

## MATHS

### BOOKS - CENGAGE MATHS (ENGLISH)

#### DETERMINANTS

##### Illustration

1. find the value of  $\begin{vmatrix} 1 & 2 & 4 \\ -1 & 3 & 0 \\ 4 & 1 & 0 \end{vmatrix}$



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2. Prove that the determinant  $\Delta = \begin{vmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$  is

independent of  $\theta$ .



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3. The parameter on which the value of the determinant  $\begin{vmatrix} 1 & a & a^2 \\ \cos(p-d)x & \cos px & \cos(p+d)x \\ \sin(p-d)x & \sin px & \sin(p+d)x \end{vmatrix}$  does not depend is

a. p.  
b. p.c.  
c. d.d.  
d. x`



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4. Let  $a, b, c$  be positive and not all equal. Show that the value of the

determinant  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$  is negative.



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5. If  $a, b, c \in R$ , then find the number of real roots of the equation  
 $= |xc - b - cxab - ax| = 0$



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$$6. \text{ If } x + y + z = 0 \text{ prove that} \begin{vmatrix} ax & by & cz \\ cy & az & bx \\ bz & cx & ay \end{vmatrix} = xyz \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$$



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$$7. \text{ If } p\lambda^4 + q\lambda^3 + r\lambda^2 + s\lambda + t = \begin{vmatrix} \lambda^2 + 3\lambda & \lambda - 1 & \lambda + 3 \\ \lambda^2 + 1 & 2 - \lambda & \lambda - 3 \\ \lambda^2 - 3 & \lambda + 4 & 3\lambda \end{vmatrix} \text{ then } t =$$



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8. The largest value of a third order determinant whose elements are equal to 1 or 0 is



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9. Prove that the value of the determinant

$$\begin{vmatrix} -7 & 5 + 3i & \frac{2}{3} - 4i \\ 5 - 3i & 8 & 4 + 5i \\ \frac{2}{3} + 4i & 4 - 5i & 9 \end{vmatrix} \text{ is real}$$





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10. Without expanding the determinants Prove that

$$\begin{vmatrix} 103 & 115 & 114 \\ 111 & 108 & 106 \\ 104 & 113 & 116 \end{vmatrix} + \begin{vmatrix} 113 & 116 & 104 \\ 108 & 106 & 111 \\ 115 & 114 & 103 \end{vmatrix} = 0$$



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11. Prove that

$$\begin{vmatrix} ax & by & cz \\ x^2 & y^2 & z^2 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} a & b & c \\ x & y & z \\ yz & xz & xy \end{vmatrix}$$



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12. for  $x, y, z > 0$  Prove that

$$\begin{vmatrix} 1 & \log_x y & \log_x z \\ \log_y x & 1 & \log_y z \\ \log_z x & \log_z y & 1 \end{vmatrix} = 0$$



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13. without expanding at any stage Prove that

$$\begin{vmatrix} 0 & a & -b \\ -a & 0 & -c \\ b & c & 0 \end{vmatrix} = 0$$



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14. consider the fourth -degree polynomial equation

$$\begin{vmatrix} a_1 + b_1x^2 & a_1x^2 + b_1 & c_1 \\ a_2 + b_2x^2 & a_2x^2 + b_2 & c_2 \\ a_3 + b_3x^2 & a_3x^2 + b_3 & c_3 \end{vmatrix} = 0$$

Without expanding the determinant find all the roots of the equation.



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15. Let  $\Delta_r = \begin{vmatrix} r-1 & n & 6 \\ (r-1)^2 & 2n^2 & 4n-2 \\ (r-1)^3 & 3n^3 & 3n^2 - 3n \end{vmatrix}$ . Show that  $\sum_{r=1}^n \Delta_r$  is constant.



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16. Find the value of

$$\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$$



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17. Find the value of determinant

$$\left| \sqrt{(13)} + \sqrt{32} \sqrt{5} \sqrt{5} \sqrt{(15)} + \sqrt{(26)} 5 \sqrt{(10)} 3 + \sqrt{(65)} \sqrt{(15)} 5 \right|$$



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18. Find the value of the determinant

$$\begin{vmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 6 & 10 \\ 1 & 4 & 10 & 20 \end{vmatrix}$$



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19. Using properties of determinants. Prove that

$$|\sin \alpha \cos \alpha \cos(\alpha + \delta) \sin \beta \cos \beta \cos(\beta + \delta) \sin \gamma \cos \gamma \cos(\gamma + \delta)| = 0$$



20. Using properties of determinants, solve the following for x:

$$\begin{vmatrix} x - 2 & 2x - 3 & 3x - 4 \\ x - 4 & 2x - 9 & 3x - 16 \\ x - 8 & 2x - 27 & 3x - 64 \end{vmatrix} = 0$$



21. By using properties of determinants, prove the following:

$$|x + 42x^2x^2 \times + 42x^2x^2 \times + 4| = (5x + 4)(4 - x)^2$$



22. prove that  $\begin{bmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{bmatrix} = (a + b + c)^3$



23. if  $x_i = a_i b_i C_i$ ,  $i = 1, 2, 3$  are three-digit positive integer such that each  $x_i$  is a multiple of 19 then prove that  $\det \begin{Bmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{Bmatrix}$  is divisible by 19.



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24. If  $a$ ,  $b$  and  $c$  are real numbers, and  $\Delta = |b + aa + bc + aa + ca + a| = 0$ . Show that either  $a + b + c = 0$  or  $a = b = c$ .



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25. Find the value of the determinant  $|baabpqr111|$ , where  $a$ ,  $b$ , and  $c$  are respectively, the  $p$ th,  $q$ th, and  $r$ th terms of a harmonic progression.



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**26.**

if  $a_1, a_2, a_3, \dots$  are in A.P, then find the value of the following determinants

$$\begin{vmatrix} a_p + a_{p+m} + a_{p+2m} & 2a_p + 3a_{p+m} + 4a_{p+2m} & 4a_p + 9a_{p+m} + 16a_{p+2m} \\ a_p + a_{q+m} + a_{q+2m} & 2a_q + 3a_{q+m} + 4a_{q+2m} & 4a_q + 9a_{q+m} + 16a_{q+2m} \\ a_r + a_{r+m} + a_{r+2m} & 2a_r + 3a_{r+m} + 4a_{r+2m} & 4a_r + 9a_{r+m} + 16a_{r+2m} \end{vmatrix}$$



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**27.** Prove that  $\begin{vmatrix} 1 & \beta\gamma + \alpha\delta & \beta^2\gamma^2 + \alpha^2\delta^2 \\ 1 & \gamma\alpha + \beta\delta & \gamma^2\alpha^2 + \beta^2\delta^2 \\ 1 & \alpha\beta + \gamma\delta & \alpha^2\beta^2 + \gamma^2\delta^2 \end{vmatrix} = 0$



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**28.**

Prove

that

$$|a, b+c, a^2, b, c+a, b^2, c, a+b, c^2| = -(a+b+c) \times (a-b)(b-c)(c-a)$$

a)



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29.

Prove

that

$$|x^2x^2 - (y-z)^2yzy^2y^2 - (z-x)^2zxz^2z^2 - (x-y)^2xy| = (x-y)(y-z)$$



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30. If  $a, b, c$  are all distinct and

$$\begin{vmatrix} a & a^3 & a^4 - 1 \\ b & b^3 & b^4 - 1 \\ c & c^3 & c^4 - 1 \end{vmatrix} = 0, \text{ show that}$$

$$abc(ab+bc+ac) = a+b+c$$



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31. Prove that

$$\begin{vmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ac & bc & c^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2$$



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32. prove that

$$\begin{vmatrix} (b+c)^2 & bc & ac \\ ba & (c+a)^2 & cb \\ ca & cb & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix}$$



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33. Let  $a, b, c$  be real numbers with  $a^2 + b^2 + c^2 = 1$ . Show that the

equation

$$\begin{vmatrix} ax - by - c & bx + ay & cx + a \\ bx + ay & -ax + by - c & cy + b \\ cx + a & cy + b & -ax - by + c \end{vmatrix} = 0$$

represents a straight line.



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34. If  $a^2 + b^2 + c^2 = 1$ , then prove that

$$\begin{vmatrix} a^2 + (b^2 + c^2)\cos\theta & ab(1 - \cos\theta) & ac(1 - \cos\theta) \\ ba(1 - \cos\theta) & b^2(c^2 + a^2)\cos\theta & bc(1 - \cos\theta) \\ ca(1 - \cos\theta) & cb(1 - \cos\theta) & c^2 + (a^2 + b^2)\cos\theta \end{vmatrix}$$

independent of  $a, b, c$ ?



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35. Find the area of a triangle whose vertices are  $A(3, 2)$ ,  $B(11, 8)$  and  $C(8, 12)$ .



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36. If the lines  $a_1x + b_1y + 1 = 0$ ,  $a_2x + b_2y + 1 = 0$  and  $a_3x + b_3y + 1 = 0$  are concurrent, show that the points  $(a_1, b_1)$ ,  $(a_2, b_2)$  and  $(a_3, b_3)$  are collinear.



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37. The number of values of  $a$  for which the lines  $2x + y - 1 = 0$ ,  $ax + 3y - 3 = 0$ , and  $3x + 2y - 2 = 0$  are concurrent is (a) 0 (b) 1 (c) 2 (d) infinite



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38. If the lines  $ax + y + 1 = 0$ ,  $x + by + 1 = 0$  and  $x + y + c = 0$  ( $a, b, c$  being distinct and different from 1) are concurrent, then prove that  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1$ .



39. Find the value of  $\lambda$  if  $2x^2 + 7xy + 3y^2 + 8x + 14y + \lambda = 0$  represents a pair of straight lines.



40. show that the determinant

$$\begin{vmatrix} a^2 + b^2 + c^2 & bc + ca + ab & bc + ca + ab \\ bc + ca + ab & a^2 + b^2 + c^2 & bc + ca + ab \\ bc + ca + ab & bc + ca + ab & a^2 + b^2 + c^2 \end{vmatrix}$$

is always non-negative.



41. Factorize the following

$$|3a + b + ca^3 + b^3 + c^3a + b + ca^2 + b^2 + c^2a^4 + b^4 + c^4a^2 + b^2 + c^2a^3 +$$



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42. prove that

$$\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-z)^2 \end{vmatrix}$$

$$\begin{vmatrix} (1+ax)^2 & (1+bx)^2 & (1+cx)^2 \\ (1+ay)^2 & (1+by)^2 & (1+cy)^2 \\ (1+az)^2 & (1+bx)^2 & (1+cz)^2 \end{vmatrix}$$

$$= 2(b-c)(c-a)(a-b) \times (y-z)(z-x)(x-y)$$



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43. If  $\alpha, \beta, \gamma$  are real numbers, then without expanding at any stage,

show

that

$$|1 \cos(\beta - \alpha) \cos(\gamma - \alpha) \cos(\alpha - \beta) 1 \cos(\gamma - \beta) \cos(\alpha - \gamma) \cos(\beta - \gamma) 1| = 1$$



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44. If  $\begin{vmatrix} 1 & x & x^2 \\ x & x^2 & 1 \\ x^2 & 1 & x \end{vmatrix} = 3$ , then find the value of  $\begin{vmatrix} x^3 - 1 & 0 & x - x^4 \\ 0 & x - x^4 & x^3 - 1 \\ x - x^4 & x^3 - 1 & 0 \end{vmatrix}$



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45. Show that  $\begin{vmatrix} bc - a^2 & ca - b^2 & ab - c^2 \\ ca - b^2 & ab - c^2 & bc - a^2 \\ ab - c^2 & bc - a^2 & ca - b^2 \end{vmatrix} = \begin{vmatrix} a^2 & c^2 & 2ca - b^2 \\ 2ab - c^2 & b^2 & a^2 \\ b^2 & 2ac - a^2 & c^2 \end{vmatrix}$ .



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46. Let  $f(x) = \begin{vmatrix} \cos x & \sin x & \cos x \\ \cos 2x & \sin 2x & 2 \cos 2x \\ \cos 3x & \sin 3x & 3 \cos 3x \end{vmatrix}$  then find the values of  $f(0)$

and  $f'(\pi/2)$ .



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47. If  $f(x) = \left| x \cap !2 \cos x \frac{\cos(n\pi)}{2} 4 \sin x \frac{\sin(n\pi)}{2} 8 \right|$  then find the value of  $\frac{d^n}{dx^n} ([f(x)])_{x=0} n \in z$ .



