $I_1 = 2I_2$

B.  $I_1 = 3I_2$

C.  $2I_1 = I_2$

D. none of these

**Answer: D**



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**143.** Let

$$f(x) = \lim_{n \rightarrow \infty} \left\{ \frac{n^n (x+n) \left(x + \frac{n}{2}\right) \dots \left(x + \frac{n}{2}\right)}{n! (x^2 + n^2) \left(x^2 + \frac{n^2}{4}\right) \dots \left(x^2 + \frac{n^2}{n^2}\right)} \right\}^{x/n} \quad \text{for all } x > 0$$

. Then,

A.  $f\left(\frac{1}{2}\right) \geq f(1)$

B.  $f\left(\frac{1}{3}\right) \leq f\left(\frac{2}{3}\right)$

C.  $f'(2) \leq 0$

$$D. \frac{f'(3)}{f(3)} \geq \frac{f'(2)}{f(2)}$$

**Answer: B::C**



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**144.** The total number of distinct  $x \in [0, 1]$  for which

$$\int_0^x \frac{t^2}{1+t^4} dt = 2x - 1, \text{ is}$$

A. 1

B. 2

C. 3

D. infinitely many

**Answer: A**



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145. For  $x \in R, x \neq 0$ , if  $y(x)$  is differentiable function such that  $\int_1^x ty(t)dt = (x + 1) \int_1^x ty(t)dt$ , then  $y(x)$  equals (where  $C$  is a constant).

A.  $Cx^3e^{1/x}$

B.  $\frac{C}{x^2}e^{-1/x}$

C.  $\frac{C}{x^2}e^{-1/x}$

D.  $\frac{C}{x^3}e^{-1/x}$

Answer: D



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## Section II - Assertion Reason Type

1. Statement-1:  $\int_0^{\pi/2} x \cot x dx = \frac{\pi}{2} \log 2$

Statement-2:  $\int_0^{\pi/2} \log \sin x dx = -\frac{\pi}{2} \log 2$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: A**

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2. Statement-1:  $\int_0^{n\pi+v} |\sin x| dx = 2n + 1 - \cos v$  where  $n \in \mathbb{N}$  and  $0 \leq v < \pi$ .

Statement-2: If  $f(x)$  is a periodic function with period  $T$ , then

(i)  $\int_0^{nT} f(x) dx = n \int_0^T f(x) dx$ , where  $n \in \mathbb{N}$

and (ii)  $\int_{nT}^{nT+a} f(x) dx = \int_0^a f(x) dx$ , where  $n \in \mathbb{N}$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: A**

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3. Let  $I_n = \int_0^{\pi/4} \tan^n x dx$ .

Statement-1:  $\frac{1}{n+1} < 2I_n < \frac{1}{n-1}$  for all  $n=2,3,4,\dots$

Statement-2:  $I_n + I_{n-2} = \frac{1}{n-1}, n=3,4,5,\dots$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for

Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: A**

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4. Statement-1: If  $f(x) = \int_1^x \frac{\log_e t}{1+t+t^2} dt$ , then

$f(x) = f\left(\frac{1}{x}\right)$  for all  $x > 0$ .

Statement-2: If  $f(x) = \int_1^x \frac{\log_e t}{1+t} dt$ , then  $f(x) + f\left(\frac{1}{x}\right) = \frac{(\log_e x)^2}{2}$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.



C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: B**



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5. Let  $n \in \mathbb{N}$  such that  $n > 1$ .

Statement-1: 
$$\int_0^{\infty} \frac{1}{1+x^n} dx = \int_0^1 \frac{1}{(1-x^n)^{1/n}} dx$$

Statement-2: 
$$\int_a^b f(x) dx = \int_a^b f(a+b-x) dx$$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: B**



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**6. Statement-1:** For any  $n \in \mathbb{N}$ , we have

$$\int_0^{n\pi} \left| \frac{\sin x}{x} \right| dx \geq \frac{2}{\pi} \left( 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right)$$

Statement-2:  $\frac{\sin x}{x} \geq \frac{2}{\pi}$  on  $\left(0, \frac{\pi}{2}\right)$

- A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.
- B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.
- C. Statement-1 is True, Statement-2 is False.
- D. Statement-1 is False, Statement-2 is True.

**Answer: B**



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7. Statement-1:  $\int_0^1 \frac{\cos x}{1+x^2} dx > \frac{\pi}{4} \cos 1$

Statement-2: If  $f(x)$  and  $g(x)$  are continuous on  $[a,b]$ , then

$$\int_a^b f(x)g(x)dx = f(c) \int_a^b g(x) \text{ for some } c \in (a, b).$$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: A**



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8. Statement-1:

$$\int_0^{\sin^2 x} \sin^{-1} \sqrt{tdt} + \int_0^{\cos^2 x} \cos^{-1} \sqrt{tdt} = \frac{\pi}{4} \text{ for all } x.$$

Statement-2:  $\frac{d}{dx} \int_{\theta(x)}^{\psi(x)} f(t) dt = \psi'(x)f(\psi(x)) - \theta'(x)f(\theta(x))$

- A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.
- B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.
- C. Statement-1 is True, Statement-2 is False.
- D. Statement-1 is False, Statement-2 is True.

**Answer: C**

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9. Statement-1:  $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} dx = \frac{\pi}{4}$

Statement-2:  $\int_0^a f(x) dx = \int_0^a f(a+x) dx$

- A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

- B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.
- C. Statement-1 is True, Statement-2 is False.
- D. Statement-1 is False, Statement-2 is True.

**Answer: C**

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10. Let  $F(x) = \int_a^{x^2} \cos \sqrt{t} dt$

Statement-1:  $F'(x) = \cos x$

Statement-2: If  $f(x) = \int_a^x \phi(t) dt$ , then  $f'(x) = \phi(x)$ .

- A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.
- B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: D**



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11.  $I_n = \int_0^{\pi/4} \tan^n x dx$ , where  $n \in \mathbb{N}$

Statement-1:  $\int_0^{\pi/4} \tan^4 x dx = \frac{3\pi - 8}{12}$

Statement-2:  $I_n + I_{n-2} = \frac{1}{n-1}$

A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.

B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.

C. Statement-1 is True, Statement-2 is False.

D. Statement-1 is False, Statement-2 is True.

**Answer: A**



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**12. Statement-1:** The value of the integral

$$\int_{\pi/6}^{\pi/3} \frac{1}{\sqrt{\tan x}} dx \text{ is equal to } \frac{\pi}{6}$$

$$\text{Statement-2: } \int_a^b f(x) dx = \int_a^b f(a + b - x) dx$$

- A. Statement-1 is true, Statement-2 is True, Statement-2 is a correct explanation for Statement-1.
- B. Statement-1 is True, Statement-2 is not a correct explanation for Statement-1.
- C. Statement-1 is True, Statement-2 is False.
- D. Statement-1 is False, Statement-2 is True.

**Answer: D**



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## Exercise

1. If  $I = \int_{-2}^2 dx$ , then I equals

A. 6

B. 8

C. 12

D. 21

**Answer: C**



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2. The value of the integral  $\int_{\alpha}^{\beta} \frac{1}{\sqrt{(x-\alpha)(\beta-x)}} dx$  for  $\beta > \alpha$ , is

A.  $\sin^{-1}(\alpha/\beta)$

B.  $\pi/2$



C.  $\sin^{-1}(\beta/2\alpha)$

D.  $\pi$

**Answer: D**

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3.  $\int_1^{\frac{4\sqrt{3}}{5}-1} \frac{x+2}{\sqrt{x^2+2x-3}} dx$  equal to

A.  $\frac{2\sqrt{3}}{3} - \frac{1}{2}\log 3$

B.  $\frac{2\sqrt{3}}{3} + \frac{1}{2}\log 3$

C.  $\frac{2\sqrt{3}}{3} - \frac{1}{2}\log(\sqrt{3}+2)$

D.  $\frac{2\sqrt{3}}{3} + \frac{1}{2}\log(\sqrt{3}+2)$

**Answer: B**

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4.  $\int_0^{\pi^2/4} \sin \sqrt{x} dx$  equals to

A. 0

B. 1

C. 2

D. 4

**Answer: C**



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5.  $\int_{1/2}^2 |\log_{10} x| dx$  equals to

A.  $\log_{10}(8/e)$

B.  $\frac{1}{2} \log_{10}(8/e)$

C.  $\log_{10}(2/e)$

D. none of these

**Answer: B**



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6. The value of the integral  $\int_{-\pi/2}^{\pi/2} \log\left(\frac{a - \sin \theta}{a + \sin \theta}\right) d\theta$ ,  $a > 0$  is

A. 0

B. 1

C. 2

D. none of these

**Answer: A**



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7. The value of the integral  $\int_{\pi/3}^{\pi/3} \frac{x \sin x}{\cos^2 x} dx$ , is

A.  $(\pi/3 - \log \tan 3\pi/2)$

B.  $2(2\pi/3 - \log \tan 5\pi/12)$

C.  $3(\pi/2 - \log \sin \pi/12)$

D. none of these

**Answer: B**



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8. The value of  $\int_1^{7\sqrt{2}} \frac{1}{x(2x^7 + 1)} dx$  is

A.  $\log(6/5)$

B.  $6 \log(6/5)$

C.  $(1/7)\log(6/5)$

D.  $(1/12)\log(6/5)$

**Answer: C**



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9. The value of  $\int_{-1}^3 (|x_2| + [x]) dx$  is ( $[x]$  stands for greatest integer less than or equal to  $x$ )

A. 7

B. 5

C. 4

D. 3

**Answer: A**



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10. If  $f(x) = \begin{vmatrix} \sin x + \sin 2x + \sin 3x & x \sin 2 & x \sin 3x \\ 3 + 4 \sin x & 3 & 4 \sin x \\ 1 + \sin x & \sin x & 1 \end{vmatrix}$  then the value of

$\int_0^{\pi/2} f(x) dx$ , is

A. 3

B.  $2/3$

C.  $1/3$

D. 0

**Answer: C**



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11. Evaluate:  $(\lim)_{x \rightarrow \infty} \frac{(\int 0xe^{x^2} dx)^2}{\int 0xe^{2x^2} dx}$

A. 1

B. 2

C. 3

D. 0

**Answer: D**



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12. The value of  $\int_1^4 e^{\sqrt{x}} dx$ , is

A.  $e^2$

B.  $2e^2$

C.  $4e^2$

D.  $3e^2$

**Answer: B**



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13. The value of  $\int_0^{1000} e^{x - [x]} dx$ , is

A.  $\frac{e^{1000} - 1}{1000}$

B.  $\frac{e^{1000} - 1}{e - 1}$

C.  $1000(e-1)$

D.  $\frac{e - 1}{1000}$

**Answer: C**



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14. The value of the integral  $\int_0^{100} \sin(x - [x])\pi dx$ , is

A.  $100/\pi$

B.  $200/\pi$

C.  $100\pi$

D.  $200\pi$

**Answer: B**



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15. The difference between the greatest and least values of the function

$$\phi(x) = \int_0^x (t + 1)dt \text{ on } [2,3], \text{ is}$$



A. 3

B. 2

C.  $7/2$

D.  $11/2$

**Answer: C**



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16. The value of  $\int_0^1 \frac{2^{2x+1} - 5^{2x-1}}{10^x} dx$  is

A.  $\frac{3}{5} \left\{ \frac{2}{\log e \left( \frac{2}{5} \right)} + \frac{1}{2 \log e \left( \frac{5}{2} \right)} \right\}$

B.  $-\frac{3}{5} \left\{ \frac{2}{\log e \left( \frac{2}{5} \right)} + \frac{1}{2 \log e \left( \frac{5}{2} \right)} \right\}$

