



## PHYSICS

### BOOKS - HC VERMA PHYSICS (HINGLISH)

#### HEAT TRANSFER

##### Examples

1. One face of a copper cube of edge 10 cm is maintained at  $100^{\circ}C$  and the opposite face is maintained at  $0^{\circ}C$ . All other surfaces are covered with an insulating material. Find the amount of heat flowing per second through the cube. Thermal conductivity of copper is  $385Wm^{-1} (^{\circ}C^{-1})$ .

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2. Find the thermal resistance of an aluminium rod of length 20cm and area of cross section  $1\text{cm}^2$ . The heat current is along the length of the rod. Thermal conductivity of aluminium  $= 200\text{Wm}^{-1}\text{K}^{-1}$ .

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3. The light from the sun is found to have a maximum intensity near the wavelength of 470nm. Assuming that the surface of the sun emits as a blackbody, calculate the temperature of the surface of the sun.

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4. A blackbody of surface area  $10\text{cm}^2$  is heated  $\rightarrow 127^\circ\text{C}$  and is suspended in a room at temperature  $27^\circ\text{C}$ . Calculate the initial rate of loss of heat from the body to the room.

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5. A liquid cools from  $70^{\circ}\text{C} \rightarrow 60^{\circ}\text{C}$  in 5 minutes. Calculate the time taken by the liquid to cool from  $60^{\circ}\text{C}$  to  $50^{\circ}\text{C}$ , if the temperature of the surroundings is constant at  $30^{\circ}\text{C}$ .



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## Worked Out Examples

1. The lower surface of a slab of stone of face-area  $3600\text{cm}^2$  and thickness  $10\text{cm}$  is exposed to steam at  $100^{\circ}\text{C}$ . A block of ice at  $0^{\circ}\text{C}$  rests on the upper surface of the slab.  $4.8\text{g}$  of ice melts in one hour. Calculate the thermal conductivity of the stone. Latent heat of fusion of ice  $= 3.36 \times 10^5 \text{ J kg}^{-1}$



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2. An icebox made of 1.5cm thick styrofoam has dimensions  $60\text{cm} \times 60\text{cm} \times 30\text{cm}$ . It contains ice at which the ice is melting. Latent heat of fusion of ice is  $3.36 \times 10^5 \text{ J kg}^{-1}$  and thermal conductivity of styrofoam is  $0.04 \text{ W m}^{-1} \text{ } ^\circ\text{C}^{-1}$ .

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3. A closed cubical box is made of perfectly insulating material and the only way for heat to enter or leave the box is through two solid cylindrical metal plugs, each of cross sectional area  $12\text{cm}^2$  and length 8cm fixed in the opposite walls of the box. The outer surface of one plug is kept at a temperature of  $100^\circ\text{C}$  while the outer surface of the other plug is maintained at a temperature of  $4^\circ\text{C}$ . The thermal conductivity of the material of the plug is  $2.0 \text{ W m}^{-1} \text{ } ^\circ\text{C}^{-1}$ . A source of energy generating 13W is enclosed inside the box. Find the equilibrium temperature of the inner surface of the box assuming that it is the same at all points on the inner surface.

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4. A bar of copper of length 75cm and a bar of steel of length 125cm are joined together end to end. Both are of circular cross section with diameter 2cm. The free ends of the copper and the steel bars are maintained at  $100^\circ C$  and  $0^\circ C$

respectively. The curved surface of the bars are thermally insulated. What is the amount of heat transmitted per unit time across the junction? The thermal conductivity of copper is  $386 \text{ Js}^{-1} \text{ m}^{-1} \text{ } ^\circ C^{-1}$  and that of steel is  $46 \text{ Js}^{-1} \text{ m}^{-1} \text{ } ^\circ C^{-1}$



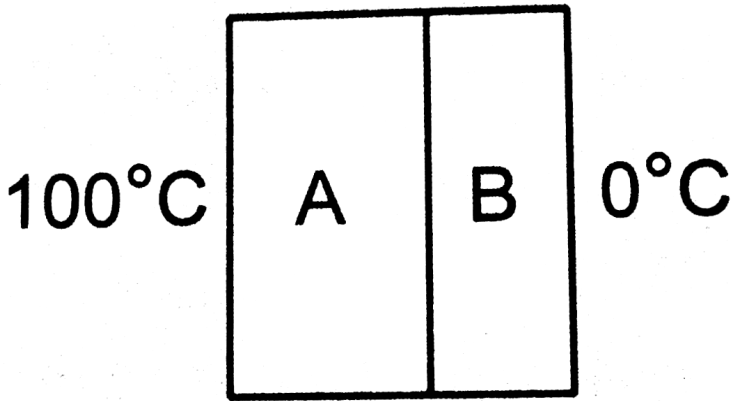
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5. Two parallel plates A and B are joined together to form a compound plate. The thicknesses of the plates are 4.0cm and 2.5cm respectively and the area of cross section is  $100 \text{ cm}^2$  for each plate. The thermal conductivities are  $K_A = 200 \text{ W m}^{-1} \text{ } ^\circ C^{-1}$

for the plate A and  $K_B = 100 \text{ W m}^{-1} \text{ } ^\circ C^{-1}$  for the plate B. The outer surface of the plate A is maintained at  $100^\circ C$  and the outer surface of the plate B is maintained at  $0^\circ C$ .

Find (a) the rate of heat flow through any cross section, (b) the temperature at the junction.

interface and (c) the equivalent thermal conductivity of the compound plate.



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6. A room has a  $4m \times 4m \times 10cm$  concrete roof ( $K = 1.26Wm^{-1} (^{\circ}C)^{-1}$ ). At some instant, the temperature outside is  $40(^{\circ}C)$  and  $t_{in}$  is  $32(^{\circ}C)$ . (a) Neglecting convection, calculate the amount of heat flowing per second into the room through the roof. (b) Bricks ( $K = 0.65Wm^{-1} (^{\circ}C)^{-1}$ ) of thickness  $7.5cm$  are laid down on the roof. Calculate the new rate of heat flow under the same temperature conditions.

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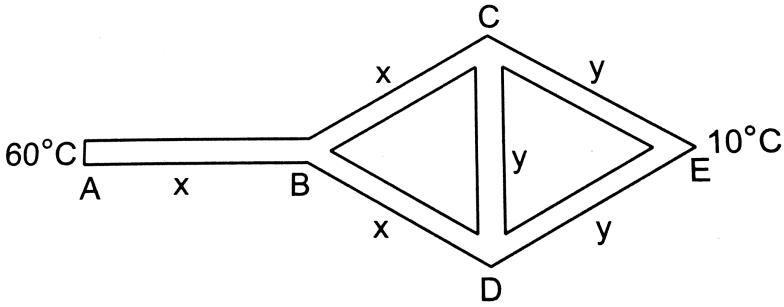
7. An electric heater is used in a room of total wall area  $137\text{m}^2$  →  $ma \int a \in$  a temperature of  $20^\circ\text{C}$  inside it, when the outside temperature is  $-10^\circ\text{C}$ . The wall has three different layers of materials. The innermost layer is of wood of thickness  $2.5\text{cm}$ , the middle layer is of cement of thickness  $1.0\text{cm}$  and the outermost layer is of brick of thickness  $25.0\text{cm}$ . Find the power of the electric heater. Assume that there is no heat loss through the floor and the ceiling. The thermal conductivities of wood, cement and brick are  $0.125\text{Wm}^{-1}\text{C}^{-1}$ ,  $1.5\text{Wm}^{-1}\text{C}^{-1}$  and  $1.0\text{Wm}^{-1}\text{C}^{-1}$  respectively.



