MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

LOGARITHM AND ITS PROPERTIES

Illustration 1 1

1. Solve for $x: 4^x 3^{x-1/2} = 3^{x+1/2} - 2^{2x-1}$.

Watch Video Solution

Illustration 1 2

1. Solve $e^{\sin x} - e^{-\sin x} - 4 = 0$.

Watch Video Solution

Illustration 1 3

1. Solve $|x-3|^{3x^2-10x+3}=1$.

Watch Video Solution

Illustration 1 4

1. Solve$(1/2)^{x^2-2x}<1/2$.

Watch Video Solution

Illustration 1 5

1. Find the smallest integral value of x satisfying $(x-2)^{x^2-6x+8}>1$.

Watch Video Solution

Illustration 1 6

1. Find the sumber of solutions of equation $(2x-3)2^x = 1$.

Watch Video Solution

Illustration 1 7

1. Find the value of $\log_{2\sqrt{3}} 1728$.

Watch Video Solution

Illustration 1 8

1. Prove that $\frac{2}{5} < \log_{10} 3 < \frac{1}{2}$.

Watch Video Solution

Illustration 1 9

1. Arrange $\log_2 5, \log_{0.5} 5, \log_7 5, \log_3 5$ in decreasing order.

Watch Video Solution

Illustration 1 10

1. Prove that number $(\log)_2 7$ is an irrational number.

Watch Video Solution

Illustration 1 11

1. Which of the following numbers are positive/negative : $(i)\log_{\sqrt{3}} \sqrt{2}$

$(ii)\log_3(4)$

Watch Video Solution

Illustration 1 12

1. Find the value of $\log \tan 1^\circ \log \tan 2^\circ \ldots \log \tan 89^\circ$.

Watch Video Solution

Illustration 1 13

1. If $\log_a 3 = 2$ and $\log_b 8 = 3$, then prove that $\log_a b = \log_3 4$.

Watch Video Solution

Illustration 1 14

1. If $\log_3 y = x$ and $\log_2 z = x$, find 72^x in terms of y and z.

Watch Video Solution

Illustration 1 15

1. If $\frac{x(y+z-x)}{\log x} = \frac{y(z+x-y)}{\log y}\frac{z(x+y-z)}{\log z}$, $provethatx^y y^x = z^x y^z = x^z$

Watch Video Solution

Illustration 1 16

1. Suppose $x; y; z > 0$ and are not equal to 1 and $\log x + \log y + \log z = 0.$ Find the value of $x^{\frac{1}{\log y}+\frac{1}{\log z}} \times y^{\frac{1}{\log z}+\frac{1}{\log x}} \times z^{\frac{1}{\log x}+\frac{1}{\log y}}$ (base 10)

Watch Video Solution

Illustration 1 17

1. Solve $2(25)^x - 5(10^x) + 2(4^x) \geq 0$.

Watch Video Solution

Illustration 1 18

1. Find the number of solution to equation $\log_2(x+5) = 6 - x$:

Watch Video Solution

Illustration 1 19

1. Find the number of solutions of the following equations:

$x^{-\frac{1}{2}}(\log)_{0.5}x = 1\, x^2 - 4x + 3 - (\log)_2 x = 0$

Watch Video Solution

Illustration 1 20

1. Find the value of the following:

(i) $\log_{10} 2 + \log_{10} 5$

(ii) $\log_3\left(\sqrt{11} - \sqrt{2}\right) + \log_3\left(\sqrt{11} + \sqrt{2}\right)$

(iii) $\log_7 35 - \log_7 5$

Watch Video Solution

Illustration 1 21

1. Find the value of $\log_2\left(2\sqrt[3]{9} - 2\right) + \log_2\left(12\sqrt[3]{3} + 4 + 4\sqrt[3]{9}\right)$.

Watch Video Solution

Illustration 1 22

1. What is logarithm of $32\sqrt[5]{4}$ to the base $2\sqrt{2}$?

Watch Video Solution

Illustration 1 23

1. If $(\log)_e\left(\frac{a+b}{2}\right)=\frac{1}{2}\left((\log)_e a+(\log)_e b\right)$, then find the relation between $aandb$.

Watch Video Solution

Illustration 1 24

1. Which of the following pairs of expression are defined for the same set of values of x ? $f_1(x)=2(\log)_2 xandf_2(x)=(\log)_{10}x^2$