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48. If  $f, g,$  and  $h$  are differentiable functions of  $x$  and  $(\delta) =$

$$\begin{vmatrix} f & g & h \\ (xf)' & (xg)' & (xh)' \\ (x^2f)'' & (x^2g)'' & (x^2h)'' \\ f & g & h \\ f' & g' & h \\ (x^3f'')' & (x^3g'')' & (x^3h'')' \end{vmatrix} \quad \text{prove that } \delta' =$$



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49. Let  $\alpha$  be a repeated root of a quadratic equation  $f(x) = 0$  and  $A(x), B(x), C(x)$  be polynomials of degrees 3, 4, and 5, respectively, then show that

$|A(x)B(x)C(x)A(\alpha)B(\alpha)C(\alpha)A'(\alpha)B'(\alpha)C'(\alpha)|$  is divisible by  $f(x)$ , where prime (') denotes the derivatives.



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50. if  $\Delta(x) = \begin{vmatrix} a_1 + x & b_1 + x & c_1 + x \\ a_2 + x & b_2 + x & c_2 + x \\ a_3 + x & b_3 + x & c_3 + x \end{vmatrix}$  then show that  $\Delta(x) = 0$

and that  $\Delta(x) = \Delta(0) + sx$ . where s denotes the sum of all the cofactors of all the elements in  $\Delta(0)$



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51. If  $\Delta(x) = \begin{vmatrix} 1 & x^2 & x^2 \\ 6 & 4x & 3 \\ 9 & x & -7 \end{vmatrix}$  then find the value of  $\int_0^1 \Delta(x)dx$

without expanding  $\Delta(x)$ .



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52. Find the value of  $a$  and  $b$  if the system of equation  
 $a^2x - by = a^2 - b$  and  $bx - b^2y = 2 + 4b$  (i) posses unique solution (ii)  
infinite solutions



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53. If a system of three linear equations  
 $x + 4ay + a = 0$ ,  $x + 3by + b = 0$ , and  $x + 2cy + c = 0$  is consistent,  
then prove that  $a, b, c$  are in H.P.



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54. Solve by Cramers rule     $x + y + z = 6$      $x - y + z = 2$   
 $3x + 2y - 4z = -5$



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55. For what values of p and q the system of equations

$2x + py + 6z = 8$ ,  $x + 2y + qz = 5$ ,  $x + y + 3z = 4$  has i no solution ii a unique solution iii in finitely many solutions.



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56. If  $2ax - 2y + 3z = 0$ ,  $x + ay + 2z = 0$ , and,  $2x + az = 0$  have a nontrivial solution, find the value of a.



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57. For what values of k, the following system of equations possesses a nontrivial solution over the set of rationals:

$x + ky + 3z = 0$ ,  $3x + ky - 2z = 0$ ,  $2x + 3y - 4z = 0$ . Also find the solution for this value of k.



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## Example

1. Prove that:  $\begin{vmatrix} -2a & a+b & a+c \\ b+a & -2b & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$



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2. If  $a, b$  and  $c$  are non-zero real numbers then prove that

$$\begin{vmatrix} b^2c^2 & bc & b+c \\ c^2a^2 & ca & c+a \\ a^2b^2 & ab & a+b \end{vmatrix} = 0$$



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3.

Prove

that

$$|ax - by - cz| + |ay + bx - cz| + |az + cx - bz| + |cy + bz - cx|$$



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4. If  $f(x)$  is a polynomial of degree  $< 3$ , prove that

$$|1af(a)/(x-a)1bf(b)/(x-b)1cf(c)/(x-c)| \div |1aa^21^21^2| = \frac{1}{(x)}$$



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5. Let  $\Delta = \begin{vmatrix} 2a_1b_1 & a_1b_2 + a_2b_1 & a_1b_3 + a_3b_1 \\ a_1b_2 + a_2b_1 & 2a_2b_2 & a_2b_3 + a_3b_2 \\ a_1b_3 + a_3b_1 & a_3b_2 + a_2b_3 & 2a_3b_3 \end{vmatrix}$ . Expressing as

the product of two determinants, show that  $\Delta = 0$



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6. Find the value of  $\begin{vmatrix} \cos\left(\frac{2\pi}{63}\right) & \cos\left(\frac{3\pi}{70}\right) & \cos\left(\frac{4\pi}{77}\right) \\ \cos\left(\frac{\pi}{72}\right) & \cos\left(\frac{2\pi}{80}\right) & \cos\left(\frac{3\pi}{88}\right) \\ 1 & \cos\left(\frac{\pi}{90}\right) & \cos\left(\frac{2\pi}{99}\right) \end{vmatrix}$



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7. Let  $f(t) = \begin{vmatrix} \cos t & t & 1 \\ 2 \sin t & t & 2t \\ \sin t & t & t \end{vmatrix}$ . Then find  $\lim_{t \rightarrow 0} \frac{f(t)}{t^2}$



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8. if  $x_1^2 + 2y_1^2 + 3z_1^2 = x_2^2 + 2y_2^2 + 3z_2^2 = x_3^2 + 2y_3^2 + 3z_3^2 = 2$  and  $x_2x_3 + 2y_2y_3 + 3z_2z_3 = x_3x_1 + 2y_3y_1 + 3z_3z_1 = x_1x_2 + 2y_1y_2 + 3z_1z_2 =$

Then find the value of  $\begin{vmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{vmatrix}$



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9. Let  $\alpha_1, \alpha_2$  and  $\beta_1, \beta_2$  be the roots of the equation  $ax^2 + bx + c = 0$  and  $px^2 + qx + r = 0$  respectively. If the system of equations  $\alpha_1y + \alpha_2z = 0$  and  $\beta_1y + \beta_2z = 0$  has a non trivial solution then prove that  $\frac{b^2}{q^2} = \frac{ac}{pr}$



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10. If  $bc + qr = ca + rp = ab + pq = -1$  and  $(abc, pqr \neq 0)$  then

$$\begin{vmatrix} ap & a & p \\ bq & b & q \\ cr & c & r \end{vmatrix}$$
 is (A) 1 (B) 2 (C) 0 (D) 3



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### Concept Application Exercise 12.1

1. Evaluate  $\begin{vmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos \alpha \end{vmatrix}$



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2. If A,B,C are the angles of a non right angled triangle ABC. Then find the

value of:  $\begin{vmatrix} \tan A & 1 & 1 \\ 1 & \tan B & 1 \\ 1 & 1 & \tan C \end{vmatrix}$



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3. If  $e^{i\theta} = \cos \theta + i \sin \theta$ , find the value of

$$\left| 1e^{i\pi/3} e^{i\pi/4} e^{-i\pi/3} 1 e^{i2\pi/3} e^{-i\pi/4} e^{-i2\pi/3} 1 \right|$$



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4. Find the number of real root of the equation

$$|0x - ax - bx + a|0x - cx + bx + c| = 0, a \neq b \neq c \text{ and } b(a + c) > ac$$



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5. If  $\alpha, \beta, \gamma$  are the roots of  $ax^3 + bx^2 + cx + d = 0$  and

$$\begin{vmatrix} \alpha & \beta & \gamma \\ \beta & \gamma & \alpha \\ \gamma & \alpha & \beta \end{vmatrix} = 0, \alpha \neq \beta \neq \gamma \text{ then find the equation whose roots are}$$

$\alpha + \beta - \gamma, \beta + \gamma - \alpha, \text{ and } \gamma + \alpha - \beta$ .



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6. A triangle has vertices  $A_i(x_i, y_i)$  for  $i=1,2,3$ . If the orthocenter of triangle is  $(0,0)$  then prove that

$$\begin{vmatrix} x_2 - x_3 & y_2 - y_3 & y_1(y_2 - y_3) + x_1(x_2 - x_3) \\ x_3 - x_1 & y_3 - y_1 & y_2(y_3 - y_1) + x_2(x_3 - x_1) \\ x_1 - x_2 & y_1 - y_2 & y_3(y_1 - y_2) + x_3(x_1 - x_2) \end{vmatrix} = 0$$



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7. if  $\omega \neq 1$  is cube root of unity and  $x+y+z \neq 0$  then

$$\begin{vmatrix} \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} \\ \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} & \frac{x}{1+\omega} \\ \frac{z}{\omega^2+1} & \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} \end{vmatrix} = 0 \text{ if}$$



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## Concept Application Exercise 12 2

1. Prove that the value of determinant  $\begin{vmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{vmatrix} = 0$

where  $\omega$  is complex cube root of unity .



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2. Prove that  $\begin{vmatrix} a & a^2 & bc \\ b & b^2 & ac \\ c & c^2 & ab \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$



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3. if  $\Delta = \begin{vmatrix} abc & b^2c & c^2b \\ abc & c^2a & ca^2 \\ abc & a^2b & b^2a \end{vmatrix} = 0$ , ( $a, b, c \in R$  and are all different and non-zero) then prove that  $a + b + c = 0$



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4. if  $a_r = (\cos 2r\pi + i \sin 2r\pi)^{1/9}$  then prove that

$$|(a_1, , a_2, , a_3), a_4, , a_5, , a_6), (a_7, , a_8, , a_9) : \} | = 0$$



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5. Given  $A = \begin{vmatrix} a & b & 2c \\ d & e & 2f \\ l & m & 2n \end{vmatrix}$ ,  $B = \begin{vmatrix} f & 2d & e \\ 2n & 4l & 2m \\ c & 2a & b \end{vmatrix}$ , then the value of  $B/A$  is \_\_\_\_\_.



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### Concept Application Exercise 12 3

1. Prove that the value of the following determinant is zero:

$$\begin{vmatrix} a_1 & la_1 + mb_1 & b_1 \\ a_2 & la_2 + mb_2 & b_2 \\ a_3 & la_3 + mb_3 & b_3 \end{vmatrix}$$



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2. using properties of determinants evaluate

$$\begin{vmatrix} 18 & 40 & 89 \\ 40 & 89 & 198 \\ 89 & 198 & 440 \end{vmatrix}$$



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3. Prove:  $\begin{vmatrix} b+c & a-b & a \\ c+a & b-c & b \\ a+b & c-a & c \end{vmatrix} = 3abc - a^3 - b^3 - c^3$



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4. Show that

$$|11 + p1 + p + q23 + 2p1 + 3p + 2q36 + 3p106p + 3q| = 1.$$



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5. Solve the equation  $\begin{vmatrix} a-x & c & b \\ c & b-x & a \\ b & a & c-x \end{vmatrix} = 0$  where  $a + b + c \neq 0$ .



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6. Show that:

$$|3a - a + b - a + c - b + a3b - b + c - c + a - c + b3c| = 3(a + b + c)(a - b + c)$$



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7. Using properties of determinants Prove that

$$\begin{vmatrix} a+b+c & -c & -b \\ -c & a+b+c & -a \\ -b & -a & a+b+c \end{vmatrix} = 2(a+b)(b+c)(c+a)$$



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8. Solve:  $\begin{vmatrix} x^2 - 1 & x^2 + 2x + 1 & 2x^2 + 3x + 1 \\ 2x^2 + x - 1 & 2x^2 + 5x - 3 & 2x^2 + 4x - 3 \\ 6x^2 - x - 2 & 6x^2 - 7x + 2 & 12x^2 - 5x - 2 \end{vmatrix} = 0.$



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9. Show that

$$\begin{vmatrix} 1 + a^2 - b^2 & 2ab & -2b \\ 2ab & 1 - a^2 + b^2 & 2a \\ 2b & -2a & 1 - a^2 - b^2 \end{vmatrix} = (1 + a^2 + b^2)^3$$



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**10.** Show that if  $x_1, x_2, x_3 \neq 0$

$$\begin{vmatrix} x_1 + a_1 b_1 & a_1 b_2 & a_1 b_3 \\ a_2 b_1 & x_2 + a_2 b_2 & a_2 b_3 \\ a_3 b_1 & a_3 b_2 & x_3 + a_3 b_3 \end{vmatrix} = x_1 x_2 x_3 \left( 1 + \frac{a_1 b_1}{x_1} + \frac{a_2 b_2}{x_2} + \frac{a_3 b_3}{x_3} \right)$$



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**11.** If  $A, B$  and  $C$  are the angles of a triangle, show that

$$-1 + \cos B \cos C + \cos B \cos B \cos C + \cos A - 1 + \cos A \cos A - 1 + \cos$$



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**12.** If  $\begin{vmatrix} a^2 & b^2 & c^2 \\ (a+1)^2 & (b+1)^2 & (c+1)^2 \\ (a-1)^2 & (b-1)^2 & (c-1)^2 \end{vmatrix} = k(a-b)(b-c)(c-a)$  then the

value of  $k$  is a. 4 b. -2 c. -4 d. 2



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13. Prove that  $\Delta = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc + a^2 & ac + b^2 & ab + c^2 \end{vmatrix}$

$$= 2(a - b)(b - c)(c - a)$$



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14. Evaluate  $\begin{vmatrix} .^x C_1 & .^x C_2 & .^x C_3 \\ .^y C_1 & .^y C_2 & .^y C_3 \\ .^z C_1 & .^z C_2 & .^z C_3 \end{vmatrix}$



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15. If  $r = |2^r 2.3^r - 14.5^r - 1\alpha\beta\gamma 2^n - 13^n - 15^n - 1|$ , then find the value of  $r$ .



