



# **PHYSICS**

# **BOOKS - DHANPAT RAI & CO PHYSICS (HINGLISH)**

# PHYSICAL WORLD AND MEASUREMENTS

#### Example

- **1.** Write the order of magnitude of the following measurements:
- (i) 25,710,000 m
- (ii) 0. 00000521 kg



2. Express 1 light year in terms of metre. What is its order of magnitude?

3. Express 1 parsec in terms of meters . What its order of magnitude .



**4.** A student measures the thickness of a human hair by looking at it through a microscope of magnification 100. He makes 20 observations and findsd that the average width of the hair in the field of view of the microscope is 3.5mm. What is his estimate on the thickness of hair?

5. If the size of a nucleus  $(\approx 10^{-15}m)$  is scaled up to the tip of a sharp pin  $(\approx 10^{-5}m)$ , what roughly is the size of an atom?

**6.** The photograph fo a house occupies an area of  $1.7cm^2$  on a 35 slide. The slide is projected on to a screen, and the area of the house on the screen is  $1.55m^2$  What is the liner magnification of the projector screen arrangement?

Watch Video Solution

**7.** What is the distance in km of a quaser from which ligth takes 3.0 billion years to reach us ?

Watch Video Solution

**8.** A SONAR (sound navigation and ranging) uses ultrasonic waves to detect and locate object under water. In a submarine equaipped with as SONAR, the time delay between genration of a probe wave and the recption of its echo after refection from an enemy submarine is found to be 77.0 s. What is the distance of the enemy submarine ? (speed of sound in water  $= 1450ms^{-1}$ 



**9.** A laser light beamed at the moon the takes 2.56s to return after reflection at the moon 's surface . How much is the radius of the lunar obit around the earth ?

> Watch Video Solution

**10.** The shadow of a tower standing on a level plane is found to be 50m longer when sun's altitude is  $30^{\circ}$  then when it is  $60^{\circ}$ . Find the height of tower.

Watch Video Solution

**11.** The moon subtends an angle of 57 minutes at the base line equal to radius of earth. What is the distance of moon from earth. Given radius of earth is 6400 km.

**12.** When planet Jupiter is at a distance of 824.7 million km from earth, its angular diameter is measured to be 35.72" of arc. Calculate the diameter of Jupiter.

Watch Video Solution

**13.** It is a well known fact that during a total solar eclipes the disc of the moon almost completely covers the disc of the sun. From this fact and from the information you can gather from Solved Examples 3 and 4 on page 1//44, determine the approximate diameter of the moon.



**14.** The nearest star to our solar system is 4.29 light years away. How mcuh is this distance in terms of par sec ? How mcuh parallax would this



a mole of hydrogen ? Take size of hydrogen molecule to be 1 Å. Why is this

ratio so large?



**17.** A drop of olive oil of radius 0.25 mm spreads into a circular film of diameter 20cm on the water surface. Estimate the size of the oil molecule.

### Watch Video Solution

**18.** The sun is a hot plasma (ionised matter) with its linner core at a temperature excedding  $10^7$  K, and its outer surface at a temperature of about 6000K. At such high temps, no substance remains in a solid or liquid phase. In what range do you expect the mass density of the sun to be? In the range of densities of solids, liquieds or gases ? Check if your guess is correct from the following data : mass of sun  $= 2.0 \times 10^{30} kg$ , radius of the sun  $= 7.0 \times 10^8 m$ 

#### Watch Video Solution

**19.** Estimate the averaage atomic mass density of a sodium atom, assuming its size ot be 2.5 Å. Compare it with density of sodium in its

crystalline phase  $(970 kgm^{-3})$ . Are the two denities of the same order of magnitude ? If so, why ?

#### Watch Video Solution

**20.** The unit of length convenient on nuclear scale is a fermi,  $1f = 10^9 - 15$ )m. Nuclear sizes obey rougholy the following empricial relation :  $r = r_0 A^{1/3}$ , where r is radius of the nucleus and  $r_0$  is a constant equal to 1.2 f. show that the rule implies that nuclear mass density in nearly constant for different neclei. Estimate the mass density of sodium nucleus. Compare it with avarge mass density of sodium atom is Q. 27  $(4.67 \times 10^3 kg/m^3)$ .

### Watch Video Solution

**21.** The avarage life of an Indian is 56 years .Find the number of times the human heart beats in the life of an Indian ,If the heat beats once in 0.8 s.

**22.** It is claimed that two cesium clocks, if allowed to run for 100 years, free from any disturbance, may differ by only about 0.02s. What does this imply for the accuracy of the standard cesium clock in measuring a time interval of 1s ?

Watch Video Solution

**23.** The mean life of an elementary particle pion is  $2 \times 10^{-7}$  ns. The age of the univers is about  $4 \times 10^9$  years. Identify a physically meaning time that is approximately half way between these two on a logarithmic scale.

Watch Video Solution

**24.** Deduce the dimensinal formulae for the ollowing physical quantites: Graviatinal constant (ii) Powr (iii) Young's modulus (iv) Coeffcient of viscosity (v) Surface tension (vi) Planck,s constant . **25.** Deduce the dimensinal formulae for the ollowing physical quantites: (i) Heat (ii) Specific heart (iii) Latent heat (iv) Gas constant (v) Boltzmann's constant (vi) Coffcient of thermal conductivity (vii) Meachanical equivalent of heart .

Watch Video Solution

26. Find the dimensional formulae of (i) charge (ii) potential (iii) resistance

(iv) capacitance.

Watch Video Solution

27. Name the physical quantites whose dimensional formulae are as

follows:

(i) 
$$ML^2T^{-2}(ii)ML^2T^{-3}(iii)MT^{-2}(iv)ML^{-1}T^{-1}(v)ML^{-1}T^{-2}$$
,

**28.** Taking velocity , time and force as the fundamental quantities , find the dimension of mass .

Watch Video Solution

**29.** If density (D), acceleration due to gravity (g) and frequency (v) are taken as base quantities , find the dimensions of force.

