# ©゙’ doubtnut 

## MATHS

## BOOKS - NDA PREVIOUS YEARS

## CARTESIAN COORDINATE SYSTEM AND

## STRAIGHT LINE

Maths

1. the lines $(p+2 q) x+(p-3 q) y=p-q$ for
different values of $p \& q$ passes trough the
fixed point is:
A. $\left(\frac{3}{2}, \frac{5}{2}\right)$
B. $\left(\frac{2}{5}, \frac{2}{5}\right)$
C. $\left(\frac{3}{5}, \frac{3}{5}\right)$
D. $\left(\frac{2}{5}, \frac{3}{5}\right)$

Answer: D

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2. The angle between the lines
$y=(2-\sqrt{3}) x+5$ and $y=(2+\sqrt{3}) x-7$
is
A. $60^{\circ}$
B. $45^{\circ}$
C. $30^{\circ}$
D. $15^{\circ}$

Answer: A

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3. What is the image of the point $(2,3)$ in the line $y=-x$ ?

$$
\begin{aligned}
& \text { A. }(-3,-2) \\
& \text { B. }(-3,2) \\
& \text { C. }(-2,-3) \\
& \text { D. }(3,2)
\end{aligned}
$$

Answer: B

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4. The middle point of $A(1,2)$ and $B(x, Y)$ is $C$
(2, 4). If $B D$ is perpendicular to $A B$ such that $C D=3$ unit, then what is the length $B D$ ?
A. $2 \sqrt{2}$ unit
B. 2 unit
C. 3 unit
D. $3 \sqrt{2}$ unit

Answer: A

## 5. If the points $A(1,2), B(2,4)$ and $C(3, a)$ are

 collinear, what is the length $B C$ ?A. $\sqrt{2}$ unit
B. $\sqrt{3}$ unit
C. $\sqrt{5}$ unit
D. 5 unit

Answer: C

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6. What is the acute angle between the lines
$A x+B y=A+B$

$$
A(x-y)+B(x+y)=2 B ?
$$

A. $45^{\circ}$
B. $\tan ^{-1}\left(\frac{A}{\sqrt{A^{2}+B^{2}}}\right)$
C.
D. $60^{\circ}$

Answer: A

## 7. If $p$ be the length of the perpendicular from

the origin on the straight line $x+2 b y=2 p$
.then what is the value of b ?

> A. $\frac{1}{p}$
> B. $p$
> C. $\frac{1}{2}$
> D. $\frac{\sqrt{3}}{2}$

Answer: D

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8. In what ratio does the line $y-x+2=0$ cut the line joining ( $3,-1$ ) and $(8,9)$ ?
A. $2: 3$
B. 3:2
C. $3:-2$
D. 1:2

Answer: A

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9. The points $(2,-2),(8,4),(4,6)$ and $(-1,1)$ in order are the vertices of which one of the following quadrilaterals ?
A. Square
B. Rhombus
C. Rectangle (but not square)
D. Trapezium

## Answer: D

10. If $p$ be the length of the perpendicular from the origin on the straight line
$a x+b y=p$ and $b=\frac{\sqrt{3}}{2}$, then what is the angle between the perpendicular and the positive direction of $x$-axis?
A. $30^{\circ}$
B. $45^{\circ}$
C. $60^{\circ}$
D. $90^{\circ}$

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11. The straight line $a x+b y+c=0$ and the coordinate axes form an isosceles triangle under which one of the following consitions ?
A. $|a|=|b|$
B. $|a|=|c|$
C. $|b|=|c|$
D. none of these
12. The coordinates of $P$ and $Q$ are $(-3,4)$ and
$(2,1)$, respectively. If $P Q$ is extended to $R$ such
that $P R=2 Q R$, then what are the coordinates of R ?
A. $(3,7)$
B. $(2,4)$
C. $\left(-\frac{1}{2}, \frac{5}{2}\right)$
D. $(7,-2)$

## Answer: D

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13. The point on the line $2 x-3 y=5$ which is equidistant from $(1,2)$ and $(3,4)$ is
A. $(7,3)$
B. $(4,1)$
C. $(1,-1)$
D. $(-2,-3)$

Answer: B

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14. The following question consist of two stateements, one labelled as the 'Assertion (A)'
and the other as 'Reason (R)'. You are to examine these two statement carafully and select the answer.

Assertion (A) : If two triangles with vertices
$\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{3}, y_{3}\right)$
and
$\left(a_{1}, b_{1}\right),\left(a_{2}, b_{2}\right),\left(a_{3}, b_{3}\right)$ satisfy the relation

Reason (R) : For the given triangles satisfying the above relation impolies that the triangles have equal area.
$A$. Both $A$ and $R$ are individually true, and $R$
is the correct explanation of $A$.
B. Both $A$ and $R$ are individually true but $R$
is not the correct explanation of A .
C. $A$ is true but $R$ is false.
D. $A$ is false but $R$ is true.

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15. If $A(2,3), B(1,4), C(0-2)$ and $D(x, y)$ are the vertices of a parallelogram, then what is the value of ( $\mathrm{x}, \mathrm{y}$ ) ?
A. $(1,-3)$
B. $(2,4)$
C. $(1,1)$
D. $(0,0)$
16. If O be the origin and $A\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$
are two points, then what is
$(O A)(O B) \cos \angle A O B$ ?
A. $x_{1}^{2}+x_{2}^{2}$
B. $y_{1}^{2}+y_{2}^{2}$
C. $x_{1} x_{2}+y_{1} y_{2}$
D. $x_{1} y_{1}+x_{2} y_{2}$
17. The numerical value of the perimeter of a square exceeds that of its area by 4 . what is the side of the square?
A. 1 unit
B. 2 unit
C. 3 unit
D. 4 unit
18. If ( $a, b)$, (c, d) and ( $a-c, b-d$ ) are collinear, then which one of the following is correct ?
A. $b c-a d=0$
B. $a b-c d=0$
C. $b c+a d=0$
D. $a b+c d=0$