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16. Prove that  $|1 + a11111 + b11111 + c11111 + d| = abcd \left( a + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d} \right)$ .

Hence find the value of the determinant if  $a, b, c, d$  are the roots of the equation  $px^4 + qx^3 + rx^2 + sx + t = 0$ .



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17. Prove that  $\begin{vmatrix} 1 & ab & \frac{1}{a} + \frac{1}{b} \\ 1 & bc & \frac{1}{b} + \frac{1}{c} \\ 1 & ca & \frac{1}{c} + \frac{1}{a} \end{vmatrix} = 0$



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18. Prove the identities:  $\begin{vmatrix} b^2 + c^2 & ab & ac \\ ab & c^2 + a^2 & bc \\ ca & bc & a^2 + b^2 \end{vmatrix} = 4a^2b^2c^2$



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19. Show that  $\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & b + a & c \end{vmatrix} = (a + b + c)(a^2 + b^2 + c^2)$



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## Concept Application Exercise 12 4

1. If  $x_1, x_2, x_3$  as well as  $y_1, y_2, y_3$  are in G.P. with same common ratio, then prove that the points  $(x_1, y_1), (x_2, y_2)$ , and  $(x_3, y_3)$  are collinear.



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2. If lines  $px + qy + r = 0$ ,  $qx + ry + p = 0$  and  $rx + py + q = 0$  are concurrent, then prove that  $p + q + r = 0$  (where,  $p, q, r$  are distinct).



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3.

if

$$(x_1 - x_2)^2 + (y_1 - y_2)^2 = a^2, (x_2 - x_3)^2 + (y_2 - y_3)^2 = b^2, (x_3 - x_1)^2 + (y_3 - y_1)^2 = c^2$$

where  $a, b, c$  are positive then prove that

$$4 \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = (a + b + c)(b + c - a)(c + a - b)(a + b - c)$$



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4. it is known that the equation of hyperbola and that of its pair of asymptotes differ by constant . If equation of hyperbola is  $x^2 + 4xy + 3y^2 - 4x + 2y + 1 = 0$  then find the equation of its pair of asymptotes.



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### Concept Application Exercise 12 5

1.

Prove

that

$$|(b+x)(c+x)(v+x)(a+x)(a+x)(b+x)(b+y)(c+y)(c+x)(a+t)|$$



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$$2. \Delta = \begin{vmatrix} 1 + a^2 + a^4 & 1 + ab + a^2b^2 & 1 + ac + a^2c^2 \\ 1 + ab + a^2b^2 & 1 + b^2 + b^4 & 1 + bc + b^2c^2 \\ 1 + ac + a^2c^2 & 1 + bc + b^2c^2 & 1 + c^2c^4 \end{vmatrix} \text{ is equal to}$$



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3.

Prove

that

$$|2\alpha + \beta + \gamma + \delta\alpha\beta + \gamma\delta\alpha + \beta + \gamma + \delta^2(\alpha + \beta)(\gamma + \delta)\alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta)^2| = 0$$



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4. For all values of  $A, B, C$  and  $P, Q, R$  show that

$$|\cos(A - P)\cos(A - Q)\cos(A - R)\cos(B - P)\cos(B - Q)\cos(B - R)\cos(C - P)\cos(C - Q)\cos(C - R)| = 1$$



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5. Show that:  $|b^2 + c^2abacbac^2 + a^2bccacba^2 + b^2| = 4a^2b^2c^2$



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6. Express  $\Delta = \begin{vmatrix} 2bc - a^2 & c^2 & b^2 \\ c^2 & 2ca - b^2 & a^2 \\ b^2 & a^2 & 2ab - c^2 \end{vmatrix}$  as square of a

determinant of hence evaluate if.



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### Concept Application Exercise 12 6

1. Let  $f(x) = \begin{vmatrix} \cos(x + x^2) & \sin(x + x^2) & -\cos(x + x^2) \\ \sin(x - x^2) & \cos(x - x^2) & \sin(x - x^2) \\ \sin 2x & 0 & \sin(2x^2) \end{vmatrix}$ . Find the

value of  $f'(0)$ .



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2. If  $f(x)$ ,  $g(x)$  and  $h(x)$  are three polynomial of degree 2, then prove that

$$\phi(x) = \begin{vmatrix} f(x) & g(x) & h(x) \\ f'(x) & g'(x) & h'(x) \\ f''(x) & g''(x) & h''(x) \end{vmatrix}$$

is a constant polynomial.



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3. If  $g(x) = \frac{f(x)}{(x-a)(x-b)(x-c)}$ , where  $f(x)$  is a polynomial of degree  $< 3$ , then prove that

$$\frac{dg(x)}{dx} = \begin{vmatrix} 1 & a & f(a)(x-a)^{-2} \\ 1 & b & f(b)(x-b)^{-2} \\ 1 & c & f(c)(x-c)^{-2} \end{vmatrix} \div \begin{vmatrix} a^2 & a & 1 \\ b^2 & b & 1 \\ c^2 & c & 1 \end{vmatrix}.$$



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4. If  $f(x) = \begin{vmatrix} \cos(x+\alpha) & \cos(x+\beta) & \cos(x+\gamma) \\ \sin(x+\alpha) & \sin(x+\beta) & \sin(x+\gamma) \\ \sin(\beta-\gamma) & \sin(\gamma-\alpha) & \sin(\alpha-\beta) \end{vmatrix}$  and

$f(0) = 2$  then find the value of  $\sum_{r=1}^{30} |f(r)|$ .



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5.  $f(x) = \begin{vmatrix} \cos x & x & 1 \\ 2 \sin x & x^2 & 2x \\ \tan x & x & 1 \end{vmatrix}$  then find the value of

$$\lim_{x \rightarrow 0} \frac{f(x)}{x}$$



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## Concept Application Exercise 12.7

1. Find the following system of equations is consistent,  
 $(a+1)^3x + (a+2)^3y = (a+3)^3$     $(a+1)x + (a+2)y = a+3$     $+1$ ,  
then find the value of  $a$ .



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2. Solve the system of the equations:  $ax + by + cz = d$ ,  
 $a^2x + b^2y + c^2z = d^2$ ,  $a^3x + b^3y + c^3z = d^3$ .



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3. consider the system of equations : Itbr.
- $$3x - y + 4z = 3$$
- $$x + 2y - 3z = -2$$
- $$6x + 5y + \lambda z = -3$$

Prove that system of equation has at least one solution for all real values of  $\lambda$ . also prove that infinite solutions of the system of equations satisfy

$$\frac{7x - 4}{-5} = \frac{7y + 9}{13} = z$$

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4. If the equation

$2x + 3y + 1 = 0, 3x + y - 2 = 0,$  and  $ax + 2y - b = 0$  are consistent, then prove that  $a - b = 2.$

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5. if  $x, y$  and  $z$  are not all zero and connected by the equations

$a_1x + b_1y + c_1z = 0, a_2x + b_2y + c_2z = 0$  and

$(p_1 + \lambda q_1)x + (p_2 + \lambda q_2)y + (p_3 + \lambda q_3)z = 0$  show that

$$\lambda = - \left| \begin{array}{ccc} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ p_1 & p_2 & p_3 \end{array} \right| \div \left| \begin{array}{ccc} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ q_1 & q_2 & q_3 \end{array} \right|$$

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## Single Correct Answer Type

1. if  $\theta \in R$  then maximum value of  $\Delta = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 1 + \sin \theta & 1 \\ 1 & 1 & 1 + \cos \theta \end{vmatrix}$  is

A.  $\sqrt{3}/2$ )

B.  $1/2$

C.  $1/\sqrt{2}$

D. None of these

**Answer: B**



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2. If  $p + q + r = a + b + c = 0$ , then the determinant  $\begin{vmatrix} pa & qb & rc \\ qc & ra & pb \\ rb & pc & qa \end{vmatrix}$  equals

A. 0

B.  $pa + qb + rc$

C. 1

D. none of these

**Answer: A**



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3. If  $\alpha, \beta, \gamma$  are the roots of  $px^3 + qx^2 + r = 0$ , then the value of the

determinant 
$$\begin{vmatrix} \alpha\beta & \beta\gamma & \gamma\alpha \\ \beta\gamma & \gamma\alpha & \alpha\beta \\ \gamma\alpha & \alpha\beta & \beta\gamma \end{vmatrix}$$
 is p b. q c. 0 d. r

A. p

B. q

C. 0

D. r

**Answer: C**



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4. If  $f(x) = a = bx + cx^2$  and  $\alpha, \beta, \gamma$  are the roots of the equation  $x^3 = 1$ , then  $|abcbcacab|$  is equal to  $f(\alpha) + f(\beta) + f(\gamma)$
- $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha)$   $f(\alpha)f(\beta)f(\gamma) - f(\alpha)f(\beta)f(\gamma)$
- A.  $f(\alpha) + f(\beta) + f(\gamma)$   
B.  $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha)$   
C.  $f(\alpha)f(\beta)f(\gamma)$   
D.  $-f(\alpha)f(\beta)f(\gamma)$

**Answer: D**



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5. If  $[ ]$  denotes the greatest integer less than or equal to the real number under consideration, and  $-1 \leq x < 0, 0 \leq y < 1, 1 \leq a < 2$ , then the value of the determinant  $|[x] + 1[y][z][x][y] + 1[z][x][y][z] + 1|$  is [x] b.  
[y] c. [z] d. none of these

A.  $[x]$

B.  $[y]$

C.  $[z]$

D. none of these

**Answer: C**



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6. if  $a = \cos 0 + i \sin 0$ ,  $b = \cos 20 - i \sin 20$ ,  $c = \cos 30 + i \sin 30$  and if

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0 \text{ then}$$

A.  $0 = 2k\pi, k \in Z$

B.  $0 = (2k + 1)\pi k \in Z$

C.  $0 = (4k + 1)\pi k \in Z$

D. none of these

**Answer: A**



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7. If  $\begin{vmatrix} x^n & x^{n+2} & x^{n+3} \\ y^n & y^{n+2} & y^{n+3} \\ z^n & z^{n+2} & z^{n+3} \end{vmatrix} = (x - y)(y - z)(z - x) \left( \frac{1}{x} + \frac{1}{y} + \frac{1}{z} \right)$ , then  $n$  equals a. 1 b. -1 c. 2 d. -2

A. 1

B. -1

C. 2

D. -2

**Answer: B**



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8. If the determinant  $\begin{vmatrix} \cos 2x & \sin^2 x & \cos 4x \\ \sin^2 x & \cos 2x & \cos^2 x \\ \cos 4x & \cos^2 x & \cos 2x \end{vmatrix}$  is expanded in powers of  $\sin x$ , then the constant term is

A. 1

B. 0

C. -1

D. 2

**Answer: C**



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9. If a determinant of order  $3 \times 3$  is formed by using the numbers 1 or -1

then minimum value of determinant is :

A. -2

B. -4

C. 0

D. -8

**Answer: B**



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10. If  $A, B, C$  are angles of a triangles, then the value of

$e^{2iA}e^{-iC}e^{-iB}e^{-iC}e^{2iB}e^{-iA}e^{-iB}e^{-iA}e^{2iC}$  is

- 1 b. -1 c. -2 d. -4

A. 1

B. -1

C. -2

D. -4

**Answer: D**



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11. If  $a, b, c$  are different, then the value of  $\begin{vmatrix} 0 & x^2 - a & x^3 - b \\ x^2 + a & 0 & x^2 + c \\ x^4 + b & x - c & 0 \end{vmatrix}$  is a.