Watch Video Solution

**30.** If C ( the velocity of light ) g , ( the acceleration due to gravity), P ( the atmospheric pressure) are the fundamental quantities in MKS system , then the dimensions of length will be same as that of



**31.** Number of particles is given by  $n = -D\frac{n_2 - n_1}{x_2 - x_1}$  crossing a unit area perpendicular to X-axis in unit time, where  $n_1$  and  $n_2$  are number of particles per unit volume for the value of x meant to  $x_2$  and  $x_1$ . Find dimensions of D called as diffusion constant

Watch Video Solution

32. Fill in the blanks by suitable conversion of units :

(a) 
$$1kgm^2s^{-2} = gcm^2s^{-2}$$
 (b) 1m = ...... Light year (c )  
 $3ms^{-2} = \dots Kmh^{-2}$   
(d)  $G = 6.67 \times 10^{-11}Nm^2kg^{-2} = \dots cm^3s^{-2}g^{-1}$ 

Watch Video Solution

**33.** The value fo universal gravitationla constant G in CGS system is  $6.67 imes 10^{-8}$  dyne  $cm^2g^{-2}$ . Its value in SI system is

**34.** Convert an energy of 1 joule into ergs.

**Watch Video Solution** 

**35.** Find the value of 60 J per min on a system that has 100g, cm and 1 min.

as the base units.

Watch Video Solution

**36.** A calorie is a unit of heat or energy and it equals about 4.2J,  $where 1J = 1kgm^2s^{-2}$ . Suppose we employ a system of units in which the unit of mass equals  $\alpha kg$ , the unit of length equals is  $\beta m$ , the unit of time is  $\gamma s$ . Show that a calorie has a magnitude  $4.2\alpha^{-1}\beta^{-1}\gamma^2$  in terms of the new units.



37. Relative density of an oil is 0.8. Find the absolute density of oil in CGS

and SI units.



**38.** The Young's modulus of steel is  $1.9 imes 10^{11} Nm^{-2}$  . Calculate its value

in dyne  $cm^{-2}$ .

Watch Video Solution

**39.** The value of Stefan's constant is  $\sigma = 5.76 imes 10^{-8} J s^{-1} m^{-2} K^{-4}$ .

Find its value in cgs system.



**40.** A new unit of length is chosen such that the speed of light in vecuum is unity. What is the distance between the sun and the earth in terms of

the new unit, if light takes 8 min and 20 sec. to cover the distance ?



**41.** If the unit of force is 1 kN, unit of length 1 km and unit of time is 100s,

what will be the unit of mass?

Watch Video Solution

**42.** If the fundamental units are the velocity of light in air  $(3 \times 10^{10} cms^{-1})$ , the acceleration due to gravity  $(981 cms^{-1})$ , the density of mercury  $(13.6 gcm^{-3})$ , fing the units of mass , length and time.

# Watch Video Solution

**43.** Check the correctness of following equation by the method of dimensions :

$$S=ut+rac{1}{2}at^2\,.$$

where S is the distance covered bu a body in time t, having initial velocity

u and acceleration a.



44. Check the correctness of the equation,

$$FS=rac{1}{2}mv^2-rac{1}{2}\mu^2$$

where F is the force acting on a body of mass m and S is the distacne

moved by the body when its velocity changes from u to v.

Watch Video Solution

**45.** Check the correctness of the relation  $\pi = I \alpha$  whare  $\pi$  is torque

acting on the body, I is moment of inertia and  $\alpha$  is angular acceleration.

46. Check the dimensional consistency of the following equations :

(i) de-Broglie wavelength , 
$$\lambda=rac{h}{mv}$$
 (ii) Escape velocity , $v=\sqrt{rac{2GM}{R}}.$ 



**47.** Check by the method of dimensions whether the following relations are true.

(i)
$$t=2\pi\sqrt{rac{l}{g}}$$
 , (ii) $v=\sqrt{rac{P}{D}}$  where v= velocity of sound P=pressure

D=density of medium .

(iii) $n = rac{1}{2l} = \sqrt{rac{F}{m}}$  where n= frequency of vibration l=length of the

string, F=stretching force m=mass per unit length of the string .

### Watch Video Solution

48. By the method of dimensions, test the accuracy of the equation :

$$\delta = rac{mgl^3}{4bd^3Y}$$
 where  $\delta$  is depression in the middle of a bar of length I,

breadth b, depth d, when it is loaded in the middle with mass m. Y is Young's modulus of material of the bar.



Watch Video Solution

**51.** Write the dimensions of a and b in the relation  $P = rac{\left(b-x
ight)^2}{at}$  Where

P is power, x is distance and t is time.

**52.** In Vander Wall's equation  $\left(P + \frac{a}{V^2}\right)(V - b) = RT$  What are the dimensions of a and b ? Here, P is pressure, V is volume, T is temperature and R is gas constant.

Watch Video Solution

**53.** When white light travels through glass, the refractive index of glass ( $\mu$  =velocity of light in air/velocity of light in glass) is found to vary with wavelength as  $\mu = A + \frac{B}{\lambda^2}$ . Using the principle of homogeneity of dimensions, Find the SI units in which the constants A and B expressed.

#### Watch Video Solution

54. Find the dimensions of the quantity v in the equation,

$$v=rac{\pi pig(a^2-x^2ig)}{2\eta l}$$

where a is the radius and I is he length of the tube in which the fluid of

coefficient of viscosity  $\eta$  is flowing , x is the distacne from the axis of the

tube and p is the pressure differnece.

Watch Video Solution

**55.** A particles of mass m moving in a circle of radius r with unform speed v. The force F acting on a particle is proportional to  $m^a v^b r^c$ . Find the values of a, b and c.

Watch Video Solution

**56.** In the equation  $y = A\sin(\omega t - kx)$ , obtain the dimensional formula

of  $\omega$  and k. Given x is distnace and t is time.



57. A book with many printing errors contains four different forumlae for

the displacement y of a particle undergoing a certain periodic motion : (i)

 $y = a \frac{\sin(2\pi t)}{T}$  (ii)  $y = a \sin vt$  (iii) $y = \frac{a}{T} \frac{\sin(t)}{a}$  (iv)  $y = \frac{a}{\sqrt{2}} \left[ \frac{\sin(2\pi t)}{T} + \frac{\cos(2\pi t)}{T} \right]$  Here, a is maximum displacement of particle, v is speed of particle, T is time period of motion. Rule out the wrong forum lae on dimensinal grounds.