Answer: A
19. The point of intersection of the two lines
$2 x+3 y+4=0$ and $4 x+3 y+2=0$ is at $a$ distance $d$ from origin. What is the value of $d$ ?
A. $\sqrt{2}$
B. $\sqrt{3}$
C. $\sqrt{5}$
D. $\sqrt{7}$
20. The line through the points $(4,3)$ and $(2,5)$
cuts off intercepts of length $\lambda$ and $\mu$ on the axes. Which one of the following is correct ?
A. $\lambda>\mu$
B. $\lambda<\mu$
C. $\lambda>-\mu$
D. $\lambda=\mu$
21. What is the locus of a point which is equidistant from the points $(a+b, a-b)$ and $(b-a, a+b)$ ?
A. $b x-a y=0$
B. $b x+a y=0$
C. $-a x+b y=0$
D. $a x+b y=0$
22. What is the area of the triangle formed by
the lines $y-x=0, y+x=0, x=c$ ?
A. $c / 2$
B. $c^{2}$
C. $2 c^{2}$
D. $c^{2} / 2$

Answer: B
23. What is the foot of the perpendicular from the point $(2,3)$ on the line $x+y-11=0$ ?
A. $(1,10)$
B. $(5,6)$
C. $(6,5)$
D. $(7,4)$

Answer: B

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24. Consider the following statements :
25. The equation to a straight line parallel to
the axis of x is $y=d$, where d is a constant.
26. The equation to the axis of x is $x=0$.

Which of the statement (s) given above is/are

## correct ?

A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

Answer: A

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25. What is the product of the perpendiculars
from the two points $\left( \pm \sqrt{b^{2}-a^{2}}, 0\right)$ to the
line $a x \cos \phi+b y \sin \phi=a b$ ?
A. $a^{2}$
B. $b^{2}$
C. $a b$
D. $a / b$

## Answer: A

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26. The middle point of the segment of the straight line joining the points
$(p, q)$ and $(q,-p)$ is $\left(\frac{r}{2}, \frac{s}{2}\right)$. What is the length of the segment?
A. $\left[\left(s^{2}+r^{2}\right)^{1 / 2}\right] / 2$
B. $\left[\left(s^{2}+r^{2}\right)^{1 / 2}\right] / 4$
C. $\left(s^{2}+r^{2}\right)^{1 / 2}$

## D. $s+r$

## Answer: C

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27. What is the locus of a point which is
equidistant from the point $(m+n, n-m)$
and the point $(m-n, n+m)$ ?
A. $m x=n y$
B. $n x=-m y$
C. $n x=m y$

$$
\text { D. } m x=-n y
$$

## Answer: C

## D Watch Video Solution

28. Let $O(0,0,0), P(3,4,5),(m, n, r)$ and $R(1,1$,
1) be the vertices of a parallelogram taken in order. What is the value of $m+n+r$ ?
A. 6
B. 12
C. 15
D. More than 15

Answer: C

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29. What is the image of the point $(1,2)$ on the
line $3 x+4 y-1=0$ ?

$$
\text { A. }\left(-\frac{7}{5},-\frac{6}{5}\right)
$$

B. $\left(\frac{7}{8}, \frac{1}{2}\right)$
C. $\left(\frac{7}{8},-\frac{1}{2}\right)$
D. $\left(-\frac{7}{5}, \frac{1}{2}\right)$

Answer: A

## D Watch Video Solution

30. In what ratio do the coordinate axes divide
the line segment joining $(-2,5)$ and $(3,-4)$.

$$
\text { A. } 8 x+5 y+20=0
$$

B. $5 x+8 y-7=0$
C. $8 x-5 y+60=0$
D. $5 x-8 y+57=0$

## Answer: C

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31. What is the equation on the straight line joining the origin to the point of intersection of the lines $\frac{x}{a}+\frac{y}{b}=1$ and $\frac{x}{b}+\frac{y}{a}=1 ?$
A. $x+y=0$
B. $x+y+1=0$
C. $x-y=0$
D. $x+y+2=0$

Answer: C

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32. If the straight lines $x-2 y=0$ and $k x+y=1$ intersects at the point $\left(1, \frac{1}{2}\right)$
then what is the value of $k$ ?
A. 1
B. 2
C. $1 / 2$
D. $-1 / 2$

Answer: C
33. What is the maximum number of straight
lines that can be drawn with any four points in
a plane such that each line contains at least two of these points?
A. 2
B. 4
C. 6
D. 12

Answer: C
34. A square is drawn by joining mid pint of the sides of a square. Another square is drawn inside the second square in the same way and the process is continued in definitely. If the side of the first square is 16 cm , then what is the sum of the areas of all the squares ?
A. 256 sq cm
B. 512 sq cm
C. 1024 sq cm

## D. $512 / 3 \mathrm{sq} \mathrm{cm}$

Answer: B

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35. What is the slope of the line perpendicular
to the line $\frac{x}{4}+\frac{y}{3}=1$ ?
A. $\frac{3}{4}$
B. $-\frac{3}{4}$
C. $-\frac{4}{3}$
D. $\frac{4}{3}$

## Answer: D

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36. If the area of a triangle with vertices
$(-3,0),(3,0)$ and $(0,0$ is 9 sq. units. Then
the value of $k$ will be
A. 3
B. 6
C. 9
D. 12

Answer: A

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37. The locus of a point which is equidistant from the $x$ - axis and the $y$ - axis is
A. $x \pm y=0$
B. $x+2 y=0$
C. $2 x+y=0$
D. none of these

## Answer: A

## D Watch Video Solution

38. What is the equation of the line joining the origin with the point of intersection of the lines $4 x+3 y=12$ and $3 x+4 y=12$ ?
A. $x+y=1$

$$
\text { B. } x-y=1
$$

C. $3 y=4 x$
D. $x=y$

## Answer: D

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39. If the sum of the squares of the distances
of the point $(x, y)$ from the points $(a, 0)$ and ( $-a$,
0 ) is $2 b^{2}$, then which one of the following is
A. $x^{2}+a^{2}=b^{2}+y^{2}$
B. $x^{2}+a^{2}=2 b^{2}-y^{2}$
C. $x^{2}-a^{2}=b^{2}+y^{2}$
D. $x^{2}+a^{2}=b^{2}-y^{2}$

Answer: D

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40. The line $m x+n y=1$ passes through the
points $(1,2)$ and $(2,1)$. What is the value of
A. 1
B. 3
C. $\frac{1}{2}$
D. $\frac{1}{3}$

