# びdoubtnut 

India's Number 1 Education App

## MATHS

# BOOKS - NDA PREVIOUS YEARS 

## SEQUENCE AND SERIES

## Math

1. It the sum of first 10 terms of an arithmetic progression with first term $p$ and common difference $q$, is 4 times the sum of the first 5 terms, then what is the ratio $p: q$ ?
A. 1:2
B. 1: 4
C. 2:1
D. $4: 1$

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2. One of the roots of a quadratic equation with real coefficients is $\frac{1}{(2-3 i)}$. Which of the following implications is/are true?
3. The second root of the equation will be $\frac{1}{(3-2 i)}$.
4. The equation has no real root.
5. The equation is $13 x^{2}-4 x+1=0$.

Which of the above is/are correct?
A. 1 and 2 only
B. 3 only
C. 2 and 3 only
D. 1,2 and 3

## Answer: C

3. What is the sum of the first 50 terms of the series $(1 \times 3)+(3 \times 5)+(5 \times 7)+\ldots \ldots \ldots \ldots \ldots$
A. 1,71,650
B. 26600
C. 26650
D. 26900

## Answer: A

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4. If $x=1+\frac{y}{2}+\left(\frac{y}{2}\right)^{2}+\left(\frac{y}{2}\right)^{3}+\ldots$. . where $|y|<2$, what is 1y equal to ?
A. $\frac{x-1}{x}$
B. $\frac{x-1}{2 x}$
C. $\frac{2 x-2}{x}$
D. $\frac{2 x+1}{2 x}$

## Answer: C

## D Watch Video Solution

5. What is the product of first $2 n+1$ terms of a geometric progression ?
A. The $(n+1)$ th power of the nth term of the GP
B. The $(2 n+1)$ th power of the $n$th term of the GP
C. The $(2 n+1)$ th power of the $(n+1)$ th term of the GP
D. The nth power of the $(n+1)$ th terms of the GP

## Answer: C

6. The following question consist of two statements, one labelled as the 'Assertion (A)' and the other as 'Reason (R)'. You are to examine these two statements carefully and select the answer. Assertion (A) : $1 / 8, \log _{a^{2}} a \rightarrow$ exponent should be to the base, $\log _{a} a^{2}$ are in GP but no Reason :(R) :x,y,z are in GP but not in AP.
A. Both $A$ and $R$ are individually true and $R$ is the correct explanation of $A$
B. Both A and R are individually true but R is not the correct explanation A
C. A is true but $R$ is false
D. $A$ is false but $R$ is true

## Answer: A

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7. If $x+1,4 x+1$, and $8 x+1$ are in geometric progrssion, then what is the non-trivial value of x ?
A. -1
B. 1
C. $\frac{1}{8}$
D. $\frac{1}{4}$

## Answer: C

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8. The equation $\left(a^{2}+b^{2}\right) x^{2}-2 b(a+c) x+\left(b^{2}+c^{2}\right)=0$ has equal roots. Which one of the following is correct about $\mathrm{a}, \mathrm{b}$ and c ?
A. They are in AP
B. They are in GP
C. They are in HP
D. They are neither in AP, nor in GP, nor in HP

## Answer: B

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9. If $p^{t h}$ term of an AP is q , and its $q^{t h}$ term is p , then what is the common difference?
A. -1
B. 0
C. 2
D. 1

## Answer: A

10. If $a, b, c$ are in geometric progression and $a, 2 b, 3 c$ are in arithmetic progression, then what is the common ratio r such that $0<r<1$ ?
A. $\frac{1}{3}$
B. $\frac{1}{2}$
C. $\frac{1}{4}$
D. $\frac{1}{8}$

## Answer: A

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11. For an AP with first term u and common difference v , the $p^{\text {th }}$ term is 15 uv more than the $q^{\text {th }}$ term. Which one of the following is correct?
A. $p=q+15 v$
B. $p=q+15 u$
C. $p=q+14 v$
D. $p=q+14 u$

## Answer: B

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12. If $a, b$ and $c$ are three positive numbers in an arithmetic progression, then:
A. $a c>b^{2}$
B. $b^{2}>a+c$
C. $a b+b c \leq 2 a c$
D. $a b+b c \geq 2 a c$

Answer: D

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13. If $|x|<\frac{1}{2}$, what is the value of
$1+\left[\frac{x}{1-x}\right]+\left[\frac{n(n+1)}{2!}\right]\left[\frac{x}{1-x}\right]^{2}+\ldots \ldots \ldots \ldots+\infty ?$
A. $\left[\frac{1-x}{1-2 x}\right]^{n}$
B. $(1-x)^{n}$
C. $\left[\frac{1-2 x}{1-x}\right]^{n}$
D. $\left(\frac{1}{1-x}\right)^{n}$

## Answer: A

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14. The sum of the first $(2 p+1)$ terms of an AP is $\{(p+1) \cdot(2 p+1)\}$. Which one of the following inferences can be drawn ?
A. The $(p+1)^{t h}$ term of the AP is $(2 p+1)$
B. The $(2 p+1)^{\text {th }}$ term of the AP is $(2 p+1)$
C. The $(2 p+1)^{t h}$ term of the AP is $(p+1)$
D. The $(p+1)^{\text {th }}$ term of the AP is $(p+1)$

## Answer: D

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15. $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in G.P. with $1<a<b<n$, and $n>1$ is an integer. $\log _{a} n, \log _{b} n, \log _{c} n$ form a sequence. This sequence is which one of the following ?
A. Harmonic progression
B. Arthmetic progression
C. Geometric progression
D. None of these

## Answer: A

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16. What is the sum of the series $1-\frac{1}{2}+\frac{1}{4}-\frac{1}{8}+\ldots$. equal to?
A. $\frac{1}{2}$
B. $\frac{3}{4}$
C. $\frac{3}{2}$
D. $\frac{2}{3}$