b b. c c. b d. 0

A. a

B. c

C. b

D. 0

**Answer: D**



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12. if the value of the determinant  $\begin{vmatrix} a & 1 & 1 \\ 1 & b & 1 \\ 1 & 1 & c \end{vmatrix}$  is positivie then

$(a, b, c < 0)$

A.  $abc > 1$

B.  $abc > -8$

C.  $abc > -8$

D.  $abc > -2$

**Answer: B**



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13. if  $A_1, B_1, C_1 \dots$  are respectively the cofactors of the elements  $a_1, b_1, c_1 \dots$  of the determinant

$$\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}, \Delta \neq 0 \text{ then the value of } \begin{vmatrix} B_2 & C_2 \\ B_3 & C_3 \end{vmatrix} \text{ is equal to}$$

A.  $a_1^2 \Delta$

B.  $a_1 \Delta$

C.  $a_1 \Delta^2$

D.  $a_1^2 \Delta^2$

**Answer: B**



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14. If  $a, b, c, d, e, \text{ and } f$  are in G.P. then the value of  $|a^2d^2xb^2e^2yc^2f^2z|$

depends on  $x$  and  $y$  b.  $x$  and  $z$  c.  $y$  and  $z$  d. independent of  $x, y, \text{ and } z$

A.  $x$  and  $y$

B.  $x$  and  $z$

C.  $y$  and  $z$

D. independent of  $x, y$  and  $z$

**Answer: D**



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15. Let  $x < 1$ , then value of  $\begin{vmatrix} x^2 + 2 & 2x + 1 & 1 \\ 2x + 1 & x + 2 & 1 \\ 3 & 3 & 1 \end{vmatrix}$  is a. none-negative b.

none-positive c. negative d. positive

A. non-negative

B. non-positive

C. negative

D. positive

**Answer: C**



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16. The value of  $\begin{vmatrix} -1 & 2 & 1 \\ 3 + 2\sqrt{2} & 2 + 2\sqrt{2} & 1 \\ 3 - 2\sqrt{2} & 2 - 2\sqrt{2} & 1 \end{vmatrix}$  is equal to

A. 0

B.  $-16\sqrt{2}$

C.  $-8\sqrt{2}$

D. none of these

**Answer: B**



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17. Let  $\{D_1, D_2, D_3, D_n\}$  be the set of third order determinant that can be made with the distinct non-zero real numbers  $a_1, a_2, a_q$ . Then

$$\sum_{i=1}^n D_i = 1 \text{ b. } \sum_{i=1}^n D_i = 0 \text{ c. } D_i = D_j, \forall i, j \text{ d. none of these}$$

A.  $\sum_{i=1}^n D_i = 1$

B.  $\sum_{i=1}^n D_i = 0$

C.  $D_i D_j, \forall I, j$

D. None of these

**Answer: B**



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18. if w is a complex cube root to unity then value of

$$\Delta = \begin{vmatrix} a_1 + b_1w & a_1w^2 + b_1 & c_1 + b_1\bar{w} \\ a_2 + b_2w & a_2w^2 + b_2 & c_2 + b_2\bar{w} \\ a_3 + b_3w & a_3w^2 + b_3 & c_3 + b_3\bar{w} \end{vmatrix} \text{ is}$$

A. 0

B. -1

C. 2

D. none of these

**Answer: A**



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**19.** If  $a + b + c = 0$ , one root of  $|a - xcbcb - xabac - x| = 0$  is  $x = 1$

b.  $x = 2$  c.  $x = a^2 + b^2 + c^2$  d.  $x = 0$

A.  $x = 1$

B.  $x = 2$

C.  $x = a^2 + b^2 + c^2$

D.  $x = 0$

**Answer: D**



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20. If  $x, y, z$  are in A.P., then the values of the determinant

$$\begin{vmatrix} a+2 & a+3 & a+2y \\ a+3 & a+4 & a+2y \\ a+4 & a+5 & a+2z \end{vmatrix}, \text{ is}$$

A. 1

B. 0

C.  $2a$

D.  $a$

**Answer: B**



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21. If  $a_1, a_2, a_3, \dots$  are in G.P. then the value of determinant

$$\begin{vmatrix} \log(a_n) & \log(a_{n+1}) & \log(a_{n+2}) \\ \log(a_{n+3}) & \log(a_{n+4}) & \log(a_{n+5}) \\ \log(a_{n+6}) & \log(a_{n+7}) & \log(a_{n+8}) \end{vmatrix} \text{ equals (A) 0 (B) 1 (C) 2 (D) 3}$$

A. 1

B. 0

C. 2a

D. a

**Answer: B**



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**22.** Value of  $|x + yzzxy + zxyyz + x|$ , where  $x, y, z$  are nonzero real number, is equal to  
a.  $xyz$  b.  $2xyz$  c.  $3xyz$  d.  $4xyz$

A.  $xyz$

B.  $2xyz$

C.  $3xyz$

D.  $4xyz$

**Answer: D**



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23. Which of the following is not the root of the equation

$$|x - 6 - 12 - 3x - 3 - 32x + 2| = 0?$$

A. 2

B. 0

C. 1

D. -3

**Answer: B**



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24. The value of the determinant  $|kak^2 + a^2 1kbk^2 + b^2 1kck^2 + c^2 1|$  is

$$k(a+b)(b+c)(c+a) - kabc(a^2 + b^2 + c^2) - k(a-b)(b-c)(c-a)$$
$$k(a+b-c)(b+c-a)(c+a-b)$$

A.  $k(a+b)(b+c)(c+a)$

B.  $kabc(a^2 + b^2 + c^2)$

C.  $k(a - b)(b - c)(c - a)$

D.  $k(a + b - c)(b + c - a)(c + a - b)$

**Answer: C**



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25. If  $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = (a - b)(b - c)(c - a)(a + b + c)$

where  $a, b, c$  are all different, then the determinant

$$\begin{vmatrix} 1 & 1 & 1 \\ (x - a)^2 & (x - b)^2 & (x - c)^2 \\ (x - b)(x - c) & (x - c)(x - a) & (x - a)(x - b) \end{vmatrix} \text{ vanishes when}$$

A.  $a + b + c = 0$

B.  $x = \frac{1}{3}(a + b + c)$

C.  $x = \frac{1}{2}(a + b + c)$

D.  $x = a + b + c$

**Answer: B**



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26. If  $f'(x) = \begin{vmatrix} mx & mx - p & mx + p \\ n & n + p & n - p \\ mx + 2n & mx + 2n + p & mx + 2n - p \end{vmatrix}$ , then

$y = f(x)$  represents a.

- a straight line parallel to x-axis
- b. a straight line parallel to y-axis
- c. parabola
- d. a straight line with negative slope

A. a straight line parallel to x-axis

B. a straight line parallel to y-axis

C. parabola

D. a straight line with negative slope

**Answer: B**



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27. if  $\begin{vmatrix} x & 3 & 6 \\ 3 & 6 & x \\ 6 & x & 3 \end{vmatrix} = \begin{vmatrix} 2 & x & 7 \\ x & 7 & 2 \\ 7 & 2 & x \end{vmatrix} = \begin{vmatrix} 4 & 5 & x \\ 5 & x & 4 \\ x & 4 & 5 \end{vmatrix} = 0$  then x is equal to

A. 0

B. -9

C. 3

D. none of these

**Answer: B**



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28. If  $\begin{vmatrix} x^n & x^{n+2} & x^{2n} \\ 1 & x^a & a \\ x^{n+5} & x^{a+6} & x^{2n+5} \end{vmatrix} = 0, \forall x \in R, \text{ where } n \in N,$  then value of  $a$  is

a.  $n$  b.  $n - 1$  c.  $n + 1$  d. none of these

A. n

B. n-1

C.  $n+1$

D. none of these

**Answer: C**



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29. for the equation  $\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = 0$

A. There are exactly two distinct roots

B. there is one pair of equation real roots

C. There are three pairs of equal roots

D. Modulus of each root is 2

**Answer: C**



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**30.**

If

$$a^2 + b^2 + c^2 = -2 \text{ and } f(x) =$$

$|1 + a^2x(1 + b^2)x(1 + c^2)x(1 + a^2)x| + b^2x(1 + c^2)x(1 + a^2)x(1 + b^2)x$ , then  $f(x)$  is a polynomial of degree

- a. 0  
b. 1  
c. 2  
d. 3

A. 0

B. 1

C. 2

D. 3

**Answer: C**



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**31.** The value of the determinant  $\begin{vmatrix} 1 & 1 & 1 \\ .^m C_1 & .^{m+1} C_1 & .^{m+2} C_1 \\ .^m C_2 & .^{m+1} C_2 & .^{m+2} C_2 \end{vmatrix}$  is equal to

A. 1

B. -1

C. 0

D. none of these

**Answer: A**



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**32. the value of the determinant**

$$\begin{vmatrix} .^n C_{r-1} & .^n C_r & (r+1)^{n+2} C_{r+1} \\ .^n C_r & .^n C_{r+1} & (r+2)^{n+2} C_{r+2} \\ .^n C_{r+1} & .^n C_{r+2} & (r+3)^{n+2} C_{r+3} \end{vmatrix} \text{ is}$$

A.  $n^2 + n - 1$ )

B. 0

C.  $.^{n+3} C_{r+3}$

D.  $.^n C_{r-1} + ^n C_r + ^n C_{r+1}$

**Answer: B**



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**33.** if  $f(x) = \begin{vmatrix} x & a & a \\ a & x & a \\ a & a & x \end{vmatrix} = 0$  then

- A.  $f(x) = 0$  and  $f(x) = 0$  has one common root
- B.  $f(x) = 0$  and  $f(x) = 0$  has one common root
- C. sum of roots of  $f(x) = 0$  is  $-3a$
- D. none of these

**Answer:** B



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**34.** If  $x \neq y \neq z$  and  $\begin{vmatrix} x & x^2 & 1+x^3 \\ y & y^2 & 1+y^3 \\ z & z^2 & 1+z^3 \end{vmatrix} = 0$ , then  $xyz =$

A. 1

B. 2

C. -1

D. -2

**Answer: C**



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**35.** if  $x \neq 0, y \neq 0, z \neq 0$  and  $\begin{vmatrix} 1+x & 1 & 1 \\ 1+y & 1+2y & 1 \\ 1+z & 1+z & 1+3z \end{vmatrix} = 0$  then  $x^{-1} + y^{-1} + z^{-1}$  is equal to

A. -1

B. -2

C. -3

D. none of these

**Answer: C**



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**36.** if  $a_1b_1c_1$ ,  $a_2b_2c_2$  and  $a_3b_3c_3$  are three-digit even natural numbers

and  $\Delta = \begin{vmatrix} c_1 & a_1 & b_1 \\ c_2 & a_2 & b_2 \\ c_3 & a_3 & b_3 \end{vmatrix}$  then  $\Delta$  is

A. divisible by 2 but not necessarily by 4

B. divisible by 4 but not necessarily by 8

C. divisible by 8

D. none of these

**Answer:** A



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**37.** if  $\begin{vmatrix} b+c & c+a & a+b \\ a+b & b+c & c+a \\ c+a & a+b & b+c \end{vmatrix} = k \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$  then the value of

k is

A. 1

B. 2

C. 3

D. 4

**Answer: B**



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38. suppose  $D = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$  and

$$D' = \begin{vmatrix} a_1 + pb_1 & b_1 + qc_1 & c_1 + ra_1 \\ a_2 + pb_2 & b_2 + qc_2 & c_2 + ra_2 \\ a_3 + pb_3 & b_3 + qc_3 & c_3 + ra_3 \end{vmatrix}. \text{ Then}$$

A.  $D' = D$

B.  $D' = D(1 - pqr)$

C.  $D = D(1 + p + q + r)$

D.  $D' = D(1 + pqr)$

**Answer: D**



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39. The value of the determinant

$$\begin{vmatrix} \log_a\left(\frac{x}{y}\right) & \log_a\left(\frac{y}{z}\right) & \log_a\left(\frac{z}{x}\right) \\ \log_b\left(\frac{y}{z}\right) & \log_b\left(\frac{z}{x}\right) & \log_b\left(\frac{x}{y}\right) \\ \log_c\left(\frac{z}{x}\right) & \log_c\left(\frac{x}{y}\right) & \log_c\left(\frac{y}{z}\right) \end{vmatrix}$$