#### Watch Video Solution

**58.** A famous relation in phyics relates the moving mass m to the rest mass  $m_0$  of a particle in terms of its speed v and the speed of light c.( This relation first arose as a consequence of the special theory of relativity due to Albert Einstein). A body recalls the relation almost correctly but forgets where to put the constant c. He writes  $m = \frac{m_0}{(1 - V^2)^{1/2}}$ . Guess where to put the missing c.

### Watch Video Solution

**59.** A man wlaking briskly in rain with speed v must slant his umbrella forward making an angle  $\theta$  with the vertical . A student derives the

following relation between  $\theta$  and v :

an heta = v

and checks that the relations has a correct limit : as  $v \to 0, \theta \to 0$ , as expected . (We are assuming there is no string wing and that the rains falls vertically for a stationary man). Do you think this relation can be correct ? If not, guess at the correct relation .

Watch Video Solution

**60.** Derive an expression for time period (t) of a simple penduleum, which may depend upon : mass of bob (m), length of pendulum (I) and acceleration due to gravity(g).

Watch Video Solution

**61.** The velocity of water wave v may depend on their wavelength  $\lambda$ , the density of water  $\rho$  and the acceleration due to gravity g. The method of dimensions gives the relation between these quantities as



**62.** The time period 'T' of a body executing SHM may be supposed to depend upon (i) the amplitude 'A' , (ii) the force constant 'k' and (iii) the mass 'm' . Deduce by the method of dimensions the formula for T.

Watch Video Solution

**63.** Assuming that the mass m of the largest stone that can be moved by a flowing river depends upon the velocity v, of water, its density  $\rho$  and acceleration due to gravity g, then m is directly proportional to

Watch Video Solution

**64.** The velocity of sound waves 'v' through a medium may be assumed to depend on :

(i) the density of the medium 'd' and (ii) the modulus of elasticity 'E' .

Deduce by the method of dimensions the formula for the velocity of sound . Take dimensional constant K=1.

Watch Video Solution

**65.** The frequency of vibration (v) of a string may depend upon length (I) of the string, tension (T) in the string and mass per unit length (m) of the string. Using the method of dimensions, derive the formula for v.

Watch Video Solution

66. A planet moves around the sun in nearly circular orbit. Its period of

revolution 'T' depends upon :

(i) radius 'r' or orbit (ii) mass 'M' of the sum and

(iii) the gravitational constant G.

Show dimensionally that  $T^2 \propto r^2$ .

**67.** Reynold number  $N_R$  a dimensionless quantity determines the condition of laminar flow of a viscous liquied through a pipe.  $N_R$  is a function of density  $\rho$  of liquid, average speed v and coeff. Of viscosity  $\eta$ . Given that  $N_R \propto D$ , diameter of pipe. Show by the method of dimensions that  $N_R \propto \frac{\rho v D}{\eta}$ 

Watch Video Solution

**68.** Derive by the method of dimensions, an expression for the volume of a liquid flowing out per second through a narrow pipe. Asssume that the rate of flow of liwquid depends on (i) the coeffeicient of viscosity  $\eta$  of the liquid (ii) the radius 'r' of the pipe and (iii) the pressure gradient  $\frac{P}{l}$  along the pipte. Take  $K = \frac{\pi}{8}$ . Watch Video Solution **69.** The period of vibration of a tunign fork depends on the length I of its prong, density d and Young's modulus Y of the meterial. Deduce an expression for the period of vibration (T) using dimensional analysis.



**70.** The frequency (V) of an oscillating drop may depends upon radius (r ) of the drop density  $(\rho)$  of liquid and the surface tension (S) of the liquid. Deduce of formula dimensionally.

Watch Video Solution

**71.** The rate of volume of flow of water (V) through a canal is found to be a function of the area of cross section A of the canal and velocity of water v. Show that the rate of volume flow is proportional to the velocity of flow of water. **72.** The escape velocity v of a body depends upon the acceleration due to gravity of the planet and the radius of the planet R. Establish dimensionally the relationship between v, g and R.

C	Watch	Video	Solution	
---	-------	-------	----------	--

73. State the number of significant figures in the following:

(i) 453.5 (ii) 53,000,000 (iii) 400.08

(iv) 0.000243 (v) 0.0650 (vi)  $2.43 imes 10^5$ 

Watch Video Solution

74. State the number of significant figures in the following:

(i)  $0.007m^2$  (ii)  $2.64 imes 10^{24}kg$  (iii)  $0.2370cm^{-3}$ 

(iv) 6.320J (v) $6.032nM^{-2}$  (vi) 0.0006032

(vii) 2.000m (viii) 5100kg (ix) 0.050cm.

**75.** Round off the following numbers as indicated:

(i) 18.35 upto 3 digits (ii) 143.45 upto 4 digits

(iii) 18967 upto 3 digits (iv) 12.653 upto3 digits

(v) 248337 upto 3 digits (vi) 321.135 upto 5 digits

(vii)  $101.55 imes 10^6$ upto 4 digits (viii)  $31.325 imes x 10^{-5}$ upto 4 digits.

Watch Video Solution

**76.** Add 7.21, 12.41 and 0.0028, and express the result the rsult to an appropriate number of significant figures.

> Watch Video Solution

77. Subtract 4.27153 from 6.807 and express the result to an appropriate

number of significant figures.



78. Subtract  $2.5 imes 10^4 {
m from} 3.9 imes 10^5$  with due regard to significant

figures.

**Watch Video Solution** 

**79.** Subtract  $2.5 \times 10^6 {\rm from} 4.0 \times 10^4$  with due regard to significant figures.

Watch Video Solution

80. Express the result of the following calcultaeion to an appropriate

number of significant figures:

(i) 943.0.00345 (ii)  $\frac{3.24 imes 0.08666}{5.006}$ 

Watch Video Solution

81. Solve the following and express the result to an appropriate number

of significant figures:

(i) Add 6.2g, 4.33g, and 17.456g.