## Answer: D

## - Watch Video Solution

17. If $b_{1}, b_{2}, b_{3}$ are three consecutive terms of an arithmetic progression with common difference $d>0$, then what is the value of $d$ for which $b \frac{2}{3}=b_{2} b_{3}+b_{1} d+2$ ?
A. $\frac{1}{2}$
B. 0
C. 1

## D. 2

## Answer: C

## - Watch Video Solution

18. If $1, x, y, z, 16$ are in geometric progression, then what is the value of $x+y+z$ ?
A. 8
B. 12
C. 14
D. 16

## Answer: C

19. If the $n$th term of an arithmetic progression is $3 n+7$, then what is the sum of its first 50 terms?
A. 3925
B. 4100
C. 4175
D. 8200

## Answer: C

## - Watch Video Solution

20. If, for positive real numbers $\mathrm{x}, \mathrm{y}, \mathrm{z}$, the numbers $x+y, 2 \mathrm{y}$ and $\mathrm{y}+\mathrm{z}$ are in harmonic progression, then which one of the following is correct ?
A. $x, y, z$ are in geometric progression
B. $x, y, z$ are in arithmetic progression
C. $x, y, z$ are in harmonic progression
D. None of the above

## Answer: A

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21. What is the sum of the series
$1+\frac{1}{8}+\frac{1.3}{8.16}+\frac{1.3 .5}{8.16 .24}+\ldots \infty ?$
A. $\frac{2}{\sqrt{3}}$
B. $2 \sqrt{3}$
C. $\frac{\sqrt{3}}{2}$
D. $\frac{1}{2 \sqrt{3}}$

## Answer: A

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22. What is the geometric mean of the ratio of corresponding terms of two series where $G_{1}$ and $G_{2}$ are geometric means of the two series ?
A. $\log G_{1}-\log G_{2}$
B. $\log G_{1}+\log G_{2}$
C. $\frac{G_{1}}{G_{2}}$
D. $G_{1} G_{2}$

## Answer: C

## - Watch Video Solution

23. If the points with the coordinates (a, ma), $\{b,(m+1) b\},\{c,(m+2) c\}$ are collinear, then which one of the following is correct ?
A. $a, b, c$ are in arithmetic progression for all $m$
B. a, b, c are in geometric progression for all m
C. $a, b, c$ are in harmonic progression for all $m$
D. a, b, c are in arithmetic progression only for $\mathrm{m}=1$

## Answer: C

## - Watch Video Solution

24. The following question consist of two statements, one labelled as the 'Assertion (A)' and the other as 'Reason (R)'. You are to examine these two statements carefully and select the answer.
Assertion (A) : $0.3+0.03+0.003+\ldots \ldots=\frac{1}{3}$.
Reason (R) : For each (+) ve integer n , let $a_{n}=a+n d$, a and d are real numbers. The, $a_{1}+\ldots \ldots+a_{n}=\frac{n}{2}[2 a+(n+1) d]$.
A. Both $A$ and $R$ are individually true and $R$ is the correct explanation of $A$
B. Both $A$ and $R$ are individually true but $R$ is not the correct explanation A
C. $A$ is true but $R$ is false
D. $A$ is false but $R$ is true

## Answer: B

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25. Let the positive numbers $a, b, c, d$ be in AP. Then $a b c, a b d, a c d, b c d$ are (2001, 1M) not in AP/GP/HP (b) in AP in GP (d) in HP
A. are in AP
B. are in GP
C. are in HP
D. are in none of the above progressions

## Answer: C

## - Watch Video Solution

26. Find the value of $9^{\frac{1}{3}}, 9^{\frac{1}{9}} .9^{\frac{1}{27}} \ldots u p$ to $\infty$.
A. 9
B. 3
C. $9^{1 / 3}$
D. 1

## Answer: B

## - Watch Video Solution

27. If $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}$ are in harmonical progrssion such that $a>d$, then which one of the following is correct ?
A. $a+c=b+d$
B. $a+c>b+d$
C. $a c=b d$
D. $a b=c d$

## Answer: B

## - Watch Video Solution

28. After paying 30 out of 40 installments of a debt of Rs. 3600 , one third of the debt is unpaid. If the installments are forming an arithmetic series, then what is the first instalment ?
A. Rs. 50
B. Rs. 51
C. Rs. 105
D. Rs. 110

## Answer: B

29. The product of first nine terms of a GP is, in general, equal to which one of the following ?
A. The 9 th power of the 4 th term
B. The 4th power of the 9th term
C. The 5th power of the 9 th term
D. The 9th power of the 5th term

## Answer: D

## - Watch Video Solution

30. The difference between the nth term and $(n-1)$ th term of a sequence is independent of $n$. Then the sequence follows which one of the following?
A. AP
B. GP
C. HP
D. None of these

## Answer: A

## - Watch Video Solution

31. Which one of the following is correct?

If $\frac{1}{b-c}+\frac{1}{b-a}=\frac{1}{a}+\frac{1}{c}$, then $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in
A. AP
B. HP
C. GP
D. None of these

## Answer: B

32. What is the $15^{\text {th }}$ term of the series $3,7,13,21,31,43, \ldots \ldots .$. ?
A. 205
B. 225
C. 238
D. 241

## Answer: D

33. If the nth term of an arithmetic progression is $2 n-1$, then what is the sum upto n terms?
A. $n^{2}$
B. $n^{2}-1$
C. $n^{2}+1$
D. $\frac{1}{2} n(n+1)$

## D Watch Video Solution

34. If the three observations are $3,-6$ and -6 , then what is their harmonic mean?
A. 0
B. $\infty$
C. $-1 / 2$
D. -3

## Answer: B

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35. Sum of first n natural numbers is given by $\frac{n(n+1)}{2}$. What is the geometric mean of the series $1,2,4,8, \ldots \ldots .2^{n}$ ?
A. $2^{n}$
B. $2^{\frac{n}{2}}$
C. $2^{1 / 2}$
D. $2^{n-1}$