$f_1(x)=(\log)_{\times}^2 andf_2(x)=2$

$f_1(x)=(\log)_{10}(x-2)+(\log)_{10}(x-3)andf_{2(x)}=(\log)_{10}(x-2)(x-3)$

Watch Video Solution

Illustration 1 25

1. Find the value of $7\log\left(\frac{16}{15}\right)+5\log\left(\frac{25}{24}\right)+3\log\left(\frac{81}{80}\right)$.

Watch Video Solution

Illustration 1 26

1. If sum $\log_2 x+\log_4 x+\log_{16} x+\log_{256} x+\ldots=6$, then find the value of x.

Watch Video Solution

Illustration 1 27

1. Suppose that a and b are positive real numbers such that $\log_{27} a+\log_9(b)=\frac{7}{2}$ and $\log_{27} b+\log_9 a=\frac{2}{3}$.Then the value of the ab

equals

Watch Video Solution

Illustration 1 28

1. Solve for x: $11^{4x-5} \cdot 3^{2x} = 5^{3-x} \cdot 7^{-x}$.

Watch Video Solution

Illustration 1 29

1. Which is greater : $x = \log_3 5$ or $y = \log_{17}(25)$

Watch Video Solution

Illustration 1 30

1. If $n > 1$ then prove that $\frac{1}{\log_2 n} + \frac{1}{\log_3 n} + \ldots\ldots\ldots\ldots\ldots + \frac{1}{\log_{53} n} = \frac{1}{\log_{53!} n}$

Watch Video Solution

Illustration 1 31

1. Let $a = \log_3 20, b = \log_4 15$ and $c = \log_5 12$. Then find the value of $\frac{1}{a+1} + \frac{1}{b+1} + \frac{1}{c+1}$.

Watch Video Solution

Illustration 1 32

1. If $\log_a(ab) = x$ then $\log_b(ab)$ is equals to

Watch Video Solution

Illustration 1 33

1. If $(\log)_{12}27 = a,$ then find $(\log)_6 16$ $\int ermsofa$

Watch Video Solution

Illustration 1 34

1. If $a^x = b, b^y = c, c^z = a,$ then find the value of xyz.

Watch Video Solution

Illustration 1 35

1. Find the value of

$((\log)_3 4)((\log)_4 5)((\log)_5 6)((\log)_6 7)((\log)_7 8)((\log)_8 9)$.

Watch Video Solution

Illustration 1 36

1. Simplify: $\frac{1}{1+(\log)_a bc}+\frac{1}{1+(\log)_b ca}+\frac{1}{1+(\log)_c ab}$

Watch Video Solution

Illustration 1 37

1. If $x=\log_{2a} a, y=\log_{3a} 2a$ and $z=\log_{4a} 3a$ then prove that $xyz+1=2yz$

Watch Video Solution

Illustration 1 38

1. If $\log_a a.\log_c a+\log_c b.\log_a b+\log_a c.\log_b c=3$(where a, b, c are different positive real nu then find the value of abc.

Watch Video Solution

Illustration 1 39

1. If y= $2^{\frac{1}{\log_x 4}}$ then prove that $x = y^2$.

Watch Video Solution

Illustration 1 40

1. Find the value of $81^{(1/(\log)_5 3)} + 27^{\log 36} + 3^{\left(\frac{4}{(\log)_7 9}\right)}$

Watch Video Solution

Illustration 1 41

1. Prove that $\frac{2^{\log_{2^{1/4}} x} - 3^{\log_{27}\left(x^2+1\right)^3} - 2x}{7^{4\log_{49} x} - x - 1} > 0,\ \forall x \in (0, \infty).$