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8. Three rods of material x and three of material y are connected as shown in figure. All the rods are identical in length and cross sectional area. If the end A is maintained at  $60^\circ\text{C}$  and the junction E at  $10^\circ\text{C}$ , calculate the temperature of the junction B. The thermal conductivity of x

is  $800 \text{ W m}^{-1} (\text{C}^{-1})$  and  $t_{\text{fyis}} 400 \text{ W m}^{-1} (\text{C}^{-1})$ .

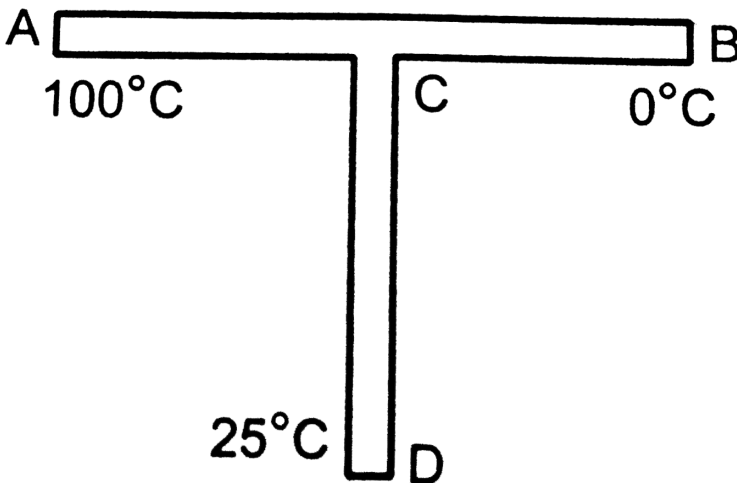


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9. A rod CD of thermal resistance

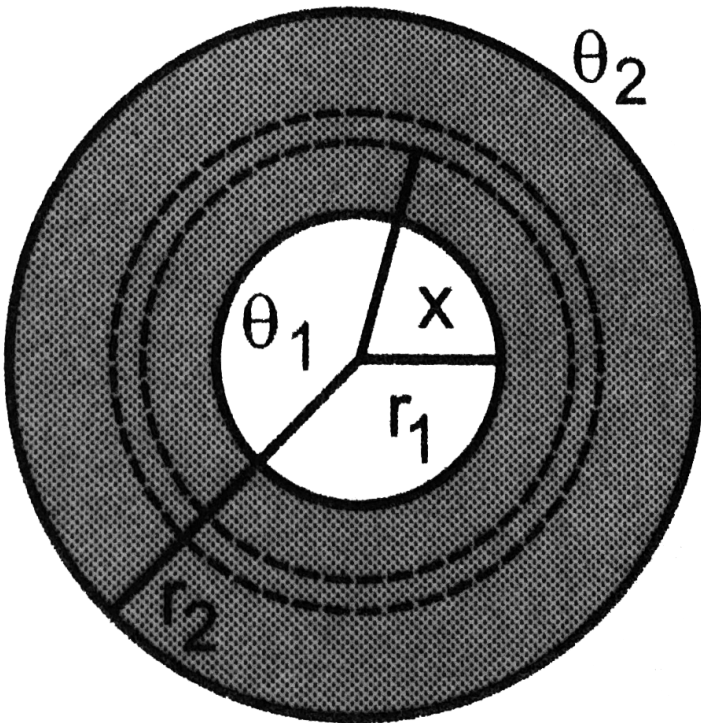
$5.0 \text{ KW}^{-1}$  is joined at the middle of an identical rod AB as shown in figure.

$100^\circ\text{C}$ ,  $0^\circ\text{C}$  and  $25^\circ\text{C}$  respectively. Find the heat current in CD.

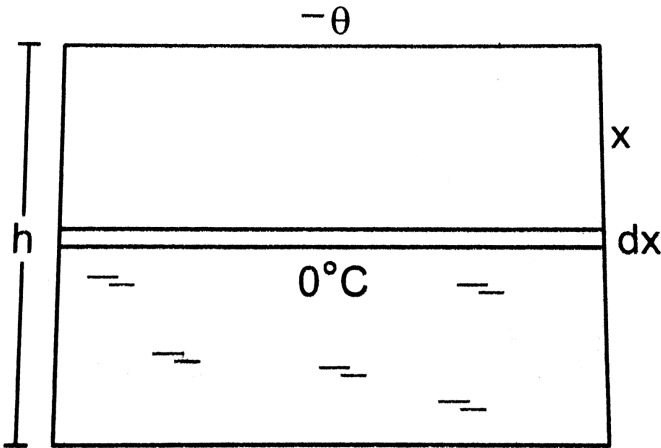




10. Two thin metallic spherical shells of radii  $r_1$  and  $r_2$  ( $r_1 < r_2$ ) are placed with their centres coinciding. A material of thermal conductivity  $K$  is filled in the space between the shells. The inner shells. Is maintained at temperature  $\theta_1$  .and the outer shell at temperature  $\theta_2$  ( $\theta_1 < \theta_2$ ). Calculate the rate at which heat flows radially through the material.



11. On a cold winter day, the atmospheric temperature is  $-\theta$  (on Celsius scale) which is below  $0^\circ\text{C}$ . A cylindrical drum of height  $h$  made of a bad conductor is completely filled with water at  $0^\circ\text{C}$  and is kept outside without any lid. Calculate the time taken for the whole mass of water to freeze. Thermal conductivity of ice is  $K$  and its latent heat of fusion is  $L$ . Neglect expansion of water on freezing.



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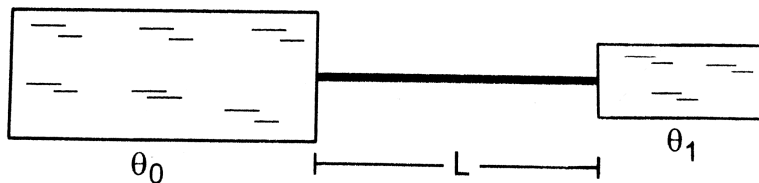
12. Figure shows a large tank of water at a constant temperature  $\theta_0$  . and a small vessel containing a mass  $m$  of water at an initial temperature

$\theta_1 < \theta_0$ . Amplitude of  $\leq n > hL$ , area of cross section  $A$  and thermal conductivity

$\in$  thermal vessel  $\rightarrow$  become

$\theta_2 - \theta_1 = \frac{L}{kA} \frac{dQ}{dt}$ . Specific heat capacity of water

is  $s$  and all other heat capacities are negligible.