## Answer: B

## - Watch Video Solution

36. If there are $(2 n+1)$ terms in A.P., then prove that the ratio of the sum of odd terms and the sum of even terms is $(n+1): n$.
A. $\frac{n}{n+1}$
B. $\frac{n^{2}}{n+1}$
C. $\frac{n+1}{n}$
D. $\frac{n+1}{2 n}$

## Answer: C

37. If the sum of ' $n$ ' terms of an arithmetic progression is $n^{2}-2 n$, then what is the $n^{\text {th }}$ term?
A. $3 n-n^{2}$
B. $n 2 n-3$
C. $2 n+3$
D. $2 n-5$

## Answer: B

## - Watch Video Solution

38. If $a, 2 a+2,3 a+3$ are in GP, then what is the fourth term of the GP?
A. -13.5
B. 13.5
C. -27
D. 27

## Answer: A

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39. What is sum to the 100 terms of the series $9+99+999+\ldots$ ?
A. $\frac{10}{9}\left(10^{100}-1\right)-100$
B. $\frac{10}{9}\left(10^{99}-1\right)-100$
C. $100\left(100^{10}-1\right)$
D. $\frac{9}{100}\left(10^{100}-1\right)$

## Answer: A

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40. If the $A M$ and $G M$ of two numbers are 5 and 4 respectively, then what is the HM of those numbers?
A. $\frac{5}{4}$
B. $\frac{16}{5}$
C. $\frac{9}{2}$
D. 9

## Answer: B

## - Watch Video Solution

41. The harmonic mean of two numbers is 21.6 . If one of the numbers is 27 , then what is the other number?
A. 16.2
B. 17.3
C. 18
D. 20

## Answer: C

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42. If the sum of the first two terms and the sum of the first four terms of a geometric progression with positive common ratio are 8 and 80 respectively, then what is the 6th term?
A. 88
B. 243
C. 486
D. 1458

## Answer: C

## - Watch Video Solution

43. If $x>1$ and $\log _{2} x, \log _{3} x, \log _{x} 16$ are in GP, then what is x equal to ?
A. 9
B. 8
C. 4
D. 2

## Answer: A

## - Watch Video Solution

44. In a geometric progression with first term a and common ratio $r$, what is the arithmetic mean of first five terms?
A. $a+2 r$
B. $a r^{2}$
C. $a\left(r^{5}-1\right) /(r-1)$
D. $a\left(r^{5}-1\right) /[5(r-1)]$

## Answer: D

## - Watch Video Solution

45. If $(1+3+5++p)+(1+3+5++q)=(1+3+5++r)$ where each set of parentheses contains the sum of consecutive odd integers as shown, the smallest possible value of $p+q+r($ wherep $>6)$ is 12 b .21 c .45 d .54
A. 12
B. 21
C. 45
D. 54

## Answer: B

46. If $x^{2}, y^{2}, z^{2}$ are in AP, then $y+z, z+x, x+y$ are in
A. AP
B. HP
C. GP
D. None of these

Answer: A

## D Watch Video Solution

47. If $x, 2 x+2,3 x+3$ are the first three terms of a GP, then what is its fourth term?
A. $-27 / 2$
B. $27 / 2$
C. $-33 / 2$
D. $33 / 2$

## - Watch Video Solution

48. Which term of the sequence $20,19 \frac{1}{4}, 18 \frac{1}{2}, 17 \frac{3}{4}$, is the first negative term?
A. 27 th
B. 28 th
C. 29th
D. No such term exists

## Answer: B

## - Watch Video Solution

49. If $m$ th term of an AP is $1 / n$ and its $n$th term is $1 / m$, then show that its (mn)th term is 1
A. $1 /(m n)$
B. $m / n$
C. $n / m$
D. 1

## Answer: D

## - Watch Video Solution

50. The 59th term of an AP is 449 and the 449th term is 59 . Which term is equal to 0 (zero)?
A. $501^{\text {st }}$ term
B. $502^{\text {nd }}$ term
C. $508^{t h}$ term
D. $509^{\text {th }}$ term

## Answer: C

51. If the AM and HM of two numbers are 27 and 12 respectively, then what is their GM equal to ?
A. 12
B. 18
C. 24
D. 27

## Answer: B

## - Watch Video Solution

52. Find the sum of all numbers between 200 and 400 which are divisible by 7 .
A. 6729
B. 8712
C. 8729
D. 9276

## Answer: C

## - Watch Video Solution

53. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ be in AP.

Consider the following statements:

1. $\frac{1}{a b}, \frac{1}{c a}$ and $\frac{1}{b c}$ are in AP.
2. $\frac{1}{\sqrt{b}+\sqrt{c}}, \frac{1}{\sqrt{c}+\sqrt{a}}$ and $\frac{1}{\sqrt{a}+\sqrt{b}}$ are in AP.

Which of the statements given above is/are correct?
A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

## Answer: C

## D Watch Video Solution

54. If $p$ times the $p$ th term of an $A P$ is $q$ times the $q$ th term, then what is the $(p+q) t h$ term equal to ?
A. $p+q$
B. pq
C. 1
D. 0

## Answer: D

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55. The geometric mean of three numbers was conputed as 6 . It was subsequently found that, in this computation, a number 8 was wrongly
read as 12. What is the correct geometric mean ?
A. 4
B. $\sqrt[3]{5}$
C. $2 \sqrt[3]{18}$
D. None of these

## Answer: C

## - Watch Video Solution

56. The arithmetic mean of two numbers exceeds their geometric mean by 2 and the geometric mean exceeds their harmonic mean by 1.6 . What are the two numbers ?
A. 16,4
B. 81,9
C. 256,16
D. 625,25

## Answer: A

## - Watch Video Solution

57. The sum of an infinite geometric progression is 6 , If the sum of the first two terms is $9 / 2$, then what is the first term?
A. 1
B. $5 / 2$
C. 3 or $3 / 2$
D. 9 or 3

