

MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

GRAPHS OF TRIGONOMETRIC FUNCTIONS

Illustration

1. Plot $y = \sin x$ and $y = \sin 2x$.



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2. Plot $y = \sin x$ and $y = \sin\left(\frac{x}{2}\right)$



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3. Draw the graph of $y = \tan(3x)$



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4. Draw the graph of $y = \sec^2 x - \tan^2 x$. Is $f(x)$ periodic? If yes, what is its fundamental period?



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5. Draw the graph of $y = \sec^2 x - \tan^2 x$. Is $f(x)$ periodic? If yes, what is its fundamental period?



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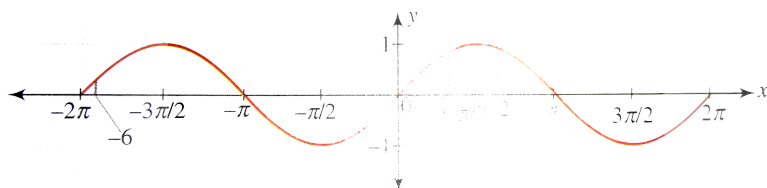
6. Which of the following is highest?

(a) cosec 1

(b) cosec 2

(c) cosec 4

(d) cosec (- 6)



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7. Draw the graph of the function

$$y = f(x) = \lim_{n \rightarrow \infty} \cos^{2n} x \text{ and find its period.}$$



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8. Find the number of solution to the equation

$$x^2 \tan x = 1, x \in [0, 2\pi].$$



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9. Solve $\tan x > \cot x$, where $x \in [0, 2\pi]$.



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10. Let $f(x) = x \sin \pi x$, $x > 0$. Then for all natural numbers n , $f'(x)$ vanishes at (a) A unique point in the interval $\left(n, n + \frac{1}{2}\right)$ (b) a unique point in the interval $\left(n + \frac{1}{2}, n + 1\right)$ (c) a unique point in the interval $(n, n + 1)$ (d) two points in the interval $(n, n + 1)$



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11. If $0 < \alpha < \frac{\pi}{3}$, then prove that $\alpha(\sec \alpha) < \frac{2\pi}{3}$.



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12. Draw the graph of $y = [\sin x]$, $x \in [0, 2\pi]$, where $[\cdot]$ represents the greatest integer function.



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13. Draw the graph of $f(x) = [\tan x]$, $0 \leq x \leq 5\pi/12$, where $[\cdot]$ represents the greatest integer function.



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14. Draw the graph of $f(x) = e^{\sin x}$.



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15. Draw the graph of $y = \sin^2 x$.



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16. Draw the graph of $y = (\sin 2x) \sqrt{1 + \tan^2 x}$, find its domain and range.



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17. Draw the graph $y = \sin^2 x$.



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18. Draw the graph of $y = \sin^3 x$.



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19. Draw the graph of

$$f(x) = |\sin x| + |\cos x|, x \in R.$$



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20. Draw the graph of $f(x) = \sqrt{\sin x}$.



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21. Draw the graph of $y = \frac{\cos\left(|x| + \frac{\pi}{2}\right)}{\sin x}$. Is the function periodic?



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22. Draw the graph of $f(x) = \cos \pi[x]$, where $[\cdot]$ represents the greatest integer function. Find the period of the function.



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23. Draw the graph of

$$f(x) = \sec x + \operatorname{cosec} x, x \in (0, 2\pi) - \{\pi/2, \pi, 3\pi/2\}$$

Also find the values of 'a' for which the equation $\sec x + \operatorname{cosec} x = a$ has two distinct root and four distinct roots.



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24. Draw the graph of $f(x) = \frac{\sin x}{\sqrt{1 + \tan^2 x}} - \frac{\cos x}{\sqrt{1 + \cot^2 x}}$. Then find the range of $f(x)$.



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25. Find the area bounded by the following curve :

(i) $f(x) = \sin x, g(x) = \sin^2 x, 0 \leq x \leq 2\pi$

(ii) $f(x) = \sin x, g(x) = \sin^4 x, 0 \leq x \leq 2\pi$



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26. Write the equivalent (piecewise) definition of

$$f(x) = \operatorname{sgn}(\sin x).$$



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27. Draw the graph of $f(x) = \{\sin x\}$, where $\{\cdot\}$ represents the fractional part function.



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28. Draw a graph of $f(x) = \sin\{x\}$, where $\{x\}$ represents the greatest integer function.



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29. Draw the graph of

$f(x) = \max \{2 \sin x, 1 - \cos x\}, x \in (0, \pi)$.

Also find the range of

$g(x) = \min \{2 \sin x, 1 - \cos x\}, x \in (0, \pi)$



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30. Draw the graph of $y = \log_e(\sin x)$.



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31. Draw the graph of $[y] = \sin x, x \in [0, 2\pi]$ where $[\cdot]$ denotes the greatest integer function



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32. Draw the graph of $y = x \sin x$.



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33. Draw the graph of $y = e^x \sin 2\pi x$.