C.  $\frac{3}{5} \left\{ \frac{2}{\log e \left( \frac{2}{5} \right)} - \frac{1}{2 \log e \left( \frac{5}{2} \right)} \right\}$

D. none of these

**Answer: B**



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17. The value of  $\int_0^{\pi/2} \frac{\cos 3x + 1}{2 \cos x - 1} dx$  is

A. 2

B. 1

C.  $1/2$

D. 0

**Answer: B**



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18. The value of  $\int_0^{16\pi/3} |\sin x| dx$  is

A. 21

B.  $21/2$

C. 10

D. 11

**Answer: B**



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19. If  $\int_0^{n\pi} f(\cos^2 x) dx = k \int_0^{\pi} f(\cos^2 x) dx$ , then the value of  $k$ , is

A. 1

B.  $n$

C.  $n/2$

D. none of these

**Answer: B**



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20. The value of  $\int_{-\pi}^{\pi} \sin x f(\cos x) dx$  is

A.  $\pi$

B.  $2\pi$

C.  $2f(1)$

D. none of these

**Answer: D**



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21. If  $a < \int_0^{2\pi} \frac{1}{10 + 3 \cos x} dx < b$ . Then the ordered pair (a,b) is

A.  $\left(\frac{2\pi}{7}, \frac{2\pi}{3}\right)$

B.  $\left(\frac{2\pi}{13}, \frac{2\pi}{7}\right)$

C.  $\left(\frac{\pi}{10}, \frac{2\pi}{13}\right)$

D. none of these

**Answer: B**



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22. The value of the integral  $\int_0^{\infty} \frac{x \log x}{(1+x^2)} dx$  is

A. 1

B. 0

C. 2

D. none of these

**Answer: B**



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23. The value of the integral  $\int_{-\pi/2}^{\pi/2} \sqrt{\cos x - \cos^2 x} dx$  is

A. 0

B.  $2/3$

C.  $4/3$

D. none of these

**Answer: C**

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24. The value of the integral  $\int_{-\pi/2}^{\pi/2} \sqrt{\frac{1 + \cos^2 x}{2}} dx$  is

A. -2

B. 2

C. 0

D. -3

**Answer: B**

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25. Let  $I_1 = \int_1^2 \frac{1}{\sqrt{1+x^2}} dx$  and  $I_2 = \int_1^2 \frac{1}{x} dx$ . Then

A.  $I_1 > I_2$

B.  $I_2 > I_1$

C.  $I_1 = I_2$

D.  $I_2 > 2I_1$

**Answer: B**

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26.  $\int_0^{\pi/4} \frac{\sin x + \cos x}{3 + \sin 2x} dx$  is equal to

A.  $-\frac{1}{4} \log 3$

B.  $\frac{1}{4} \log 3$

C.  $-\frac{1}{3} \log 4$

D. none of these

**Answer: B**



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27. The value of the integral  $\int_0^{\pi/4} \frac{\sin \theta + \cos \theta}{9 + 16 \sin 2\theta} d\theta$ , is

A.  $\log 3$

B.  $\log 2$

C.  $\frac{1}{20} \log 3$

D.  $\frac{1}{20} \log 2$

**Answer: C**



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28. Let  $\frac{d}{dx}(f(x)) = \frac{e^{\sin x}}{x}$ ,  $x > 0$ . If  $\int_1^4 \frac{3}{x} e^{\sin x^3} dx = F(k) - f(1)$ , then

one of the possible values of  $k$ , is



A. 64

B. 15

C. 16

D. 63

**Answer: A**



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29. If  $I = \int_{-1}^1 \left\{ [x^2] + \log\left(\frac{2+x}{2-x}\right) \right\} dx$  where  $[x]$  denotes the greatest integer less than or equal to  $x$ , the  $I$  equals

A. -2

B. -1

C. 0

D. 1

**Answer: C**



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30. The value of  $\int_{-\pi/2}^{\pi/2} (x^2 + x \cos x + \tan^5 x + 1) dx$  is equal to

A. 0

B. 2

C.  $\pi$

D. none of these

Answer: D



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31. If  $\int_{-1}^4 f(x) dx = 4$  and  $\int_2^7 (3 - f(x)) dx = 7$ , then the value of  $\int_2^{-1} f(x) dx$ , is

A. 2

B. -3

C. -5

D. none of these

**Answer: C**



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32. The value of  $I = \int_0^{\pi/2} \frac{1}{1 + \cos x} dx$  is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{2}$

C. 1

D.  $\pi$

**Answer: C**



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33.  $\int_0^{\pi/2} \frac{\sin^2 x}{\sin x + \cos x} dx$  is equal to

A.  $\frac{\pi}{2}$

B.  $\sqrt{2} \log(\sqrt{2} + 1)$

C.  $\frac{1}{\sqrt{2}} \log(\sqrt{2} + 1)$

D. none of these

**Answer: C**



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34. The value of the integral  $\int_a^b \frac{|x|}{x} dx$ ,  $a < b$  is

A.  $|a| - |b|$

B.  $|b| - |a|$

C.  $|a| - |b|$

D.  $|b| - |a|$

**Answer: B**



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**35.** The value of the integral

$$\int_0^{2\pi} \frac{\sin 2\theta}{a - b \cos \theta} d\theta \text{ when } a > b > 0, \text{ is}$$

A. 1

B.  $\pi$

C.  $\pi/2$

D. 0

**Answer: D**



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**36.** The value of the integral  $\int_0^1 x(1-x)^n dx$ , is

A.  $\frac{1}{n+1} + \frac{1}{n+2}$

B.  $\frac{1}{(n+1)(n+2)}$

C.  $\frac{1}{n+2} - \frac{1}{n+1}$

D.  $2\left(\frac{1}{n+1} - \frac{1}{n+2}\right)$

**Answer: B**



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**37.** The value of the integral

$$\int_0^{3\alpha} \operatorname{cosec}(x - \alpha) \operatorname{cosec}(x - 2\alpha) dx \text{ is}$$

A.  $2\operatorname{cosec} \alpha \log\left(\frac{1}{2}\operatorname{cosec} \alpha\right)$

B.  $2\operatorname{cosec} \alpha \log\left(\frac{1}{2}\sec \alpha\right)$

C.  $2\operatorname{cosec} \alpha \log(\sec \alpha)$

D.  $2 \operatorname{cosec} \alpha \log\left(\frac{1}{2}\sec \alpha\right)$

**Answer: D**



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38. The value of the integral  $\int_0^\pi \frac{\sin kx}{\sin x} dx$  ( $k$  is an even integer) is equal to

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $\frac{k\pi}{2}$

D. 0

Answer: D



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39. The value of the integral  $\int_0^1 \frac{1}{x^2 + 2x \cos \alpha + 1} dx$  is equal to

A.  $\sin \alpha$

B.  $\alpha \sin \alpha$

C.  $\frac{\alpha}{2 \sin \alpha}$

D.  $\frac{\alpha}{2} \sin \alpha$

**Answer: C**



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40. The greater value of  $F(x) = \int_1^x |t| dt$  on the interval  $[-1/2, 1/2]$ ,

is

A.  $\frac{3}{8}$

B.  $\frac{1}{2}$

C.  $-\frac{3}{8}$

D.  $-\frac{1}{2}$

**Answer: C**



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41. The value of the integral  $\int_0^{\pi/2} |\sin x - \cos x| dx$ , is

A. 0

B.  $2(\sqrt{2} - 1)$

C.  $2\sqrt{2}$

D.  $2(\sqrt{2} + 1)$

**Answer: B**



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42. The value of the integral  $\int_0^{\pi/4} \sin^{-4} x dx$ , is

A.  $-\frac{8}{3}$

B.  $\frac{3}{2}$

C.  $\frac{8}{3}$

D. none of these

**Answer: A**



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43. The value of the integral  $I = \int_1^{\infty} \frac{x^2 - 2}{x^3 \sqrt{x^2 - 1}} dx$ , is

A. 0

B.  $\frac{2}{3}$

C.  $\frac{4}{3}$

D. none of these

**Answer: A**



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44.  $\int_0^1 |\sin 2\pi x| dx$  is equal to

A. 0

B.  $-\frac{1}{\pi}$

C.  $\frac{1}{\pi}$

D.  $\frac{2}{\pi}$

**Answer: D**



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45. The value of integral  $\int_{-\pi}^{\pi} (\cos ax - \sin bx)^2 dx$ , where (a and b are integers), is

A.  $-\pi$

B. 0

C.  $\pi$

D.  $2\pi$

**Answer: D**



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46. The value of the definite integral  $\int_0^1 (1 + e^{-x^2}) dx$  is

A. -1

B. 2

C.  $1 + e^{-1}$

D. none of these

**Answer: D**



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47. If  $I = \int_{-\pi}^{\pi} \frac{\sin^2}{1 + a^x} dx$ ,  $a > 0$ , then I equals

A.  $\pi$

B.  $\frac{\pi}{2}$

C.  $a\pi$

D.  $a \frac{\pi}{2}$

**Answer: B**



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**48.** If  $n$  is an odd natural number, then

$$\int_{-\pi/6}^{\pi/6} \frac{\pi + 4x^n}{-\sin\left(pq + \frac{\pi}{6}\right)} dx =$$



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**49.** If  $I_1 = \int_0^x e^{zx} e^{-z^2} dz$  and  $I_2 = \int_0^x e^{-z^2/4} dz$ , then

A.  $I_1 = e^x I_2$

B.  $I_1 = e^{x^2} I_2$

C.  $I_1 = e^{x^2/2} I_2$

D. none of these

**Answer: D**



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50.  $\int_0^{1/2} |\sin \pi s| dx$  is equal to

A. 0

B.  $\pi$

C.  $-\pi$

D.  $1/\pi$

**Answer: D**



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51. The function  $F(x) = \int_0^x \log\left(\frac{1-x}{1+x}\right) dx$ , is

A. an even function

B. an odd function

C. a periodic function

D. none of these

**Answer: A**



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52.  $\int_{1/3}^3 \frac{1}{x} \sin\left(\frac{1}{x} - x\right) dx$  is equal to

A.  $\frac{\sqrt{3}}{2}$

B.  $\frac{\sqrt{3}\pi}{2}$

C. 0

D. none of these

**Answer: C**



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53. If  $F(x) = \int_{x^2}^{x^3} \log t dt (x > 0)$ , then  $F'(x)$  equals

A.  $(9x^2 - 4x) \log x$

B.  $(4x - 9x^2) \log x$

C.  $(9x^2 + 4x) \log x$

D. none of these

**Answer: A**



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54. If  $F(x)$  and  $g(x)$  are two integrable functions defined on

$[a, b]$ , then  $\left| \int_a^b f(x)g(x) dx \right|$ , is

A. less than  $\sqrt{\int_a^b f(x) dx \int_a^b g(x) dx}$

B. less than or equal to  $\sqrt{\int_a^b f^2(x) dx \int_a^b g^2(x) dx}$



C. less than or equal to  $\sqrt{\left\{ \int_a^b f^2(x) dx \right\} \left\{ \int_a^b g^2(x) dx \right\}}$

D. none of these

**Answer: C**

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55. If  $I = \int_0^1 \frac{dx}{\sqrt{1+x^4}}$  then

A.  $I > 2$

B.  $I \neq \frac{\sqrt{5}}{2}$

C.  $I > \frac{\sqrt{7}}{2}$

D. none of these

**Answer: C**

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56. If  $I = \int_0^1 \frac{dx}{1+x^4}$ , then