## Answer: D

## - Watch Video Solution

58. If the $A M$ and $G M$ between two number are in the ratio $m: n$, then what is the ratio between the two numbers?
A. $\frac{m+\sqrt{m^{2}-n^{2}}}{m-\sqrt{m^{2}-n^{2}}}$
B. $\frac{m+n}{m-n}$
C. $\frac{m^{2}-n^{2}}{m^{2}+n^{2}}$
D. $\frac{m^{2}+n^{2}-n m}{m^{2}+n^{2}+m n}$

## Answer: A

## - Watch Video Solution

59. What is the geometric mean of the data $2,4,8,16,32$ ?
A. 2
B. 4
C. 8
D. 16

## Answer: C

## - Watch Video Solution

60. If $A, B$ and $C$ are in $A P$ and $b: c=\sqrt{3}: \sqrt{2}$, then what is the value of sin C?
A. 1
B. $\frac{1}{\sqrt{3}}$
C. $\sqrt{3}$
D. $\frac{1}{\sqrt{2}}$

## Answer: D

## - Watch Video Solution

61. In a GP of positive terms, any term is equal to one-third of the sum of next two terms. What is the common ratio of the GP?
A. $\frac{\sqrt{13}+1}{2}$
B. $\frac{\sqrt{13}-1}{2}$
C. $\frac{\sqrt{13}+1}{3}$
D. $\sqrt{13}$

## Answer: B

## - Watch Video Solution

62. Which term of the G.P $\frac{1}{4},-\frac{1}{2}, 1, \ldots$ is -128
A. 9th
B. 10th
C. 11th
D. 12 th

Answer: B
63. If $\frac{1}{b-a}+\frac{1}{b-c}=\frac{1}{a}+\frac{1}{c}$, then $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in (A) AP (B) GP (C) HP (D) NONE
A. AP
B. GP
C. HP
D. None of these

## Answer: C

## - Watch Video Solution

64. What is the sum of $\sqrt{3}+\frac{1}{\sqrt{3}}+\frac{1}{3 \sqrt{3}}+\ldots \ldots$ ?
A. $\frac{\sqrt{3}}{2}$
B. $\frac{3 \sqrt{3}}{2}$
C. $\frac{2 \sqrt{3}}{3}$
D. $\sqrt{3}$

## Answer: B

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65. Which one of the following options is correct ?
A. $\sin ^{2} 30^{\circ}, \sin ^{2} 45^{\circ}, \sin ^{2} 60^{\circ}$, are in GP
B. $\cos ^{2} 30^{\circ}, \cos ^{2} 45^{\circ}, \cos ^{2} 60^{\circ}$ are in GP
C. $\cot ^{2} 30^{\circ}, \cot ^{2} 45^{\circ}, \cot ^{2} 60^{\circ}$ are in GP
D. $\tan ^{2} 30^{\circ}, \tan ^{2} 45^{\circ}, \tan ^{2} 60^{\circ}$ are in GP

Answer: D

## - Watch Video Solution

66. What is the 10th common term between the series
$2+6+10+\ldots$. and $1+6+11+\ldots . ?$
A. 180
B. 186
C. 196
D. 206

## Answer: B

## - Watch Video Solution

67. If the 10th term of a GP is 9 and 4 th term is 4 , then what is its 7 th term?
A. 6
B. 14
C. $27 / 14$
D. $56 / 15$

## Answer: A

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68. If $\log _{10} 2, \log _{10}\left(2^{x}-1\right), \log _{10}\left(2^{x}+3\right)$ are three consecutive terms of an AP, then which one of the following is correct?
A. $x=0$
B. $x=1$
C. $x=\log _{2} 5$
D. $x=\log _{5} 2$

## Answer: C

## - Watch Video Solution

69. If $n!, 3 \times(n!)$ and $(n+1)$ ! are in GP, then the value of $n$ will be
A. 3
B. 4
C. 8
D. 10

## Answer: C

## - Watch Video Solution

70. If $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}, \mathrm{e}, \mathrm{f}$ are in AP, then $(e-c)$ is equal to which one of the following?
A. $2(c-a)$
B. $2(d-c)$
C. $2(f-d)$
D. $(d-c)$

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71. What is the geometric mean of 10,40 and 60 (appox)?
A. 10
B. 28
C. 29.6
D. 70

## Answer: B

## - Watch Video Solution

72. If the arithmetic and geometric means of two numbers are 10, 8 respectively, then one number exceeds the other number by
A. 8
B. 10
C. 12
D. 16

## Answer: C

## - Watch Video Solution

73. If the sequence $\left\{S_{n}\right\}$ is a geometric progression and $S_{2} S_{11}=S_{p} S_{8}$, then what is the value of $p$ ?
A. 1
B. 3
C. 5
D. cannot be determined

## Answer: C

74. If $1 / 4,1 / x, 1 / 10$ are in $H P$, then what is the value of x ?
A. 5
B. 6
C. 7
D. 8

## Answer: C

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75. If $p, q, r$ are in AP as well as G.P., then which one of the following is correct?
A. $p=q \neq r$
B. $p \neq q \neq r$
C. $p \neq q=r$
D. $p=q=r$

## Answer: D

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76. The geometric mean and harmonic mean of two non negative observations are 10 and 8 respectively. Then what is the arithmetic mean of the observations equal to?
A. 4
B. 9
C. 12,5
D. 2

## Answer: C

77. What is the $n$th term of the sequence $1,5,9,13,17, \ldots$ ?
A. $2 n-1$
B. $2 n+1$
C. $4 n-3$
D. None of the above

## Answer: C

## - Watch Video Solution

78. What does the series
$1+3^{-\frac{1}{2}}+3+\frac{1}{3 \sqrt{3}}+\ldots$ represents?
A. AP
B. GP
C. HP
D. None of the above series

## Answer: D

## - Watch Video Solution

79. What is the sum of the series $1-\frac{1}{2}+\frac{1}{4}-\frac{1}{8}+\ldots$. equal to?
A. $\frac{1}{2}$
B. $\frac{3}{2}$
C. 2
D. $\frac{2}{3}$

## Answer: D

## - Watch Video Solution

80. Consider the following statements:
81. The sum of cubes of first 20 natural numbers is 44400 .
82. The sum of squares of first 20 natural numbers is 2870 .