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**13.** One mole of an ideal monatomic gas is kept in a rigid vessel. The vessel is kept inside a steam chamber whose temperature is  $97^\circ C$ . Initially, the temperature of the gas is  $5.0^\circ C$ . The walls of the vessel have an inner surface of area  $800\text{cm}^2$  and thickness  $1.0\text{cm}$ . If the temperature of the gas increases to  $9.0^\circ C$  in  $0.5$  second, find the thermal conductivity of the material of the walls.

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14. monatomic ideal gas is contained in a rigid container of volume  $V$  with walls of total inner surface area  $A$ , thickness  $x$  and thermal conductivity  $K$ . The gas is at an initial temperature  $t_0$  and pressure  $P_0$ . Find the pressure of the gas as a function of time if the temperature of the surrounding air is  $T_s$ . All temperatures are in absolute scale.



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15. Consider a cubical vessel of edge  $a$  having a small hole in one of its walls of radius  $r$ . At time  $t = 0$ , it contains air at atmospheric pressure  $p_a$  and temperature  $T(0)$ . The temperature of the surrounding air is  $T_a$  ( $T_a > T(0)$ ). The amount of gas ( $m \leq M$ ) in the vessel at time  $t$ . Take  $C_v$  of air  $\rightarrow \frac{5R}{2}$ .



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16. A blackbody of surface area  $1\text{cm}^2$  is placed inside an enclosure. The enclosure has a constant temperature  $27(^{\circ})\text{C}$  and the blackbody is maintained at  $327(^{\circ})\text{C}$  by heating it electrically. What electric power is needed to maintain the temperature?  $\sigma = 6.0 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ .

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17. An electric heater emits  $100\text{W}$  of thermal radiation. The coil has a surface area of  $0.02\text{m}^2$ . Assuming that the coil radiates like a blackbody, Find its temperature.  $\sigma = 6.00 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ .

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18. The earth receives solar radiation at a rate of  $8.2\text{Jcm}^{-2}\text{min}^{-1}$ . Assuming that the sun radiates like a blackbody, calculate the surface of the sun. The angle subtended by the sun on the earth is  $0.55(^{\circ})\text{C}$  and the stefan constant  $\sigma = 5.67 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ .

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19. The temperature of a body falls from  $40^{\circ}C$  to  $36(^{\circ})C$  in 5 minutes when placed in a surrounding of constant temperature  $16(^{\circ})C$ . Find the time taken for the temperature of the body to become  $32(^{\circ})C$ .

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20. A hot body placed in air is cooled down according to Newton's law of cooling, the rate of decrease of temperature being  $k$  times the temperature difference from the surrounding. Starting from  $t = 0$ , find the time in which the body will lose half the maximum heat it can lose.

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## Short Answer

1. The heat current is written as  $\frac{\Delta Q}{\Delta t}$ . Why don't we write  $\frac{dQ}{dt}$ ?



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2. Does a body at  $20^{\circ}C$  radiate in a room, where the room temperature is  $30^{\circ}C$  ? If yes, why does its temperature not fall further?



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3. Why does blowing over a spoonful of hot tea cools it ? Does evaporation play a role ? Does radiation play a role ?



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4. On a hot summer day we want to cool our room by opening the refrigerator door and closing all the windows and doors. Will the process work ?



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5. On a cold winter night you are asked to sit on a chair. Would you like to choose a metal chair or a wooden chair? Both are kept in the same lawn and are at the same temperature.

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6. Two identical metal balls one at  $T_1 = 300K$  and the other  $T_2 = 600K$  are kept at a distance of 1m in vacuum. Will the temperatures equalise by radiation? Will the rate of heat gained by the colder sphere be proportional to  $T_2^4 - T_1^4$  as may be expected from the Stefan's law?

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7. An ordinary electric fan does not cool the air, still it gives comfort in summer. Explain.

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8. The temperature of the atmosphere at a high altitude is around  $-50^{\circ}\text{C}$ . Yet an animal there would freeze to death and not boil. Explain.

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9. Standing in the sun is more pleasant on a cold winter day than standing in shade. Is the temperature of air in shade?

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10. Cloudy nights are warmer than the nights with clean sky. Explain.

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11. Why is a white dress more comfortable than a dark dress in summer?

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## Objective 1

1. The thermal conductivity of a rod depends on

- A. length
- B. mass
- C. area of cross section
- D. material of the rod.

**Answer: D**



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2. In a room containing air,, heat can go from one place to another

- A. by conduction only
- B. by convection only

C. by radiation only

D. by all the three modes.

**Answer: D**



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3. A solid at temperature  $T_1$  is kept in an evacuated chamber at temperature  $T_2 > T_1$ . The rate of increase of temperature of the body is proportional to

A.  $T_2 - T_1$

B.  $T_2^2 - T_1^2$

C.  $T_2^3 - T_1^3$

D.  $T_2^2 - T_1^4$ .

**Answer: D**



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4. The thermal radiation emitted by a body is proportional to  $T^n$  where T is its absolute temperature. The value of n is exactly 4 for

- A. a blackbody
- B. all bodies
- C. bodies painted black only
- D. polished bodies only.

**Answer: B**



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5. Two bodies A and B having equal surface areas are maintained at temperatures  $10^\circ C$  . And  $20^\circ C$  . The thermal radiation emitted in a given time by A and B are in the ratio

- A. 1: 1.15

B. 1:02

C. 1:04

D. 1:16 .

**Answer: A**



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6. One end of a metal rod is kept in a furnace. In steady state, the temperature of the rod

A. increases

B. decreases

C. remains constant

D. is non uniform.

**Answer: D**



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7. Newton's law of cooling is a special case of

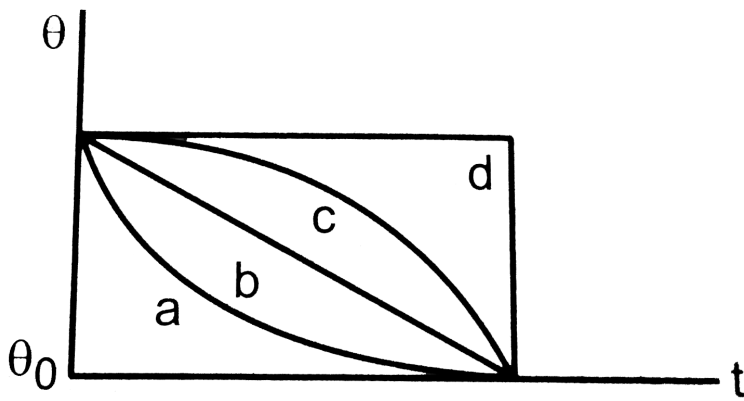
- A. Wien's displacement law
- B. Krichhoff's law
- C. Stefan's law
- D. planck's law.