A.  $I > 0.78$

B.  $I < 0.78$

C.  $I > 1$

D. none of these

**Answer: A**



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57. The value of  $\int_{-1}^1 x|x|dx$ , is

A. 2

B. 1

C. 0

D. none of these

**Answer: C**



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58. If  $\int_0^{\pi/2} \cos^n x \sin^n x dx = \lambda \int_0^{\pi/2} \sin^n x dx$ , then  $\lambda =$

A.  $\frac{1}{2^{n-1}}$

B.  $\frac{1}{2^{n+1}}$

C.  $\frac{1}{2^n}$

D.  $\frac{1}{2}$

**Answer: C**



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59. The value of  $\int_{1/e}^e \frac{|\log x|}{x^2} dx$ , is

A. 2

B.  $\frac{2}{e}$

C.  $2\left(1 - \frac{1}{e}\right)$

D. 0

**Answer: C**



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60. Assuming that  $f$  is everywhere continuous,  $\frac{1}{c} \int_{ac}^{bc} f\left(\frac{x}{c}\right) dx$  is equal to

A.  $\frac{1}{c} \int_a^b f(x) dx$

B.  $\int_a^b f(x) dx$

C.  $c \int_a^b f(x) dx$

D.  $c \int_{ac^2}^{bc^2} f(x) dx$

**Answer: B**



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61.  $\frac{d}{dx} \left( \int_{f(x)}^{g(x)} \phi(t) dt \right)$  is equal to

A.  $\phi(g(x)) - \phi(f(x))$

B.  $\frac{1}{2}[\phi(g(x))]^2 - \frac{1}{2}[\phi(f(x))]^2$

C.  $g'(x)\phi(g(x)) - f'(x)\phi(f(x))$

D.  $\phi(g(x))g'(x) - \phi(f(x))f'(x)$

Answer: C



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62. If  $f(x) = ae^{2x} + be^x + cx$  satisfies the conditions  $f(0)=-1$ ,  $f'(\log 2)=31$ ,

$$\int_0^{\log 4} (f(x) - cx) dx = \frac{39}{2}, \text{ then}$$

A.  $a=5, b=-6, c=-7$

B.  $a=5, b=6, c=7$

C.  $a=-5, b=6, c=-7$

D. none of these

**Answer: A**



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63. The value of  $\int_0^2 \left| \cos\left(\frac{\pi x}{2}\right) \right| dx$  is

A.  $2\pi$

B.  $\pi/2$

C.  $3/4\pi$

D.  $4/\pi$

**Answer: D**



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64. If  $\int_0^1 \cot^{-1}(1 - x - x^2) dx = k \int_0^1 \tan^{-1} x dx$ , then  $k =$

A. 1

B. 2

C.  $\pi$

D.  $2\pi$

**Answer: B**



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65. If  $0 < a < 1$ , then  $\int_{-1}^1 \frac{1}{\sqrt{1 - 2ax + a^2}} dx$  is equal to

A. 1

B.  $2\pi$

C.  $\pi/2$

D.  $3\pi/2$

Answer: D



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66. The value of  $\int_0^{\pi/2} \frac{x + \sin x}{1 + \cos x} dx$ , is

A.  $\pi$

B.  $2\pi$

C.  $\pi/2$

D.  $3\pi/2$

Answer: C



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67.  $f(x) = \begin{vmatrix} \sec x & \cos x & \sec^2 x + \cos ecx \cot x \\ \cos^2 x & \cos^2 x & \cos ec^2 x \\ 1 & \cos^2 x & \cos^2 x \end{vmatrix}$  then,

$\int_0^{\pi/2} f(x) dx$  equals



A. 0

B. 1

C.  $-\left(\frac{\pi}{4} + \frac{8}{15}\right)$

D. -1

**Answer: C**

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68. If  $a$  is a fixed real number such that  $f(a-x)+f(a+x)=0$ , then  $\int_0^{2a} f(x) dx=$

A.  $\frac{a}{2}$

B. 0

C.  $-\frac{a}{2}$

D.  $2a$

**Answer: B**

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69. The value of  $\int_0^1 \log\left(\frac{4 + 3 \sin x}{4 + 3 \cos x}\right) dx$ , is

A. 2

B.  $3/4$

C. 0

D. 1

**Answer: C**



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70. The value of  $\int_0^1 \tan^{-1}\left(\frac{2x - 1}{1 + x - x^2}\right) dx$  is

A. 1

B. 0

C. -1

D. 2

**Answer: B**



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71. The value of  $\int_0^{2\pi} |\cos x - \sin x| dx$  is

A.  $\frac{4}{\sqrt{2}}$

B.  $2\sqrt{2}$

C.  $\frac{2}{\sqrt{2}}$

D.  $4\sqrt{2}$

**Answer: D**



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72. If  $I_1 = \int_0^1 2^{x^2} dx$ ,  $I_2 = \int_0^1 2^{x^3} dx$ ,  $I_3 = \int_1^2 2^{x^2} dx$   
and  $I_4 = \int_1^2 2^{x^2} dx$  then

A.  $I_1 > I_2$  and  $I_4 > I_3$

B.  $I_2 > I_1$  and  $I_3 > I_4$

C.  $I_1 > I_2$  and  $I_3 > I_4$

D. none of these

**Answer: A**



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73. Consider the integrals

$$I_1 = \int_0^1 e^{-x} \cos^2 x dx, I_2 = \int_0^1 e^{-x^2} \cos^2 x dx, I_3 = \int_0^1 e^{-x^2} dx$$

and  $I_4 = \int_0^1 e^{-x^{1/2} x^2} dx$ . The greatest of these integrals, is

A.  $I_1$

B.  $I_2$

C.  $I_3$

D.  $I_4$

**Answer: D**



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74. If  $f(x)=f(a+b-x)$  for all  $x \in [a, b]$  and  $\int_a^b x f(x) dx = k \int_a^b f(x) dx$ , then

the value of k, is

A.  $\frac{a + b}{2}$

B.  $\frac{a - b}{2}$

C.  $\frac{a^2 + b^2}{2}$

D.  $\frac{a^2 - b^2}{2}$

**Answer: A**



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75. To find the numerical value of  $\int_{-2}^2 (px^3 + qx + 8) dx$  it is necessary to know the values of the constants:

- A. p
- B. q
- C. s
- D. p and s

**Answer: C**



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76. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be continuous functions. Then the value of the integral

$$\int_{-\pi/2}^{\pi/2} [f(x) + f(-x)][g(x) - g(-x)] dx \text{ is}$$

- A.  $\pi$
- B. 1
- C. -1

D. 0

**Answer: D**



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77. The value of  $\int_{-1/2}^{1/2} \left| x \cos\left(\frac{\pi x}{2}\right) \right| dx$  is

A.  $\frac{\pi\sqrt{2} + 4\sqrt{2} - 8}{\pi^2}$

B.  $\frac{\sqrt{2} + 4\pi\sqrt{2} - 8}{\pi^2}$

C.  $\frac{\pi\sqrt{2} + 4\sqrt{2} + 8}{\pi^2}$

D. none of these

**Answer: A**



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78. The value of the integral  $\int_0^{\pi/2} \frac{f(x)}{f(x) + f\left(\frac{\pi}{2} - x\right)} dx$  is

A.  $\pi/4$

B.  $\pi/2$

C.  $\pi$

D. 0

**Answer: A**



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79. The value of  $\int_{\pi/2}^0 \frac{1}{9 \cos x + 12 \sin x} dx$  is

A.  $\frac{1}{15} \log_{10} 6$

B.  $\frac{1}{15} \log_e 6$

C.  $\log\left(\frac{6}{15}\right)$

D.  $\log\left(\frac{15}{6}\right)$

**Answer: B**



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80. If  $I = \int_3^4 \frac{1}{3\sqrt{\log x}} dx$  then

A.  $0.92 < I < 1$

B.  $I > 1$

C.  $I < 0.92$

D. none of these

**Answer: A**



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81. If  $I = \int_0^{1/2} \frac{1}{\sqrt{1-x^{2n}}} dx$  then which one of the following is not true

?

A.  $I < \frac{\pi}{6}$

B.  $I \geq \frac{1}{2}$

C.  $I > 0$

D. none of these

**Answer: D**

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82. If  $I = \int_0^{1/2} \frac{\sin^2 nx}{\sin^2 x} dx$  then which one of the following is not true ?

A.  $I_n = \frac{n\pi}{2}$

B.  $I_n = 2 \int_0^{\pi/2} \frac{\sin x \cos x 2nx}{\sin x} dx$

C.  $I_1, I_2, I_3, \dots, I_n \dots$  is a A.P.

D.  $\sin(I_{15})=0$

**Answer: D**

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83. For any integer  $n$ , the integral  $\int_0^\pi e^{\cos x} \cos^3(2n+1)x dx$  has the value

A.  $\pi$

B. 1

C. 0

D. none of these

**Answer: C**



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84. The value of the integral  $\int_0^{2a} \frac{f(x)}{f(x) + f(2a-x)} dx$  is equal to

A. 0

B.  $2a$

C.  $a$

D. none of these

**Answer: C**

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85. If  $\int_0^{\infty} \frac{\log(1+x^2)}{1+x^2} dx = k \int_0^{\infty} \frac{\log(1+x)}{1+x^2} dx$ , then  $k =$

A. 4

B. 8

C.  $\pi$

D.  $2\pi$

**Answer: B**

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86. If  $\int_{\log 2}^x \frac{1}{\sqrt{e^x - 1}} dx = \frac{\pi}{6}$  then  $x$  is equal to

A.  $e^2$

B.  $1/e$

C.  $\log 4$

D. none of these

**Answer: C**

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87. The value of the integral  $\int_0^{\pi} \log(1 + \cos x) dx$  is

A.  $\frac{\pi}{2} \log 2$

B.  $-\pi \log 2$

C.  $\pi \log 2$

D. none of these

**Answer: B**

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88. The integral  $\int_0^\pi \frac{1}{a^2 - 2a \cos x + 1} dx$  ( $a < 1$ ) is

A.  $\frac{\pi}{1 - a^2}$

B.  $\frac{\pi}{a^2 - 1}$

C.  $\frac{2\pi}{a^2 - 1}$

D.  $\frac{3\pi}{4}$

**Answer: A**



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89. The integral  $\int_0^{\pi/2} f(\sin 2x) \sin x dx$  is equal to

A.  $\int_0^{\pi/2} f(\cos 2x) \sin x dx = \sqrt{2} \int_0^{\pi/2} f(\cos 2x) \sin x dx$

B.  $\int_0^{\pi/2} f(\sin 2x) \cos x dx = \sqrt{2} \int_0^{\pi/4} f(\cos 2x) \cos x dx$

C.  $\int_0^{\pi/2} f(\cos 2x) \cos x dx = \sqrt{2} \int_0^{\pi/2} f(\cos 2x) \cos x dx$

$$D. \int_0^{\pi/2} f(\sin 2x) \cos x dx = \sqrt{2} \int_0^{\pi/2} f(\cos 2x) \cos x dx$$

**Answer: B**

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90.  $\int_0^{\pi} k(\pi x - x^2)^{100} \sin 2x \, dx$  is equal to

A.  $\pi^{100}$

B.  $\frac{1}{2}(\pi^{100} - \pi^{97})$

C.  $\frac{1}{2}(\pi^{100} + \pi^{97})$

D. 0

**Answer: D**

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91. The value of the integral  $\int_2^4 \frac{\sqrt{x^2 - 4}}{x^4} dx$  is