Which of the above statement is/are correct?
A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

## Answer: B

## - Watch Video Solution

81. What is the sum of first eight terms of the series
$1-\frac{1}{2}+\frac{1}{4}-\frac{1}{8}+\ldots . ?$
A. $\frac{89}{128}$
B. $\frac{57}{384}$
C. $\frac{85}{128}$
D. None of the above

## Answer: C

## - Watch Video Solution

82. The sum of first 10 terms and 20 terms of an AP are 120 and 440 respectively.

What is its first term?
A. 2
B. 3
C. 4
D. 5

## Answer: B

83. The sum of first 10 terms and 20 terms of an AP are 120 and 440 respectively.

What is the common difference?
A. 1
B. 2
C. 3
D. 4

## Answer: B

## - Watch Video Solution

84. What is the number of diagonals which can be drawn by joining the angular points of a polygon of 100 sides?
A. 4850
B. 4850
C. 5000
D. 10000

## Answer: A

## - Watch Video Solution

85. The angles of a triangle are in AP and the least angle is $30^{\circ}$. What is the greatest angle (in radian)?
A. $\frac{\pi}{2}$
B. $\frac{\pi}{3}$
C. $\frac{\pi}{4}$
D. $\pi$
86. What is the geometric mean of the sequence $1,2,4,8, \ldots, 2^{n}$
A. $2^{n / 2}$
B. $2^{(n+1) / 2}$
C. $2^{(n+1)}-1$
D. $2^{(n-1)}$

## Answer: A

Watch Video Solution
87. If the numbers $-3,4 n-2,5 n+1$ are in AP, what is the value of n ?
A. 1
B. 2
C. 3

## Answer: A

## - Watch Video Solution

88. The harmonic mean of two numbers is 4. Their arithmetic mean $A$ and the geometric mean $G$ satisfy the relation $2 A+G^{2}=27$. Find two numbers.
A. 6, 3
B. 9,5
C. 12,7
D. 3, 1

## Answer: A

## - Watch Video Solution

89. Let the positive numbers $a, b, c, d$ be in AP. Then $a b c, a b d, a c d, b c d$ are (2001, 1M) not in AP/GP/HP (b) in AP in GP (d) in HP
A. HP
B. $A P$
C. GP
D. None of the above

## Answer: A

## - Watch Video Solution

90. What is the value of $0.9+0.09+0.009+\ldots$ equal to?
A. 1
B. 1.01
C. 1.001
D. 1.1

## Answer: A

## - Watch Video Solution

91. The sum of the first five terms and the sum of the first ten terms of an

AP are same. Which one of the following is the correct statement?
A. The first term must be negative
B. The common difference must be negative
C. Either the first term or the common difference is negative but not both
D. Both the first term and the common difference are negative

## Answer: C

## - Watch Video Solution

92.     - What is the 7 th rank of sequence $0,3,8,15,24, \ldots$ (a) $63(b) 48$ (c) 35
A. 63
B. 48
C. 35
D. 33

## Answer: B

## - Watch Video Solution

93. The sum of an infinite GP is $x$ and the common ratio $r$ is such that $|r|<1$. If the first term of the GP is 2 , then which one of the following is correct ?
A. $-1<x<1$
B. $-\infty<x<1$
C. $1<x<\infty$
D. None of these

## - Watch Video Solution

94. The sum of the series formed by the sequence $3, \sqrt{3}, 1 \ldots \ldots$ upto infinity is:
A. $\frac{3 \sqrt{3}(\sqrt{3}+1)}{2}$
B. $\frac{3 \sqrt{3}(\sqrt{3}-1)}{2}$
C. $\frac{3(\sqrt{3}+1)}{2}$
D. $\frac{3(\sqrt{3}-1)}{2}$

## Answer: A

## - Watch Video Solution

95. Let $S_{n}$ denote the sum of first $n$ terms of an A.P. If $S_{2 n}=3 S_{n}$, then find the ratio $S_{3 n} / S_{n}$.
A. $4: 1$
B. 6:1
C. $8: 1$
D. 10: 1

## Answer: B

## - Watch Video Solution

96. Let $S_{n}$ denote the sum of first n terms of an AP and $3 S_{n}=S_{2 n}$ What is $S_{3 n}: S_{n}$ equal to? What is $S_{3 n}: S_{2 n}$ equal to?
A. $2: 1$
B. $3: 1$
C. $4: 1$
D. $5: 1$
97. Let $f(x)=a x^{2}+b x+c \operatorname{such}$ that $f(1)=f(-1)$ and $\mathrm{a}, \mathrm{b}, \mathrm{c}$, are in Arithmetic Progression.

What is the value of $b$ ?
A. -1
B. 0
C. 1
D. Cannot be determined deu to insufficient data

## Answer: B

## Watch Video Solution

98. Let $f(x)=a x^{2}+b x+c$ such that $f(1)=f(-1)$ and $\mathrm{a}, \mathrm{b}, \mathrm{c}$, are in Arithmetic Progression.
$f^{\prime}(a), f^{\prime}(b), f^{\prime}(c)$ are
A. A.P.
B. GP.
C. H.P.
D. Arithmetico-geometric progression

## Answer: A

## - Watch Video Solution

99. Let $f(x)=a x^{2}+b x+c$ such that $f(1)=f(-1)$ and $\mathrm{a}, \mathrm{b}, \mathrm{c}$, are in Arithmetic Progression.
$\mathrm{f}^{\prime \prime}(\mathrm{a}), \mathrm{f}^{\prime \prime}(\mathrm{b}), \mathrm{f}^{\prime \prime}(\mathrm{c})$ are
A. in A.P. only
B. in GP. Only
C. in both A.P. and G.P.
D. neither in A.P. nor in G.P.