## Answer: D

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41. What is the equation of the line passing through (2, -3) and parallel to $Y$-axis
A. $Y=-3$
B. $Y=2$
C. $X=2$
D. $X=-3$

## Answer: C

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42. What is the locus of the point which is at distance 8 units to the left of Y -axis ?
A. $X=8$
B. $Y=8$
C. $X=-8$
D. $Y=-8$

Answer: C

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43. Two straight lines $x-3 y-2=0$ and

$$
2 x-6 y-6=0
$$

A. never intersect
B. intersect at a single point
$C$. intersect at infinite number of points
D. intersect at more than one point (but
finite number of points)

Answer: A

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44. If $(a, 0),(0, b)$ and $(1,1)$ are collinear, what is $(a+b-a b)$ equal to ?
A. 2
B. 1
C. 0
D. -1

Answer: C

D Watch Video Solution
45. What is the foot of the perpendicular from the point $(2,3)$ on the line $x+y-11=0$ ?
A. $(2,9)$
B. $(5,6)$
C. $(-5,6)$
D. $(6,5)$

Answer: B

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46. Write the number of diagonals of an $n$ sided polygon.

$$
\begin{aligned}
& \text { A. } \frac{n(n-1)}{2} \\
& \text { B. } \frac{n(n-3)}{2} \\
& \text { C. } n^{2}-n \\
& \text { D. } \frac{n(n+1)}{2}
\end{aligned}
$$

Answer: B
47. If $(p, q)$ is a point on $x$-axis, which is equidistant from ( 1,2 ) and ( 2,3 ). Find p and q :

$$
\begin{aligned}
& \text { A. } p=0, q=4 \\
& \text { B. } p=4, q=0 \\
& \text { C. } p=3 / 2, q=0 \\
& \text { D. } p=1, q=0
\end{aligned}
$$

Answer: B

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48. If $p$ is the length of perpendicular from the origin to the line whose intercepts on the axes
are a and b , then show that $\frac{1}{p^{2}}=\frac{1}{a^{2}}+\frac{1}{b^{2}}$.

$$
\begin{aligned}
& \text { A. } \frac{1}{p^{2}}=\frac{1}{a^{2}}+\frac{1}{b^{2}} \\
& \text { B. } \frac{1}{p^{2}}=\frac{1}{a^{2}}-\frac{1}{b^{2}} \\
& \text { C. } \frac{1}{p}=\frac{1}{a}+\frac{1}{b} \\
& \text { D. } \frac{1}{p}=\frac{1}{a}-\frac{1}{b}
\end{aligned}
$$

## Answer: A

49. 

$x+2 y-9=0$ and $2 x+4 y+5=0$ are parallel.
A. 2
B. -1
C. 1
D. 0

Answer: A

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50. Find the equation of a line parallel to the $x$ axis ata distance of
(i) 4 units above it (ii) 5 units below it.
A. $x=5$
B. $x=-5$
C. $y=5$
D. $y=-5$

Answer: D

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51. What is the equation of line passing through $(0,1)$ and making an angle with the $Y$-axis equal to the inclination of the line $x-y=4$ with X -axis?
A. $y=x+1$
B. $x=y+1$
C. $2 x=y+2$
D. None of the above

Answer: A
52. what is the perimeter of the triangle with vertices
$A(-4,2), B(0,-1)$ and $C(3,3) ?$
A. $7+3 \sqrt{2}$
B. $10+5 \sqrt{2}$
C. $11+6 \sqrt{2}$
D. $5+\sqrt{2}$

Answer: B
53. If the mid point between the points $(a+b, a-b)$ and $(-a, b)$ lies on the line $a x+b y=k$, what is k equal to ?
A. $a / b$
B. $a+b$
C. $a b$
D. $a-b$

Answer: C

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54. The acute angle which the perpendicular from origin on the line $7 x-3 y=4$ makes with the $x$-axis is
A. zero
B. positive but not $\pi / 4$
C. negative
D. $\pi / 4$
55. What is the distance between the lines $3 x+4 y=9$ and $6 x+8 y=18 ?$
A. 0
B. 3 units
C. 9 units
D. 18 units

Answer: A
56. What is the perpendicular distance of the point ( $x$, $y$ ) from $x$-axis ?
A. $x$
B. $y$
C. $|x|$
D. $|y|$

Answer: D

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57. Find the equation of a line passing through
the origin and making an angle of $120^{\circ}$ with the positive direction of the $x$-axis.
A. first quadrant
B. second quadrant
C. third quadrant

D. fourth quadrant

## Answer: C

58. The locus of a point equidistant from three collinear points is
A. a straight line
B. a pair of points
C. a point
D. the null set

Answer: D
59. The equation to the locus of a point which
is always equidistant from the points $(1,0)$ and
$(0,-2)$ is :
A. $2 x+4 y+3=0$
B. $4 x+2 y+3=0$
C. $2 x+4 y-3=0$
D. $4 x+2 y-3=0$

Answer: A
60. The points ( 5,1 ), ( $1,-1$ ) and ( 11,4 ) are :

A. collinear

B. vertices of right angled triangle
C. vertices of equilateral triangle
D. vertices of an isosceles triangle

Answer: A
61. What is the perpendicular distance between the parallel lines $3 x+4 y=9$ and

$$
9 x+12 y+28=0 ?
$$

A. $\frac{7}{3}$ units
B. $\frac{8}{3}$ units
C. $\frac{10}{3}$ units
D. $\frac{11}{3}$ units

Answer: D

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62. Let $p, q, r, s$ be the distances from origin of
the points $(2,6),(3,4),(4,5)$ and $(-2,5)$
respectively. Which one of the following is a whole number?
A. $p$
B. $q$
C. r
D. s

Answer: B

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63. From the point $(4,3)$ a perpendicular is dropped on the $x$-axis well as on the $y$-axis. If
the lengths of perpendiculars are $\mathrm{p}, \mathrm{q}$ respectively, then which one of the following is correct ?