A. 1

B. -1

C. 0

D.  $\frac{1}{6} \log_a xyz$

**Answer: C**



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40. If  $a > 0, b > 0, c > 0$  are respectively the pth, qth, rth terms of a G.P., then the value of the determinant

$$\begin{vmatrix} \log a & p & 1 \\ \log b & q & 1 \\ \log c & r & 1 \end{vmatrix}, \text{ is}$$

A. 0

B.  $\log(abc)$

C.  $-(p+q+r)$

D. none of these

**Answer: A**



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41. If  $a > 0$  and discriminant of  $ax^2 + 2bx + c$  is negative, then

$$\Delta = \begin{vmatrix} a & b & ax+b \\ b & c & bx+c \\ ax+b & bx+c & 0 \end{vmatrix} \text{ is}$$

a.  $+ve$

b.  $(ac - b)^2(ax^2 + 2bx + c)$

c.  $-ve$

d. 0

A.  $+ve$

B.  $(ac - b)^2(ax^2 + 2bx + c)$

C.  $-ve$

D. 0

**Answer: C**



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42. The number of distinct real roots of  $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$  in the interval  $-\frac{\pi}{4} \leq x \leq \frac{\pi}{4}$  is

A. 0

B. 2

C. 1

D. 3

**Answer: C**



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43.

if

$$D_k = \begin{vmatrix} 1 & n & n \\ 2k & n^2 + n + 1 & n^2 + n \\ 2k - 1 & n^2 & n^2 + n + 1 \end{vmatrix} \text{ and } \sum_{k=1}^n D_k = 56$$

then n equals

A. 4

B. 6

C. 8

D. 7

Answer: D



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44. the value of  $\sum_{r=2}^n (-2)^r \begin{vmatrix} n-2 C_{r-2} & n-2 C_{r-1} & n-2 C_r \\ -3 & 1 & 1 \\ 2 & -1 & 0 \end{vmatrix}$  ( $n > 2$ )

A.  $2n - 1 + (-1)^n$

B.  $2n + 1 + (-1)^{n-1}$

C.  $2n - 3 + (-1)^n$

D. none of these

**Answer: A**



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45. if  $\Delta = \begin{vmatrix} 3 & 4 & 5 & x \\ 4 & 5 & 6 & y \\ 5 & 6 & 7 & z \\ x & y & z & 0 \end{vmatrix} = 0$  then

A.  $x, y, z$  are in A.P.

B.  $x, y, z$  are in G.P

C.  $x, y, z$  are in H.P

D. none of these

**Answer: A**



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**46.** Roots of the equations  $\begin{vmatrix} x & m & n & 1 \\ a & x & n & 1 \\ a & b & x & 1 \\ a & b & c & 1 \end{vmatrix} = 0$  are

- A. independent of m and n
- B. independent of a,b and c
- C. depend on m,n and a,b,c
- D. inedependent of m,n and a,b,c

**Answer:** A



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**47.** If  $x, y, z$  are different from zero and

$$\text{Delta} = \begin{vmatrix} a & b-y & c-z \\ a-x & b & c-z \\ a-x & b-y & c \end{vmatrix} = 0, \text{ then the value of the expression } \frac{a}{x} + \frac{b}{y} + \frac{c}{z} \text{ is a. 0 b. -1 c. 1 d. 2}$$

- A. 0

B. -1

C. 1

D. 2

**Answer: D**



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**48. about to only mathematics**

A. 0

B. 3

C. 6

D. 12

**Answer: B**



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49. In triangle ABC, if

$$\begin{vmatrix} 1 & 1 & 1 \\ \cot\left(\frac{A}{2}\right) & \cot\left(\frac{B}{2}\right) & \cot\left(\frac{C}{2}\right) \\ \tan\left(\frac{B}{2}\right) + \tan\left(\frac{C}{2}\right) & \tan\left(\frac{C}{2}\right) + \tan\left(\frac{A}{2}\right) & \tan\left(\frac{A}{2}\right) + \tan\left(\frac{B}{2}\right) \end{vmatrix} \text{ then}$$

the triangle must be (A) Equilateral (B) Isoceless (C) Right Angle (D) none of these

A. equilateral

B. isosceles

C. obtuse angled

D. none of these

**Answer: B**



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50. If  $\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & a + b & c \end{vmatrix} = 0$ , then the line  $ax + by + c = 0$  passes through the fixed point which is

A. (1, 2)

B. (1, 1)

C. (- 2, 1)

D. (1, 0)

**Answer: B**



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51. The determinant  $\begin{vmatrix} y^2 & -xy & x^2 \\ a & b & c \\ a' & b' & c' \end{vmatrix}$  is equal to

A. (a)  $\begin{vmatrix} bx + ay & cx + by \\ b'x + a'y & c'x + b'y \end{vmatrix}$

B. (b)  $\begin{vmatrix} ax + by & bx + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$

C. (c)  $\begin{vmatrix} bx + cy & ax + by \\ b'x + c'y & a'x + b'y \end{vmatrix}$

D. (d)  $\begin{vmatrix} ax + by & bc + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$

**Answer: D**

52. Let  $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$ ,  $r = 1, 2, 3$  three mutually perpendicular

unit vectors then the value of  $\begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$  is equal to

- A. zero
- B.  $\pm 1$
- C.  $\pm 2$
- D. none of these

**Answer: B**



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53. Let

$$\begin{vmatrix} y^5 z^6 (z^3 - y^3) & x^4 z^6 (x^3 - z^3) & x^4 y^5 (y^3 - x^3) \\ y^2 z^3 (y^6 - z^6) & x z^3 (z^6 - x^6) & x y^2 (x^6 - y^6) \\ y^2 \wedge (3) (z^3 - y^3) & x z^3 (x^3 - z^3) & x y^2 (y^3 - x^3) \end{vmatrix} \text{ and } \Delta_2 = \begin{vmatrix} x \\ x^4 \\ x^7 \end{vmatrix}$$

.Then  $\Delta_1 \Delta_2$  is equal to

A.  $\Delta_2^6$

B.  $\Delta_2^4$

C.  $\Delta_2^3$

D.  $\Delta_2^2$

**Answer: C**



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**54.** the value of the determinant

$$\begin{vmatrix} (a_1 - b_1)^2 & (a_1 - b_2)^2 & (a_1 - b_3)^2 & (a_1 - b_4)^2 \\ (a_2 - b_1)^2 & (a_2 - b_2)^2 & (a_2 - b_3)^2 & (a_2 - b_4)^2 \\ (a_3 - b_1)^2 & (a_3 - b_2)^2 & (a_3 - b_3)^2 & (a_3 - b_4)^2 \\ (a_4 - b_1)^2 & (a_4 - b_2)^2 & (a_4 - b_3)^2 & (a_4 - b_4)^2 \end{vmatrix} \text{ is}$$

A. dependant on  $a_i$ ,  $i = 1, 2, 3, 4$

B. dependant on  $b_i$ ,  $i = 1, 2, 3, 4$

C. dependant on  $a_{ij}$ ,  $b_i$ ,  $i = 1, 2, 3, 4$

**Answer: D****Watch Video Solution**

55. if  $\Delta(x) = \begin{vmatrix} \tan x & \tan(x+h) & \tan(x+2h) \\ \tan(x+2h) & \tan x & \tan(x+h) \\ \tan(x+h) & \tan(x+2h) & \tan x \end{vmatrix}$ , then

The value of  $\lim_{h \rightarrow 0} \cdot \left( \frac{\Delta(\pi/3)}{(\sqrt{3})h^2} \right)$  is

A. 144

B. 216

C. 64

D. 36

**Answer: A****Watch Video Solution**

56. Value of  $\begin{vmatrix} 1+x_1 & 1+x_1x & 1+x_1x^2 \\ 1+x_2 & 1+x_2x & 1+x_2x^2 \\ 1+x_3 & 1+x_3x & 1+x_3x^2 \end{vmatrix}$  depends upon

- A. x only
- B.  $x_1$  only
- C.  $x_2$  only
- D. none of these

**Answer: D**



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57. If  $\begin{vmatrix} a^2 + \lambda^2 & ab + c\lambda & ca - b\lambda \\ ab - c\lambda & b^2 + \lambda^2 & bc + a\lambda \\ ca + b\lambda & bc - a\lambda & c^2 + \lambda^2 \end{vmatrix} \begin{vmatrix} \lambda & c & -b \\ -c & \lambda & a \\ b & -a & \lambda \end{vmatrix} = (1 + a^2 + b^2 + c^2)^3$

, then the value of  $\lambda$  is a. 8 b. 27 c. 1 d. -1

A. 8

B. 27

C. 1

D. -1

**Answer: C**



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58. Let  $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = Ax^4 + Bx^3 + Cx^2 + Dx + E$ . Then the value of  $5A + 4B + 3C + 2D + E$  is equal to a. zero b. -16 c. 11 d. -11

A. zero

B. -16

C. 16

D. -11

**Answer: D**



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59. If  $\Delta_1 = \begin{vmatrix} x & b & b \\ a & x & b \\ a & a & x \end{vmatrix}$  and  $\Delta_2 = \begin{vmatrix} x & b \\ a & x \end{vmatrix}$  are the given determinants then

- A.  $\Delta_1 = 3(\Delta_2)^2$
- B.  $\frac{d}{dx}(\Delta_1) = 3\Delta_2$
- C.  $\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$
- D.  $\Delta_1 = 3\Delta_2^{3/2}$

**Answer: B**



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60. if  $y = \sin mx$ , then the value of the determinant

$$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_8 \end{vmatrix} \quad \text{Where } y_n = \frac{d^n y}{dx^n} \text{ is}$$

A.  $m^9$

B.  $m^2$

C.  $m^3$

D. 0

**Answer: D**



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61. Let  $f(x) = \begin{vmatrix} 2\cos^2 x & \sin 2x & -\sin x \\ \sin 2x & 2\sin^2 x & \cos x \\ \sin x & -\cos x & 0 \end{vmatrix}$ , then the value of  $\int_0^{\pi/2} \{f(x) + f'(x)\} dx$  is

A.  $\pi$

B.  $\pi/2$

C.  $2\pi$

D.  $3\pi/2$

**Answer: A**



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62.  $a, b, c$  are distinct real numbers not equal to one. If  $ax + y + z = 0, x + by + z = 0$ , and  $x + y + cz = 0$  have nontrivial solution, then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  is equal to  
a. 1 b. -1  
c. zero d. none of these

A. -1

B. 1

C. zero

D. none of these

**Answer: B**



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63. If the system of linear equation  $x + y + z = 6, x + 2y + 3z = 14$ , and  $2x + 5y + \lambda z = \mu(\lambda, \mu R)$  has a unique solution, then

A.  $\lambda \neq 8$

B.  $\lambda = 8, \mu \neq 36$

C.  $\lambda = 8, \mu = 36$

D. none of these

**Answer: A**



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**64.** If  $\alpha, \beta, \gamma$  are the angles of a triangle and system of equations

$$\cos(\alpha - \beta)x + \cos(\beta - \gamma)y + \cos(\gamma - \alpha)z = 0$$

$$\cos(\alpha + \beta)x + \cos(\beta + \gamma)y + \cos(\gamma + \alpha)z = 0$$

$\sin(\alpha + \beta)x + \sin(\beta + \gamma)y + \sin(\gamma + \alpha)z = 0$  has non-trivial solutions,

then triangle is necessarily a. equilateral b. isosceles c. right angled d.

acute angled

A. equiliateral

B. isosocleles

C. right angled

D. acute angled

**Answer: B**



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**65.**

Given

$a = x/(y - z)$ ,  $b = y/(z - x)$ , and  $c = z/(x - y)$ , where  $x, y$  and  $z$  are not all zero, then the value of  $ab + bc + ca$  is

a. 0 b. 1 c. -1 d. none of these

A. 0

B. 1

C. -1

D. none of these

**Answer: C**



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66. If  $pqr \neq 0$  and the system of equation  $(p+a)x + by + cz = 0$ ,  $ax + (q+b)y + cz = 0$ ,  $ac + by + (r+c)z = 0$  has nontrivial solution, then value of  $\frac{a}{p} + \frac{b}{q} + \frac{c}{r}$  is  
a. -1 b. 0 c. 0 d. -2

A. -1

B. 0

C. 1

D. 2

**Answer: A**



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67. The value of  $|\alpha|$  for which the system of equation  $\alpha x + y + z = \alpha - 1$ ,  $x + \alpha y + z = \alpha - 1$ ,  $x + y + \alpha z = \alpha - 1$  has no solutions, is \_\_\_\_\_.