(ii) Subtract 63.54kg, from 187.2kg. (iii) 75.5 xx 125.2 xx 0.51.

(iv) 
$$rac{2.13 imes 24.78}{458.2}$$
 (v)  $rac{2.51 imes 10^{-4} imes 1.81 imes 10^{7}}{0.4463}$ 

Watch Video Solution

**82.** The mass of a box measured by a grocer's balance is 2.300kg. Two gold pieces of masses 20.15 g and 20.17 g are added to the box. What is (a) the total mass of the box, (b) the difference in the masses of the pieces to correct significant figures?



**83.** Each side of a cube is measured to be 6.203m. What is the total surface area and volume of the cube to appropriate significant figures?

84. The length , breath and thickness of a metal sheet are 4.234m, 1.005m, and 2.01cm respectively then the volume of the sheet is

Watch	Video	Solution	
THUCH	11460	501001011	

**85.** The diameter of circle is 1.06m. Calculate the area enclosed by the circle in correct number of significant figures.

Watch Video Solution

86. The radius of a sphere is 1.41. its volume to an appropring number of

significant figure is



**87.** The length and the radius of a cylinder measured with a slide cllipers re found to be 4.54 cm and 1.75 cm respectively. Calculate the volume of

the cyli	inder.
----------	--------



Watch Video Solution

**89.** The radius of the earth is  $6.37 imes 10^6 m$  and its mass is  $5.975 imes 10^{24} kg$ .

Find the earth's average density to approopriate significant figures.

Watch Video Solution

**90.** The length of a rod as measured in an experiment was found to be 2.48m, 2.46 m, 2.49 m, 2.50 m and 2.48m. Find the average length, absolute arror in each observation and the percentage error.

**91.** In successive measurement, the reading of the period of oscillation of a simple pendulum were found to be 2.63s, 2.56s, 2.71s and 2.80s in an experiment. Calculate (i) mean value of the period oscillation (ii) absolute errer in each measurement (iii) mean absolute error (iv) releative error (v) percentage error and (vi) express the result in proper form.

- 92. In an experiment the refractive index of glass was observed to be
- 1.45, 1.56, 1.54, 1.44, 1.54, and 1.53. Calculate
- (a). Mean value of refractive index
- (b). Mean absolute error
- (c) Fractional error
- (d) Percentage error
- (e) Express the result in terms of absolute error and percentage error



**93.** Two resistance  $R_1 = 100 \pm 3\Omega \, ext{ and } R_2 = 200 \pm 4\Omega$  are connected in

seriesg. What is their equivalent resistance?



Watch Video Solution

**95.** The initial and final temperatures of a water bath are  $(18 \pm 0.5)$ .° C and  $(40 \pm 0.3)$ .° C. What is the rise in temperature of the path



**96.** A capacitor of capacitance  $(2.0\pm0.1)\mu F$  is charged to a voltage V=

 $(2.0\pm0.2) \mathrm{volt}.$  What will be the charge on the capcitor?

Watch Video Solution
----------------------

**97.** The length and breadth of a rectangular block are 25.2 cm and 16.8 cm, which have both been measurd to an accurancy of 0.1 cm find the area of the rectangular block.

> Watch Video Solution

98. A force of  $(2500\pm5)$ N is applied over an area of  $(0.32\pm0.02)m^2$ 

Calculate the pressure exerted over the area.



**99.** The resistance  $R = \frac{V}{I}$ , where V=100  $\pm$  5V and  $I = 10 \pm 0.2A$ . The pressure error in V is 5% and in I is 2%. What is the total percentage error in R?



**100.** If the error involved in the measurement of mass and length of one side of a cube are 4% and 3% respectively. What is the maximum permissible relative error in calculation of density of meterail of the cube?

Watch Video Solution

**101.** The error in the measurement of radius of a sphere of radius of a sphere is 2%. What would bet the volume of sphere?


**102.** The percentage errors in the measurement of mass and speed are 2% and 3%, respectively. How much will be the maximum error in the estimation of *KE* obtained by measuring mass and speed?



**103.** the length , breadth and heigth of a rectangular block of wood wre measured to be :

 $l = 12.13 \pm 0.02 cm, b = 8.16 \pm .01 cm, h = 3.46 \pm 0.01 cm$ 

Determine the percentage error in the volume of the block .

# Watch Video Solution

104. To find the value of 'g' by using a simple pendulum, the following observations were made: Length of the thread,  $I = (100 \pm 0.1)cm$  Time period of oscillation,  $T = (2 \pm 0.1)s$  Calculate the maximum permissible in measurement of 'g' which quanitiy should be measured more accurately and why?



**105.** A physcial quantity P is realted to four observables a, b, c and d as follows :  $P = a^3b^2/(\sqrt{c}d)$  The percentage errors of measurement in a, b,c, and d are 1 % 3%, 4% and 2%, respectively. What is the percentage error in the quantity P ? If the value of P calculate using the above relation turns out to be 3.763, to what value should you round off the result ?

Watch Video Solution

**106.** In an experiment, the following observations were recorded:

L = 2.820m, M = 3.00kg, l = 0.087cm, diameter, D = 0.041cm.

Taking  $g=9.81ms^{-2}$  and using the formula ,  $Y={4MgL\over \pi D^2 l}$  , find the maximum permissible error in Y.

**107.** The specific resistance  $\rho$  of a thin wire of radius r cm, resistance R ohm and length L is given by  $\rho = \frac{\pi r^2 R}{L}$ .  $IfL = 78 \pm 0.01 cm$  $r = 0.26 \pm 0.02$  and  $R = 32 \pm 1\Omega$ , What is the percentage error in  $\rho$ ?



#### Problem

**1.** if the velocity of light c, the constant of gravitation G and plank,s constant h be chosen os fundamentad units , find the dimensions of mass

, length and time in terms of c , G and h.



**3.** A gas bubble, from an explosion under water, oscillates with a period T proportional in  $P^a D^b E^c$ , where p is the static pressure, d is the density of water and E is the total energy of the explosion. Find the value of a, b and c.