$$
\text { A. } p=q
$$

B. $3 p=4 q$
C. $4 p=3 q$
D. $p+q=5$

Answer: C

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64. The line $y=0$ divides the line joining the points $(3,-5)$ and $(-4,7)$ in the ratio :
A. $3: 4$
B. $4: 5$
C. 5:7
D. $7: 9$

Answer: C

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65. The equation of a straight line which makes an angle $45^{\circ}$ with the $x$-axis with $y$ intercept 101 units is :
A. $10 x+101 y=1$
B. $101 x+y=1$
C. $x+y-101=0$
D. $x-y+101=0$

## Answer: D

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66. Prove that the points $A(2,4), B(2,6)$ and $C(2$
$+\sqrt{3}, 5)$ are the vertices of an equilateral triangle.
A. 6
B. 5
C. -3
D. 1

Answer: B

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67. what is the equation of a straight line which passes through $(3,4)$ and sum of whose $x$ and $y$ intercepts is 14 ?
A. $4 x+3 y=24$
B. $x+y=14$
C. $4 x-3 y=0$
D. $3 x+4 y=25$

Answer: A

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68. The point whose abscissa is equal to its
ordinate and which is equidistant from
$A(-1,0)$ and $B(0,5)$ is
A. $(1,1)$
B. $(2,2)$
C. (-2, -2)
D. $(3,3)$

Answer: B

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69. What is the area of the triangle whose
vertices are $(3,0),(0,4)$ and $(3,4) ?$
A. 6 sq. unit
B. 7.5 sq. unit
C. 9 sq. unit
D. 12 sq. unit

## D Watch Video Solution

70. A straight line passes through the points
$(5,0)$ and $(0,3)$. The length of perpendicular
from the point $(4,4)$ on the line is

> A. $\frac{\sqrt{17}}{2}$
> B. $\sqrt{\frac{17}{2}}$
> C. $\frac{15}{\sqrt{34}}$
> D. $\frac{17}{2}$

Answer: B

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71. What is the inclination of the line

$$
\sqrt{3} x-y-1=0 ?
$$

A. $30^{\circ}$
B. $60^{\circ}$
C. $135^{\circ}$
D. $150^{\circ}$

Answer: B

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72. Two straight line paths are represented by
the equation $2 x-y=2$ and $-4 x+2 y=6$.
Then the paths will
A. cross each other at one point
B. not cross each other
C. cross each other at two points

# D. cross each other at infinitely many 

 pointsAnswer: B

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73. For what value of $k$, the equations
$3 x-y=8$ and $9 x-k y=24$ will have infinitely many solutions ?
A. 6
B. 5
C. 3
D. 1

## Answer: C

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74. What is the area of the triangle bounded by the side $x=0, y=0$ and $x+y=2 ?$
A. 1 square unit

## B. 2 square unit

C. 4 square unit
D. 8 square unit

Answer: B

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75. If the three vertices of the parallelogram

ABCD are $A(1, a), B(3, a), C(2, b)$, then D is equal to
A. $(3, b)$
B. $(6, b)$
C. $(0, b)$
D. $(5, b)$

Answer: C

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76. What is the equation of the line which passes through $(4,-5)$ and is perpendicular to $3 x+4 y+5=0 ?$
А. $4 x-3 y-31=0$
B. $3 x-4 y-41=0$
C. $4 x+3 y-1=0$
D. $3 x+4 y+8=0$

Answer: A

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77. For what value of $k$ are the two straight
lines $3 x+4 y=1$ and $4 x+3 y+2 k=0$ equidistant from the point $(1,1)$ ?
A. $\frac{1}{2}$
B. 2
C. -2
D. $-\frac{1}{2}$

## Answer: D

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78. A points $P$ moves such that its distances from $(1,2)$ and $(-2,3)$ are equal. Then, the locus of $P$ is
A. straight line
B. Parabola
C. ellipse
D. hyperbola

Answer: A

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79. The locus of a point which is equidistant from the $x$ - axis and the $y$ - axis is
A. $y=2 x$
B. $x=2 y$
C. $y= \pm x$
D. $2 y+x=0$

Answer: C

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80. What angle does the line joining the points $(5,2)$ and $(6,-15)$ subtend on $(0,0)$
A. $\frac{\pi}{6}$
B. $\frac{\pi}{4}$
C. $\frac{\pi}{2}$
D. $\frac{3 \pi}{4}$

Answer: C

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81. The length of latus rectum of the ellipse
$4 x^{2}+9 y^{2}=36$ is
A. $\frac{4}{3}$
B. $\frac{8}{3}$
C. 6
D. 12

Answer: B

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82. What is the equation to the straight line passing through $(5,-2)$ and $(-4,7)$ ?
A. $5 x-2 y=4$

$$
\text { B. }-4 x+7 y=9
$$

C. $x+y=3$
D. $x-y=-1$

Answer: C

## D Watch Video Solution

83. What is the angle between the lines
$x+y=1$ and $x-y=1 ?$
A. $\frac{\pi}{6}$
B. $\frac{\pi}{4}$
C. $\frac{\pi}{3}$
D. $\frac{\pi}{2}$

## Answer: D

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84. The centroid of the triangle with vertices
$(2,3),(-2,-5)$ and $(3,5)$ is at
A. $(1,1)$
B. $(2,-1)$
C. $(1,-1)$
D. $(1,2)$

Answer: A

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85. The equation of the line, the reciprocals of whose intercepts on the axis are $m$ and $n$, is given by
A. $n x+m y=m n$
B. $m x+n y=1$
C. $m x+n y=m n$
D. $m x-n y=1$

Answer: B

D Watch Video Solution
86. Consider the following points :

1. $(0,5) 2 .(2,-1)$
2. $(3,-4)$

Which of the above lie on the line $3 x+y=5$ and at a distance $\sqrt{10}$ from $(1,2)$ ?
A. 1 only
B. 2 only
C. 1 and 2 only
D. 1, 2 and 3

Answer: C
( Watch Video Solution
87. What is the equation of the line through
$(1,2)$ so that the segment of the line intercepted between the axis is bisected at this point?

$$
\begin{aligned}
& \text { A. } 2 x-y=4 \\
& \text { B. } 2 x-y+4=0 \\
& \text { C. } 2 x+y=4 \\
& \text { D. } 2 x+y+4=0
\end{aligned}
$$