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34. Let $[x]$ denotes the greatest integer less than or equal to x . If $f(x) = [x \sin \pi x]$, then $f(x)$ is



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35. Evaluate : $\left[\lim_{x \rightarrow 0} \frac{\sin x}{x} \right]$, where $[\cdot]$ represents the greatest integer function.



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36. Discuss maxima/minima of

$$f(x) = \frac{x}{1 + x \tan x}, x \in \left(0, \frac{\pi}{2}\right)$$



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37. Find the values of a if equation

$$1 - \cos x = \frac{\sqrt{3}}{2}|x| + a, x \in (0, \pi), \text{ has exactly one solution.}$$



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38. Find the number of solution to the equation

$$\sin x = x^2 + 2x + 1.$$

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39.

Prove

that

$\sin x + 2x \geq \frac{3x(x+1)}{\pi}, \forall x \in \left[0, \frac{\pi}{2}\right]$ (Justify the inequality, if any used).

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40. Find the ratio of the areas of two regions of the curve $C_1 \equiv 4x^2 + \pi^2 y^2 = 4\pi^2$ divided by the curve $C_2 \equiv y = -\left(\operatorname{sgn}\left(x - \frac{\pi}{2}\right)\right)\cos x$ (where $\operatorname{sgn}(x) = \operatorname{signum}(x)$).

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41. Solve $\tan x < 2$.



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42. Solve $\sin x > -\frac{1}{2}$ or find the domain of $f(x) = \frac{1}{\sqrt{1 + 2\sin x}}$



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43. Solve : $2\cos^2 \theta + \sin \theta \leq 2$, where $\frac{\pi}{2} \leq \theta \leq \frac{3\pi}{2}$.



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44. Solve $\sin \theta + \sqrt{3} \cos \theta \geq 1$, $-\pi < \theta < \pi$.



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45. Let
$$f(x) = \begin{cases} x^2 + 3x, & -1 \leq x < 0 \\ -\sin x, & 0 \leq x < \pi/2 \\ -1 - \cos x, & \frac{\pi}{2} \leq x \leq \pi \end{cases}.$$

Draw the graph of the function and find the following

(a) Range of the function

(b) Point of inflection

(c) Point of local minima



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46. If $0 < x_1 < x_2 < x_3 < \pi$, then prove that

$$\sin\left(\frac{x_1 + x_2 + x_3}{3}\right) < \frac{\sin x_1 + \sin x_2 + \sin x_3}{3}.$$

Hence or otherwise prove that if A, B, C are angles of a triangle, then the maximum value of $\sin A + \sin B + \sin C$ is $\frac{3\sqrt{3}}{2}$



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Exercises

1. Draw the graph of $y = \operatorname{cosec}^2 x - \cot^2 x$. Is $f(x)$ periodic? If yes, what is its fundamental period?



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2. Draw the graph of $y = \cos \pi x$.



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3. Draw the graph of $y = \cos^2 x$.



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4. Find the value of x for which

$f(x) = \sqrt{\sin x - \cos x}$ is defined, $x \in [0, 2\pi)$.



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5. Draw the graph of $y = \tan^2 x$.



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6. Draw the graph of $y = \sin x + \cos x, x \in [0, 2\pi]$.



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7. Draw the graph of $y = [\cos x], x \in [0, 2\pi]$, where $[\cdot]$ represents the greatest integer function.



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8. Draw the graph of $y = \sin \pi \sqrt{x}$.



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9. Find the number of roots of the equation

$$x \sin x = 1, x \in [-2\pi, 0) \cup (0, 2\pi].$$



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10. Evaluate : $\left[\lim_{x \rightarrow 0} \frac{\tan x}{x} \right]$, where $[\cdot]$ represents the greatest integer function.



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11. For $f(x) = \sin x - x^2 + 1$, check whether the function is increasing, decreasing or has a point of extremum ?



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12. Draw the graph of the function $f(x) = \max(\sin x, \cos 2x)$, $x \in [0, 2\pi]$. Write the equivalent definition of $f(x)$ and find the range of the function.



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13. Draw the graph of $[y] = \cos x, x \in [0, 2\pi]$, where

$[\cdot]$ denotes the greatest integer function.



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14. The total number of solution of $\sin\{x\} = \cos\{x\}$

(where $\{\}$ denotes the fractional part) in $[0, 2\pi]$ is

equal to 5 (b) 6 (c) 8 (d) none of these



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15. Draw the graph of $f(x) = |\tan x| + |\cot x|$.



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16. Find the number of solutions to $\cos x = \frac{x}{10}, x > 0$.



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17. The number of solutions of $\tan x - mx = 0, m > 1$, in $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ is 1 (b) 2 (c) 3 (d) m



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18. Find the number of solutions to $\log_e |\sin x| = -x^2 + 2x$ in $\left[-\frac{\pi}{2}, \frac{3\pi}{2}\right]$.



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19. Solve : $\cos x \leq -\frac{1}{2}$.



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20. Prove that the least positive value of x , satisfying $\tan x = x + 1$, lies in the interval $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$



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21. Draw the graph of $y = \frac{x^2}{10} \sin x$.



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22. Draw the graph of $y = \frac{\sin x}{x}$.



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