A. either -2 or 1

B. -2

C. 1

D. not-2

**Answer: B**



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**68.** the set of equations  $\lambda x - y + (\cos \theta)z = 0$ ,  $3x + y + 2z = 0$

$(\cos \theta)x + y + 2z = 0$ ,  $0 \leq \theta < 2\pi$  has non-trivial solution (s)

A. for no value of  $\lambda$  and 0

B. for all values of  $\lambda$  and 0

C. for all values of  $\lambda$  and only tow values of 0

D. for only one value of  $\lambda$  and all values of 0

**Answer: A**



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69. If  $c < 1$  and the system of equations  $x + y - 1 = 0$ ,  $2x - y - c = 0$ , and  $-bx + 3by - c = 0$  is consistent, then the possible real values of  $b$  are

- A.  $b \in \left( -3, \frac{3}{4} \right)$
- B.  $b \in \left( -\frac{3}{2}, 4 \right)$
- C.  $b \in \left( -\frac{3}{4}, 3 \right)$
- D. none of these

Answer: C



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70. If  $a, b, c$  are in G.P. with common ratio  $r_1$  and  $\alpha, \beta, \gamma$  are in G.P. with common ratio  $r_2$  and equations

$ax + \alpha y + z = 0$ ,  $bx + \beta y + z = 0$ ,  $cx + \gamma y + z = 0$  have only zero solution, then which of the following is not true?

- A.  $r_1 \neq 1$
- B.  $r_2 \neq 1$
- C.  $r_1 \neq r_2$
- D. none of these

**Answer: D**



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**71.** if the system of equations

$$(a - t)x + by + cz = 0$$

$$bx + (c - t)y + az = 0$$

$$cx + ay + (b - t)z = 0$$

has non-trivial solutions then product of all possible values of t is

A.  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$

B.  $a + b + c$

C.  $a^2 + b^2 + c^2$

D. 1

**Answer: A**



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72. Let  $\lambda$  and  $\alpha$  be real. Then the numbers of intergral values  $\lambda$  for which the system of linear equations

$$\lambda x + (\sin \alpha)y + (\cos \alpha)z = 0$$

$$x + (\cos \alpha)y + (\sin \alpha)z = 0$$

$-x + (\sin \alpha)y - (\cos \alpha)z = 0$  has non-trivial solutions is

A. 0

B. 1

C. 2

D. 3

**Answer: D**



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**Multiple Correct Answers Type**

1. Which of the following has / have value equal to zero ?

- A. 
$$\begin{vmatrix} 8 & 2 & 7 \\ 12 & 3 & 5 \\ 16 & 4 & 3 \end{vmatrix}$$
- B. 
$$\begin{vmatrix} 1/a & a^2 & bc \\ 1/b & b^2 & ac \\ 1/c & c^2 & ab \end{vmatrix}$$
- C. 
$$\begin{vmatrix} a+b & 2a+b & 3a+b \\ 2a+b & 3a+b & 4a+b \\ 4a+b & 5a+b & 6a+b \end{vmatrix}$$
- D. 
$$\begin{vmatrix} 2 & 43 & 6 \\ 7 & 35 & 4 \\ 3 & 17 & 2 \end{vmatrix}$$

**Answer: A::B::C**



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2. If  $f(\alpha, \beta) = \begin{vmatrix} \cos \alpha & -\sin \alpha & 1 \\ \sin \alpha & \cos \alpha & 1 \\ \cos(\alpha + \beta) & -\sin(\alpha + \beta) & 1 \end{vmatrix}$ , then

A.  $f(300,200)=f(400,200)$

B.  $f(200,400)=f(200,600)$

C.  $f(100,200)=f(200,200)$

D. none of these

**Answer: A::C**



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3. if  $f(0) = \begin{vmatrix} \sin 0 & \cos 0 & \sin 0 \\ \cos 0 & \sin 0 & \cos 0 \\ \cos 0 & \sin 0 & \sin 0 \end{vmatrix}$  then

A.  $f(0)=0$  has exactly 2 real solutions in  $[0, \pi]$

B.  $f(0)=0$  has exactly 3 real solutions in  $[0, \pi]$

C. range of function  $\frac{f(0)}{1 - \sin 20}$  is  $[-\sqrt{2}, \sqrt{2}]$

D. range of function  $\frac{f(0)}{\sin 20 - 1}$  is  $[-3, 3]$  is  $[-3, 3]$

**Answer: A::C**



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4. If  $f(x) = \begin{vmatrix} a & -1 & 0 \\ ax & a & -1 \\ ax^2 & ax & a \end{vmatrix}$ , then  $f(2x) - f(x)$  is divisible by

- 1)  $a$
- 2)  $b$
- 3)  $c, d, e$
- 4). none of these

A.  $x$

B.  $a$

C.  $2a + 3x$

D.  $x^2$

**Answer: A::B::C**



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5.  $\Delta = \begin{vmatrix} 1 & 1+ac & 1+bc \\ 1 & 1+ad & 1+bd \\ 1 & 1+ae & 1+be \end{vmatrix}$  is independent of

A. a

B. b

C. c,d,e

D. none of these

**Answer: A::B::C**



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6. if  $\Delta = \begin{vmatrix} -x & a & b \\ b & -x & a \\ a & b & -x \end{vmatrix}$  then a factor of  $\Delta$  is

A.  $a + b + x$

B.  $x^2 - (a - b)x + a^2 + b^2 + ab$

C.  $x^2 + (a+b)x + a^2 + b^2 - ab$

D.  $a + b - x$

**Answer: C::D**



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7. the determinant  $\Delta = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$  is divisible by

A. x

B.  $x^2$

C.  $x^3$

D. none of these

**Answer: A::B**



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8.  $\begin{vmatrix} a & a^2 & 0 \\ 1 & 2a+b & (a+b) \\ 0 & 1 & 2a+3b \end{vmatrix}$  is divisible by

a.  $a + b$

b.  $a + 2b$

c.  $2a + 3b$

d.  $a^2$

A.  $a + b$

B.  $a + 2b$

C.  $2a + 3b$

D.  $a^2$

**Answer: A**



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9. the roots of the equations  $\begin{vmatrix} .^x C_r & .^{n-1} C_r & .^n C_r \\ .^{x+1} C_r & .^n C_r & .^{n+1} C_r \\ .^{x+2} C_r & .^{n+1} C_r & .^{n+2} C_r \end{vmatrix} = 0$

A.  $x = n$

B.  $x = n + 1$

C.  $x = n - 1$

D.  $x = n - 2$

**Answer: A::C**



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10. If  $f(x) = \begin{vmatrix} 3 & 3x & 3x^2 + 2a^2 \\ 3x & 3x^2 + 2a^2 & 3x^3 + 6a^2x \\ 3x^2 + 2a^2 & 3x^3 + 6a^2x & 3x^4 + 12a^2x^2 + 2a^4 \end{vmatrix}$

then

A.  $f'(x)=0$

B.  $y=f(x)$  is a straight line parallel to x-axis

C.  $\int_0^2 f(x)dx = 32a^4$

D. none of these

**Answer: A::B**



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11. Let  $f(n) = \begin{vmatrix} n & n+1 & n+2 \\ .^n P_n & .^{n+1} P_{n+1} & .^{n+2} P_{n+2} \\ .^n C_n & .^{n+1} C_{n+1} & .^{n+2} C_{n+2} \end{vmatrix}$  where the symbols have their usual meanings .then  $f(n)$  is divisible by

A.  $n^2 + n + 1$

B.  $(n + 1)!$

C.  $n!$

D. none of these

**Answer: A::C**



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12. the determinant  $\begin{vmatrix} a & b & a\alpha + b \\ b & c & b\alpha + c \\ a\alpha + b & b\alpha + c & 0 \end{vmatrix} = 0$  is equal to zero if

- A. a,b,c are in A.P
- B. a,b,c are in G.P.
- C.  $\alpha$  is a root of the equation  $ax^2 + bx + c = 0$
- D.  $(x - \alpha)$  is a factor of  $ax^2 + 2bx + c$

**Answer: B::D**



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13. if  $\begin{vmatrix} \sin x & \sin y & \sin z \\ \cos x & \cos y & \cos z \\ \cos^3 x & \cos^3 y & \cos^3 z \end{vmatrix} = 0$  then which of the following is / are possible ?

- A.  $x = y$
- B.  $y = z$

C.  $x = z$

D.  $x + y + z = \pi/2$

**Answer: A::B::C::D**



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14. If  $\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = xA + B$  then find A and B

A.  $\begin{vmatrix} 1 & 1 & 1 \\ -1 & -3 & 3 \\ 4 & 0 & 0 \\ 0 & 1 & 2 \end{vmatrix}$

B.  $\begin{vmatrix} 1 & -2 & 3 \\ -4 & 0 & 0 \end{vmatrix}$

C.  $\begin{vmatrix} 1 & 1 & -2 \\ -3 & -2 & 3 \\ 4 & 0 & 1 \\ 0 & 1 & -2 \end{vmatrix}$

D.  $\begin{vmatrix} -1 & -3 & 3 \\ 4 & 0 & 0 \end{vmatrix}$

**Answer: A::D**



15. if  $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc & ca & ab \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix}$  where a,b,c are distinct positive reals then the possible values of abc is / are

A.  $\frac{1}{18}$

B.  $\frac{1}{63}$

C.  $\frac{1}{27}$

D.  $\frac{1}{9}$

**Answer: A::B**



16.  $\begin{vmatrix} .^x C_r & .^x C_{r+1} & .^x C_{r+2} \\ .^y C_r & .^y C_{r+1} & .^y C_{r+2} \\ .^z C_r & .^z C_{r+1} & .^z C_{r+2} \end{vmatrix}$  is equal to



17. If  $\begin{vmatrix} \sin \theta \cos \phi & \sin \theta \sin \phi & \cos \theta \\ \cos \theta \cos \phi & \cos \theta \sin \phi & -\sin \theta \\ -\sin \theta \sin \phi & \sin \theta \cos \phi & \theta \end{vmatrix}$  then

A.  $\Delta$  is independent of theta

B.  $\Delta$  is independent of  $\phi$

C.  $\Delta$  is a constant

D.  $\left[ \frac{d\Delta}{d}(\theta) \right]_{\theta=\pi/2} = 0$

**Answer: B::D**



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18. If  $f(\theta) = |\sin^2 A \cot A + \sin^2 B \cot B + \sin^2 C \cot C|$ , then  
 $\tan A + \tan B + \tan C = \cot A \cot B \cot C \sin^2 A + \sin^2 B + \sin^2 C$

A.  $\tan A + \tan B + \tan C$

B.  $\cot A \cot B \cot C$

C.  $\sin^2 A + \sin^2 B + \sin^2 C$

D. 0

**Answer: D**



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19. if determinant  $\begin{vmatrix} \cos(\theta + \phi) & -\sin(\theta + \phi) & \cos 2\phi \\ \sin \theta & \cos \theta & \sin \phi \\ -\cos \theta & \sin \theta & \cos \phi \end{vmatrix}$  is

- A. non-negative
- B. independent of theta
- C. independent of  $\phi$
- D. none of these

**Answer: A::B**



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20. If  $g(x) = \begin{vmatrix} a^{-x} & e^{x \log_e a} & x^2 \\ a^{-3x} & e^{3x \log_e a} & x^4 \\ a^{-5x} & e^{5x \log_e a} & 1 \end{vmatrix}$  then

A. graphs of  $g(x)$  is symmetrical about the origin

B. graphs of  $g(x)$  is symmetrical about the y-axis

C.  $\frac{d^4 g(x)}{dx^4} \Big|_{x=0} = 0$

D.  $f(x) = g(x) \times \log_e \left( \frac{a-x}{a+x} \right)$  is an odd function

**Answer: A::C**



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21.