## Answer: C

88. What is the equation of straight line passing through the point $(4,3)$ and making equal intercepts on the coordinate axes ?
A. $x+y=7$
B. $3 x+4 y=7$
C. $x-y=1$
D. None of these

Answer: A
89. $A(3,4)$ and $B(5,-2)$ are two points and $P$ is
a point such that $P A=P B$. If the area of triangle PAB is 10 square unit, what are the coordinates of P ?
A. $(1,0)$ only
B. $(7,2)$ only
C. $(1,0)$ or $(7,2)$
D. Neither $(1,0)$ nor $(7,2)$

## Answer: C

## D Watch Video Solution

90. Which of the following is correct in respect of the equations $\frac{x-1}{2}=\frac{y-2}{3}$ and $2 x+3 y=5 ?$
A. They represent two lines which are parallel.
B. They represent two lines which are perpendicular.
C. They represent two lines which are neither parallel nor perpendicular.
D. The first equation does not represent a line.

Answer: B

## D Watch Video Solution

91. Consider the triangle $A B C$ with vertices
$A(-2,3), B(2,1)$ and $C(1,2)$. What is the circumcentre of the triangle $A B C$ ?
A. $(-2,-2)$
B. $(2,2)$
C. $(-2,2)$
D. $(2,-2)$

Answer: A

## D Watch Video Solution

92. Consider the triangle $A B C$ with vertices
$A(-2,3), B(2,1)$ and $C(1,2)$. What is the circumcentre of the triangle ABC?
A. $\left(\frac{1}{3}, 1\right)$
B. $\left(\frac{1}{3}, 2\right)$
C. $\left(1, \frac{2}{3}\right)$
D. $\left(\frac{1}{2}, 3\right)$

Answer: B

## D Watch Video Solution

93. Consider the $\triangle A B C$ with vertices
$A(-2,3), B(2,1)$ and $C(1,2)$. what is the
foot of the altitude from the vertex $A$ of the triangle $A B C$ ?
A. $(1,4)$
B. $(-1,3)$
C. $(-2,4)$
D. $(-1,4)$

Answer: D
( Watch Video Solution
94. A line passes through the point $(2,2)$ and
is perpendicular to the line $3 x+y=3$, then
its $y$-intercept is
A. $\frac{3}{4}$
B. $\frac{4}{3}$
C. $\frac{1}{3}$
D. 3

Answer: B

D Watch Video Solution
95. The perpendicular distance between the
straight lines $6 x+8 y+15=0 \quad$ and
$3 x+4 y+9=0$ is
A. $\frac{3}{2}$ units
B. $\frac{3}{10}$ unit
C. $\frac{3}{4}$ unit
D. $\frac{2}{7}$ unit

Answer: B

D Watch Video Solution
96. The length of perpendicular from the origin to a line is 5 units and the line makes an angle $120^{\circ}$ with the positive direction of $x$ axis. The equation of the line is
A. $x+\sqrt{3} y=5$
B. $\sqrt{3} x+y=10$
C. $\sqrt{3} x-y=10$
D. None of these

Answer: B
97. What is the equation on the straight line
joining the origin to the point of intersection
of the lines $\frac{x}{a}+\frac{y}{b}=1$ and $\frac{x}{b}+\frac{y}{a}=1$ ?

$$
\begin{aligned}
& \text { A. } x-y=0 \\
& \text { B. } x+y=0 \\
& \text { C. } x=0 \\
& \text { D. } y=0
\end{aligned}
$$

Answer: A
98. If a line is perpendicular to the line $5 x-y=0$ and forms a triangle with coordinate axes of area 5 sq. units, then its equation is :

$$
\begin{aligned}
& \text { A. } x+5 y \pm 5 \sqrt{2}=0 \\
& \text { B. } x-5 y \pm 5 \sqrt{2}=0 \\
& \text { C. } 5 x+y \pm 5 \sqrt{2}=0 \\
& \text { D. } 5 x-y \pm 5 \sqrt{2}=0
\end{aligned}
$$

Answer: A

## D Watch Video Solution

## 99.

The three
lines
$4 x+4 y=1,8 x-3 y=2, y=0$ are
A. the sides of an isosceles triangle
B. concurrent
C. mutually perpendicular
D. the sides of an equilateral triangle

Answer: B

## D Watch Video Solution

100. If the point $3 x+4 y-24=0$ intersects
the $X$-axis at the point $A$ and the $Y$-axis at
the point $B$, then the incentre of the triangle
$O A B$, where $O$ is the origin, is
A. $(2,3)$
B. $(3,3)$
C. $(4,3)$

## D. None of the above

## Answer: C

## D Watch Video Solution

101. The product of $y$ the perpendiculars from
the two points $( \pm 4,0)$ to the line
$3 x \cos \phi+5 y \sin \phi=15$ is
A. 25
B. 16
C. 9
D. 8

## Answer: C

## D Watch Video Solution

102. The angle between the lines
$2 x=3 y=-z$ and $6 x=-y=-4 z \quad$ is
(A) $0^{0}$ (B) $90^{0}$ (C) $45^{0}$ (D) $30^{0}$
A. are perpendicular
B. are parallel
C. intersect at an angle $45^{\circ}$
D. intersect at an angle $60^{\circ}$

## Answer: A

## D Watch Video Solution

103. Two straight lines passing through the point $\mathrm{A}(3,2)$ cut the line $2 y=x+3$ and x -axis perpendicularly at $P$ and $Q$ respectively. The equation of the line $P Q$ is
A. $7 x+y-21=0$
B. $x+7 y+21=0$
C. $2 x+y-8=0$
D. $x+2 y+8=0$

Answer: A

D Watch Video Solution
104. A straight line intersect $x$ and $y$ axes at $P$ and $Q$ respectively. If $(3,5)$ is the middle point
of PQ , then what is the area of the triangle OPQ ?
A. 12 square units
B. 15 square units
C. 20 square units
D. 30 square units

Answer: D
( Watch Video Solution
105. Consider the lines $y=3 x, y=6 x$ and
$y=9$

What is the area of the triangle formed by these lines ?
A. $\frac{27}{4}$ square units
B. $\frac{27}{2}$ square units
C. $\frac{19}{4}$ square units
D. $\frac{19}{2}$ square units