A.  $\sqrt{\frac{3}{32}}$

B.  $\frac{\sqrt{3}}{32}$

C.  $\frac{32}{\sqrt{3}}$

D.  $-\frac{\sqrt{3}}{32}$

**Answer: B**



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92. The value of the integral  $\int_0^\pi \frac{1}{a^2 - 2a \cos x + 1} dx (a > 1)$ , is

A.  $\frac{\pi}{1 - a^2}$

B.  $\frac{\pi}{a^2 - 1}$

C.  $\frac{2\pi}{a^2 - 1}$

D.  $\frac{2\pi}{1 - a^2}$

**Answer: A**



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93. If  $f(x)$  and  $g(x)$  are continuous functions satisfying  $f(x) = f(a - x)$  and  $g(x) + g(a - x) = 2$ , then  $\int_0^a f(x) g(x) dx$  is equal to

A.  $\int_0^a g(x) dx$

B.  $\int_0^a f(x) dx$

C. 0

D. none of these

**Answer: B**

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94.  $\int_0^{\pi/2} x(\sqrt{\tan x} + \sqrt{\cot x}) dx$  equals

A.  $\frac{\pi}{2\sqrt{2}}$

B.  $\frac{\pi^2}{2}$

C.  $\frac{\pi^2}{2\sqrt{2}}$

D.  $\frac{\pi^2}{2\sqrt{3}}$

**Answer: C**



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**95.** The value of the integral

$$\int_{1/3}^1 \frac{(x - x^3)^{1/3}}{x^4} dx \text{ is}$$

A. 6

B. 0

C. 3

D. 4

**Answer: A**



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96. The value of the integral  $\int_0^{100\pi} \sqrt{1 - \cos 2x} \, dx$  is

A.  $100\sqrt{2}$

B.  $200\sqrt{2}$

C. 0

D.  $400\sqrt{2}$

**Answer: B**



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97. The value of the integral

$$\int_{-1/2}^{1/2} \left\{ \left( \frac{x+1}{x-1} \right)^2 + \left( \frac{x-1}{x+1} \right)^2 - 2 \right\} dx \text{ is}$$

A.  $\log\left(\frac{4}{3}\right)$

B.  $4 \log\left(\frac{3}{4}\right)$

C.  $4 \log\left(\frac{4}{3}\right)$

D.  $\log\left(\frac{3}{4}\right)$

**Answer: C**



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98. The value of the integral  $\int_{1/e}^e |\log x| dx$ , is

A.  $2\left(\frac{e-1}{e}\right)$

B.  $2\left(\frac{1-e}{e}\right)$

C.  $2 - \frac{1}{e}$

D. none of these

**Answer: A**



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99. The value of  $\int_0^{\pi/2} \frac{\sin 8x \log \cot x}{\cos 2x} dx$ , is

A. 0

B.  $\pi$

C.  $\frac{5\pi}{2}$

D.  $\frac{3\pi}{2}$

**Answer: A**



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100. The value of  $\int_0^{\pi/2} x^{10} \sin x \, dx$ , is then the value of  $\mu_{10} + 90\mu_8$ , is

A.  $9\left(\frac{\pi}{2}\right)^8$

B.  $\left(\frac{\pi}{2}\right)^9$

C.  $10\left(\frac{\pi}{2}\right)^9$

D.  $9\left(\frac{\pi}{2}\right)^9$

**Answer: C**



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101. The value of  $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} dx$  is

A. 0

B. 1

C.  $\pi/2$

D.  $\pi/4$

**Answer: D**



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102. The value of  $\int_0^{\pi} \frac{\sin\left(n + \frac{1}{2}\right)x}{\sin\left(\frac{x}{2}\right)} dx$  is

A.  $\frac{\pi}{2}$

B. 0

C.  $\pi$

D.  $2\pi$

**Answer: C**

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103. If  $\frac{d}{dx} f(x) = g(x)$  for  $a \leq x \leq b$  then,  $\int_a^b f(x)g(x)dx$  equals

A.  $f(b) - f(a)$

B.  $g(b) - g(a)$

C.  $\frac{[f(b)]^2 - [f(a)]^2}{2}$

D.  $\frac{[g(b)]^2 - [g(a)]^2}{2}$

**Answer: C**

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104. For any integer  $n$ , the integral  $\int_0^3 e^{\sin^2 x} \cos^3(2n+1)x \, dx$  has the value

A.  $\pi$

B. 1

C. 0

D. none of these

**Answer: C**



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105. The value of the integral  $\int_0^3 \sqrt{3+x^3} dx$  lies in the interval

A. (1,3)

B. (2,30)



C.  $(4, 2\sqrt{30})$

D. none of these

**Answer: C**

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106. The value of the integral  $\int_0^1 \frac{1}{(1+x^2)^{3/2}} dx$  is

A.  $1/2$

B.  $1/\sqrt{2}$

C. 1

D.  $\sqrt{2}$

**Answer: B**

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107. If  $I = \int_0^{2\pi} \sin^2 x \, dx$ , then

A.  $I = 4 \int_0^{\pi} \sin^2 x \, dx = 4 \int_0^{\pi/2} \sin^2 x \, dx$

B.  $I = \int_0^{\pi/2} \cos^2 x \, dx$

C.  $I = 8 \int_0^{\pi/4} \sin^2 x \, dx$

D. none of these

**Answer: D**



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108. If  $\int_0^1 f(x) = M$ ,  $\int_0^1 g(x) dx = N$ , then which of the following is correct ?

A.  $\int_0^1 (f(x) + g(x)) dx = M + N$

B.  $\int_0^1 (f(x) + g(x)) dx = MN$

$$C. \int_0^1 (1)/(f(x))dx=(1)/(M)$$

$$D. \int_0^1 \frac{f(x)}{g(x)} dx = \frac{M}{N}$$

**Answer: A**



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**109.** The value of  $\int_0^{\pi/4} (\pi x - 4x^2) \log(1 + \tan x) dx$  is

A.  $\frac{\pi^3}{192} \log_e 2$

B.  $\frac{\pi^3}{192} \log \sqrt{2}$

C.  $\frac{\pi^3}{36} \log 2$

D.  $\frac{\pi^3}{48} \log \sqrt{2}$

**Answer: A**



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110. The value of  $\int_{-\pi/2}^{\pi/2} \sin\left\{\log\left(x + \sqrt{x^2 + 1}\right)\right\} dx$  is

A. 1

B. -1

C. 0

D. none of these

**Answer: C**



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111. The value of  $\int_0^{2\pi} \cos^{99} x dx$ , is

A. 1

B. -1

C. 99

D. 0

**Answer: D**

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112. If  $f(a+x)=f(x)$ , then  $\int_0^{na} f(x)dx$  is equal to ( $n \in N$ )

A.  $(n - 1) \int_0^a f(x)dx$

B.  $n \int_0^a f(x)dx$

C.  $\int_0^{(n-1)a} f(x)dx$

D. none of these

**Answer: B**

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113. If  $f(t)$  is a continuous function defined on  $[a,b]$  such that  $f(t)$  is an odd

function, then the function  $\phi(x) = \int_a^x f(t)dt$

- A. is an odd function
- B. is an even function
- C. is an increasing function on  $[a,b]$
- D. none of these

**Answer: B**

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**114.** If  $f(x)$  is an integrable function over every interval on the real line such that  $f(t+x)=f(x)$  for every  $x$  and real  $t$ , then

$\int_a^{a+1} f(x) dx$  is equal to

A.  $\int_0^a f(x) dx$

B.  $\int_0^t f(x) dx$

C.  $\int_a^t f(x) dx$

D. none of these

**Answer: B**



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115. If  $I_1 = \int_{3\pi}^0 f(\cos^2 x) dx$  and  $I_2 = \int_{\pi}^0 f(\cos^2 x)$  then

A.  $I_1 = I_2$

B.  $I_1 = 2I_2$

C.  $I_1 = 5I_2$

D. none of these

**Answer: D**



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116. If  $f(x)$  is a quadratic polynomial in  $x$  such that

$$6 \int_0^1 f(x) dx - \left\{ f(0) + 4f\left(\frac{1}{2}\right) \right\} = kf(1), \text{ then } k =$$

A. -1

B. 0

C. 1

D. 2

**Answer: C**

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117. The value of integral  $\int_{-2}^4 x[x] dx$  is

A.  $41/2$

B. 20

C.  $21/2$

D. none of these

**Answer: A**

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118. If  $h(a)=h(b)$ , the value of the integral

$$\int_a^b \left[ f(g(h(x)))^{-1} f'(g(h(x))) g'(h(x)) h'(x) \right] dx \text{ is equal to}$$

- A. 0
- B.  $f(a)-f(b)$
- C.  $f(g(a))-f(g(b))$
- D. none of these

**Answer: A**



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119. If  $F(x) = \frac{1}{x^2} \int_4^x [4t^2 - 2F'(t)] dt$  then  $F'(4)$  equals

- A. 32
- B.  $32/3$

C.  $32/9$

D. none of these

**Answer: C**



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120. If  $f(x)$  is an odd function defined on  $[-T/2, T/2]$  and has period  $T$ ,

then  $\phi(x) = \int_a^x f(t) dt$  is

A. a periodic function with period  $T/2$

B. a periodic function with period  $T$

C. not a periodic function

D. a periodic function with period  $T/4$

**Answer: B**



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121. If for every integer  $n$ ,  $\int_n^{n+1} f(x)dx = n^2$ , then the value of

$$\int_{-2}^4 f(x)dx, \text{ is}$$

- A. 16
- B. 14
- C. 19
- D. none of these

**Answer: C**



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122.  $\int_{-\pi+4}^{\pi/4} \frac{\tan^2 x}{1+a^x} dx$  is equal to

- A.  $\frac{\pi + 4}{4}$
- B.  $\frac{\pi - 4}{4}$
- C.  $\frac{a\pi}{4}$

D.  $\frac{a + \pi}{4}$

**Answer: B**

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123. The value of  $\int_0^{\pi/2} \cos ec(x - \pi/3) \cos ec(x - \pi/6) dx$  is

A.  $2 \log 3$

B.  $-2 \log 3$

C.  $\log 3$

D. none of these

**Answer: B**

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124. The value of  $\int_{-1}^1 x|x| dx$ , is

A. 2

B. 1

C. 0

D. none of these

**Answer: C**

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125.  $\int_0^3 |x^3 + x^2 + 3x| dx$  is equal to

A.  $\frac{171}{2}$

B.  $\frac{171}{4}$

C.  $\frac{170}{4}$

D.  $\frac{170}{3}$

**Answer: B**

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126. The value of the integral  $\int_0^3 \frac{dx}{\sqrt{x+1} + \sqrt{5x+1}}$  is

A.  $\frac{11}{15}$

B.  $\frac{14}{15}$

C.  $\frac{2}{5}$

D. none of these

**Answer: D**



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127.  $\int_1^{-1} \frac{x^3 + |x| + 1}{x^2 + 2|x| + 1} dx$  is equal to

A.  $\ln 3$

B.  $2 \ln 3$

C.  $\frac{1}{2} \ln 3$

D. none of these

**Answer: D**

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128.  $\int_{-\frac{\pi}{2}}^{\pi/2} \log_e \left\{ \left( \frac{ax^2 + bx + c}{ax^2 - bx + c} \right) (a + b) |\sin x| \right\} dx$  is equal to