**Answer: C**



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8. A hot liquid is kept in a big room. Its temperature is plotted as a function of time. Which of the following curves may represent the plot?



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9. A hot liquid is kept in a big room. The logarithm of the numerical value of the temperature difference between the liquid and the room is plot will be very nearly

- A. a straight line
- B. a circular arc
- C. a parabola
- D. an ellipse.

**Answer: A**



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10. A body cools down from  $65^{\circ}C$  to  $60^{\circ}C$  in 5 minutes. It will cool down from  $60^{\circ}C$  to  $55^{\circ}C$  in

A. 5 minutes

B. less than 5 minutes

C. more than 5 minutes

D. less than or more than 5 minutes depending on whether its mass is more than or less than  $1kg$

Answer: C



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Objective 2



1. One end of a metal rod is dipped in boiling water and the other is dipped in melting ice.

- A. all parts of the rod are in thermal equilibrium with each other
- B. we can assign a temperature to the rod
- C. we can assign temperature to the rod after steady state is reached.
- D. the state of the rod does not change after steady state is reached

**Answer: D**



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2. A blackbody does not

- A. emit radiation
- B. absorb radiation
- C. reflect radiation
- D. refract radiation.

**Answer: C::D**



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**3.** In summer, a mild wind is often found on the shore of a clam river. This is caused due to

- A. difference in thermal conductivity of water and soil
- B. convection currents
- C. conduction between air and the soil
- D. radiation from the soil

**Answer: B**



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**4.** A piece of charcol and a piece of shining steel of the same surface area are kept for a long time in an open lawn in bright sun.

- A. The steel will absorb more heat than the charcoal.
- B. The temperature of the steel will be higher than that of the charcoal.
- C. If both are picked up by bare hands, the steel will be felt hotter than the charcoal.
- D. If the two are picked up from the lawn and kept in a cold chamber, the charcoal will lose heat at a faster rate than the steel.

**Answer: C::D**



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5. A hotter body emits radiation which has maximum intensity near the frequency  $\nu_0$ . The emissivity of the material is  $\frac{1}{5}$ . If the absolute temperature of the body is doubled,

- A. the maximum intensity of radiation will be near the frequency  $2\nu_0$
- B. the maximum intensity of radiation will be near the frequency  $\frac{\nu_0}{2}$

C. the total energy emitted will increase by a factor of 16

D. the total energy emitted will increase by a factor of 8.

**Answer: A:C**



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6. A solid sphere and a hollow sphere of the same material and of equal radii are heated to the same temperature.

A. Both will emit equal amount of radiation per unit time in the beginning.

B. Both will absorb equal amount of radiation from the surrounding in the beginning.

C. The initial rate of cooling  $\left(\frac{dT}{dt}\right)$  will be the same for the two spheres.

D. The two spheres will have equal temperature at any instant.

Answer: A::B



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## Exercises

1. A uniform slab of dimension  $10\text{cm} \times 10\text{cm} \times 1\text{cm}$  is kept between two heat reservoirs at temperatures  $10^\circ\text{C}$  and  $90^\circ\text{C}$ . The thermal conductivity of the slab is  $0.80\text{Wm}^{-1}\text{K}^{-1}$ . Find the amount of heat flowing through the slab per minute.



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2. A liquid-nitrogen container is made of a  $1\text{cm}$  thick styrofoam sheet having thermal conductivity  $0.025\text{Js}^{-1}\text{m}^{-1}\text{K}^{-1}$ . Liquid nitrogen is kept in it. The area of the top surface is  $0.80\text{m}^2$ . The atmospheric temperature is  $30^\circ\text{C}$ .

300K. Calculate the rate of heat flow from the atmosphere to the liquid nitrogen.

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3. The normal body-temperature of a person is  $97(^{\circ}F)$ . Calculate the rate at which heat is flowing out of this body through the clothes assuming the following values. Room temperature  $= 47^{\circ}F$ , surface of the body under clothes  $= 1.6m^2$ , conductivity of the cloth  $= 0.04Js^{-1}m^{-1} (^{\circ}C)^{-1}$ , thickness of the cloth  $= 0.5cm$ .

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4. Water is boiled in a container having a bottom of surface area  $25cm^2$ , thickness  $1.0mm$  and thermal conductivity  $50Wm^{-1} (^{\circ}C)^{-1}$ , 100g of water is converted into steam per minute in the steady state after the boiling starts. Assuming that no heat is lost to the atmosphere, calculate the temperature of the lower surface of the bottom. Latent heat of vaporization of water  $= 2.26 \times 10^6 Jkg^{-1}$ .



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5. One end of a steel rod ( $K = 46 \text{ Js}^{-1} \text{ m}^{-1} \text{ } ^\circ\text{C}^{-1}$ ) of length  $l = 1.0 \text{ m}$  is kept in ice at  $0^\circ\text{C}$  and the other end is kept in boiling water at  $100^\circ\text{C}$ . The area of cross section of the rod is  $0.04 \text{ cm}^2$

. As  $\sum \in$  no heat loss  $\rightarrow$  the atmosphere,  $f \in$  the mass of the ice melted  $<$   
 $= 3.36 \times 10^5 \text{ J kg}^{-1}$ .



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6. An icebox almost completely filled with ice at  $0^\circ\text{C}$  is dipped into a large volume of water at  $20^\circ\text{C}$ . The box has walls of surface area  $2400 \text{ cm}^2$  thickness  $2.0 \text{ mm}$  and thermal conductivity  $0.06 \text{ W m}^{-1} \text{ } ^\circ\text{C}^{-1}$ . Calculate the rate at which the ice melts in the box. Let latent heat of fusion of ice  $= 3.4 \times 10^5 \text{ J kg}^{-1}$ .



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7. A pitcher with  $1 - mm$  thick porous walls contain  $10kg$  of water. ,Water comes to its outer surface and evaporates at the rate of  $0.1gs^{-1}$  . The surface area of the pitcher (one side) =  $200cm^2$  . The room temperature =  $42^{\circ}C$  , latent heat of vaporization =  $2.27 \times 10^6 Jkg^{-1}$  , and the thermal conductivity of the porous walls =  $0.80js^{-1}m^{-1}^{\wedge}(@)C^{\wedge}(-1)^{\wedge}$  . Calculate the temperature of water in the pitcher when it attains a constant value.

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8. A steel frame ( $K = 45Wm^{-1}^{\wedge}(@)C^{\wedge}(-1)^{\wedge}$ ) of  $\rightarrow tal \leq n > h60cm$  and *cross section area*  $0.02cm^{\wedge}(2)$  ,  $F$  or  $msthreeside$  of a  $\square$  . The  $\rightarrow ends$  are at  $20^{\wedge}(@)C$  and  $40^{\wedge}(@)C$  . Find the rate of heat flow through a cross section of the frame.