**4.** A small steel ball of radius r is allowed to fall under gravity through a column of a viscous liquid of coefficient of viscosity  $\eta$ . After some time the

velocity of the ball attains a constant value known as terminal velocity  $v_T$ . The terminal velocity depends on (i) the mass of the ball m (ii)  $\eta$ , (iii) r and (iv) acceleration due to gravity g . Which of the following relations is dimensionally correct?



5. Derive dimensionally the relation  $:S=ut+rac{1}{2}at^2.$ 

Watch Video Solution

**6.** Assuming that the vibration frequency v of atoms in a crystal depends

on the atomic mass m , the atomic spacing  $\alpha$  and compressibility  $\beta,$  find

an expression for frequency.



7. The pressure on a square plate is measured by measuring the force on the plate and the length of the sides of the plate . If the maximum error in the measurement of force and length are , respectively , 4% and 2%. Find the maximum error in the measurement of pressure.

Watch Video Solution

**8.** An experiment measures quantites a, b, c and X is calculated from the

formula

$$X=rac{ab^2}{c^3}$$

If the percentage errors in a, b, c are  $\pm 1~\%$  ,  $\pm 3~\%$  ,  $\pm 2~\%$  respectively,

the perentage error in X can be

# Watch Video Solution

**9.** The specific heats of a gas are measured as  $C_p = (12.28 \pm 0.2)$  units and C\_(upsilon =(3.97 +- 03)` units. Find the value of gas constant R and percentage error in R.

**10.** The heat generated in a circuit is given by  $Q = I^2 R t$ , where I is current, R is resistance, and t is time. If the percentage errors in measuring I, R, and tare 2%, 1%, and 1%, respectively, then the maximum error in measuring heat will be

Watch Video Solution

**Problem For Self Practice** 

1. Write the order of magnitude of the following :

(i) 8 (ii) 49 (iii)52 (iv) 999 (v) 1001 (vi) 753000 (vii) 0.05 (viii) 0.99



2. What is one astronomical unit ? Express it in metres . Write its order og

magnitude.



4. IF the size of an atom ( = 1Å) were enlarged to the tip of a sharp pin  $(\cong 10^{-5}m)$ , how large would the height of mout everest  $(\cong 10^4m)$  be?

## Watch Video Solution

5. If an atom of size  $10^{-10}$ m were enlarged to the size of the earth  $(\cong 10^7 m)$ , how large would its nucleus be ? Take size of nucleus





**6.** if the universe were shrunk to the size, of earth, how large would the earth be on this scale?

Watch Video Solution

7. A 35 mm wide slide with 24 mm  $\times$  36 mm picture is projected ona screen placed 12 cm from the slide. The image of the slide picture on the screen measures  $1.0m \times 1.5m$ . What is the linear magnification of the arrangement ?



**8.** In a submarine fitted with a SONAR, the time between the genretaion of an ultrasonicwave and the reciept of its echo is 200 s. What is the

dsistance of the enemy sun=bmrine ? The speed of the sound in water is

 $1.450 km s^{-1}$ 

Watch Video Solution

**9.** A radar signal is beamed towards a planet and its echo is recived 7 minutes later. If the distance between the planet and earth is  $6.3 imes 10^{10} m$ , calculate the speed of the signal.

> Watch Video Solution

**10.** A rock under water is 1595 m deep. Find the time in which an ultrasonic signal returns after reflection from the rock. Speed of ultrasonic waves in water = 1450m/s.

**11.** The angle of elevation of the top of a hill is  $30^{\circ}$  from a point on the ground. On walking 1 km towards the hill, angle is found to be  $45^{\circ}$ . Calculate the height of the hill.

Watch Video Solution

12. Find the distance of the moon from the earth if the parralrtic angle as measured from two places locaterd  $6.4 imes10^6$ m apart is  $1^\circ$ .

Watch Video Solution

13. The parallex of a heavenly body measured ffrom two points diametrically opposite on equater of earth is 1.0 minutes. If the radius of the earth is 6400 m, find the distance of the heavenly body from the centre of the earth in AU. Given  $1AU = 1.5 \times 10^{11}$ m.

14. The angular diameter of the sun is 1920". If the distance of the sun from the earth is  $1.5 imes10^{11}$ m, what is the linear diameter of the sun ?

## Watch Video Solution

**15.** The moon is observed from two diametrically opposite points A and B on earth. The angle  $\theta$  substended at the moon by the two directions of observation is 1°54′. Given the diameter of earth to be about  $1.276 \times 10^7 m$ , calculate the distance of moon from earth.

Watch Video Solution

16. The radius of a muonic hydrogen atom is  $2.5 \times 10^{-13} m$ . What is the total atomic volume in  $m^3$  of a mole of such hydrogen atom.

**17.** A drop of olive oil of radius 0.3 mm spreads into a rectangular film of  $30cm \times 15cm$  on the water surface. Calculate the size of the oil molecule.



**18.** Consider a white dwarf and a nutron star beach of one solar mass. The radius of the white dwarf is same as that of the eartyh (=6400km) and the radius of the neutron star is 10 km. Determine the densities of the two types of the stars. Take mass of the sun  $= 2.0 \times 10^{30}$ kg.



**19.** A neutron star has a density equal to that of nuclear matter  $(\cong 2.8X0^{17}kgm^{-3})$ . Assuming the star to be spherical, find the radius of the neutron star whose mass is  $4.0X10^{30}kg$ .

**20.** Assume that trhe mass of the nucleus is given by  $M=Am_p$ , where A in the mass number and radius of a nuclear  $r=r_0A^{1/3}$ , where  $r_0=1.2$  f. Estimate the density of the nuclear matter in kg  $m^{-3}$ . Given  $m_p = 1.67 \times 10^{-27}$ kg.

Watch Video Solution

**21.** Find the number of seconds in 1 year. Express them in order magnitude.

Watch Video Solution

22. Human heart beats one in 0.8s. Calculate how many times the human

heart beats in the life of a person of 60 years.



**23.** Two atomic clocks allowend to run for a average life of an indian (say 70 years) differ by 0.2 s only. Calculate the accuracy of standard atomic clock in measuring a time interval of 1 sec.