A.  $\pi \log_e (a + b)$

B.  $\pi \log_e \left( \frac{a + b}{2} \right)$

C.  $\frac{\pi}{2} \log_e (a + b)$

D. none of these

**Answer: B**

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129. For any natural number  $n$ , the value of the integral

$$\int_0^{\sqrt{n}} [x^2] dx \text{ is}$$

A.  $n\sqrt{n} + \sum_{r=1}^n \sqrt{r}$

B.  $n\sqrt{n} - \sum_{r=1}^n \sqrt{r}$

C.  $\sum_{r=1}^n \sqrt{r} - n\sqrt{n}$

D. none of these

**Answer: B**



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130. For any  $n \in R^+$ , the value of the integral

$$\int_0^{n[x]} (x - [x]) dx \text{ is}$$

A.  $n[x]$

B.  $[x]$



C.  $\frac{n}{2}[x]$

D. none of these

**Answer: C**



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131. If  $\phi'(x) = \frac{\log_e |\sin x|}{x}$ ,  $x \neq \pi$ ,  $n \in Z$  and

$\int_1^3 \frac{3 \log_e |\sin x^3|}{x} dx = \phi(k) - \phi(1)$ , then the possible value of k, is

A. 27

B. 18

C. 9

D. none of these

**Answer: A**



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132. The equation

$$\int_{-\pi/4}^{\pi/4} \left\{ a|\sin x| + \frac{b \sin x}{1 + \cos x} + c \right\} dx = 0 \text{ where } a, b, c \text{ are constants,}$$

gives a relation between

A. a, b and c

B. a and c

C. a and b

D. b and c

**Answer: B**



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133. Let  $f(x)$  be a continuous function such that  $f(a-x)+f(x)=0$  for all  $x \in [0, a]$ . Then, the value of the integral

$$\int_0^a \frac{1}{1 + e^{f(x)}} dx \text{ is equal to}$$

A. a

B.  $\frac{a}{2}$

C.  $f(a)$

D.  $\frac{1}{2}f(a)$

**Answer: B**

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134. The value of  $\int_{\alpha}^{\beta} x|x|dx$ , where  $a < 0 < \beta$ , is

A.  $\frac{1}{2}(\alpha^2 + \beta^2)$

B.  $\frac{1}{3}(\beta^2 - \alpha^2)$

C.  $\frac{1}{3}(\alpha^2 + \beta^2)$

D. none of these

**Answer: D**

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135.  $\int_{-\pi/2}^{\pi/2} \frac{|x|}{8 \cos^2 2x + 1} dx$  has the value

A.  $\frac{\pi^2}{6}$

B.  $\frac{\pi^2}{12}$

C.  $\frac{\pi^2}{24}$

D. none of these

**Answer: B**



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136. If  $[.]$  denotes the greatest integer function and

$$f(x) = \begin{cases} 3[x] - \frac{5|x|}{x}, & x \neq 0 \\ 2, & x = 0 \end{cases}$$

then  $\int_{-3/2}^2 f(x) dx$  is equal to

A.  $-\frac{11}{2}$

B.  $-\frac{7}{2}$

C. -6

D.  $-\frac{17}{2}$

**Answer: A**



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137. Find the value of  $\int_{-1}^1 [x^2 + \{x\}] dx$ , where  $[.]$  and  $\{.\}$  denote the greatest function and fractional parts of  $x$ , respectively.

A.  $\frac{5 + \sqrt{5}}{2}$

B.  $\frac{5 - \sqrt{5}}{2}$

C.  $-\frac{5 + \sqrt{5}}{2}$

D. none of these

**Answer: B**



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138. The value of

$$\int_{-1}^1 \sin^{-1} \left[ x^2 + \frac{1}{2} \right] dx + \int_{-1}^1 \cos^{-1} \left[ x^2 - \frac{1}{2} \right] dx, \text{ where } [.] \text{ denotes the}$$

greatest integer function, is

A.  $\pi$

B.  $2\pi$

C.  $4\pi$

D. 0

Answer: B

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139. Let  $\Delta(y) = \begin{vmatrix} y+a & y+b & y+a-c \\ y+b & y+c & y-1 \\ y+c & y+d & y-b+d \end{vmatrix}$

and,  $\int_0^2 \Delta(y) dy = -16$ , where a,b,c,d are in A.P., then the common difference of the A.P. is equal to

A.  $\pm 1$

B.  $\pm 2$

C.  $\pm 3$

D. none of these

**Answer: B**



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140. If  $I = \int_0^1 \frac{1}{1 + x^{\pi/2}} dx$ , then\

A.  $I > \ln 2$

B.  $I < \ln 2$

C.  $I < \frac{\pi}{4}$

D.  $I > \frac{\pi}{4}$

**Answer: A**



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141. If  $\int_0^x f(t) dt = x^2 + 2x - \int_0^x t f(t) dt$ ,  $x \in (0, \infty)$ . Then,  $f(x)$  is

- A. Periodic
- B. Periodic but fundamental does not exist
- C. Periodic but fundamental period exists
- D. Nothing can be said

**Answer: A::B**



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142. The value of  $\int_{-6}^6 \max(|2 - |x||, 4 - |x|, 3) dx$  is

- A. 40
- B. 50
- C. 1
- D.  $\frac{2}{5}$



**Answer: A**



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**143.** If  $I_n = \int_0^\pi e^x (\sin x)^n dx$ , then  $\frac{I_3}{I_1}$  is equal to

A.  $\frac{3}{5}$

B.  $\frac{1}{5}$

C. 1

D.  $\frac{2}{5}$

**Answer: A**



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**144.** Given that

$$\lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{\log(n^2 + r^2) - 2 \log n}{n} = \log 2 + \frac{\pi}{2} - 2, \text{ then}$$

$$\lim_{n \rightarrow \infty} \frac{1}{n^{2m}} \left[ (n^2 + 1^2)^m (n^2 + r^2)^m \dots (n^2)^m \right]^{1/n} \text{ is equal to}$$

A.  $2^m e^{m\left(\frac{\pi}{2}-2\right)}$

B.  $2^m e^{m\left(2-\frac{\pi}{2}\right)}$

C.  $e^m\left(\frac{\pi}{2}-2\right)$

D.  $e^{2m\left(\frac{\pi}{2}-2\right)}$

**Answer: A**



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**145.** Let  $f(x)$  be a differentiable function such that

$$f'(x) = f(x) + \int_0^2 f(x) dx \text{ and } f(0) = \frac{4 - e^2}{3}. \text{ Then } f(x) =$$

A.  $e^x - \left(\frac{e^2 - 1}{3}\right)$

B.  $e^x + \left(\frac{e^2 - 1}{3}\right)$

C.  $e^x - \left(\frac{e^2 + 1}{3}\right)$

D. none of these

**Answer: A**



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146. Let  $f(x)$  be a differentiable function satisfying  $f'(x) = f(x) + \int_0^2 f(x) dx$  such that  $f(0) = \frac{4 - e^2}{3}$ . Then the number of solutions of  $f(x) + x = 0$ , is

A. 0

B. 1

C. 2

D. 3

Answer: B



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147. The value of the integral  $\int_{-10}^0 \frac{\left| \frac{2[x]}{3x - [x]} \right|}{\left( \frac{2[x]}{3x - [x]} \right)} dx$  where  $[.]$  denotes GIF

A.  $\frac{28}{3}$

B. 0

C. 10

D. -10

**Answer: A**

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## Chapter Test 1

1.  $\int_{-\pi/2}^{\pi/2} \sin^2 x \cos^2 x (\sin x + \cos x) dx =$

A.  $2/15$

B.  $4/15$

C.  $2/15$

D. 0

**Answer: D**



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2.  $\lim_{n \rightarrow \infty} \frac{1}{n^2} \sum_{r=1}^n r e^{r/n} =$

A. 0

B. 1

C. e

D. 2e

**Answer: B**



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3. The value of the integral  $\int_{-1}^1 \sin^{11} x \, dx$  is

A.  $\frac{10}{11} \cdot \frac{8}{9} \cdot \frac{6}{7} \cdot \frac{4}{5} \cdot \frac{2}{3}$

B.  $\frac{10}{11} \cdot \frac{8}{9} \cdot \frac{6}{7} \cdot \frac{4}{5} \cdot \frac{2}{3} \cdot \frac{\pi}{2}$

C. 1

D. 0

**Answer: D**



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4. The value of  $\int_{-\pi}^{\pi} (1 - x^2) \sin x \cos^2 x \, dx$ , is

A. 0

B.  $\pi - \frac{\pi^3}{3}$

C.  $2\pi - \pi^3$

D.  $\frac{\pi}{2} - 2\pi^3$

**Answer: A**



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5.  $\int_{-\pi}^{\pi} [\cos px - \sin qx]^2 dx$  where  $p, q$  are integers is equal to

A.  $-\pi$

B. 0

C.  $\pi$

D.  $2\pi$

**Answer: D**



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6. If  $\int_0^{\pi/3} \frac{\cos x}{3 + 4 \sin x} dx = k \log \left( \frac{3 + 2\sqrt{3}}{3} \right)$ , then  $k$  is

A.  $1/2$

B.  $1/3$

C.  $1/4$

D.  $1/8$

**Answer: C**

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7. The value of  $\int_3^5 \frac{x^2}{x^2 - 4} dx$ , is

A.  $2 - \log_e \left( \frac{15}{7} \right)$

B.  $2 + \log_e \left( \frac{15}{7} \right)$

C.  $2 + 4 \log_e 3 - 4 \log_e 7 + 4 \log_e 5$

D.  $2 - \tan^{-1} \left( \frac{15}{7} \right)$

**Answer: B**

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8. The greater value of  $(x) = \int_{-1/2}^x |t| dt$  on the interval  $[-1/2, 1/2]$ , is

A.  $\frac{3}{8}$



B.  $\frac{1}{4}$

C.  $-\frac{3}{8}$

D.  $-\frac{1}{2}$

**Answer: B**



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9.  $f(x) = \begin{cases} 1 - x, & 0 \leq x \leq 1 \\ 0, & 1 \leq x \leq 2 \\ (2 - x)^2, & 2 \leq x \leq 3 \end{cases}$  and  $\phi(x) = \int_0^x f(t) dt$ . Then for any

$x \in [2, 3]$ ,  $\phi(x)$  equals

A.  $\frac{(x - 2)^3}{3}$

B.  $\frac{1}{2} - \frac{(x - 2)^3}{3}$

C.  $\frac{1}{2} + \frac{(x - 2)^3}{3}$

D. none of these

**Answer: C**

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10. If  $f(x) = \int_x^{-1} |t| dt$ , then for any  $x \geq 0$ ,  $f(x)$  equals

A.  $\frac{1}{2}(1 - x^2)$

B.  $\frac{1}{2}x^2$

C.  $\frac{1}{2}(1 + x^2)$

D. none of these

**Answer: C**

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11.  $\int_0^2 (x - \log_2 a) dx = 2 \log\left(\frac{2}{a}\right)$ , if

A.  $a=2$

B.  $a > 2$

C. 3

D. 4

**Answer: A**



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12. If  $\int_1^a (a - 4x)dx \geq 6 - 5a$ ,  $a > 1$ , then  $a$  equals

A. 1

B. 2

C. 3

D. 4

**Answer: B**



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13. The value of  $\int_1^2 \{f(g(x))\}^{-1} f'(g(x)) g'(x) dx$ , where  $g(1)=g(2)$ , is equal to

A. 1

B. 2

C. 0

D. none of these

**Answer: C**



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14. If  $\frac{C_0}{1} + \frac{C_1}{2} + \frac{C_2}{3} = 0$ , where  $C_0, C_1, C_2$  are all real, the equation  $C_2x^2 + C_1x + C_0 = 0$  has

A. at least one root in (0,1)

B. one root in (1,2) and the other in (3,4)

C. one root in (-1,1) and the other in (-5,2)

D. both roots imaginary

**Answer: A**



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15. The solution of the equation  $\int_{\log_2}^x \frac{1}{e^x - 1} dx = \frac{\log(3)}{2}$  is given by x=