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9. Water at  $50^\circ\text{C}$  is filled in a closed cylindrical vessel of height  $10\text{cm}$  and cross sectional area  $10\text{cm}^2$ . The walls of the vessel are adiabatic but the flat parts are made of  $1\text{mm}$  thick aluminium ( $K = 200\text{Js}^{-2}\text{m}^{-1}$ ).

The density of water is  $1000\text{kgm}^{-3}$

and the specific heat capacity of water  $= 4200\text{Jkg}^{-1}\text{ }^\circ\text{C}^{-1}$

Estimate the time taken for the temperature to fall by  $1.0^\circ\text{C}$ . Make any simplifying assumption you need but specify them.

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10. The left end of a copper rod ( $l = 20\text{cm}$ . Area of cross section  $= 0.02\text{cm}^2$ ) is maintained at  $20^\circ\text{C}$  and the right end is maintained at  $80^\circ\text{C}$ . Neglecting any loss of heat through radiation, find (a) the temperature at a point  $11\text{cm}$  from the left end and (b) the heat current through the rod. thermal conductivity of copper  $= 385\text{Wm}^{-1}\text{ }^\circ\text{C}^{-1}$ .

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11. The ends of a metre stick are maintained at  $100^\circ C$  and  $0^\circ C$ . One end of a rod is maintained at  $25^\circ C$ . Where should its other end be touched on the metre stick so that there is no heat current in the rod in steady state?

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12. A cubical box of volume  $216\text{cm}^3$  is made up of  $0.1\text{cm}$  thick wood. The  $\in$  side is heated  $\le$  ctrically by  $100\text{W}$  heater. It is for  $5^\circ C$ . In steady state. Assuming that the entire electrically energy spent appears as heat, find the thermal conductivity of the material of the box.

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13. Figure shows water in a container having  $2.0\text{mm}$  thick walls made of a material of thermal conductivity  $0.50\text{Wm}^{-1}^\circ C^{-1}$

. The contact area  $\in$   $0.05 \text{ m}^2$  and  $g = 10 \text{ m/s}^2$

. The wheel is clamped to the side of the water and its surface area is  $0.05 \text{ m}^2$

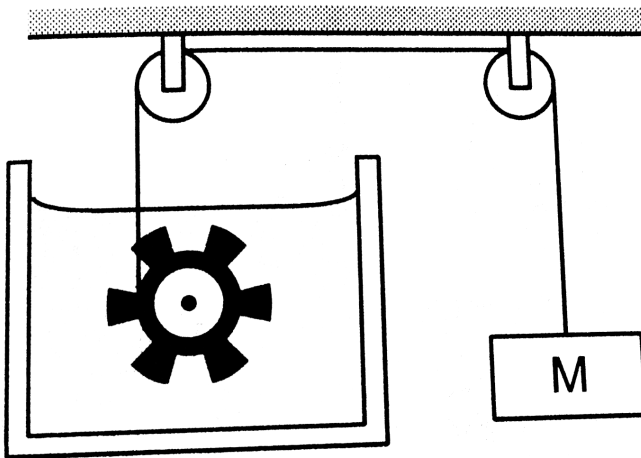
. A block of mass  $M$  is suspended from the other end of the string. The system is released from rest at  $t = 0$  and the temperature of the water remains constant at  $10^\circ \text{C}$

. The temperature of the water remains constant at  $10^\circ \text{C}$

.  $g = 10 \text{ m/s}^2$

.  $F$  is the force exerted by the water on the block. As  $\sum \vec{F} = 0$  the heat flow out of the water only through the surface of the block.

$g = 10 \text{ m/s}^2$



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14. On a winter day when the atmospheric temperature drops to  $-10^\circ \text{C}$ , ice forms on the surface of a lake. (a) Calculate the rate of increase of

thickness of the ice when 10cm of ice is already formed. (b) Calculate the total time taken in forming 10cm of ice. Assume that the temperature of the entire water reaches  $0^\circ C$  before the ice starts forming. Density of water =  $1000 \text{ kg m}^{-3}$ , latent heat of fusion of ice =  $3.36 \times 10^5 \text{ J kg}^{-1}$  and thermal conductivity of ice =  $1.7 \text{ W m}^{-1} \text{ } ^\circ\text{C}^{-1}$ . Neglect the expansion of water on freezing.

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15. Consider the situation of the previous problem. Assume that the temperature of the water at the bottom of the lake remains constant at  $4^\circ C$  as the ice forms on the surface (the heat required to maintain the temperature of the bottom layer may come from the bed of the lake). The depth of the lake is 1.0m. Show that the thickness of the ice is not a steady state phenomenon. Take other relevant data from the previous problem.

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16. Three rods of lengths 20cm each and area of cross section  $1\text{cm}^2$  are joined to form a triangle ABC. The conductivities of the rods are

$$k_{AB} = 50\text{Js}^{-1}\text{m}^{-1}(\text{C}^{-1}), k_{BC} = 200\text{Js}^{-1}\text{m}^{-1}(\text{C}^{-1}), \text{ and}$$

$$k_{AC} = 400\text{Js}^{-1}\text{m}^{-1}(\text{C}^{-1})$$

The junctions A, B and C are maintained at  $40^\circ\text{C}$ ,  $80^\circ\text{C}$  and

$80^\circ\text{C}$  respectively. Find the rate of heat flowing through the rods AB, AC and BC.

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17. A semicircular rod is joined at its end to a straight rod of the same material and the same cross-sectional area. The straight rod forms a diameter of the other rod. The junctions are maintained at different temperatures. Find the ratio of the heat transferred through a cross section of the straight rod in a given time.

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18. A metal rod of cross sectional area  $1.0\text{cm}^2$  is being heated at one end. At one time, the temperature gradient is  $5.0^\circ\text{Ccm}^{-1}$  at cross section A and is  $2.5^\circ\text{Ccm}^{-1}$  at cross section B. calculate the rate at which the temperature is increasing in the part AB of the rod. The heat capacity of the part AB =  $0.40\text{J}^\circ\text{C}^{-1}$ , thermal conductivity of the material of the rod.  $K = 200\text{Wm}^{-1}\text{C}^{-1}$ . Neglect any loss of heat to the atmosphere.



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19. Steam at  $120^\circ\text{C}$  is continuously passed through a 50-cm long tube of  $\frac{1}{2}$  inch inner radius and outer radius 1.0cm and 1.2cm. The steam temperature is  $30^\circ\text{C}$ . Calculate the rate of heat flow through the wall of the tube. Thermal conductivity =  $0.15\text{Js}^{-1}\text{m}^{-1}(\text{ }^\circ\text{C})^{-1}$ .



