



## PHYSICS

### BOOKS - BHARATI BHAWAN PHYSICS

### (HINGLISH)

### ELASTICITY

#### Example

1. A wire of length 3m and stretched by hanging a weight of 2kg from it and the elongation is 2mm.

Calculate the Young's modulus and the strain potential energy of the wire.

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2. A steel wire 2mm in diameter is stretched between two fixed points at a temperature of  $20^{\circ}C$ .

Determine its tension when its temperature falls to  $10^{\circ}C$ . Linear expansivity of steel

$= 11 \times 10^{-6} / K$ , Young's modulus  $= 2 \times 10^{11} / m^{-2}$

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3. Find the formula for the work done in stretching a wire and apply it to find the elastic energy stored in a wire originally 5 metre long and 1mm in diameter, which is stretched by 0.3mm due to a load of 10kg. Also calculate the Young's modulus of the wire.

$$= g = 9.8 \text{ms}^{-2}$$



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4. When a rubber cord is stretched, the change in volume is negligible compared to the change in its linear dimension. Then Poisson's ratio for rubber is



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5. A load of 7.6kg hangs from the lower end of a steel wire is rigidly clamped at the upper end. When the load immersed in water, the length of the wire changes by 1mm. Calculate the length of the wire.. (Young's modulus of steel  $=2 \times 10^{11} \text{ Nm}^{-2}$  diameter of the wire = 0.4mm density of material of load  $=7600 \text{ kgm}^{-3}$  and  $g = 9.8 \text{ ms}^{-2}$ ).



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6. A steel wire of length 1m and diameter 4mm is stretched horizontally between two rigid supports

attached to its end. What load would be required to be hung from the mid-point of the wire to produce a depression of 1cm? ( $Y = 2 \times 10^{11} Nm^{-2}$ )

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7. A steel spiral spring has an unstretched length of 8cm and when a mass is hung on it, its length becomes 10cm. Calculate the periodic time of the oscillation that would occur if the mass were displaced vertically.

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8. Find the increment in the length of a steel wire of length  $5m$  and radius  $6mm$  under its own weight. Density of steel  $= 8000kg/m^3$  and young's modulus of steel  $= 2 \times 10^{11}N/m^2$ . What is the energy stored in the wire ? (Take  $g = 9.8m/s^2$ )

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9. A uniform elastic plank moves due to a constant force  $F_0$  applied at one end whose area is  $S$ . The Young's modulus of the plank is  $Y$ . The strain produced in the direction of force is

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## Exercies A

1. A copper wire 2 m long and 0.5m in diameter supports a mass of 10kg It is stretched by 2.38 mm . Calculate the Young's modulus of the wire.



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2. Calculate the strain potential energy of a horizontal rod 1 m long and  $0.4 \times 10^{-4} M^2$  in cross - section fixed at both ends , which is cooled from  $25^\circ$  c to  $10^\circ$  C Linear expansivity of the material of the

rod  $= 11 \times 10^{-6} / K$  and Young's modulus  
 $= 2.1 \times 10^{11} Nm^{-2}$



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3. A wire of length  $3m$  diameter  $0.4mm$  and young's modulus  $8 \times 10^{10} N/m^2$  is suspended from a point and supports a heavy cylinder of volume  $10^{-3}m^3$  at its lower end . Find the decrease in length when the metal cylinder is immersed in a liquid of density  $800kg/m^3$ .



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4. The wire of a Young's modulus apparatus is elongated by 2 mm when a brick is suspended from it. When the brick is immersed in water the wire contracts by 0.6 mm. Calculate the density of the brick given that the density of water is  $1000 \text{ kg m}^{-3}$ .



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5. A bar is heated to a temperature of  $500^\circ \text{C}$ . Its ends are then clamped at two points 1 m apart and it is allowed to cool. Find the temperature at which it will break, assuming linear expansivity of steel  $= 11 \times 10^{-6} / \text{K}$ , Young's modulus of steel

$= 2 \times 10^{11} Nm^{-2}$  and braking stress for steel

$= 8 \times 10^8 Nm^{-2}$



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6. Find the greatest length of steel wire that can hang vertically without breaking. Breaking stress of steel  $= 8.0 \times 10^8 N/m^2$ . Density of steel  $= 8.0 \times 10^3 kg/m^3$ . Take  $g = 10 m/s^2$ .



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7. What work has to be done to make a hoop out of a copper band of length  $l = 3m$ , width  $h = 6$  cm and

thickness  $\delta = 1\text{mm}$ ? (Y of copper  
 $= 1.3 \times 10^{11} \text{Nm}^{-2}$ )

[Hint: Consider strain energy in a thin layer and  
intergrate from  $r - \delta/2$  to  $r + \delta/2$ ]



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8. A wire of length 2 m and radius 2 mm is stretched by 2.5 mm when a load of 5 kg is suspended from it. Another wire of the same material but of length 1 m and radius 1 mm is attached below the load and a load of 3 kg is suspended from this wire. What is the total increase in length and what are the individual extensions of the wires?