A.  $e^2$

B.  $1/e$

C.  $\log 4$

D. none of these

**Answer: C**



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16. If  $\int_a^b \frac{x^n}{x^n + (16 - x)^n} dx = 6$ , then

A.  $a = 4, b = 12, n \in R$

B.  $a = 2, b = 14, n \in R$

C.  $a = -4, b = 20, n \in R$

D.  $a = 2, b = 8, n \in R$

**Answer: B**

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17. Let  $m$  be any integer. Then, the integral  $\int_0^\pi \frac{\sin 2mx}{\sin x} dx$  equals

A. 0

B.  $\pi$

C. 1

D. none of these

**Answer: A**

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18.  $\int_{-\pi/4}^{\pi/4} e^{-x} \sin x \, dx$  is

A.  $-\frac{\sqrt{2}}{2}e^{\pi/4}$

B.  $\frac{\sqrt{2}}{2}e^{-\pi/4}$

C.  $\sqrt{2}(e^{-\pi/4} - e^{\pi/4})$

D. zero

**Answer: A**



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19.  $\frac{d}{dx}(f(x)) = \phi(x)$  for  $a \leq x \leq b$ ,  $\int_a^b f(x)\phi(x)dx =$

A.  $f(b) - f(a)$

B.  $\phi(b) - \phi(a)$

C.  $\frac{[f(b)]^2 - [f(a)]^2}{1 + e^x}$

D.  $\frac{[\phi(b)]^2 - [\phi(a)]^2}{2}$

**Answer: C**



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20.  $\int_{-\pi/2}^{\pi/2} \frac{\cos x}{1 + e^x} dx =$

A. 1

B. 0

C. -1

D. none of these

**Answer: A**



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21.  $\int_0^{\infty} \frac{dx}{[x + \sqrt{x^2 + 1}]^3} dx =$



A.  $\frac{3}{8}$

B.  $\frac{1}{8}$

C.  $-\frac{3}{8}$

D. none of these

**Answer: A**



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22.  $\int_0^{\infty} \frac{x}{(1-x)^{3/4}} dx =$

A.  $\frac{12}{5}$

B.  $\frac{16}{5}$

C.  $-\frac{16}{5}$

D. none of these

**Answer: B**



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23.  $\int_0^{\pi} x \sin x \cos^4 x dx =$

A.  $\frac{\pi}{10}$

B.  $\frac{\pi}{5}$

C.  $-\frac{\pi}{5}$

D. none of these

**Answer: B**



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24.  $\int_0^{\pi} [2 \sin x] dx =$

A.  $2\pi/3$

B.  $-5\pi/3$

C.  $-\pi$

D.  $-2\pi$

**Answer: A**



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25.  $\int_{\pi/2}^{3\pi/2} [2 \cos x] dx$  is equal to

A.  $\frac{5\pi}{3}$

B.  $-\frac{5\pi}{3}$

C.  $-\pi$

D.  $-2\pi$

**Answer: B**



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26. If  $f(x)$  satisfies the conditions of Rolle's theorem in  $[1,2]$  and is continuous on  $[1,2]$ , then  $\int_1^2 f'(x) dx$  is equal to

A. 3

B. 0

C. 1

D. 2

**Answer: B**



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27. For  $y = f(x) = \int_0^x 2|t|dt$ , the tangent lines parallel to the bi-sector of the first quadrant angle are

A.  $y = x \pm \frac{1}{4}$

B.  $y = x \pm \frac{3}{2}$

C.  $y = x \pm \frac{1}{2}$

D. none of these

**Answer: A**



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28. If  $f(x) = ae^{2x} + be^x + cx$ , satisfies the conditions  $f(0)=-1$ ,  $f'(\log 2)=31$ ,

$$\int_0^{\log 4} (f(x) - cx) dx = \frac{39}{2}, \text{ then}$$

A.  $a=5, b=6, c=3$

B.  $a=5, b=-6, c=3$

C.  $a=-5, b=6, c=3$

D. none of these

**Answer: B**



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29.  $\int_{\pi}^{2\pi} [\sqrt{2} \cos x] dx =$

A.  $-\pi/2$

B.  $\pi/2$

C.  $\pi$

D. none of these

**Answer: A**



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30.  $\int_0^{\pi/3} [\sqrt{3} \tan x] dx =$

A.  $\frac{5\pi}{6}$

B.  $\frac{5\pi}{6} - \tan^{-1}\left(\frac{2}{\sqrt{2}}\right)$

C.  $\frac{\pi}{2} - \tan^{-1}\left(\frac{2}{\sqrt{2}}\right)$

D. none of these

**Answer: D**

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31.  $\int_{3\pi/2}^{5\pi/3} [2 \cos x] dx =$

A.  $\frac{5\pi}{3}$

B.  $\frac{4\pi}{3}$

C.  $\frac{2\pi}{3}$

D. none of these

**Answer: D**

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32.  $\int_0^{50\pi} \cos x \, dx =$

A. 100

B. 50

C. 0

D. none of these

**Answer: A**



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33. If  $a$  be a positive integer, the number of values of  $a$  satisfying

$$\int_0^{\pi/2} \left\{ a^2 \left( \frac{\cos 3x}{4} + \frac{3}{4} \cos x \right) + a \sin x - 20 \cos x \right\} dx \leq -\frac{a^2}{2}, \text{ is}$$

A. only one

B. two

C. three

D. four

**Answer: D**



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34. The values of 'a' for which  $\int_0^a (3x^2 + 4x - 5) dx < a^3 - 2$  are

A.  $\frac{1}{2} < a < 2$

B.  $\frac{1}{2} \leq a \leq 2$

C.  $a \leq \frac{1}{2}$

D.  $a \geq 2$

**Answer: A**



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35. If  $(-1,2)$  and  $(2,4)$  are two points on the curve  $y=f(x)$  and if  $g(x)$  is the gradient of the curve at point  $(x,y)$  then the value of the integral

$$\int_{-1}^2 g(x) dx \text{ is}$$

A. 2

B. -2

C. 0

D. 1

**Answer: A**



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36. If  $I_1 = \int_{1-x}^k x \sin\{x(1-x)\}dx$  and  $I_2 = \int_{1-x}^k \sin\{x(1-x)\}dx$ ,

then

A.  $I_1 = 2I_2$

B.  $2I_1 = I_2$

C.  $I_1 = I_2$

D. none of these

**Answer: B**



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37. If  $\int_{-\pi/3}^{\pi/3} \left( \frac{a}{3} |\tan x| + \frac{b \tan x}{1 + \sec x} + c \right) dx = 0$  where a, b, c are constants, then c =

A.  $a \ln 2$

B.  $\frac{a}{\pi} \ln 2$

C.  $-\frac{a}{\pi} \ln 2$

D.  $\frac{2a}{\pi} \ln 2$

Answer: C



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38. If  $x = \int_2^{\sin t} \sin^{-1} \theta d\theta$  and  $y = \int_n^{\sqrt{t}} \frac{\sin \theta^2}{\theta} d\theta \frac{dy}{dx}$  is equal to

A.  $\frac{\sin t}{2t^2}$

B.  $\frac{2t^2}{\tan t}$

C.  $\frac{\tan t}{t^2}$

D. none of these

**Answer: A**



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39.  $\left| \int_{10}^{19} \frac{\sin x}{1+x^8} dx \right|$  is less than

A.  $10^{-10}$

B.  $10^{-11}$

C.  $10^{-7}$

D.  $10^{-9}$

**Answer: C**



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40. The smallest interval  $[a, b]$  such that

$$\int_0^1 \frac{1}{\sqrt{1+x^4}} dx \in [a, b], \text{ is}$$

A.  $\left[ \frac{1}{\sqrt{2}}, 1 \right]$

B.  $[0, 1]$

C.  $\left[ \frac{1}{2}, 1 \right]$

D.  $\left[ \frac{3}{4}, 1 \right]$

**Answer: A**



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41. Let  $I_n = \int_0^{\pi/2} \sin^n x dx, n \in N$ . Then

A.  $I_n : I_{n-2} = n : (n-1)$

B.  $I_n > I_{n-2}$

C.  $n(I_{n-2} - I_n) = I_{n-2}$

D. none of these

**Answer: C**



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42. If  $f(x) = \int_0^x \sin^4 t dt$ , then  $f(x + 2\pi)$  is equal to

A.  $f(x)$

B.  $f(x) + f(2\pi)$

C.  $gf(x) - f(2\pi)$

D.  $f(x) \cdot f(2\pi)$

**Answer: B**



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43.  $\int_0^\pi \frac{1}{1 + 3^{\cos x}} dx$  is equal to

A.  $\pi$

B. 0

C.  $\pi/2$

D. none of these

**Answer: C**



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44. Let  $\int_0^a f(x)dx = \lambda$  and  $\int_0^a f(2a - x)dx = \mu$ . Then,  
 $\int_0^{2a} f(x)dx$  equal to

A.  $\lambda + \mu$

B.  $\lambda - \mu$

C.  $2\lambda - \mu$

D.  $\lambda - 2\mu$

**Answer: A**



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45. The value of  $\int_{\pi/4}^{3\pi/4} \frac{x}{1 + \sin x} dx$  is equal to

A.  $(\sqrt{2} - 1)\pi$

B.  $(\sqrt{2} + 1)\pi$

C.  $\pi$

D. none of these

**Answer: A**



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46. Let  $I_n = \int_0^{\pi/2} \cos^n x \cos nx dx$ . Then,  $I_n : I_{n+1}$  is equal to

A. 3 : 1

B. 2 : 3



C. 2:1

D. 3:4

**Answer: C**



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47. The value of  $\int_{-1}^1 \max [2 - x, 2, 1 + x] dx$  is

A. 4

B.  $9/2$

C. 2

D. none of these

**Answer: B**



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48.  $\int_0^{\pi/4} \sin(x - [x]) dx$  is equal to

A.  $\frac{1}{2}$

B.  $1 - \frac{1}{\sqrt{2}}$

C. 1

D. none of these

**Answer: B**



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49. The value of the integral  $\int_{-1}^1 (x - [2x]) dx$ , is

A. 1

B. 0

C. 2

D. 4

**Answer: A**



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50. Let  $f: R \in R$  be a continuous function such that  $f(1)=2$ . If

$$\lim_{x \rightarrow 1} \int - (2)^{f(x)} \frac{2t}{x-1} dt = 4, \text{ then the value of } f'(1) \text{ is}$$

A. 1

B. 2

C. 4

D. none of these

**Answer: A**



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51. Let  $f: R \in R$  be a continuous function such that  $f(x)$  is not identically

equal to zero. If  $\int_0^x |x-2| dx, x \geq 0$ . Then,  $f'(x)$  is

- A. an even function
- B. an odd function
- C. a periodic function
- D. none of these

**Answer: D**

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52. Let  $f(x) = \int_0^x |x - 2| dx, \geq 0$ . Then,  $f'(x)$  is

- A. continuous and non differentiable at  $x=2$
- B. discontinuous at  $x=4$
- C. neither continuous nor differentiable at  $x=2$
- D. non-differentiable at  $x=4$