If

$$(x) = \left| [x^2 + 4x - 32x + 413] [2x^2 + 5x - 94x + 526] [8x^2 - 6x + 116x - 108] \right|$$

then a = 3 b = 0 c. c = 0 d. none of these

A.  $a = 3$

B.  $b = 0$

C.  $c = 0$

D. None of these

**Answer: B::C**



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22. if 
$$\begin{vmatrix} yz - x^2 & zx - y^2 & xy - z^2 \\ xz - y^2 & xy - z^2 & yz - x^2 \\ xy - z^2 & yz - x^2 & zx - y^2 \end{vmatrix} = \begin{vmatrix} r^2 & u^2 & u^2 \\ u^2 & r^2 & u^2 \\ u^2 & u^2 & r^2 \end{vmatrix}$$
 then

A.  $r^2 = x + y + z$

B.  $r^2 = x^2 = y^2 + z^2$

C.  $u^2 = yz + zx + xy$

D.  $u^2 = xyz$

**Answer: B::C**



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23. which of the following is / are true for

$$\Delta = \begin{vmatrix} a^2 & 1 & a+c \\ 0 & b^2 + 1 & b+c \\ 0 & b+c & c^2 + 1 \end{vmatrix} ?$$

A.  $\Delta \geq 0$  for real values of a,b,c

B.  $\Delta \leq 0$  for real values of a,b,c

C.  $\Delta = \begin{vmatrix} bc - 1 & 0 & 0 \\ 1 & ac & -a \\ -b & -a & ab \end{vmatrix}$

D.  $\Delta = 0$  if  $bc = 1$  where a,b,c are non-zero

**Answer: A::C::D**



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24. The values of  $k \in R$  for which the system of equations  $x + ky + 3z = 0, kx + 2y + 2z = 0, 2x + 3y + 4z = 0$  admits of nontrivial solution is  
a. 2 b.  $5/2$  c. 3 d.  $5/4$

A. 2

B.  $5/2$

C. 3

D.  $5/4$

**Answer: A::B**



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25. The system of equations  $-2x + y + z = a$   $x - 2y + z = b$   $x + y - 2z = c$  has

A. no solution if  $a + b + c \neq 0$

B. unique solution if  $a + b + c = 0$

C. infinite number of solutions if  $a + b + c = 0$

D. None of these

**Answer: A::C**



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26. Let  $\alpha, \beta$  and  $\gamma$  be the roots of the equations  $x^3 + ax^2 + bx + c = 0$ , ( $a \neq 0$ ). If the system of equations  $\alpha x + \beta y + \gamma z = 0$  and  $\beta x + \gamma y + \alpha z = 0$  and  $\gamma x = \alpha y + \beta z = 0$  has non-trivial solution then

A.  $a^2 = 3b$

B.  $a^3 = 27c$

C.  $b^3 = 27c^2$

D.  $\alpha + \beta + \gamma = 0$

**Answer: A::B::C**



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**Linked Comprehension Type**

1. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

In which of the following interval  $f(x)$  is strictly increasing

- A.  $f(x) = 0$  and  $f'(x) = 0$  have one positive common root
- B.  $f(x) = 0$  and  $f'(x) = 0$  have one negative common root
- C.  $f(x) = 0$  and  $f'(x) = 0$  have no common root
- D. None of these

**Answer: D**



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2. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

In which of the following interval  $f(x)$  is strictly increasing

- A.  $f(x)$  has one +ve point of maxima.
- B.  $f(x)$  has one -ve point of minima

C.  $f(x)=0$  has three distinct roots

D. Local minimum value of  $f(x)$  is zero

**Answer: D**



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3. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

In which of the following interval  $f(x)$  is strictly increasing

A.  $(-\infty, \infty)$

B.  $(-\infty, 0)$

C.  $(0, \infty)$

D. None of these

**Answer: C**



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4. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

if  $\Delta = 27$  and  $a^2 + b^2 + c^2 = 3$  then

A.  $r^2 / p^2$

B.  $r^3 / p^3$

C.  $-s / p$

D. none of these

**Answer: B**



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5. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

if  $\Delta = 27$  and  $a^2 + b^2 + c^2 = 3$  then

A.  $\leq 9r^2/p^2$

B.  $\geq 27s^2/p^2$

C.  $\leq 27s^3/p^3$

D. none of these

**Answer: B**



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6. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

if  $\Delta = 27$  and  $a^2 + b^2 + c^2 = 3$  then

A.  $3p + 2q = 0$

B.  $4p + 3q = 0$

C.  $3p + q = 0$

D. none of these

**Answer: C**



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7. if  $x > m, y > n, z > r (x, y, z > 0)$  such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value of  $\frac{m}{x-m} + \frac{n}{y-n} + \frac{z}{z-r}$  is

A. 1

B. -1

C. 2

D. -2

**Answer: C**



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8. if  $x > m, y > n, z > r$  ( $x, y, z > 0$ ) such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value of  $\frac{m}{x-m} + \frac{n}{y-n} + \frac{z}{z-r}$  is

A. -2

B. -4

C. 0

D. -1

**Answer: D**



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9. if  $x > m, y > n, z > r$  ( $x, y, z > 0$ ) such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value  $\frac{xyz}{(x-m)(y-n)(z-r)}$  is

A. 27

B.  $\frac{8}{27}$

C.  $\frac{64}{27}$

D. None of these

**Answer: B**



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**10.**

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Coefficient of  $x$  in  $f(x)$  is

A.  $\frac{g(a) - f(b)}{b - a}$

B.  $\frac{g(-a) - g(-b)}{b - a}$

C.  $\frac{g(a) - g(b)}{b - a}$

D. none of these

**Answer: C**



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11.

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Coefficient of  $x$  in  $f(x)$  is

- A.  $\frac{bg(a) - ag(b)}{(b - a)}$
- B.  $\frac{bf(a) - af(-b)}{(b - a)}$
- C.  $\frac{bf(-a) - ag(b)}{(b - a)}$
- D. none of these

Answer: D



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12.

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Which of the following is not true ?

- A.  $f(-a) = g(a)$
- B.  $f(-a) = g(-a)$
- C.  $f(-b) = g(b)$
- D. none of these

**Answer: B**



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13. Suppose  $f(x)$  is a function satisfying the following conditions:

$f(0) = 2, f(1) = 1$   $f$  has a minimum value at  $x = \frac{5}{2}$  For all  $x, f'(x) = |2ax^2 - 12ax + b + 1| - 12(ax + b)$

where  $a, b$  are some constants. Determine the constants  $a, b$ , and the function  $f(x)$

A.  $1/4$

B.  $1/2$

C.  $-1$

D.  $3$

**Answer: B**



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14. Suppose  $f(x)$  is a function satisfying the following conditions:

$f(0) = 2, f(1) = 1$   $f$  has a minimum value at  $x = \frac{5}{2}$  For all

$x, f'(x) = |2ax^2 - 12ax + b + 1| - 12(ax + b)^2$

where  $a, b$  are some constants. Determine the constants  $a, b$ , and the

function  $f(x)$

A. both roots positive

B. both roots negative

C. roots of opposite sign

D. imaginary roots

**Answer: D**



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15. Suppose  $f(x)$  is a function satisfying the following conditions:

$f(0) = 2$ ,  $f(1) = 1$   $f$  has a minimum value at  $x = \frac{5}{2}$  For all

$x$ ,  $f'(x) = |2ax^2 - 12ax + b + 1| + 1 - 12(ax + b)$

where  $a, b$  are some constants. Determine the constants  $a, b$ , and the

function  $f(x)$

A.  $[7/16, \infty)$

B.  $(-\infty, 15/16]$

C.  $[3/4, \infty)$

D. none of these

**Answer: A**



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**16.** Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^a & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix} \quad a, b \text{ being positive}$$

integers. The constant term in  $f(x)$  is

A. 2

B. 1

C. -1

D. 0

**Answer: D**



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**17.** Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

The constant term in  $f(x)$  is

A.  $2^a$

B.  $2^a - 3 \times 2^b + 1$

C. 0

D. none of these

**Answer:** C



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**18.** Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

The constant term in  $f(x)$  is

- A. All the roots of the equation  $f(x)=0$  are positive
- B. All the roots of the equation  $f(x)=0$  are negative
- C. At least one of the equation  $f(x)=0$  is repeating one .
- D. None of these

**Answer: C**



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**19.** Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and and

at least one of the a,b,c is a proper fraction.

$a^2 + b^2 + c^2$  is

A.  $> 2$

B.  $> 3$

C.  $< 3$

D.  $< 2$

**Answer: C**



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20. Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and

at least one of the  $a,b,c$  is a proper fraction.

$abc$  is

A.  $> -1$

B.  $> 1$

C.  $< 2$

D.  $< 3$

**Answer: A**



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21. Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and at least one of the  $a, b, c$  is a proper fraction.

$abc$  is

A.  $x, y, z \equiv (1 - 2a^2) : (1 - 2b^2) : (1 - 2c^2)$

B.  $x, y, z \equiv \frac{1}{1 - 2a^2} : \frac{1}{1 - 2b^2} : \frac{1}{1 - 2c^2}$

C.  $x, y, z \equiv \frac{a}{1 - a^2} : \frac{b}{1 - b^2} : \frac{c}{1 - c^2}$

D.  $x, y, z \equiv \sqrt{1 - a^2} : \sqrt{1 - b^2} : \sqrt{1 - c^2}$

**Answer: D**



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22. Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has unique solution if (a)  $\lambda \neq 3$  (b)  $\lambda = 3, \mu = 10$  (c)  $\lambda = 3, \mu \neq 10$  (d) none of these

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D. none of these

**Answer: A**



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**23.** Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has infinite solutions if (a)  $\lambda \neq 3$  (b)  $\lambda = 3, \mu = 10$  (c)

$\lambda = 3, \mu \neq 10$  (d)  $\lambda = 3, \mu \neq 10$

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D.  $\lambda = 3, \mu \neq 10$

**Answer: B**



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**24.** Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

The system has no solution if (a)  $\lambda \neq 3$  (b)  $\lambda = 3, \mu = 10$  (c)

$\lambda = 3, \mu \neq 10$  (d) none of these

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D. none of these

**Answer: C**



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### Numerical Value Type

1. If  $a_1, a_2, a_3, 5, 4, a_6, a_7, a_8, a_9$  are in *H. P.* and the value of the

determinant 
$$\begin{vmatrix} a_1 & a_2 & a_3 \\ 5 & 4 & a_6 \\ a_7 & a_8 & a_9 \end{vmatrix}$$
 is  $D$  then the value of  $21D/10$  is



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2. The sum of values of p for which the equations  $x+y+z=1$ ,  $x+2y+4z=p$  and  $x+4y+10z=p^2$  have a solution is \_\_\_\_\_



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3. The sum of roots of the equations

$$\begin{vmatrix} x + 2 & 2x + 3 & 3x + 4 \\ 2x + 3 & 3x + 4 & 4x + 5 \\ 3x + 5 & 5x + 8 & 10x + 17 \end{vmatrix} = 0 \text{ is } _____$$



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4. about to only mathematics



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5. If  $f(x) = \begin{vmatrix} 1 & x & x + 1 \\ 2x & x(x - 1) & (x + 1)x \\ 3x(x - 1) & x(x - 1)(x - 2) & (x + 1)x(x - 1) \end{vmatrix}$  then

the value of  $f(500)$  \_\_\_\_\_



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6. If  $\begin{vmatrix} x & x+y & x+y+z \\ 2x & 3x+2y & 4x+3y+2z \\ 3x & 6x+3y & 10x+6y+3z \end{vmatrix} = 64$  then the real value of x is



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7.

Let

$$D_1 = |aba + bc dc + d ab a - b| \text{ and } D_2 = |aca + cb db + da ca + b + c|$$

then the value of  $\left| \frac{D_1}{D_2} \right|$ , where  $b \neq 0$  and  $a \neq bc$ , is \_\_\_\_.