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20. A hole of radius  $r_1$  is made centrally in a uniform circular disc of thickness  $d$  and radius  $r_2$ . The inner surface (a cylinder of length  $d$  and radius  $r_1$  is maintained at a temperature  $\theta_1$  and the outer surface (a cylinder of length  $d$  and radius  $r_2$ . The is maintained at a temperature  $\theta_2$  ( $\theta_1 > \theta_2$ ). The thermal conductivity of the material of the disc is  $K$ . Calculate the heat flowing per unit time through the disc.

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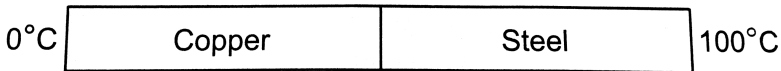
21. A hollow tube has a length  $l$ , inner radius  $R_1$  and outer radius  $R_2$ . The material has a thermal conductivity  $K$ . Find the heat flowing through the walls of the tube if (a) the flat ends are maintained at temperature  $T_1$  and  $T_2$  ( $T_2 > T_1$ ) (b) the inside of the tube is maintained at temperature  $T_1$  and the outside is maintained at  $T_2$ .

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22. A composite slab is prepared by pasting two plates of thickness  $L_1$  and  $L_2$  and thermal conductivities  $K_1$  and  $K_2$ . The slab has equal cross-sectional area. Find the equivalent conductivity of the composite slab.

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23. Figure shows a copper rod joined to a steel rod. The rods have equal length and the equal cross-sectional area. The free end of the copper rod is kept at  $0^\circ\text{C}$  and that of the steel rod is kept at  $100^\circ\text{C}$ . Find the temperature at the junction of the rods. Conductivity of copper  $= 390\text{Wm}^{-1}\text{C}^{-1}$  and  $k_{\text{steel}} = 46\text{Wm}^{-1}\text{C}^{-1}$ .

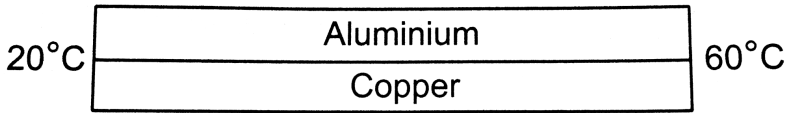


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24. An aluminium rod and a copper rod of equal length  $1.0\text{m}$  and cross-sectional area  $1\text{cm}^2$  are welded together as shown in figure. One end is

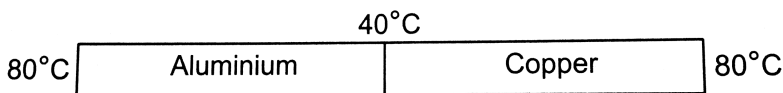


kept at a temperature of  $20^{\circ}\text{C}$  and the other at  $60^{\circ}\text{C}$ . Calculate the amount of heat taken out per second from the hot end. Thermal conductivity of aluminium =  $200\text{Wm}^{-1}\text{C}^{-1}$  and of copper =  $390\text{Wm}^{-1}\text{C}^{-1}$ .



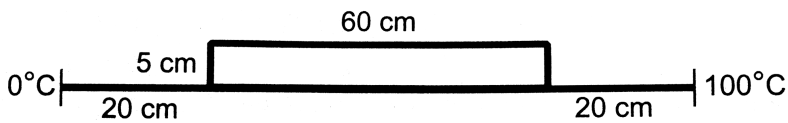
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25. Figure shows an aluminium rod joined to a copper rod. Each of the rods has a length of  $20\text{cm}$  and area of cross section  $0.20\text{cm}^2$ . The junction is maintained at a constant temperature  $40^{\circ}\text{C}$  and the two ends are maintained at  $80^{\circ}\text{C}$ . Calculate the amount of heat taken out from the cold junction  $\epsilon \neq \text{min utea}$ .  
 $K_{\text{Al}} = 200\text{Wm}^{-1}\text{C}^{-1}$  and  $K_{\text{Cu}} = 400\text{Wm}^{-1}\text{C}^{-1}$ .



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26. Consider the situation shown in figure. The frame is made of the same material and has a uniform cross-section area everywhere. Calculate the amount of heat flowing per second through a cross section of the bent part if the total heat taken out per second from the end at  $100^\circ\text{C}$  is  $130\text{J}$ .



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27. Suppose the bent part of the frame of the previous problem has a thermal conductivity of  $780\text{ s}^{-1}\text{ m}^{-1}\text{ }^\circ\text{C}^{-1}$  whereas it is  $390\text{ J s}^{-1}\text{ m}^{-1}\text{ }^\circ\text{C}^{-1}$  for the straight part. Calculate the rate of heat flow through the straight part.

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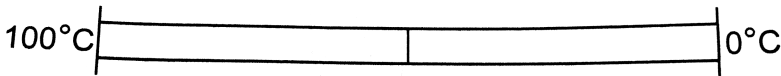
28. A room has a window fitted with a single  $0.1\text{m} \times 2.0\text{m}$  glass of thickness 2mm. (a) Calculate the rate of heat flow through the closed window when the temperature inside the room is  $32^\circ\text{C}$  and  $t_{\text{outside}} = 40^\circ\text{C}$

(b) The glass is now replaced by two glass panes, each having a thickness  $\neq s$  so that the rate of heat flow under the same condition of temperature. Thermal conductivity of glass is  $1.0\text{Js}^{-1}\text{m}^{-1}\text{C}^{-1}$  and that of air is  $0.025\text{Js}^{-1}\text{m}^{-1}\text{C}^{-1}$ .



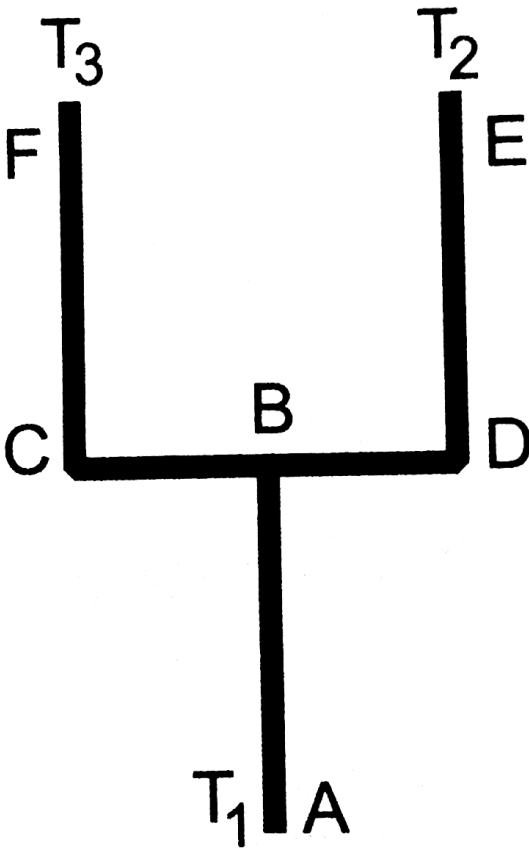
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29. The two rods shown in figure have identical geometrical dimensions. They are in contact with two heat baths at temperatures  $100^\circ\text{C}$  and  $0^\circ\text{C}$ . The temperature of the junction is  $70^\circ\text{C}$ . Find the temperature of the junction if the rods are interchanged.