**24.** If two celsium clocks differ only by 0.02 s in 200 yaers, what is the accuracy of cesium clock in measuring time intervals ?

Watch Video Solution

**25.** Age of the universe is about  $10^{10}$  years whereas the mankind has existed for  $10^6$  years. How many seconds would the man have existed if age of universe were one day.



**26.** Deduce dimensional formulae for (i) angle (ii) angular velocity (iii) angular acceleration (iv) torque (v) angukar momentum and (vi) moment of inertia.

	Watch	Video	Solution
1		11000	50141011

**27.** Obtain dimensions of (i) impulse (ii) power (iii) surface energy (iv) cofficent of viscecity (v) bulk modules (vi) force constant.

Watch Video Solution

28. By the use of dimensions, show that energy per unit volume is equal

to pressure.



**29.** Show that angular momentum has the same dimensions as the Planck's constant.

Watch Video Solution

**30.** If force (F), length(L) and time (T) as chosen as the fundamental quantities, then what would be the dimensional formula for the density?

> Watch Video Solution

**31.** Calculate the dimensions of ther force and impulse taking velocity, density and frequency as basic quantities.



**32.** Calculate the dimensions of linear momentum and surface tension in terms of velocity (v), density  $(\rho)$  and frequency (V) as fundamental

### units.



**33.** If E, M, J, and G, respectively, denote energy, mass, angular momentum, and gravitational constant, then  $EJ^2/M^5G^2$  has the dimensions of

Watch Video Solution

**34.** If 'slap' times speed equals power, what is the dimensional formula for

'slap' ?

Watch Video Solution

**35.** By the method of dimensions, show that  $1N=10^5$  dynes .



**40.** The surface tension of water is 72 dyne/cm. Express is in SI units.



**44.** Find the value of 100 J on a system which has 20 cm, 250g and half minute as fundamental units of length, mass and time.

Watch Video Solution
<b>45.</b> If the unit of force energy and velocity are 20 N, 200J and 5m//s, find the units of mass, length and time.
Watch Video Solution

**46.** When 1m, 1kg and 1min. Are taken as the fundamental units, the magnitude of force is 36 units. What will be the value of this force is CGS system?

**47.** If the units of length and force be increased three times, show that

the unit pof energy is increased by 9 times.



**48.** If velocity of light is taken as the unit of velocity and an year is taken as the unit of time, what is the unit of length? What is it called?

Watch Video Solution

49. Test the dimensional consistency of the following equations :

$$(i)v = u + at \qquad (ii)v^2 = u^2 + 2as \qquad (iii)E = mc^2 \qquad (iv)rac{1}{2}mv^2 + 2as$$



**50.** Use principle of homogenity of dimensions to find which one of the following relations is correct : (i)  $T^2 = 4\pi^2 r^2$ 

(ii) 
$$T^2 = rac{4\pi^2 r^3}{G}$$
  
(iii)  $T^2 = rac{4\pi^2 r^3}{GM}$ 

Watch Video Solution

**51.** A student conclude that the velocity v of a body falling freely under gravity from a height is equal to  $\sqrt{gh}$ . Using the method of dimensions, verify whether his coclusion is correct.

Watch Video Solution

**52.** The viscous force 'F' acting on a small sphere of rtadius 'r' moving with velocity v through the liquid is gib=ven by F=  $6\pi nrv$ . Calculate the dimensions of n, the cofficent of viscosity.

**53.** The dimensions of 'k' in the relation V = k avt (where V is the volume of a liquid passing through any point in time t, 'a' is area of cross section, v is the velocity of the liquid) is

Watch Video Solution

**54.** The cirtical velocity (v) of flow of a liquied through a pipe of radius (r ) is given by  $v = \frac{\eta}{\rho r}$  where  $\rho$  is density of liquid and  $\eta$  is coefficient of visocity of the liquied. Check if the relaiton is correct dimensinally.

Watch Video Solution

**55.** The rate of flow (V) of a liquid flowing through a pipe of radius r and pressure gradient (P/I) is given by Poiseuille's equation  $V = \frac{\pi}{8} \frac{Pr^4}{\eta I}$ Chack the dimensional correctness of this relation.



56. Test if the following equations are dimensionally correct: (a)

$$h=rac{2S\cos heta}{
ho rg}$$
 (b)  $u=\sqrt{rac{P}{
ho}}$ , (c)  $V=rac{\pi Pr^4t}{8\eta l},\,$  (d)  $v=rac{1}{2\pi}rac{\sqrt{mgl}}{I}$  where

h = height, S= surface tension,  $\rho$ = density, P= pressure, V=volume,  $\eta$  = coefficient of viscosity, v= frequency and I = moment of inertia.

# Watch Video Solution

57. The time period of a compound pendulum is given by

$$T=2\pi\sqrt{rac{I}{mgl}}$$

where I=moment of inertia about the centre of the suspension, g=acceleration due to gravity, m=mass of the pendulam l=distance of the centre of the gravity from the centre of the susp

Watch Video Solution

**58.** Find the dimensions of the quantity q from the expression  $T=2\pi\sqrt{\frac{ml^3}{3Yq}}$ , where T is time period of a bar of length l, mass m and

Young's modulus Y.



**59.** An artificial satellite of mass m is revolving in a circualr orbit around a planet of mass M and radius R. If the radius of the orbit of satellite be r, then period of satellite is

$$T=rac{2\pi}{R}\sqrt{rac{r^3}{g}}$$

Justify the relation using the method of dimensions.

Watch Video Solution

**60.** Check by the method of dimensions, the formula  $v=rac{1}{\lambda}\sqrt{rac{K}{d}},\,$  where

v is velocity of longitudinal waves,  $\lambda$  is wavelength of wave, K is coefficient

of volume elasticity and d is density of the medium.



**61.** Check the correctness of the equation :  $y = a {
m sin}(\omega t + \phi)$ , where y =

displacement , a = amplitude ,  $\omega$  = angular frequency and  $\phi$  is an angle .



pressure, x is distance and t is time are -----?