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8. if  $a_1, a_2, a_3, \dots, a_{12}$  are in A.P and

$$\Delta_1 = \begin{vmatrix} a_1 a_5 & a_1 & a_2 \\ a_2 a_6 & a_2 & a_3 \\ a_3 a_7 & a_3 & a_4 \end{vmatrix} \quad \Delta_2 = \begin{vmatrix} a_2 a_{10} & a_2 & a_3 \\ a_3 a_{11} & a_3 & a_4 \\ a_4 a_{12} & a_4 & a_5 \end{vmatrix}$$

then  $\Delta_1 : \Delta_2 = \text{_____}$



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9. if  $(1 + ax + bx^2)^4 = a_0 + a_1x + a_2x^2 + \dots + a_8x^8$ , where

$a, b, a_0, a_1, \dots, a_8 \in R$  such that  $a_0 + a_1 + a_2 \neq 0$  and

$$\begin{vmatrix} a_0 & a_1 & a_2 \\ a_1 & a_2 & a_0 \\ a_2 & a_0 & a_1 \end{vmatrix} = 0 \text{ then the value of } 5 \cdot \frac{a}{b} \text{ is } \underline{\hspace{2cm}}$$



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10.  $\begin{vmatrix} 5\sqrt{\log_5 3} & 5\sqrt{\log_5 3} & 5\sqrt{\log_5 3} \\ 3^{-\log_{1/3} 4} & (0.1)^{\log_{0.01} 4} & 7^{\log_7 3} \\ 7 & 3 & 5 \end{vmatrix}$  is equal to  $\underline{\hspace{2cm}}$



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11. Let  $a+b+c=s$  and  $\begin{vmatrix} s+c & a & b \\ c & s+a & b \\ c & a & s+b \end{vmatrix} = 432$  then the value of  $s$  is  $\underline{\hspace{2cm}}$



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12. Let  $a, b, c \in R$  not all are equal and  $\Delta_1 = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$

$$\Delta_2 = \begin{vmatrix} a+2b & b+3c & c+4a \\ b+2c & c+3a & a+4b \\ c+2a & a+3b & b+4c \end{vmatrix} \text{ then } \frac{\Delta_2}{\Delta_1} = \underline{\hspace{2cm}}$$



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13. Three distinct points  $P(3u^2, 2u^3); Q(3v^2, 2v^3)$  and  $R(3w^2, 2w^3)$  are collinear then



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14. if  $\Delta_r = \begin{vmatrix} r & 612 & 915 \\ 101r^2 & 2r & 3r \\ r & \frac{1}{r} & \frac{1}{r^2} \end{vmatrix}$  then the value of

$$\lim_{n \rightarrow \infty} \cdot \frac{1}{n^3} (\sum_{r=1}^n \Delta_r) \text{ is } \underline{\hspace{2cm}}$$



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15. if  $x=31, y=32$  and  $z=33$  then the value of

$$\begin{vmatrix} (x^2 + 1)^2 & (xy + 1)^2 & (xz + 1)^2 \\ (xy + 1)^2 & (y^2 + 1)^2 & (yz + 1)^2 \\ (xz + 1)^2 & (yz + 1)^2 & (z^2 + 1)^2 \end{vmatrix} \text{ is } \underline{\hspace{2cm}}$$



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16. Let  $\alpha, \beta, \gamma$  are the real roots of the equation  $x^3 + ax^2 + bx + c = 0$  ( $a, b, c \in R$  and  $a \neq 0$ ). If the system of equations  $(u, v, w)$  given by  $\alpha u + \beta v + \gamma w = 0$ ,  $\beta u + \gamma v + \alpha w = 0$ ,  $\gamma u + \alpha v + \beta w = 0$  has non-trivial solutions then the value of  $a^2/b$  is \_\_\_\_\_.



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17. The value of  $|\alpha|$  for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution , is \_\_\_\_\_



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18. Number of values of  $\theta$  lying in  $[0, 100\pi]$  for which the system of equations  $(\sin 3\theta) x - y + z = 0$ ,  $(\cos 2\theta) x + 4y + 3z = 0$ ,  $2x + 7y + 7z = 0$  has non-trivial solution is \_\_\_\_\_



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19. Let  $\omega$  be the complex number  $\cos\left(\frac{2\pi}{3}\right) + i \sin\left(\frac{2\pi}{3}\right)$ . Then the number of distinct complex cos numbers  $z$  satisfying

$$\Delta = \begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0 \text{ is}$$



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20. The total number of distinct  $x \in R$  for which

$$\begin{vmatrix} x & x^2 & 1+x^3 \\ 2x & 4x^2 & 1+8x^3 \\ 3x & 9x^2 & 1+27x^3 \end{vmatrix} = 10 \text{ is } \begin{array}{l} \text{(A) 0} \\ \text{(B) 1} \\ \text{(C) 2} \\ \text{(D) 3} \end{array}$$



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21. For a real number  $\alpha$ , if the system  $[1\alpha\alpha^2\alpha 1\alpha\alpha^2\alpha 1][xyz] = [1 - 11]$  of linear equations, has infinitely many solutions, then  $1 + \alpha + \alpha^2 =$



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22. Let P be a matrix of order  $3 \times 3$  such that all the entries in P are from the set  $\{-1, 0, 1\}$ . Then, the maximum possible value of the determinant of P is \_\_\_\_\_



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1. Let  $a, b, c$  be such that  $b(a+c) \neq 0$ . If

$$\begin{vmatrix} a & a+1 & a-1 \\ -b & b+1 & b-1 \\ c & c-1 & c+1 \end{vmatrix} + \begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ (-1)^{n+2}a & (-1)^{n+1}b & (-1)^nc \end{vmatrix} = 0 \text{ then the}$$

value of  $n$  is

- A. zero
- B. any even integer
- C. any odd integer
- D. any integer

**Answer: 3**



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2. Consider the system of linear equations:

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

The system has

- A. no solution
- B. infinite number of solutions
- C. exactly three solutions.
- D. a unique solution

**Answer: 1**



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3. The number of values of  $k$  for which the linear equations  
 $4x + ky + 2z = 0$   $kx + 4y + z = 0$   $2x + 2y + z = 0$  posses a non-zero  
solution is : (1) 3 (2) 2 (3) 1 (4) zero

- A. zero
- B. 3
- C. 2

D. 1

**Answer: 3**



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4. The number of values of  $k$  for which the system of equations:

$$kx + (3k + 2)y = 4k$$

$(3k - 1)x + (9k + 1)y = 4(k + 1)$  has no solution, are

A. infinite

B. 1

C. 2

D. 3

**Answer: 2**



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5. If  $\alpha, \beta \neq 0$ , and  $f(n) = \alpha^n + \beta^n$  and  
 $|31 + f(1)1 + f(2)1 + f(1)1 + f(2)1 + f(3)1 + f(2)1 + f(3)1 + f(4)| = .$   
, then K is equal to (1)  $\alpha\beta$  (2)  $\frac{1}{\alpha\beta}$  (3) 1 (4) -1
- A.  $\alpha\beta$   
B.  $\frac{1}{\alpha\beta}$   
C. 1  
D. -1

**Answer:** 3



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6. The set of all values of  $\lambda$  for which the system of linear equations
- $$2x_1 - 2x_2 + x_3 = \lambda x_1$$
- $$2x_1 - 3x_2 + 2x_3 = \lambda x_2$$
- $$-x_1 + 2x_2 = \lambda x_3$$
- has a non-trivial solution,

- A. is an empty set

B. is a singleton set

C. contains two elements

D. contains more than two elements

**Answer: 3**



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7. The system of linear equations  $x + \lambda y - z = 0$   $\lambda x - y - z = 0$   $x + y - \lambda z = 0$  has a non-trivial solution for : (1) infinitely many values of  $\lambda$  . (2) exactly one value of  $\lambda$  . (3) exactly two values of  $\lambda$  . (4) exactly three values of  $\lambda$  .

A. Exactly one value of  $\lambda$

B. Exactly two values of  $\lambda$

C. Exactly three values of  $\lambda$

D. Infinitely many values of  $\lambda$

**Answer: 3**



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8. If  $S$  is the set of distinct values of ' $b$ ' for which the following system of linear equations  $x + y + z = 1$   $x + ay + z = 1$   $ax + by + z = 0$  has no solution, then  $S$  is :  
a finite set containing two or more elements  
(2) a singleton  
an empty set  
(4) an infinite set

A. a singleton set

B. an empty set

C. an infinite set

D. a finite set containing two or more elements

**Answer: 1**



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9. Let  $\omega$  be a complex number such that  $2\omega + 1 = z$  where  $z = \sqrt{-3}$ .

If  $\begin{vmatrix} 1 & 1 & 1 \\ -\omega^2 & -1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k$ , then  $k$  is equal to :

A. 1

B.  $-z$

C.  $z$

D. -1

Answer: 2



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10. If the system of linear equations  $x+ky+3z=0$   $3x+ky-2z=0$   $2x+4y-3z=0$  has a non-zero solution  $(x,y,z)$  then  $\frac{xz}{y^2}$  is equal to

A. 30

B. -10

C. 10

D. -30

**Answer: 3**



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11. If  $\begin{vmatrix} x-4 & 2x & 2x \\ 2x & x-4 & 2x \\ 2x & 2x & x-4 \end{vmatrix} = (A+Bx)(x-A)^2$  then the ordered pair (A,B) is equal to

A. (4, 5)

B. (-4, -5)

C. (-4, 3)

D. (-4, 5)

**Answer: 4**



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1. Which of the following values of  $\alpha$  satisfying the equation
- $$|(1 + \alpha)^2(1 + 2\alpha)^2(1 + 3\alpha)^2(2 + \alpha)^2(2 + 2\alpha)^2(2 + 3\alpha)^2(3 + \alpha)^2(3 + 2\alpha)|$$
- a. -4 b. 9 c. -9 d. 4
- A. -4
- B. 9
- C. -9
- D. 4

**Answer:** 2,3



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2. Let  $a, \lambda, \mu \in R$ , Consider the system of linear equations  
$$\begin{aligned} ax + 2y &= \lambda \\ 3x - 2y &= \mu \end{aligned}$$
 Which of the following statement(s) is (are) correct?

- A. If  $\alpha = -3$  then the system has infinitely many solutions for all values of  $\lambda$  and  $\mu$
- B. If  $\alpha \neq -3$  then the system has a unique solution for all values of  $\lambda$  and  $\mu$
- C. If  $\lambda + \mu = 0$  then the system has infinitely many solutions for  $\alpha = -3$
- D. if  $\lambda + \mu \neq 0$  then the system has no solution for  $\alpha = -3$

**Answer: B,C,D**



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**Matrix Match Type**

# 1. Match the following lists :

List I ( $A, B, C$ are matrices)	List II
a. If $ A  = 2$ , then $ 2A^{-1}  =$ (where $A$ is of order 3)	p. 1
b. If $ A  = 1/8$ , then $ \text{adj}(\text{adj}(2A))  =$ (where $A$ is of order 3)	q. 4
c. If $(A + B)^2 = A^2 + B^2$ , and $ A  = 2$ , then $ B  =$ (where $A$ and $B$ are of odd order)	r. 24
d. $ A_{2 \times 2}  = 2$ , $ B_{3 \times 3}  = 3$ and $ C_{4 \times 4}  = 4$ , then $ ABC $ is equal to	s. 0
	t. does not exist



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**2. Match the following lists:**

List I	List II
<p>a. If <math>f(x)</math> is an integrable function for  <math>x \in \left[\frac{\pi}{6}, \frac{\pi}{3}\right]</math> and</p> $I_1 = \int_{\pi/6}^{\pi/3} \sec^2 \theta f(2\sin 2\theta) d\theta, \text{ and}$ $I_2 = \int_{\pi/6}^{\pi/3} \operatorname{cosec}^2 \theta f(2\sin 2\theta) d\theta, \text{ then } I_1/I_2 =$	p. 3
<p>b. If <math>f(x+1) = f(3+x) \forall x</math>, and the value of  <math>\int_a^{a+b} f(x) dx</math> is independent of <math>a</math>, then the  value of <math>b</math> can be</p>	q. 1
<p>c. The value of</p> $2 \int_1^4 \frac{\tan^{-1}[x^2]}{\tan^{-1}[x^2] + \tan^{-1}[25+x^2-10x]} dx$ <p>(where <math>[.]</math> denotes the greatest integer function) is</p>	r. 2
<p>d. If <math>I = \int_0^2 \sqrt{x + \sqrt{x + \sqrt{x + \dots}}} dx</math></p> <p>(where <math>x &gt; 0</math>), then <math>[I]</math> is equal to (where <math>[.]</math> denotes the greatest integer function)</p>	s. 4



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$$3. \text{ If } \alpha, \beta, \gamma \text{ are the roots of } x^3 - 3x^2 + 3x - 1 = \begin{vmatrix} 1^2 & 2^2 & 3^2 \\ 2^2 & 3^2 & 4^2 \\ 3^2 & 4^2 & 5^2 \end{vmatrix}$$

then match the list I with list II



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4. consider the system of equations

$$\lambda x + y + z = 1$$

$$x + \lambda y + z = \lambda:$$

$$x + y + \lambda z = \lambda^2$$

Now match the following lists:



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5. consider determinant  $\Delta = |a_{ij}|$  of order 3. If  $\Delta = 2$  the match the following lists.



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