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30. Four identical rods AB, CD, CF and DE are joined as shown in figure. The length, cross-sectional area and thermal conductivity of each rod are  $l$ ,  $A$  and  $K$  respectively. The ends A, E and F are maintained at temperature  $T_1$ ,  $T_2$  and  $T_3$  respectively. Assuming no loss of heat to the atmosphere, find the temperature at B.



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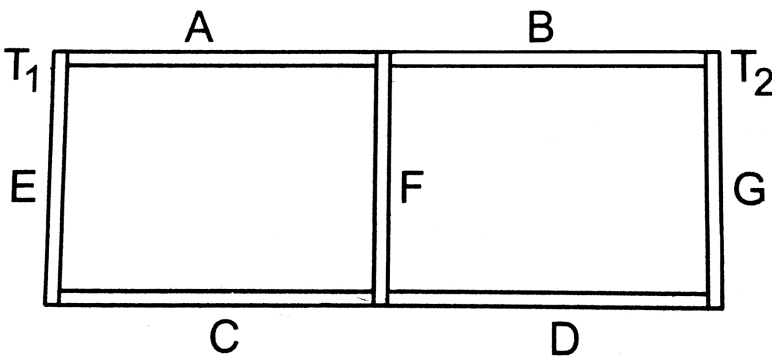
31. Seven rods A, B, C, D, E, F and G are joined as shown in figure. All the rods have equal cross-sectional area  $A$  and length  $l$ . The thermal conductivities of the rods are  $K_A = K_C = K_0$ ,  $K_B = K_D = 2K_0$ ,  $K_E = 3K_0$ ,  $K_F = 4K_0$  and  $K_G = 5K_0$

. The rod E is kept at a constant temperature  $T_1$

and the rod G is kept at a constant temperature  $T_2$  ( $T_2 > T_1$ )

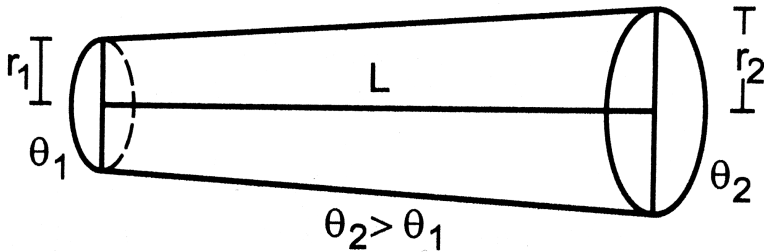
. (a) Show that the rod F has an average temperature  $T = (T_1 + 2T_2) / 3$

. (b) Find the rate of heat flow from the source which maintains the temperature  $T_2$ .



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32. Find the rate of heat flow through a cross section of the rod shown in figure ( $\theta_2 > \theta_1$ ). Thermal conductivity of the material of the rod is  $K$ .



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33. A rod of negligible heat capacity has length 20cm, area of cross section  $1.0\text{cm}^2$  and thermal conductivity  $200\text{Wm}^{-1}\text{C}^{-1}$ .

The temperature of one end is  $0^\circ\text{C}$  and the other end is  $60^\circ\text{C}$ .

and the temperature of the other end is slowly varied from  $0^\circ\text{C}$  to  $60^\circ\text{C}$  in 10 minutes.

Assuming no loss of heat through the sides, find the total heat transmitted through the rod in these 10 minutes.

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**34.** A hollow metallic sphere of radius 20cm surrounds a concentric metallic sphere of radius 5cm. The space between the two sphere is filled with a nonmetallic material. The inner and outer sphere are maintained at  $50^{\circ}C$  and  $10^{\circ}C$  respectively and it is found that 100J of heat passes from the inner sphere to the outer sphere per second. Find the thermal conductivity of the material between the sphere.

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**35.** Figure shown two adiabatic vessels, each containing a mass  $m$  of water at different temperature. The ends of a metal rod of length  $L$ , area of cross section.  $A$  and thermal conductivity  $K$ , are inserted in the water as shown in the figure. Find the time taken for the difference between the temperature in the vessels to become half of the original value. The specific heat capacity of water is  $s$ . Neglect the heat capacity of the rod

and the container and any loss of heat top the atmosphere.



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**36.** Two bodies of masses  $m_1$  and  $m_2$  and specific heat capacities  $S_1$  and  $S_2$  are connected by a rod of length  $l$ , cross-section area  $A$ , thermal conductivity  $K$  and negligible heat capacity. The whole system is thermally insulated. At time  $t = 0$ , the temperature of the first body is  $T_1$  and the temperature of the second body is  $T_2$  ( $T_2 > T_1$ ). Find the temperature difference between the two bodies at time  $t$ .

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**37.** An amount  $n$  (in moles) of a monatomic gas at initial temperature  $T_0$  is enclosed in a cylindrical vessel fitted with a light piston. The surrounding air has a temperature  $T_s$  ( $> T_0$ ). And the atmospheric



pressure is  $P_a$ . Heat may be conducted between the surrounding and the gas through the bottom of the cylinder. The bottom has a surface area  $A$ , thickness  $x$  and thermal conductivity  $K$ . Assuming all change to be slow, find the distance moved by the piston in time  $t$ .

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**38.** Assume that the total surface area of a human body is  $1.6\text{ m}^2$  and that it radiates like an ideal radiator. Calculate the amount of energy radiates per second by the body if the body temperature is  $37^\circ\text{C}$ . Stefan constant  $\sigma$  is  $6.0 \times 10^{-8}\text{ W m}^{-2}\text{ K}^{-4}$ .

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**39.** Calculate the amount of heat radiated per second by a body of surface area  $12\text{ cm}^2$  kept in thermal equilibrium in a room at temperature  $20^\circ\text{C}$ . The emissivity of the surface = 0.80 and  $\sigma = 6.0 \times 10^{-8}\text{ W m}^{-2}\text{ K}^{-4}$ .

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**40.** A solid aluminium sphere and a solid copper sphere of twice the radius are heated to the same temperature and are allowed to cool under identical surrounding temperatures. Assume that the emissivity of both the spheres is the same. Find ratio of (a) the rate of heat loss from the aluminium sphere to the rate of all of temperature of the copper sphere. The specific heat capacity of aluminium =  $900 \text{ J kg}^{-1} \text{ } ^\circ\text{C}^{-1}$  . and  $t\hat{o}fcopper = 390 \text{ J kg}^{-1} \text{ } ^\circ\text{C}^{-1}$  . The density of copper = 3.4 times the correct wattage.

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**41.** A 100W bulb has tungsten filament of total length  $1.0 \text{ m}$  and radius  $4 \times 10^{-5} \text{ m}$  . The emissivity of the filament is 0.8 and  $\sigma = 6.0 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$  . Calculate the temperature of the filament when the bulb is operating at correct wattage.