## - Watch Video Solution

100. Sum of the series $0.5+0.55+0.555+\ldots$ upto n terms is
A. $\frac{5}{9}\left[n-\frac{2}{9}\left(1-\frac{1}{10^{n}}\right)\right]$
B. $\frac{1}{9}\left[5-\frac{2}{9}\left(1-\frac{1}{10^{n}}\right)\right]$
C. $\frac{1}{9}\left[n-\frac{5}{9}\left(1-\frac{1}{10^{n}}\right)\right]$
D. $\frac{5}{9}\left[n-\frac{1}{9}\left(1-\frac{1}{10^{n}}\right)\right]$

## Answer: D

## Watch Video Solution

101. The value of the infinite product $6^{\frac{1}{2}} \times 6^{\frac{2}{4}} \times 6^{\frac{3}{8}} \times 6^{\frac{4}{16}} \times \ldots$
A. 6
B. 36
C. 216
D. $\infty$

## Answer: B

## - Watch Video Solution

102. The nth term of an AP. Is $\frac{3+n}{4}$, then the sum of first 105 terms is
A. 270
B. 735
C. 1409
D. 1470

## Answer: D

103. If $p, q, r$ are in one geometric progression and $a, b, c$ are in another geometric progression, then $\mathrm{ap}, \mathrm{bq}, \mathrm{cr}$ are in
A. Arithmetic progression
B. Geometric progression
C. Harmonic progression
D. None of the above

## Answer: B

## - Watch Video Solution

104. What is the sum of $n$ terms of the series $\sqrt{2}+\sqrt{8}+\sqrt{18}+\sqrt{32}+.$.
A. $\frac{n(n-1)}{\sqrt{2}}$
B. $\sqrt{2 n}(n+1)$
C. $\frac{n(n+1)}{\sqrt{2}}$
D. $\frac{n(n-1)}{2}$

## Answer: C

## - Watch Video Solution

105. Given that $a_{n}=\int_{0}^{\pi} \frac{\sin ^{2}\{(n+1) x\}}{\sin 2 x} d x$

Consider the following statements:

1. The sequence $\left\{a_{2 n}\right\}$ is in AP with common difference zero.
2. The sequence $\left\{a_{2 n+1}\right\}$ is in AP with common difference zero.

Which of the above statements is/are correct?
A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

## Answer: C

106. Given that $a_{n}=\int_{0}^{\pi} \frac{\sin ^{2}\{(n+1) x\}}{\sin 2 x} d x$

What is $a_{n-1}-a_{n-4}$ equal to ?
A. -1
B. 0
C. 1
D. 2

## Answer: B

## - Watch Video Solution

107. Given that $\log _{x} y, \log _{z} x, \log _{y} z$ are in GP, $x y z=64$ and $x^{3}, y^{3}, z^{3}$ are in A.P.

Which one of the following is correct ?
A. in AP only
B. in GP only
C. in both AP and GP
D. neither in AP nor in GP

## Answer: C

## D Watch Video Solution

108. Given that $\log _{x} y, \log _{z} x, \log _{y} z$ are in GP, $x y z=64$ and $x^{3}, y^{3}, z^{3}$ are in A.P.

Which one of the following is correct ?
$x y, y z$ and $z x$ are
A. in AP only
B. in GP only
C. in both AP and GP
D. neither in AP nor in GP

## D Watch Video Solution

109. If $m$ is the geometric mean of
$\left(\frac{y}{z}\right)^{\log (y z)},\left(\frac{z}{x}\right)^{\log (z x)}$ and $\left(\frac{x}{y}\right)^{\log (x y)}$
then what is the value of $m$ ?
A. 1
B. 3
C. 6
D. 9

## Answer: A

110. How many geometric progressions are possible containing 27,8 and 12 as three of its/their terms
A. One
B. Two
C. Four
D. Infinitely many

## Answer: D

## - Watch Video Solution

111. Let $a, x, y, z b$ be in AP where $x+y+z=15$ Let $a, p, q, r, b$ be in HP where $p^{-1}+q^{-1}+r^{-1}=\frac{5}{3}$ What is the value of ab What is the value of xyz What is the value of pqr
A. 10
B. 9
C. 8
D. 6

## Answer: B

## - Watch Video Solution

112. Let $\mathrm{a}, \mathrm{x}, \mathrm{y}, \mathrm{z} \mathrm{b}$ be in AP where $\mathrm{x}+\mathrm{y}+\mathrm{z}=15$ Let $\mathrm{a}, \mathrm{p}, \mathrm{q}, \mathrm{r}, \mathrm{b}$ be in HP where $p^{-1}+q^{-1}+r^{-1}=\frac{5}{3}$ What is the value of ab What is the value of $x y z$ What is the value of pqr
A. 120
B. 105
C. 90
D. Cannote be determined

## Answer: B

113. Let $\mathrm{a}, \mathrm{x}, \mathrm{y}, \mathrm{z} \mathrm{b}$ be in AP where $\mathrm{x}+\mathrm{y}+\mathrm{z}=15$ Let $\mathrm{a}, \mathrm{p}, \mathrm{q}, \mathrm{r}, \mathrm{b}$ be in HP where $p^{-1}+q^{-1}+r^{-1}=\frac{5}{3}$ What is the value of ab What is the value of xyz What is the value of pqr
A. $35 / 243$
B. $81 / 35$
C. $243 / 35$
D. Cannot be determined

## Answer: C

## - Watch Video Solution

114. The sixth term of an AP is 2 , and its common difference is greater than one. The value of the common difference of the progression so that the product of the first, fourth and fifth terms is greatest is A. $8 / 5$
B. $9 / 5$
C. 2
D. $11 / 5$

## Answer: A

## - Watch Video Solution

115. The sixth term of an AP is 2 , and its common difference is greater than one. The value of the common difference of the progression so that the product of the first, fourth and fifth terms is greatest is
A. -4
B. -6
C. -8
D. -10

## Answer: B

116. The interior angles of a polygon are in AP The smallest angle is 120 and the common difference is 5 . Find the number of sides of the polygon.
A. One
B. Two
C. Three
D. Infinitely many