**Answer: A**

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53.  $\lim_{n \rightarrow \infty} \left\{ \frac{n!}{(kn)^n} \right\}^{\frac{1}{n}}$ ,  $k \neq 0$ , is equal to (A)  $\frac{k}{e}$  (B)  $\frac{e}{k}$  (C)  $\frac{1}{ke}$  (D) none

of these

A.  $ke$

B.  $\frac{e}{k}$

C.  $\frac{k}{e}$

D.  $\frac{1}{ke}$

**Answer: D**

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54. Let  $f(x)$  be an integrable function defined on  $[a,b], b > a > 0$ . If

$$I_1 = \int_{\pi/6}^{\pi/3} f(\tan \theta + \cos \theta) \sec^2 \theta d\theta \text{ and,}$$

$$I_2 = \int_{\pi/6}^{\pi/3} f(\tan \theta + \cot \theta) \cos e c^2 \theta d\theta, \text{ then } \frac{I_1}{I_2} =$$

- A. a positive integer
- B. a negative integer
- C. an irrational number none of these
- D. none of these

**Answer: A**

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55.  $\int_0^{\sqrt{2}} [x^2] dx$ , is

- A.  $2 - \sqrt{2}$
- B.  $2 + \sqrt{2}$
- C.  $\sqrt{2} - 1$
- D.  $\sqrt{2} - 2$

**Answer: C**

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56. Let  $f(x)$  be a function satisfying  $f'(x)=f(x)$  with  $f(0)=1$  and  $g(x)$  be a function that satisfies  $f(x) + g(x) = x^2$ , Then the value of the integral

$$\int_0^1 f(x)g(x)dx, \text{ is}$$

A.  $e + \frac{e^2}{2} + \frac{5}{2}$

B.  $e - \frac{e^2}{2} - \frac{5}{2}$

C.  $e + \frac{e^2}{2} - \frac{3}{2}$

D.  $e - \frac{e^2}{2} - \frac{3}{2}$

**Answer: D**

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57. 
$$\left( \sum_{n=1}^{10} \int_{-2n-1}^{-2n} \sin^{27}(x)dx + \sum_{n=1}^{10} \int_{2n}^{2n+1} \sin^{27}(x)dx \right)$$

A.  $27^2$

B. -54

C. 54

D. 0

**Answer: D**



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58. If  $f(y) = e^y = e^y$ ,  $g(y) = y$ ,  $y > 0$  and  $F(t) = \int_0^t f(t-y)g(y)dy$ ,

then

A.  $F(t) = te^{-t}$

B.  $F(t) = 1 - e^{-t}(t + 1)$

C.  $F(t) = e^t - (1 + t)$

D.  $F(t) = te^t$

**Answer: D**



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59. If  $I_n = \int_0^{\pi/2} x^n \sin x dx$ , then  $I_4 + 12I_2$  is equal to\

A.  $4\pi$

B.  $3\left(\frac{\pi}{2}\right)^3$

C.  $\left(\frac{\pi}{2}\right)^2$

D.  $4\left(\frac{\pi}{2}\right)^3$

**Answer: C**



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60.  $\int_0^1 \sin \left\{ 2 \tan^{-1} \sqrt{\frac{1+x}{1-x}} \right\} dx =$

A.  $\pi/6$

B.  $\pi/4$

C.  $\pi/2$

D.  $\pi$

**Answer: B**

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## Chapter Test 2

1. The integral  $\int_0^{r\pi} \sin^{2x} x dx$  is equal to

A.  $r \int_0^{\pi} \sin^{2x} x dx$

B.  $2r \int_0^{\pi} \sin^{2x} x dx$

C.  $r \int_0^{\pi/2} \sin^{2x} x dx$

D. none of these

**Answer: C**

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2. The value of the integral  $\int_0^2 x[x]dx$

A.  $\frac{7}{2}$

B.  $\frac{3}{2}$

C.  $\frac{5}{2}$

D. none of these

**Answer: B**



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3. The value of integral  $\sum_{k=1}^n \int_0^1 f(k-1+x)dx$  is

A.  $\int_0^1 f(x)dx$

B.  $\int_0^2 f(x)dx$

C.  $\int_0^2 f(x)dx$

$$D. n \int_0^2 f(x) dx$$

**Answer: C**

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4. Let  $f(x)$  be a function satisfying  $f'(x)=f(x)$  with  $f(0)=1$  and  $g(x)$  be the function satisfying  $f(x) + g(x) = x^2$ . The value of integral

$$\int_0^1 f(x)g(x) dx \text{ is,}$$

A.  $\frac{1}{4}(e - 7)$

B.  $\frac{1}{4}(e - 2)$

C.  $\frac{1}{4}(e - 3)$

D. none of these

**Answer: D**

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5. If  $I = \int_0^1 \cos \left\{ 2 \cot^{-1} \sqrt{\frac{1-x}{1+x}} \right\} dx$  then

A.  $I > \frac{1}{2}$

B.  $I = -\frac{1}{2}$

C.  $0 < I < \frac{1}{2}$

D.  $I = \frac{1}{2}$

**Answer: B**



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6. The value of  $\int_a^{a+(\pi/2)} (\sin^4 x + \cos^4 x) dx$  is

A.  $\frac{3\pi}{8}$

B.  $a \left( \frac{\pi}{2} \right)^2$

C.  $\frac{3\pi a^2}{8}$

D. none of these

**Answer: A**



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7. The value of  $\int_{-1}^2 \frac{|x|}{x} dx$  is

A. 0

B. 1

C. 3

D. none of these

**Answer: B**



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8. The value of  $\int_0^1 \frac{x^3}{1+x^8} dx$  is

A.  $\frac{\pi}{4}$

B.  $\frac{\pi}{8}$

C.  $\frac{\pi}{16}$

D. none of these

**Answer: C**



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9. The value of  $\int_0^3 x\sqrt{1+x}dx$ , is

A.  $\frac{9}{2}$

B.  $\frac{27}{4}$

C.  $\frac{126}{15}$

D.  $\frac{116}{15}$

**Answer: D**



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10. The value of the integral  $\int_0^1 \log \sin\left(\frac{\pi x}{2}\right) dx$  is

A.  $\log 2$

B.  $-\log 2$

C.  $\frac{\pi}{2} \log 2$

D.  $-\frac{\pi}{2} \log 2$

**Answer: B**



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11. The value of the integral  $\int_0^\pi x \log \sin x dx$  is

A.  $\frac{\pi}{2} \log 2$

B.  $\frac{\pi^2}{2} \log 2$

C.  $-\frac{\pi^2}{2} \log 2$

D. none of these



**Answer: C**

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12. If  $I_1 = \int_0^{\infty} \frac{dx}{1+x^4}$  and  $I_2 = \int_0^{\infty} dx$  then  $\frac{I_1}{I_2} =$

A. 1

B. 2

C. 1/2

D. none of these

**Answer: A**

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13. If  $f(x) = \begin{cases} x & \text{for } x < 1 \\ x - 1 & \text{for } x \geq 1 \end{cases}$ , then  $\int_0^2 x^2 f(x) dx$  is equal to

A. 1

B.  $\frac{4}{3}$

C.  $\frac{5}{3}$

D.  $\frac{5}{2}$

**Answer: C**



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14. The value of the integral  $\int_0^2 \frac{1}{(x^2 + 1)^{3/2}} dx$  is

A.  $1/2$

B.  $\sqrt{2}/2$

C. 1

D.  $\sqrt{2}$

**Answer: B**



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15. If  $\int_0^{2a} f(x) dx = \int_0^{2a} f(x) dx$ , then

- A.  $f(2a - x) = -f(x)$
- B.  $f(2a - x) = f(x)$
- C.  $f(x)$  is an odd function
- D.  $f(x)$  is an even function

**Answer: B**



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16. If  $\int_0^{36} \frac{1}{2x + 9} dx = \log k$ , is equal to

- A. 3
- B.  $9/2$
- C. 9

**Answer: A** [Watch Video Solution](#)

17. The value of the integral  $\int_0^{\pi/2} \sin^6 x dx$ , is

A.  $\frac{3\pi}{4}$

B.  $\frac{5}{32}\pi$

C.  $\frac{3}{16}\pi$

D. none of these

**Answer: B** [Watch Video Solution](#)

18. If  $\int_0^{\infty} e^{-x^2} dx = \sqrt{\frac{\pi}{2}}$  then  $\int_0^{\infty} e^{-ax^2} dx$ ,  $a > 0$ , s

A.  $\frac{\sqrt{\pi}}{2}$

B.  $\frac{\sqrt{\pi}}{2a}$

C.  $2\frac{\sqrt{\pi}}{a}$

D.  $\frac{1}{2}\left(\sqrt{\frac{\pi}{a}}\right)$

**Answer: D**



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19. The value of the integral  $\int_0^{\infty} \frac{1}{1+x^4} dx$  is

A.  $\frac{\pi}{2}$

B.  $\frac{\pi}{\sqrt{2}}$

C.  $\frac{\pi}{2\sqrt{2}}$

D. none of these

**Answer: C**



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20. If  $\int_{\pi/2}^x \sqrt{3 - 2 \sin^2 u} dx + \int_{dx}^{dy}$  equal  $\pi/2$

A.  $\frac{\sqrt{4 - 3 \sin^2 x}}{\cos y}$

B.  $-\frac{\sqrt{3 - 2 \sin^2 x}}{\cos y}$

C.  $\sqrt{3 - 2 \sin^2 x} + \cos y$

D. none of these

**Answer: B**



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21. The value of  $\alpha \in [0, 2\pi]$  which does not satisfy the equation

$$\int_{\pi/2}^{\alpha} \sin x dx = \sin 2\alpha, \text{ is}$$

A.  $\pi$

B.  $\frac{3\pi}{2}$

C.  $\frac{7\pi}{6}$

D.  $\frac{11\pi}{6}$

**Answer: A**



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22.  $\lim_{x \rightarrow 0} \frac{\int_0^t (x^2) \sin \sqrt{t} dt}{x^3}$  is equal to

A.  $1/3$

B. 1

C.  $2/3$

D. none of these

**Answer: C**



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23. If  $x$  satisfies the equation

$$x^2 \left( \int_0^1 \frac{dt}{t^2 + 2t \cos \alpha + 1} \right) - x \left( \int_{-3}^3 \frac{t^2 + \sin 2t}{t^2 + 1} \right) - 2 = 0$$

( $0 < \alpha < \pi$ ), then the value of  $x$ , is

A.  $\pm 2\sqrt{\frac{\sin \alpha}{\alpha}}$

B.  $\pm \sqrt{\frac{\sin \alpha}{\alpha}}$

C.  $\pm 4\sqrt{\frac{\sin \alpha}{\alpha}}$

D. none of these

**Answer: A**



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24. The value of  $\alpha \in (-\pi, 0)$  satisfying  $\sin \alpha + \int_{\alpha}^{2\alpha} \cos 2x dx = 0$ , is

A.  $-\pi/2$

B.  $-\pi$



C.  $-\pi/3$

D.  $\pi$

**Answer: C**

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25. The value of  $\int_0^{\pi/2} \frac{\sin^3 x \cos x}{\sin^4 x + \cos^4 x} dx$  is

A.  $\pi/8$

B.  $\pi/4$

C.  $\pi/2$

D.  $\pi$

**Answer: A**

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26. The value of  $\int_0^\pi \frac{1}{5 + 3 \cos x} dx$ , is

A.  $\pi$

B.  $2\pi/3$

C.  $\pi/4$

D. 2

**Answer: C**



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27.  $\lim_{n \rightarrow \infty} \left[ \sin' \frac{\pi}{n} + \sin' \frac{2\pi}{n} + \dots + \sin' \frac{(n-1)}{n} \pi \right]$  is equal to :

A. 0

B.  $\pi$

C. 2

D. none of these

**Answer: C**

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28.  $\lim_{n \rightarrow \infty} \sum_{r=1}^n \left\{ \frac{r^3}{r^4 + n^4} \right\}$  equals