Answer: A
106. Consider the lines $y=3 x, y=6 x$ and
$y=9$

The centroid of the triangle is at which one of the following points ?
A. $(3,6)$
B. $\left(\frac{3}{2}, 6\right)$
C. $(3,3)$
D. $\left(\frac{3}{2}, 9\right)$

Answer: B

## D Watch Video Solution

107. For the next two (2) items that follow

Consider the curves y I x 1 and Ix 2 For What is/are the point (s) of intersection of the curves? (a) 2,3 ) only (b) $(2,1)$ only (c) $(2,3)$ and
$(2,1)$ (d) Neither $(2,3)$ nor $(2,1) 33$ What is the area of the region bounded by the curves and

4 axis (a) 3 square units (b) 4 square units

6 square units (c) 5 square units
A. $(-2,3)$ only
B. $(2,1)$ only
C. $(-2,3)$ and $(2,1)$
D. Neither $(-2,3)$ nor $(2,1)$

## Answer: C

## D Watch Video Solution

108. For the next two (2) items that follow

Consider the curves $\mathrm{y} \mid \times 1$ and Ix 2 For What is/are the point (s) of intersection of the
curves? (a) 2,3 ) only (b) $(2,1)$ only (c) $(2,3)$ and
$(2,1)$ (d) Neither $(2,3)$ nor $(2,1) 33$ What is the area of the region bounded by the curves and

4 axis (a) 3 square units (b) 4 square units (d)

6 square units (c) 5 square units
A. 3 square units
B. 4 square units
C. 5 square units
D. 6 square units

Answer: C
109. Consider the two lines $x+y+1=0$ and
$3 x+2 y+1=0$
What is the equation of the line passing
through the point of intersection of the given
lines and parallel to $x$-axis ?
A. $y+1=0$
B. $y-1=0$
C. $y-2=0$
D. $y+2=0$

## Answer: D

## D Watch Video Solution

110. Consider the two lines $x+y+1=0$ and
$3 x+2 y+1=0$

What is the equation of the line passing through the point of intersection of the given lines and parallel to $y$-axis?

$$
\text { A. } x+1=0
$$

$$
\text { B. } x-1=0
$$

$$
\text { C. } x-2=0
$$

$$
\text { D. } x+2=0
$$

Answer: B

## D Watch Video Solution

111. Consider a parallelogram whose vertices
are $A(1,2), B(4, y), C(x, 6)$ and $D(3,5)$ taken in order.

What is the value of $A C^{2}-B D^{2}$ ?
A. 25
B. 30
C. 36
D. 40

Answer: C

## D Watch Video Solution

112. Consider a parallelogram whose vertices
are $A(1,2), B(4, y), C(x, 6)$ and $D(3,5)$ taken in order.

What is the point of intersection of the diagonals?
A. $\left(\frac{7}{2}, 4\right)$
B. $(3,4)$
C. $\left(\frac{7}{2}, 5\right)$
D. $(3,5)$

Answer: A
( Watch Video Solution
113. Consider a parallelogram whose vertices
are $A(1,2), B(4, y), C(x, 6)$ and $D(3,5)$ taken in order.

What is the area of the parallelogram?
A. $\frac{7}{2}$ square units
B. 4 square units
C. $\frac{11}{2}$ square units
D. 7 square units

## Answer: D

114. $(a, 2 b)$ is the mid-point of the line segment
joining the points $(10,-6)$ and $(k, 4)$. If $a-2 b=7$, then what is the value of k ?
A. 2
B. 3
C. 4
D. 5

Answer: A
115. An equilateral triangle has one vertex at
$(0,0)$ and another at $(3, \sqrt{3})$. What are the coordinates of the third vertex ?
A. $(0,2 \sqrt{3})$ only
B. $(3, \sqrt{3})$ only
C. $(0,2 \sqrt{3})$ or $(3,-\sqrt{3})$
D. Neither $(0,2 \sqrt{3}) n$ or $(3,-\sqrt{3})$

## - Watch Video Solution

116. What is the equation of the straight line which passes through the point of intersection of the straight lines $x+2 y=5$ and $3 x+7 y=17$ and is perpendicular to the straight line $3 x+4 y=10 ?$
A. $4 x+3 y+2=0$
B. $4 x-y+2=0$
C. $4 x-3 y-2=0$

$$
\text { D. } 4 x-3 y+2=0
$$

## Answer: D

## D Watch Video Solution

117. If $(a, b)$ is at unit distance from the line
$8 x+6 y+1=0$, then which of the following
conditions are correct ?
118. $3 a-4 b-4=0$
119. $8 a+6 b+11=0$
120. $8 a+6 b-9=0$

Select the correct answer using the code given below:
A. 1 and 2 only
B. 2 and 3 only
C. 1 and 3 only
D. 1, 2 and 3

Answer: B
( Watch Video Solution
118. A straight line cuts off an intercept of 2 units on the positive direction of $x$-axis and passes through the point $(-3,5)$. What is the foot of the perpendicular drawn from the point $(3,3)$ on this line ?
A. $(1,3)$
B. $(2,0)$
C. $(0,2)$
D. $(1,1)$
119. The equation of the curve whose slope is given by $\frac{d y}{d x}=\frac{2 y}{x} ; x>0, y>0$ and which passes through the point $(1,1)$ is $x^{2}=y \mathrm{~b}$. $y^{2}=x$ c. $x^{2}=2 y$ d. $y^{2}=2 x$
A. Circle
B. Parabola
C. Ellipse
D. hyperbola

Answer: B

## - Watch Video Solution

120.21. If a vertex of a triangle is $(1,1)$ and the midpoints of two sides of the triangle through
this vertex are $(-1,2)$ and $(3,2)$, then the centroid of the triangle is
A. $\left(-\frac{1}{3}, \frac{7}{3}\right)$
B. $\left(-1, \frac{7}{3}\right)$
C. $\left(\frac{1}{3}, \frac{7}{3}\right)$
D. $\left(1, \frac{7}{3}\right)$