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42. A spherical ball of surface area  $20\text{cm}^2$  absorbs any radiation that falls on it. It is suspended in a closed box maintained at  $57^\circ\text{C}$ . (a) Find the amount of radiation falling on the ball per second. (b) Find the net rate of heat flow to or from the ball at an instant when its temperature is  $200^\circ\text{C}$ . Stefan constant  $= 6.0 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ .



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43. A spherical tungsten piece of radius  $1.0\text{cm}$  is suspended in an evacuated chamber maintained at  $300\text{K}$ . The piece is irradiated by heat energy  $F$  incident normally.  $F = 0.30$  and the Stefan constant is  $6.0 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ .



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44. A cubical block of mass  $1.0\text{kg}$  and edge  $5.0\text{cm}$  is heated to  $227^\circ\text{C}$ . It is kept in an evacuated chamber maintained at  $27^\circ\text{C}$ . Assuming that the block emits radiation like a blackbody, find the rate at which the

temperature of the block will decrease. Specific heat capacity of the material of the block is  $400 \text{ J kg}^{-1} \text{ K}^{-1}$ .

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**45.** A copper sphere is suspended in an evacuated chamber maintained at 300K. The sphere is maintained at a constant temperature of 500K by heating it electrically. A total of 210W electric power is needed to do it. When the surface of the copper sphere is completely blanked, 700W is needed to maintain the same temperature of the sphere. Calculate the emissivity of copper.

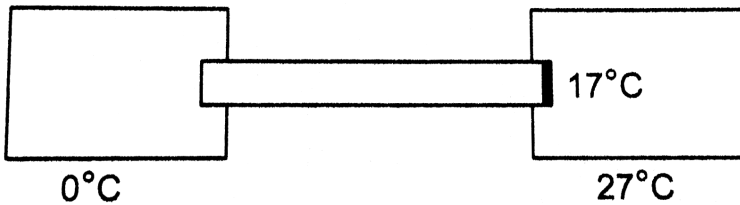
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**46.** A spherical ball A of surface area  $20 \text{ cm}^2$  is kept at the centre of a hollow spherical shell B of area  $80 \text{ cm}^2$ . The surface of A and the inner surface of B emit as blackbodies. Both A and B are at 300K. (a) How much is the radiation energy emitted per second by the ball A? (b) How much is the radiation energy emitted per second in the inner surface of B? (c)

How much of the energy emitted by the inner surface of B falls back on this surface itself?

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47. A cylindrical rod of length 50cm and cross sectional area  $1\text{cm}^2$  is fitted between a large ice chamber at  $0^\circ\text{C}$  and an evacuated chamber maintained at  $27^\circ\text{C}$  as shown in figure. Only small portions of the rod are inside the chamber and the rest is thermally insulated from the surrounding. The cross section going into the evacuated chamber is blackened so that it completely absorbs any radiation falling on it. The temperature of the blackened end is  $17^\circ\text{C}$  when steady state is reached. Stefan constant  $\sigma = 6 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$ . Find the thermal conductivity of the material of the rod.



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**48.** One end of a rod length 20cm is inserted in a furnace at 800K. The sides of the rod are covered with an insulating material and the other end emits radiation like a blackbody. The temperature of this end is 750K in the steady state. The temperature of the surrounding air is 300K. Assuming radiation to be the only important mode of energy transfer between the surrounding and the open end of the rod, find the thermal conductivity of the rod. Stefan constant  $\sigma_s = 6.0 \times 10^{-8} \text{Wm}^{-2}\text{K}^{-4}$ .

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**49.** A calorimeter of negligible heat capacity contains 100cc of water at  $40^\circ \text{C}$ . The water cools to  $35^\circ \text{C}$  in 5minutes. The water is now replaced by k-oil of equal volume at  $40^\circ \text{C}$ . Find the time taken for the temperature to become  $35^\circ \text{C}$  under similar conditions. Specific heat capacities of water and K-oil are  $4200 \text{Jkg}^{-1}\text{K}^{-1}$  and  $2100 \text{Jkg}^{-1}\text{K}^{-1}$  respectively. Density of K-oil =  $800 \text{kgm}^{-3}$ .

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50. A body cools down from  $50^{\circ}C$  to  $45^{\circ}C$  in 5 minutes and to  $40^{\circ}C$  in another 8 minutes. Find the temperature of the surrounding.



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51. A calorimeter contains 50g of water at  $50^{\circ}C$ . The temperature falls to  $45^{\circ}C$  in 10 minutes. When the calorimeter contains 100g of water at  $50^{\circ}C$  it takes 18 minutes for the temperature to become  $45^{\circ}C$ . Find the water equivalent of the calorimeter.



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52. A metal ball of mass 1kg is heated by means of a 20W heater in a room at  $20^{\circ}C$ . The temperature of the ball becomes steady at  $50^{\circ}C$ . (a) Find the area of loss of heat to the surrounding when the ball is at  $-50^{\circ}C$ . (b) Assuming Newton's law of cooling, calculate the rate of loss of heat to the surrounding when the ball is at  $30^{\circ}C$ . (c) Assume that the

temperature of the ball rises uniformly from  $20^{\circ}C$  to  $30^{\circ}C$  in 5 minutes.

Find the total loss of heat to the surrounding during this period. (d)

Calculate the specific heat capacity of the metal.

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**53.** A metal block of heat capacity  $90J/{}^{\circ}C$  placed in a room at  $25^{\circ}C$  is heated electrically. The heater is switched off when the temperature reaches  $35^{\circ}C$ . The temperature of the block rises at the rate of  $2^{\circ}C/s$

just after the heater is switched on and falls at the rate of  $0.2^{\circ}C/s$  just after the heater is switched off. Assume Newton's law of cooling to hold

(a) Find the power of the heater. (b) Find the power radiated by the block

just after the heater is switched off. (c) Find the power radiated by the

block when the temperature of the block is  $30^{\circ}C$ . (d) Assuming that the

power radiated at  $30^{\circ}C$  represents the average value in the heating

process, find the time for which the heater was kept on.

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54. A hot body placed in a surrounding of temperature  $\theta_0$  obeys Newton's law of cooling  $\frac{d\theta}{dt} = -k(\theta - \theta_0)$ . Its temperature at  $t = 0$  is  $\theta_1$  the specific heat capacity of the body is  $s$  and its mass is  $m$ . Find (a) the maximum heat that the body can lose and (b) the time starting from  $t = 0$  in which it will lose 90% of this maximum heat.



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## Exercise

1. The three rods shown in figure have identical geometrical dimensions. Heat flows from the hot end at a rate of 40W in the arrangement (a). Find the rates of heat flow when the rods are joined as in arrangement (b) and in (c). Thermal conductivities of aluminium and copper are  $200Wm^{-1} (^{\circ}C)^{-1}$  and  $100Wm^{-1} (^{\circ}C)^{-1}$  respectively.



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