## Answer: A

## - Watch Video Solution

117. The interior angles of a polygon are in AP The smallest angle is 120 and the common difference is 5 . Find the number of sides of the polygon.
A. $160^{\circ}$ only
B. $195^{\circ}$ only
C. Either $160^{\circ}$ or $195^{\circ}$
D. Nither 160 nor $195^{\circ}$

## Answer: A

## - Watch Video Solution

118. If $x^{\ln \left[\frac{y}{z}\right]} \cdot y^{\ln [x z]^{2}} \cdot z^{\ln \left[\frac{x}{y}\right]}=y^{4 \ln y}$ for any $\mathrm{x}>1, \mathrm{y}>1$ and $\mathrm{z}>1$, then which one of the following is correct?
A. $\ln \mathrm{y}$ is the GM of $\ln \mathrm{x}, \ln \mathrm{x}, \ln \mathrm{x}$ and $\ln \mathrm{z}$
B. $\ln \mathrm{y}$ is the AM of $\ln \mathrm{x}, \ln \mathrm{x}, \ln \mathrm{x}$ and $\ln \mathrm{z}$
C. $\ln \mathrm{y}$ is the HM of $\ln \mathrm{x}, \ln \mathrm{x}$ and $\ln \mathrm{z}$
D. $\ln \mathrm{y}$ is the AM of $\ln , \ln \mathrm{x}, \ln \mathrm{z}$ and $\ln \mathrm{z}$

## Answer: B

119. What is the sum of the series
$0.3+0.33+0.333+\ldots . n$ terms?
A. $\frac{1}{3}\left[n-\frac{1}{9}\left(1-\frac{1}{10^{n}}\right)\right]$
B. $\frac{1}{3}\left[n-\frac{2}{9}\left(1-\frac{1}{10^{n}}\right)\right]$
C. $\frac{1}{3}\left[n-\frac{1}{3}\left(1-\frac{1}{10^{n}}\right)\right]$
D. $\frac{1}{3}\left[n-\frac{1}{9}\left(1+\frac{1}{10^{n}}\right)\right]$

Answer: A

## - Watch Video Solution

120. If $(0,-3) \operatorname{and}(0,3)$ are the two vertices of an equilateral triangle, find the coordinates of its third vertex.
A. $m n$
B. $m+n$
C. $2(m+n)$
D. $-(m+n)$

## Answer: D

## - Watch Video Solution

121. The sum of the roots of the equation $x^{2}+b x+c=0$ (wheere b and c are non-zero) is equal to the sum of the reciprocals of their squares. Then $\frac{1}{c}, b, \frac{c}{b}$ are in
A. AP
B. GP
C. HP
D. None of the above

## Answer: C

122. The sum of the roots of the equation $a x^{2}+x+c=0$ ( where a and c are non-zero) is equal to the sum of the reciprocals of their squares. Then $a, c a^{2}, c^{2}$ are in
A. AP
B. GP
C. HP
D. None of the above

## Answer: A

## - Watch Video Solution

123. The fifth term of an AP of $n$ terms, whose sum is $n^{2}-2 n$, is
A. 5
B. 7
C. 8
D. 15

## Answer: B

## - Watch Video Solution

124. The sum of all 2 digited odd numbers is
A. 2475
B. 2530
C. 4905
D. 5049

## Answer: A

125. The sum of the first n terms of the series $\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+\ldots$. is equal to
A. $2^{n}-n-1$
B. $1-2^{-n}$
C. $2^{-n}+n-1$
D. $2^{n}-1$

## Answer: C

## - Watch Video Solution

126. Let $x, y, z$ be positive real numbers such that $x, y, z$ are in GP and $\tan ^{-1} y$ and $\tan ^{-1} z$ are in AP. Then which one of the following is correct?
A. $x=y=z$
B. $x z=1$
C. $x \neq y$ and $y=z$
D. $x=y$ and $y \neq z$

## Answer: A

## - Watch Video Solution

127. If $S_{n}=n P+\frac{n(n-1)}{2} Q$, where $S_{n}$ denotes the sum of the first $n$ terms of an A.P., then find the common difference.
A. $P+Q$
B. $2 P+3 Q$
C. $2 Q$
D. $Q$

## Answer: D

128. The value of the product $6^{\frac{1}{2}} \times 6^{\frac{1}{4}} \times 6^{\frac{1}{8}} \times 6^{\frac{1}{16}} \times \ldots$ up to infinite terms is
A. 6
B. 36
C. 216
D. 512

## Answer: A

## - Watch Video Solution

129. A person is to count 4500 currency notes. Let $a_{n}$, denote the number of notes he counts in the $n t h$ minute if $a_{1}=a_{2}=a_{3}=\ldots \ldots \ldots=a_{10}=150$ and $a_{10}, a_{11}, \ldots \ldots$. are in an $A P$ with common difference -2 , then the time taken by him to count all notes is :- (1) 24 minutes 1011 (2) 34 minutes (3) 125 minutes (4) 135 minutes
A. 24 minutes
B. 34 minutes
C. 125 minutes
D. 135 minutes

## Answer: B

## - Watch Video Solution

130. If $y=x+x^{2}+x^{3}+\ldots$ up to infinite terms where $x<1$, then which one of the following is correct?
A. $x=\frac{y}{1+y}$
B. $x=\frac{y}{1-y}$
C. $x=\frac{1+y}{y}$
D. $x=\frac{1-y}{y}$

## Answer: A

131. $\frac{1}{\log _{3} e}+\frac{1}{\log _{3} e^{2}}+\frac{1}{\log _{3} e^{4}}+\ldots=$
A. $\log _{e} 9$
B. 0
C. 1
D. $\log _{e} 3$

## Answer: A

## - Watch Video Solution

132. If $x_{1}$ and $x_{2}$ are positive quantities, then the condition for the difference between the arithmetic mean and the geometric mean to be greater than 1 is
A. $x_{1}+x_{2}>2 \sqrt{x_{1} x_{2}}$
B. $\sqrt{x_{1}}+\sqrt{\sqrt{x_{2}}>\sqrt{2}}$
C. $\left|\sqrt{x_{1}}+\sqrt{x_{2}}\right|>\sqrt{2}$
D. $x_{1}+x_{2}<2\left(\sqrt{x_{1} x_{2}}+1\right)$