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9. A wire of length 1 m and radius 1 mm is welded to another wire of length 2 m and radius 2 mm the free end of the first is clamped and a load of 5kg is applied at the free end of the second wire . What is the total increase of the compound wire ? (Y of both wires  $= 2 \times 10^{11} Nm^{-2}$ )



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10. A uniform pressure P is exerted on all sides of a solid cube at temperature be raised in

order to bring cubic volume back to what it had been before the pressure was applied (Xcubical expansivity of the material of the cube =  $\alpha$  and the bulk modulus of elasticity is  $\beta$ )

$$\left[ \text{Hint: } \frac{\text{change in volume}}{\text{original}} = \frac{P}{\beta} \quad V_t = V_0(1 + \alpha t) \right]$$



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**11.** Two springs have force constants  $K_1$  and  $K_2$ , where  $K_1 > K_2$ . On which spring, more work is done if

(i) they are stretched by the same force?

(ii) they are stretched by the same amount?



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## Exercies B

1. A steel wire of length 1 m and diameter 3 mm is stretched horizontally between supports attached at its ends. What load would be required to be hung from the mid-point of the wire would be required to produce a depression of 1 cm?

$$(y = 2 \times 10^{11} \text{ NM}^{-2}, g = 9.8 \text{ ms}^{-2})$$



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2. A light rod of length 2 m is suspended horizontally from the ceiling by means of two vertical wires of equal length tied to its ends. One wire is made of steel and is of cross-section  $0.1 \text{ cm}^2$  and the other is of brass of cross-section  $0.2 \text{ cm}^2$ . Find the position along the rod at which a weight may be hung to produce (i) equal stress in both wires (ii) equal strain in both wires ( $Y$  for brass  $= 10 \times 10^{10} \text{ Nm}^{-2}$  and  $Y$  for steel  $= 20 \times 10^{10} \text{ Nm}^{-2}$ )



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3. A 4-kg block extends a spring by 16 cm from its unstretched position. The block is removed and a 0.5 - kg body is hung from the same spring. If the spring is then stretched and released, what is the time period of oscillations of the mass suspended? What is the force constant of the spring?



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4. A uniform spring whose unstretched length is  $l$  has a force constant  $K$ . The spring is cut into two equal parts. What are the force constants  $K_1$  and  $K_2$  of the two parts in terms of  $n$  and  $K$ ?



[Hint :force constant is inversely proportional to length.]



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5. A light elastic string is suspended vertically from a point and carries a heavy mass at its lower end, which stretches it and its time period is equal to that of a simple pendulum of length  $l$ .



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6. A ring of lead (relative density = 11.3 and breaking stress  $\sigma_b = 1.5 \times 10^7 \text{ Nm}^{-2}$ ) of radius  $r = 25 \text{ cm}$  is

rotated about its axis .What is the number of rps at which the ring will rupture?



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7. A reinforced concrete column consists of concrete filled with iron bars. Assume that iron occupies one-twentieth of the total cross-section area and Young's modulus of concrete is one-tenth of that of iron. The concrete column is under a compressive load  $P$ . Determine the fraction of load on the concrete.



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8. Two steel plates are soldered on two sides of a copper plate. What tensions will arise in the plates if the temperature is increased by  $t^\circ C$ ? All the plates have the same cross-sections the coefficients of expansion of copper and steel are  $\alpha_c$  and  $\alpha_s$  and their Young's modulus are  $Y_c$  and  $Y_s$  respectively. Area of each interface is  $A$ .

[Hint : The net expansion (thermal + elastic) is the same for all the plates. The tensile force on each steel plate is half the tensile force on the copper plate.]



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9. What internal pressure (in the absence of an external pressure) can be sustained by (a) a glass tube of wall thickness and radius  $\sigma$  (b) breaking stress of glass  $= 5 \times 10^7 \text{ Pa}$ .

[Hint: outward force due to internal pressure is balanced by the inward elastic force.]



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10. An iron ring of radius 50 cm and thickness 1 cm is heated sufficiently and then put on a wooden carriage wheel of the same radius at  $40^\circ \text{C}$ . What is the force per unit area with which the ring grips over the wheel cooled to  $27^\circ \text{C}$ ? Young's modulus of iron

$= 2 \times 10^{11} \text{ Nm}^{-2}$  and linear expansivity of iron  
 $= 11 \times 10^{-6} \text{ K}^{-1}$  Neglect thermal contraction of  
the wooden wheel.

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**11.** three pieces of wire of the same intererinal and  
radius but of different length are tied to three -  
colliner , , equispesd pege in the ceiling of a room  
knotted together at their other ends so that the side  
wirs subtend the same angle  $\alpha$  with the midda one .If  
a load P is attached to the knot ,calculate the tension  
in the wires.

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**12.** A perfectly rigid and weightless rod of length  $l$  is hinged at one end to a vertical wall and is held horizontal by two vertical wires of the same length, radius and material, which are tied at distance  $a$  and  $b$  from the hinged end of the rod.



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**13.** A light rod is supported horizontally by two wires of the same length  $L$  and area of cross-section  $A$  but of different moduli of elasticity  $Y_1$  and  $Y_2$ . A heavy mass  $m$  is suspended at a distance  $a_1$  from the first

wire and  $a_2$  from the second wires Find the period of vertical oscillations of the mass.



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**14.** A cylinder of height  $H$  and radius  $R$  is filled with a liquid of density  $\rho$ . What is the disrupting stress at a height  $h$ ? where is it maximum and where minimum ?

[Hint : Disrupting stress is the elastic force per unit length Consider equilibrium of an element of the wall.]



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