**Based On Deriving Relationship** 

1. The wavelength  $\lambda$  associated with a moving electron depends on its mass m , its velocity v and Planck's constant h . Prove dimensionally that \$h\$

$$\lambda \propto \frac{n}{mv}$$

Watch Video Solution

2. Obtain an expression for the centripetal force F acting on a particle of mass m moving with velocity v in a circle of radius r . Take dimensionless constant K = 1.



**3.** The orbital velocity v of a satellite may depend on its mass m , the distane r from the centre of the earth and acceleration due to gravity g .





depends or  $r, \upsilon, \eta$ .  $TakeK = 6\pi$ 



5. The velocity of a freely falling body is a function of the distance fallen through (h) and acceleration due to gravity g . Show by the method of dimensions that  $v=K\sqrt{gh}$ .



6. Using the method of dimensions , derive an expressions for the energy

of a body executing SHM , assuming this energy depends upon its mass m

, frequency v and amplitude of vibration r .

# Watch Video Solution

7. A body of mass m hung at one end of the spring executes simple harmonic motion . The force constant of a spring is k while its period of vibration is T. Prove by dimensional method that the equation  $T = 2\pi m / k$  is correct. Dervive the correct equation , assuming that they are related by a power law.

Watch Video Solution

**8.** Assuming that the critical velocity of flow of a liquid through a narrow tube depends on the radius of the tube, density of the liquid and viscosity of the liquid, find an expression for critical velocity.

**9.** By the method of dimensions, obtain an expression for the surface tension S of a liquid rising in a capillary tube. Assume that S depends on mass m of liquied, Pressure p of liquid and radius r of the capillary tube. Take K = 1/2.

Watch Video Solution

10. The depth x to which a bullet penetrates a human body depends on (i) coeffeicint of elasticity,  $\eta$  and (ii) KE  $(E_k)$  of the bullet, By the method of dimensions, show that

$$x \propto \left(rac{E_k}{\eta}
ight)^{1/3}$$

Watch Video Solution

**11.** A U - tube of uniform cross section contains mercury upto a height h in either limb. The mercury in one limbe is depressed a little and then

relased. Obtain an expression for time period (T) of oscillation, assuming that T depends on h, $\rho$  and g, where  $\rho$  is density of mercury.

Watch Video Solution

12. The cirtical angular velocity  $\omega_c$  of a cylinder inside another cylinder containing a liquied at which its turbulance occurs depends on visocisity  $\eta$  density  $\rho$  and disntac d between wall of the cylinder. Obtain an expression for  $\omega_c$  using method of dimensios.

Watch Video Solution

## **Based On Significant**

1. Statement the number of significant figures in the following

(i)

 $2.653 imes 10^4$  (ii) 0.00368 (iii) 653 (iv) 0.368 (v) 0.0300 (vi) 876.00

2. State the number of significant figures in the following measurements :

(i)

 $0.009m^2$   $(ii)5.049Nm^{-2}$   $(iii)0.1890gcm^{-3}$   $(iv)1.90 imes 10^{11}kg$   $(v)^{10}$ 

Watch Video Solution

3. Round off the following numbers as indicated :

(i) 15.654 upto 3 digits (ii)15.75 upto 3 digits (iii)15.654 upto 4 digits (iv)15.65 upto 3 digits (v) 142667 upto 5 digits (vi)  $5.996 \times 10^5$ upto 3 digits . (vii) 0.7995 upto 1 digit (viii)  $2.5946 \times 10^{-4}$  upto 2 digits .

Watch Video Solution

4. Solve the following to the appropriate number of significant figures :

(i) 0.58 + 324.65

(ii) 3.124 imes 4.576

(iii)  $\frac{324 \times 0.08666}{5.006}$ 

$$\frac{\frac{1.35 \times 10^{-6} \times 0.4}{5.6}}{\text{(v)} \frac{2.03 \times 10^{-5} \times 3.5 \times 10^{-7}}{0.6423}}$$
(vi)  $\sqrt{3.5 - 3.31}$ 

Watch Video Solution

5. (a).Add  $3.8 \times 10^{-6} \rightarrow 4.2 \times 10^{-5}$  with due regard to significant figures.

(b). Subtract  $3.2 imes 10^{-6}$  om $4.7 imes 10^{-4}$  with regard to significant figures.

( c ). Subtract  $1.5 imes 10^3 {
m o} m 4.8 imes 10^4$  with due regard to significant figures.

Watch Video Solution

6. (a).Add  $3.8 \times 10^{-6} \rightarrow 4.2 \times 10^{-5}$  with due regard to significant figures.

(b). Subtract  $3.2 imes 10^{-6} \mathfrak{o} m 4.7 imes 10^{-4}$  with regard to significant figures.

( c ). Subtract  $1.5 imes 10^3$  om $4.8 imes 10^4$  with due regard to significant figures.

**Watch Video Solution** 

**7.** A jewaller puts a diamond weighing 5.42g in a box weighing 1.2kg. Find the total weight of the box and the diamond to correct number of significant figures.

> Watch Video Solution

**8.** The mass of a box measured by a grocer's balance is 4.2 kg. Two additional masses 10.20 g and 15.25 g are added to the box . What is the total mass of the box ?

**9.** The length , breadth and thickness of a metal block are 4.327m, 2.825m and 4.32 cm respectively . Calculate its (i) surface area and (ii) volume and express the results to an appropriate number of significant figures .

Watch Video Solution

**10.** The diameter of a circle is 2.486 m. Calculate the area with due regard

to significant figures.

Watch Video Solution

11. The diameter of a sphere is  $4.24 \mathrm{~m}$  . Calculate its surface area with due

regard to significant figures .


**12.** The diameter of a sphere is 2.78 m . Calculate its volume with due regard to significant figures .

Watch Video Solution

**13.** Each side of a cube is measured to be 7.203 m . What is (i) the total surface area and (ii) the volume of the cube to appropriate significant figures ?

Watch Video Solution

14. A thin wire has a length of 21.7 cm and radius 0.46 mm. Calculate the

volume of the wire to correct significant figures.