## Answer: C

## - Watch Video Solution

133. If the ratio of $A M$ to $G M$ of two positive numbers $a$ and $b$ is $5: 3$, then $a: b$ is equal to
A. $3: 5$
B. 2:9
C. $9: 1$
D. $5: 3$

## Answer: C

134. If $x=1-y+y^{2}-y^{3}+\ldots$. . up to infinite terms, where $|y|<1$, then which one of the following is correct?
A. $x=\frac{1}{1+y}$
B. $x=\frac{y}{1-y}$
C. $x=\frac{y}{1+y}$
D. $x=\frac{y}{1-y}$

## Answer: A

## - Watch Video Solution

135. What is the sum of all two digit numbers which when divided by 3 leaves 2 as the remainder?
(a) 1565
(b) 1585

## (c)1635

(d) 1655
A. 1565
B. 1585
C. 1635
D. 1655

## Answer: C

## - Watch Video Solution

136. The third term of a GP is 3 . What is the product of the first five terms?
A. 216
B. 226
C. 243
D. Cannot be determined due to insuffcient data

## Answer: C

## - Watch Video Solution

137. If $x, \frac{3}{2}, z$ are in AP, $x, 3, z$ are in GP, then which one of the following will be in HP?
A. $x, 6, z$
B. x,4,z
C. x,2,z
D. x,1,z

## Answer: A

## - Watch Video Solution

138. An infinite G.P has first term x and sum 5 then x belongs to ?
A. $x<-10$
B. $-10<x<0$
C. $0<x<10$
D. $x<10$

## Answer: C

## D Watch Video Solution

139. The sum of the series $3-1+\frac{1}{3}-\frac{1}{9}+\ldots$. is equal to
A. $\frac{20}{9}$
B. $\frac{9}{20}$
C. $\frac{9}{4}$
D. $\frac{4}{9}$

## Answer: C

140. Let $T_{r}$ be the $r$ th term of an A.P., for $r=1,2,3$, If for some positive integers $m, n$, we have $T_{m}=\frac{1}{n} a n d T_{n}=\frac{1}{m}$, then $T_{m n}$ equals $\frac{1}{m n}$ b. $\frac{1}{m}+\frac{1}{n}$ c. 1 d. 0
A. $(m n)^{-1}$
B. $m^{-1}+\cap^{-1}$
C. 1
D. 0

## Answer: C

## D Watch Video Solution

141. If $2^{n d}$ term of GP is 2 and the sum of infinite terms is 8 find the first term
A. $8,2, \frac{1}{2}, \frac{1}{8}, \ldots \ldots$
B. $10,2, \frac{2}{5}, \frac{2}{25}, \ldots \ldots$
C. $4,2,1, \frac{1}{2}, \frac{1}{2^{2}}, \ldots \ldots$
D. $6,3, \frac{3}{2}, \frac{3}{4}, \ldots \ldots$

## Answer: C

## - Watch Video Solution

142. If $a, b, c$ are in AP or GP or HP , then $\frac{a-b}{b-c}$ is equal to
A. $\frac{b}{a}$ or 1 or $\frac{b}{c}$
B. $\frac{c}{a}$ or $\frac{c}{b}$ or 1
C. 1 or $\frac{a}{b}$ or $\frac{a}{c}$
D. 1 or $\frac{a}{b}$ or $\frac{c}{a}$

## Answer: C

143. If $\sin \beta$ is the harmonic mean of $\sin \alpha$ and $\cos \alpha$, and $\sin \theta$ is the arithmetic mean of $\sin \alpha$ and $\cos \alpha$, then which of the following is/are correct?
144. $\sqrt{2} \sin \left(\alpha+\frac{\pi}{4}\right) \sin \beta=\sin 2 \alpha$
145. $\sqrt{2} \sin \theta=\cos \left(\alpha-\frac{\pi}{4}\right)$

Select the correct answer using the code given below:
A. 1 only
B. 2 only
C. Both 1 and 2
D. Neither 1 nor 2

## Answer: C

## - Watch Video Solution

144. If $x_{i}>0, y_{i}>0(i=1,2,3, \ldots \ldots n)$ are the values of two variable X and Y with geometric mean P and Q respectively, then the geometric
mean of $\frac{X}{Y}$ is
A. $\frac{P}{Q}$
B. $\operatorname{antilog}\left(\frac{P}{Q}\right)$
C. $n(\log P-\log Q)$
D. $n(\log P+\log Q)$

## Answer: B

## - Watch Video Solution

145. What is the $n^{\text {th }}$ term of the sequence $25,-125,625,-3125, \ldots$ ?
A. $(-5)^{2 n-1}$
B. $(-1)^{2 n} 5^{n+1}$
C. $(-1)^{2 n-1} 5^{n+1}$
D. $(-1)^{n-1} 5^{n+1}$

## Answer: D

146. The number 1,5 and 25 can be three terms (not necessarily consecutive) of
A. only one AP
B. more than one but $\widehat{u}$ nite numbers of $A P s$
C. in $\widehat{u}$ nite number of $A P s$
D. $\widehat{u}$ nite number of $G P s$

## Answer: C

## - Watch Video Solution

147. The sum of $(p+q)^{t h}$ and $(p-q)^{t h}$ terms of an AP is equal to
A. $(2 p)^{t h}$ term
B. $(2 q)^{\text {th }}$ term
C. Twice the $p^{\text {th }}$ term
D. Twice the $q^{\text {th }}$ term

## Answer: C

## - Watch Video Solution

148. What is the Fourth term of an AP of n terms whose sum is $\mathrm{n}(n+1)$ ?
A. 6
B. 8
C. 12
D. 20

## Answer: B

## - Watch Video Solution