## Answer: D

## D Watch Video Solution

121. Find the incentre of the triangle with
vertices $(1, \sqrt{3}),(0,0)$ and $(2,0)$
A. $\left(1, \frac{\sqrt{3}}{2}\right)$
B. $\left(\frac{2}{3}, \frac{1}{\sqrt{3}}\right)$
C. $\left(\frac{2}{3}, \frac{\sqrt{3}}{2}\right)$
D. $\left(1, \frac{1}{\sqrt{3}}\right)$

## Answer: D

## D Watch Video Solution

122. Three consecutive vertices of $a$ parallelogram are $(-2,-1),(1,0)$ and $(4,3)$. Find the fourth vertex
A. $(1,2)$
B. $(1,0)$
C. $(0,0)$
D. $(1,-1)$

Answer: A

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123. What is the ratio in which the point $C\left(-\frac{2}{7},-\frac{20}{7}\right)$ divides the line joining the points $A(-2,-2)$ and $B(2,-4)$ ?
A. $1: 3$
B. 3: 4
C. 1:2
D. $2: 3$

Answer: B

D Watch Video Solution
124. What is the equation of the straight line parallel to $2 x+3 y+1=0$ and passes through the point $(-1,2)$ ?
A. $2 x+3 y-4=0$
B. $2 x+3 y-5=0$
C. $x+y-1=0$
D. $3 x-2 y+7=0$

Answer: A

## D Watch Video Solution

125. If the centroid of the triangle formed by
$(7, x),(y,-6)$ and $(9,10)$ is at $(6,3)$,
then $\quad(x, y)=(4,5) \quad$ (b) $\quad(5,4)$
$\left(\begin{array}{ll}-5, & -2)(d)(5,2)\end{array}\right.$
A. 5,2
B. 2,5
C. 1,0
D. 0,0

Answer: A

D Watch Video Solution
126. The points (a, b), (0, 0), (-a, -b) and $\left(a b, b^{2}\right)$ are
A. the vertices of a parallelogram
B. the vertices of a rectangle
C. the vertices of a square

D. collinear

Answer: B
( Watch Video Solution
127. The distance of the point $(1,3)$ from the
line $2 x+3 y=6$, measured parallel to the line $4 x+y=4$, is
A. $\frac{5}{\sqrt{13}}$ units
B. $\frac{3}{\sqrt{17}}$ unit
C. $\sqrt{17}$ units
D. $\frac{\sqrt{17}}{2}$ units

## Answer: D

128. The equation of a straight line which cuts off an intercept of 5 units on negative direction of $y$-axis and makes an angle of $120^{\circ}$ with the positive direction ofx-axis is
A. $y+\sqrt{3} x+5=0$
B. $y-\sqrt{3} x+5=0$
C. $y+\sqrt{3} x-5=0$
D. $y-\sqrt{3} x-5=0$

## Answer: A

129. The equation of the line passing through
the point $(2,3)$ and the point of intersection of
lines $2 x-3 y+7=0$ and $7 x+4 y+2=0$ is
A. $21 x+46 y-180=0$
B. $21 x-46 y+96=0$
C. $46 x+21 y+155=0$
D. $46 x-21 y-29=0$

Answer: B
130. What is the distance between the points which divide the line segment joining $(4,3)$
and $(5,7)$ internally and externally in the ratio
$2: 3 ?$
A. $\frac{12 \sqrt{17}}{5}$
B. $\frac{13 \sqrt{17}}{5}$
C. $\frac{\sqrt{17}}{5}$
D. $\frac{6 \sqrt{17}}{5}$

Answer: A

## D Watch Video Solution

131. Equation to the straight line cutting off an
intercept 2 from negative direction of the axis of $y$ and inclined at $30^{\circ}$ to the positive direction of axis of $x$ is :

$$
\begin{aligned}
& \text { А. } x-2 \sqrt{3} y-3 \sqrt{2}=0 \\
& \text { В. } x+2 \sqrt{3} y-3 \sqrt{2}=0 \\
& \text { С. } x+\sqrt{3} y-2 \sqrt{3}=0
\end{aligned}
$$

$$
\text { D. } x-\sqrt{3} y-2 \sqrt{3}=0
$$

## Answer: D

## D Watch Video Solution

132. What is the equation of the line passing
through the point of intersection of the lines
$x+2 y-3=0 \quad$ and $\quad 2 x-y+5=0 \quad$ and
parallel to the line $y-x+10=0$ ?

$$
\text { A. } 7 x-7 y+18=0
$$

$$
\begin{aligned}
& \text { B. } 5 x-7 y+18=0 \\
& \text { C. } 5 x-5 y+18=0 \\
& \text { D. } x-y+5=0
\end{aligned}
$$

## Answer: C

## D Watch Video Solution

133. Consider the following statements :
134. The length $p$ of the perpendicular from the origin to the line $a x+b y=c$ satisfies the
relation $p^{2}=\frac{c^{2}}{a^{2}+b^{2}}$

The length p of the pependicular from the origin to the line $\frac{x}{a}+\frac{y}{b}=1$ satisfies the relation $\frac{1}{p^{2}}=\frac{1}{a^{2}}+\frac{1}{b^{2}}$.
3. The length $p$ of the perpendicular from the origin to the line $y=m x+c$ satisfies the relation $\frac{1}{p^{2}}=\frac{1+m^{2}+c^{2}}{c^{2}}$

Which of the above is/are correct ?
A. 1, 2 and 3
B. 1 only
C. 1 and 2 only
D. 2 only

## Answer: C

## D Watch Video Solution

134. What is the equation of the straight line passing through the point $(2,3)$ and making an intercept on the positive $y$-axis equal to twice its intercept on the positive $x$-axis ?
A. $2 x+y=5$
B. $2 x+y=7$
C. $x+2 y=7$

$$
\text { D. } 2 x-y=1
$$

## Answer: B

## - Watch Video Solution

135. Given three straight lines
$2 x+11 y-5=0,24 x+7 y-20=0, \quad$ and
$4 x-3 y-2=0$. Then, they form a triangle one line bisects the angle between the other two two of them are parallel
A. 12 and 4 respectively
B. 11 and 5 respectively
C. Equal to each other
D. Not equal to each other