A.  $\log 2$

B.  $\frac{1}{2} \log 2$

C.  $\frac{1}{3} \log 2$

D.  $\frac{1}{4} \log 2$

**Answer: D**

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29.  $\lim_{n \rightarrow \infty} \left[ \left(1 + \frac{1}{n}\right) \left(1 + \frac{2}{n}\right) \left(1 + \frac{n}{n}\right) \right]^{\frac{1}{n}}$

A.  $e/4$

B.  $4/e$

C.  $2/e$

D. none of these

**Answer: B**



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30. Evaluate:  $(\lim)_{n \rightarrow \infty} n \left[ \frac{1}{na} + \frac{1}{na+1} + \frac{1}{na+2} + \dots + \frac{1}{nb} \right]$

A.  $\log\left(\frac{b}{a}\right)$

B.  $\log\left(\frac{a}{b}\right)$

C.  $\log a$

D.  $\log b$

**Answer: A**



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31. The solution of the equation  $\int_0^x \frac{1}{x\sqrt{2^2 - 1}} dx = \frac{\pi}{12}$ , is

A.  $x=3$

B.  $x=4$

C.  $x=1$

D. none of these

**Answer: D**



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32. Let  $I_n = \int_0^{\pi/4} \tan^n x dx$ , ( $n > 1$  and  $n \in N$ ), then

A.  $I_n = I_{n-2}$

B.  $I_n + I_{n-2} = \frac{1}{n-1}$

C.  $I_n - I_{n-2} = \frac{1}{n-1}$

D. none of these

**Answer: B**



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33. If  $I_m = \int_1^x (\log x)^m dx$  satisfies the relation  $I_m = k - lI_{m-1}$  then,

A.  $k=e$

B.  $l=m$

C.  $k = \frac{1}{e}$

D. none of these

**Answer: B**



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34. If  $I_m = \int_0^\infty e^{-x} x^{m-1} dx$ , then  $\int_0^\infty e^{-\lambda x} x^{m-1} dx$

A.  $\lambda I_m$

B.  $\frac{1}{\lambda} I_n$

C.  $\frac{I_n}{\lambda^n}$

D.  $\lambda^n I_n$

**Answer: C**

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35. If  $I(m, n) = \int_0^1 x^{m-1}(1-x)^{n-1} dx$  then

A.  $I(m, n) = \int_0^{\infty} \frac{x^{m-1}}{(1+x)^{m+n}} dx = \int_0^{\infty} \frac{x^{n-1}}{(1+x)^{m+n}} dx$

B.  $I(m, n) = \int_0^{\infty} \frac{x^m}{(1+x)^{m+n}} dx = \int_0^{\infty} \frac{x^n}{(1+x)^{m+n}} dx$

C.  $I(m, n) = \int_0^{\infty} \frac{x^n}{(1+x)^{m+n-1}} dx = \int_0^{\infty} \frac{x^n}{(1+x)^{m+n-1}} dx$

D. none of these

**Answer: A**

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36. The total number of extremum(s) of  $y = \int_0^{x^2} \frac{t^2 - 5t + 4}{2 + e^t} dt$  are

A.  $x = 0, \pm 1, +_1$

B.  $X = \pm 1, \pm 2, \pm 3$

C.  $x = 0, 1, 2, 3$

D. none of these

**Answer: A**



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37. The tangent to the curve  $y = f(x)$  at the point with abscissa  $x = 1$  from an angle of  $\pi/6$  and at the point  $x = 2$  an angle of  $\pi/3$  and at the point  $x = 3$  and angle of  $\pi/4$  with positive direction of x-axis in anticlockwise direction respectively. If  $f''(x)$  is continuous, then the value of



$\int_1^3 f''(x)f'(x)dx + \int_2^3 f''(x)dx$  is  
(where  $f^n(x) = \frac{d^n y}{dx^n}$ )

A.  $\frac{4\sqrt{3} - 1}{3}$

B.  $\frac{3\sqrt{3} - 1}{2}$

C.  $\frac{4 - 3\sqrt{3}}{3}$

D.  $\frac{4 + 3\sqrt{3}}{3}$

**Answer: C**



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38.  $\int_{-\pi}^{\pi} \frac{2x(1 + \sin x)}{1 + \cos^2} dx$  is

A.  $\pi^2 / 4$

B.  $\pi^2$

C. 0

D.  $\pi / 2$

**Answer: B**



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39. The value of the inntegral  $\int_{\alpha}^{\beta} \frac{1}{\sqrt{(x - \alpha)(\beta - x)}} dx$  is

A. 0

B.  $\pi/2$

C.  $\pi$

D. none of these

**Answer: C**



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40. The value of the integral  $\int_{\alpha}^{\beta} \sqrt{(x - \alpha)(\beta - x)} dx$ , is

A.  $\frac{\pi}{4}(\beta - \alpha)^2$

B.  $\frac{\pi}{2}(\beta - \alpha)^2$

C.  $\frac{\pi}{8}(\beta - \alpha)^2$

D. none of these

**Answer: C**



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41. If  $\int_0^{x^2} \sqrt{1+t^2} dt$ , then  $f'(x)$  equals

A.  $\sqrt{1+x^2}$

B.  $\sqrt{1+x^4}$

C.  $2x\sqrt{1+x^4}$

D. none of these

**Answer: C**



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42. The value of integral  $\int_1^e (\log x)^3 dx$ , is

A.  $6 + 2e$

B.  $6 - 2e$

C.  $2e - 6$

D. none of these

**Answer: B**



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43. If  $\int_{x^2}^{x^4} \sin \sqrt{t} dt$ ,  $f'(x)$  equals

A.  $\sin x^2 - \sin x$

B.  $4x^3 \sin x^2 - 2 \sin x$

C.  $x^4 \sin x^2 - x \sin x$

D. none of these

**Answer: B**



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44.  $\lim_{n \rightarrow \infty} \left[ \left(1 + \frac{1}{n}\right) \left(1 + \frac{2}{n}\right) \left(1 + \frac{n}{n}\right) \right]^{\frac{1}{n}}$

A.  $4/e$

B.  $e/4$

C.  $4e$

D. none of these

**Answer: A**



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45. The value of  $\lim_{n \rightarrow \infty} \left[ \left(1 + \frac{1}{n^2}\right) \left(1 + \frac{2^2}{n^2}\right) \dots \left(1 + \frac{n^2}{n^2}\right) \right]^{\frac{1}{n}}$

A.  $\frac{e^{\pi/2}}{2e^2}$

B.  $2e^2e^{\pi/2}$

C.  $\frac{2}{e^2}e^{\pi/2}$

D. none of these

**Answer: C**



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46. If  $\int_0^1 e^{x^2}(x - \alpha)dx = 0$  then

A.  $1 < \alpha < 2$

B.  $\alpha < 0$

C.  $0 < \alpha < 1$

D.  $\alpha = 0$

**Answer: C**



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47. If  $f(x)$  satisfies the requirements of Rolle's Theorem in  $[1,2]$  and  $f(x)$  is continuous in  $[1,2]$  then  $\int_1^2 f'(x) dx$  is equal to

A. 0

B. 1

C. 3

D.  $-1$

**Answer: A**



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48. The value of the integral  $\int_0^1 \cot^{-1}(1 - x + x^2) dx$ , is

A.  $\pi - \log 2$

B.  $\frac{\pi}{2} - \log 2$

C.  $\pi + \log 2$

D.  $\frac{\pi}{2} + \log 2$

**Answer: B**



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49. The integral  $\int_{-1}^1 \frac{|x+2|}{x+2} dx$  is equal to

A. 1

B. 2

C. 0

D. -1

**Answer: B**



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50. Let  $I = \int_0^1 \frac{x^x}{x+1} dx$ , then the value of the integral  $\int_0^1 \frac{xe^{x^2}}{x+1} dx$ , is



A.  $I^2$

B.  $\frac{1}{2}I$

C.  $2I$

D.  $\frac{1}{2}I^2$

**Answer: B**



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51. The value of the integral  $\int_0^\pi \frac{x dx}{1 + \cos \alpha \sin x}$ ,  $0 < \alpha < \pi$ , is

A.  $\frac{\pi \alpha}{\sin \alpha}$

B.  $\frac{\pi \alpha}{1 + \sin \alpha}$

C.  $\frac{\pi \alpha}{\cos \alpha}$

D.  $\frac{\pi \alpha}{1 + \cos \alpha}$

**Answer: A**



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52.  $\int_{\pi}^{10\pi} |\sin x| dx$  is equal to

A. 20

B. 8

C. 10

D. 18

**Answer: D**



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53. If  $\int_0^{\pi} \frac{1}{a + b \cos x} dx = \frac{\pi}{\sqrt{a^2 - b^2}}$ , then  $\int_0^{\pi} \frac{1}{(a + b \cos x)^2} dx$  is

A.  $\frac{\pi a}{(a^2 - b^2)^{3/2}}$

B.  $\frac{\pi b}{(a^2 - b^2)^{3/2}}$

C.  $\frac{\pi}{(a^2 - b^2)^{3/2}}$

D. none of these

**Answer: A**



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54. If  $\int_1^{\infty} e^{-ax} dx = \frac{1}{a}$ , then  $\int_1^{\infty} x^n e^{-ax} dx$  is,

A.  $\frac{(-1)^n n!}{a^{n+1}}$

B.  $\frac{(-1)^n (n-1)!}{a^n}$

C.  $\frac{n!}{a^{n+1}}$

D. none of these

**Answer: C**



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55. The value of  $\int_{\pi}^{2\pi} [2 \sin x] dx$ , where  $[\ ]$  represents the greatest integer function, is

A.  $-\frac{5\pi}{3}$

B.  $-\pi$

C.  $\frac{5\pi}{2}$

D.  $-\pi$

**Answer: A**



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56. If  $f(x) = A \sin\left(\frac{\pi x}{2}\right) + B$ ,  $f'\left(\frac{1}{2}\right) = \sqrt{2}$  and  $\int_0^1 f(x) dx = \frac{2A}{\pi}$

then constants  $A$  and  $B$  are

A.  $\frac{\pi}{2}$  and  $\frac{\pi}{2}$

B.  $\frac{2}{\pi}$  and  $\frac{3}{\pi}$

C. 0 and  $-\frac{4}{\pi}$

D.  $\frac{4}{\pi}$  and 0

**Answer: D**



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57. If  $I_{m,n} = \int_0^1 x^m (\ln x)^n dx$  then  $I_{m,n}$  is also equal to

A.  $\frac{n}{n+1} I_{m,n-1}$

B.  $\frac{-m}{n+1} I_{m,n-1}$

C.  $\frac{-n}{n+1} I_{m,n-1}$

D.  $\frac{m}{n+1} I_{m,n-1}$

**Answer: C**



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58.  $\lim_{n \rightarrow \infty} \frac{1^{99} + 2^{99} + 3^{99} + \dots + n^{99}}{n^{100}} =$

A.  $\frac{99}{100}$

B.  $\frac{1}{100}$

C.  $\frac{1}{99}$

D.  $\frac{1}{101}$

**Answer: B**



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59. If  $I_n = \int_0^{\pi/4} \tan^n x dx$ ,  $\lim_{n \rightarrow \infty} n(I_{n+1} + I_{n-1})$  equals

A. 1

B. 2

C.  $\pi/4$

D.  $\pi$

**Answer: A**



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60.  $\int_0^a f(x)dx = \lambda$  and  $\int_0^a f(2a - x)dx = \mu$ , then  $\int_0^{2a} f(x)dx =$

- A.  $\lambda + \mu$
- B.  $\lambda - \mu$
- C.  $2\lambda + \mu$
- D.  $\lambda + 2\mu$

**Answer: B**



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