**15.** A substance weight 5.74 g occupies a volume of  $1.2cm^3$ . Caluclate its

density with due regard to significant digits.

Watch Video Solution

Based On Errors In Measurements

**1.** The diameter of a wire as measured by a screw gauge was found to be

0.026 cm, 0.028 cm, 0.029 cm, 0.027 cm, 0.024 cm and 0.027 cm. Calculate

(i) mean value of diameter

(ii) mean absoulte error

(iii) relative error (iv) percentage error. Also express the result in terms of

absolute error and percentage error.

Watch Video Solution

2. The refractive index of water as measured by the relation  $\mu = \frac{\text{Real depth}}{\text{Apparent depth}} \quad \text{was} \quad \text{found} \quad \text{to} \quad \text{have} \quad \text{the} \quad \text{values}$ 1.29, 1.33, 1.34, 1.35, 1.32, 1.36, 1.30, 1.33.

Calculate (i) mean value of  $\mu$  (ii) mean value of absolute error (iii) relative error (iv) percentage error .

Watch Video Solution

**3.** In an experiment to measure focal length of a concave mirror , the value of focal length in successive observations turns out to be 17.3 cm , 17.8 cm , 18.3 cm , 18.2 cm , 17.9 cm and 18.0 cm . Calculate the mean absolute error and percentage error . Express the result in a proper way .



**Based On Combination** 

1. The length of two rods are recorded as  $l_1=(25.2\pm0.1)$  cm and  $l_2=(16.8\pm0.1)$  cm . Find their combined length .



2. Two resistance  $(200\pm4)\Omega$  and  $(150\pm3)\Omega$  are connected in series .

What is their equivalent resistance ?

Watch Video Solution

3. The initial and final temperature of water were recorded as  $(56.3\pm0.4)^\circ C$  and  $(27.5+0.3)^\circ C$ . Determine the fall in the temperature of water .



4. If  $l_1=(10.0\pm0.1)$  cm and  $l_2=(9.0\pm0.1)$  cm , find the their sum ,

difference and error in each .



5. A capacitor  $C=(2.0\pm0.1)\mu F$  is charged to a voltage  $V=(20\pm0.5)$  volt. Calculate the charge Q with error limits.

Watch Video Solution

**6.** The resistance R of a conductor is defind as the ratio of the potential difference applied across it to the current flowing through ti . If V =  $(100 \pm 5)V$  and I = (5 + 0.1) A, what is the percentage error in R?



7. The relative density of a material is found by weighing the body first in air and then in water . If the weight in air is  $(10.0 \pm 0.1)gf$  and the weight in water is  $(5.0 \pm 0.1)gf$ , then the maximum permissible percentage error in relative density is

Watch Video Solution

**8.** The length and breadth of a rectangular block are 25.2 cm and 16.8 cm, which have both been measurd to an accurancy of 0.1 cm find the area of the rectangular block.

Watch Video Solution

9. While measuring the volume of a sphere , an error of 1.2% is commited in the measurement of radius . What percent error is introduced in the measurement of its volume ?

10. The voltage across a lamp is  $(6.0\pm0.1)V$  and the current passing through it is  $(4.0\pm0.2)$  ampare. Find the power consumed by the lamp.



11. The radius of a sphere is measured to be  $(2.1\pm0.5)$  cm. Calculate its surface area with error limits .

Watch Video Solution

12. The radius of a sphere is  $(5.3\pm0.1){
m cm}$  The perecentage error in its

volume is

Watch Video Solution

13. The measure of the diameter of a cylinder is  $(1.60\pm0.01)$  cm and its

length is  $(5.0\pm0.1)$  cm . Calculate the percentage error in its volume .

14. The measured mass and volume of a body are 2.00 g and  $5.0 \text{cm}^3$  respectively. With possible errors of 0.01 g and  $0.1 \text{cm}^3$ , what would be the percent error in density?

Watch Video Solution

15. Two resistance  $R_1$  and  $R_2$  are connected in (i) series and (ii) parallel. What is the equivalent resistance with limit of possible percentage error in each case of  $R_1=5.0\pm0.2\Omega$  and  $R_2=10.0\pm0.1\Omega$ 

## Watch Video Solution

16. A body travels uniformly a distance of  $(13.8 \pm 0.2)m$  in a time  $(4.0 \pm 0.3)s$ . Find the velocity of the body within error limits and the percentage error.

**17.** The centripetal force acting on a body of mass m moving with speed v along a circular path of radius r is given by

$$F=rac{mv^2}{r}$$

If the values of m , v and r are measured as 0.5 kg ,  $10ms^{-1}$  and 0.4 m respectively to the accuracies of 0.005 kg ,  $0.01ms^{-1}$  and 0.01 m respectively , calculate the percentage error in the force acting on the body.

Watch Video Solution

**18.** The period of oscillation of a simple pendulum is  $T = 2\pi \sqrt{\frac{L}{g}}$ . L is about 10cm and is known to 1mm accuracy. The period of oscillation is about 0.5s. The time of 100 oscillation is measured with a wrist watch of 1s resolution. What is the accuracy in the determination of g?



**19.** Calculate the percentage error in specific resistance ,  $ho = \pi r^2 R/l$ , where r = radius of wire  $= 0.26 \pm 0.02 cm$  , l = length of wire  $= 156.0 \pm 0.1 cm$ , and R = resistance of wire  $= 64 \pm 2\Omega$ .

**20.** The Young's modulus Y is determined by stretching a wire by using the formula ,

$$Y = rac{4FL}{\pi d^2 l}$$

where F is the streching force , L is length of wire , I is extension in length and d is its diameter . If F is of the order of 500 N and known to 1 part in 1000 L , is of the order of 3 m and measured with an accuracy of 1 mm , I is of the order of 5 mm measured to 0.1 mm and d is of the order of 1 mm measured correct upto 0.01 mm , estimate the percentage error in the measurement of Y .

## Watch Video Solution

**21.** A physical quantify X is related to three observations a , b, c as  $X = \sqrt{a}b^2/c^2$ . The errors of measurement in a ,b and c are 2%, 1% and 3% respectively. What is the percentage error in the quantity X?