## Answer: C

## D Watch Video Solution

136. The equation of the line, when the portion of it intercepted between the axes is divided by the point $(2,3)$ in the ratio of $3: 2$, is
A. Either $x+y$ or $9 x+y=12$
B. Either $x+y=5$ or $4 x+9 y=30$
C. Either $x+y=4$ or $x+9 y=12$
D. Either $x+y=5$ or $9 x+4 y=30$

## Answer: D

## - Watch Video Solution

137. 15. The distance between the lines $3 x+4 y$
$=9$ and $6 x+8 y=15$ IS: (c) 6 (d) 210
A. $\frac{3}{2}$
B. $\frac{3}{10}$
C. 6
D. 5

Answer: B

## D Watch Video Solution

138. The second degree equation
$x^{2}+4 y^{2}-2 x-4 y+2=0$ represents
A. A point
B. An ellipse of semi-major axis 1
C. An ellipse with eccentricity $\frac{\sqrt{3}}{2}$
D. None of the above

Answer: A

## D Watch Video Solution

139. The angle between the two lines
$1 x+m y+n=0$ and $1^{\prime} x+m^{\prime} y+n^{\prime}=0$
is given by $\tan ^{-1} \theta$. What $\theta$ equal to ?
A. $\left|\frac{l m^{\prime}-l^{\prime} m}{l l^{\prime}-m m^{\prime}}\right|$
B. $\left|\frac{l m^{\prime}+l^{\prime} m}{l l^{\prime}+m m^{\prime}}\right|$
C. $\left|\frac{l m^{\prime}-l^{\prime} m}{l l^{\prime}+m m^{\prime}}\right|$
D. $\left|\frac{l m^{\prime}+l^{\prime} m}{l l^{\prime}-m m^{\prime}}\right|$

## Answer: C

## D Watch Video Solution

140. Consider the following statements:
141. The distance between the lines
$y=m x+c_{1}$ and $y=m x+c_{2}$ is $\frac{\left|c_{1}-c_{2}\right|}{\sqrt{1-m^{2}}}$.
142. The distance between the lines
$a x+b y+c_{1} \quad$ and $\quad a x+b y+c_{2}=0 \quad$ is
$\left|c_{1}-c_{2}\right|$
$\sqrt{a^{2}+b^{2}}$.
143. The distance between the lines $x=c$ and
$x=c_{2}$ is $\left|c_{1}-c_{2}\right|$. Which of the above
statements are correct ?
A. 1 and 2 only
B. 2 and 3 only
C. 1 and 3 only
D. 1, 2 and 3

Answer: B

## - Watch Video Solution

141. What is equation of straight line pass
through the point of intersection of the line $\frac{x}{2}+\frac{y}{3}=1$ and $\frac{x}{3}+\frac{y}{2}=1$, and parallel the $4 x+5 y-6=0$ ?
A. $20 x+25 y-54=0$
B. $25 x+20 y-54=0$
C. $4 x+5 y-54=0$

## D. $4 x+5 y-54=0$

## Answer: A

## - Watch Video Solution

142. Consider the following statements :

Statement I: If the line segment joining the points $\mathrm{P}(\mathrm{m}, \mathrm{n})$ and $\mathrm{Q}(\mathrm{r} . \mathrm{s})$ subtends an angle $\alpha$ at the origin, then
$\cos \alpha=\frac{m s-n r}{\sqrt{\left(m^{2}+n^{2}\right)\left(r^{2}+s^{2}\right)}}$.
Statements II : In any triangle ABC, it is true
that $a^{2}=b^{2}+c^{2}-2 b c \cos A$.

What of the following is correct in respect of the above two statements ?
A. Both Statement I and Statement II are
true and Statement II is the correct
explanation of Statement I
B. Both Statement I and Statement II are
true, but Statement II is not the correct
explanation of statement I

# C. Statement I is true, but Statement II is 

## false

D. Statement I is false, but Statement II is

true

## Answer: D

## D Watch Video Solution

143. Consider the following statements :
144. For an equation of a line,
$x \cos q+y \sin q=p$, in normal form, the
length of the perpendicular from the point ( $a$,
b) to the line is
$|a \cos q+b \sin q+p|$.
145. The length of the perpendicular from the point $(\mathrm{a}, \mathrm{b})$ to the line $\frac{x}{a}+\frac{y}{b}=1$ is $\left|\frac{a \alpha+b \beta-a b}{\sqrt{a^{2}+b^{2}}}\right|$.

Which of the above statements is/are correct ?
A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

## Answer: D

## D Watch Video Solution

144. The points $(1,3)$ and $(5,1)$ are two opposite vert of a rectangle. The other two vertices lie on the line find the $y=2 x+c$.

Find $c$ and the remaining vertices.
A. 2
B. -2
C. 4
D. -4

## Answer: D

## D Watch Video Solution

145. If the lines $3 y+4 x=1, y=x+5$ and
$5 y+b x=3$ are concurrent the $\mathrm{n} b=$
A. 1
B. 3
C. 6
D. $\frac{1}{2}$

## Answer: C

## D Watch Video Solution

146. What is the equation of the straight line which is perpendicular to $y=x$ and passes through $(3,2)$ ?
A. $x-y=5$
B. $x+y=5$

## C. $x+y=1$

D. $x-y=1$

Answer: B

## - Watch Video Solution


$x+3 y-4=0$ form a triangle, which is
A. isosceles

## B. right-angled

C. equilateral
D. scalene

Answer: A

## D Watch Video Solution

148. The centroid of the triangle with vertices
$A(2,-3,3), B(5,-3,-4)$ and $C(2,-3,-2)$ is the point

$$
\text { A. }(-3,3,-1)
$$

B. $(3,-3,-1)$
C. $(3,1,-3)$
D. $(-3,-1,-3)$

Answer: B

## D Watch Video Solution

149. The minimum distance from the point (4,
2) to $y^{2}=8 x$ is equal to
A. $\sqrt{2}$
B. $2 \sqrt{2}$
C. 2
D. $3 \sqrt{2}$

Answer: B

D Watch Video Solution
150. What is the minimum value of $a^{2} x+b^{2} y$
where $x y=c^{2}$ ?
A. abc
B. 2 abc
C. 3abc
D. 4 abc

Answer: B

D Watch Video Solution