Watch Video Solution

Illustration 1 42

1. If 60^a=3 and $60^b = 5$ then $12^{\frac{1-a-b}{2(1-b)}}$ is equal to

Watch Video Solution

Illustration 1 43

1. Solve $\log_4(8) + \log_4(x+3) - \log_4(x-1) = 2$

Watch Video Solution

Illustration 1 44

1. Solve $\log(-x) = 2\log(x+1)$.

Watch Video Solution

Illustration 1 45

1. Solve $(\log)_2(3x-2) = (\log)_{\frac{1}{2}} x$

Watch Video Solution

Illustration 1 46

1. Solve $2^{x+2}27^{x/(x-1)} = 9$

Watch Video Solution

Illustration 1 47

1. Solve $\log_2(4 \times 3^x - 6) - \log_2(9^x - 6) = 1.$

Watch Video Solution

Illustration 1 48

1. Solve : $6\left((\log)_x 2-(\log)_4 x\right)+7=0$.

Watch Video Solution

Illustration 1 49

1. Solve $4^{\log_2 \log x}=\log x-(\log x)^2+1$ (base is e).

Watch Video Solution

Illustration 1 50

1. Solve: $4(\log)_{\frac{x}{2}}\left(\sqrt{x}\right)+2(\log)_{4x}\left(x^2\right)=3(\log)_{2x}\left(x^3\right)$.

Watch Video Solution

Illustration 1 51

1. Solve $4^{\log_9 x} - 6x^{\log_9 2} + 2^{\log_3 27} = 0.$

Watch Video Solution

Illustration 1 52

1. Solve $\frac{1}{4}x^{\log_2 \sqrt{x}} = \left(2 \cdot x^{\log_2 x}\right)^{\frac{1}{4}}.$

Watch Video Solution

Illustration 1 53

1. Solve $|x-1|^{(\log_{10} x)^2 - \log_{10} x^2} = |x-1|^3$

Watch Video Solution

Illustration 1 54

1. Solve $\log_2(x-1) > 4$.

Watch Video Solution

Illustration 1 55

1. Solve $\log_3(x-2) \leq 2$.

Watch Video Solution

Illustration 1 56

1. Solve : $(\log)_{0.3}\left(x^2 - x + 1\right) > 0$

Watch Video Solution

Illustration 1 57

1. Solve $1 < \log_2(x-2) \leq 2$.

Watch Video Solution

Illustration 1 58

1. Solve $\log_2|x-1| < 1$.

Watch Video Solution

Illustration 1 59

1. Solve $(\log)_{0.2}|x-3| \geq 0$.

Watch Video Solution

Watch Video Solution

Illustration 1 60

1. Solve $\log_2 . \dfrac{x-1}{x-2} > 0$.

Watch Video Solution

Illustration 1 61

1. Solve: $(\log)_{0.5} \dfrac{3-x}{x+2} < 0$

Watch Video Solution

Illustration 1 62

1. Solve: $(\log)_3 \left(2x^2 + 6x - 5\right) > 1$

Watch Video Solution

Watch Video Solution

Illustration 1 63

1. Solve $(\log)_{0.04}(x-1) \geq (\log)_{0.2}(x-1)$

Watch Video Solution

Illustration 1 64

1. Solve $\log_{x+3}\left(x^2-x\right) < 1.$

Watch Video Solution

Illustration 1 65

1. Solve $2\log_3 x - 4\log_x 27 \leq 5.$

Watch Video Solution

Watch Video Solution

Illustration 1 66

1. Solve: $(\log)_{x+\frac{1}{x}}\left(\frac{\log_2(x-1)}{x-2}\right)>0$

Watch Video Solution

Illustration 1 67

1. Solve: $(\log)_{(\log)_2\left(\frac{x}{x}\right)}\left(x^2-10x+22\right)>0$

Watch Video Solution

Illustration 1 68

1. Solve: $(\log)_{0.1}\left((\log)_2\left(\frac{x^2+1}{x-1}\right)\right)<0$

Watch Video Solution

Watch Video Solution

Illustration 1 69

1. Solve: $\frac{x-1}{(\log)_3(9-3^x)} \leq 1.$

Watch Video Solution

Illustration 1 70

1. Solve: $\left(\frac{1}{2}\right)^{\log^{10a^2}} + 2 > \frac{3}{2^{(\log)_{10}(-a)}}$

Watch Video Solution

Illustration 1 71

1. Write the characteristic of each of the following numbers by using their standard forms: 1235.5 (ii) 346.41 (iii) 62.723 (iv) 7.12345 0.35792 (vi) 0.034239 (vii) 0.002385 (viii) 0.0009468

Watch Video Solution

Illustration 1 72

1. Write the significant digits in each of the following numbers to compute the mantissa of their logarithms: 3.239 (ii) 8 (iii) 0.9 (iv) 0.02 0.0367 (vi) 89 (vii) 0.0003 (viii) 0.00075

Watch Video Solution

Illustration 1 73

1. Find the mantissa of the logarithm of the number 5395

Watch Video Solution

Illustration 1 74

1. Find the mantissa of the logarithm of the number 0.002359

Watch Video Solution

Illustration 1 75

1. Use the logarithm tables to find the logarithm of the following numbers 25975 (ii) 25.795

Watch Video Solution

Illustration 1 76

1. Find the antilogarithm of each of the following: 2.7523 (ii) 3.7523 (iii) 5.7523 (iv) 0.7523 1.7523 (vi) 2.7523 (vii) 3.7523

Watch Video Solution

Illustration 1 77

1. Evaluate $(72.3)^{\frac{1}{3}}$ if $\log 0.723 = 1.8591$.

Watch Video Solution

Illustration 1 78

1. Using logarithms, find the value of 6.45 x 981.4

Watch Video Solution

Illustration 1 79

1. Let $x = (0.15)^{20}$. Find the characteristic and mantissa of the logarithm of x to the base 10. Assume $\log_{10} 2 = 0.301$ and $\log_{10} 3 = 0.477$.

Watch Video Solution

Illustration 1 80

1. If $(\log)_{10} 2 = 0.30103, (\log)_{10} 3 = 0.47712,$ then find the number of digits in $3^{12} x 2^8$.

Watch Video Solution

Illustration 1 81

1. In the 2001 census, the population of India was found to be $8.7x10^7$. If the population increases at the rate of 2.5% every year, what would be

the population in 2011?

Watch Video Solution

Illustration 1 82

1. Find the compound interest on Rs. 12000 for 10 years at the rate of 12% per annum compounded annually.

Watch Video Solution

Illustration 1 83

1. If P is the number of natural numbers whose logarithms to the base 10 have the characteristic $pandQ$ is the number of natural numbers logarithms of whose reciprocals to the base 10 have the characteristic $-q$, then find the value of $\log_{10} P - (\log)_{10} Q$.

Watch Video Solution

Illustration 1 84

1. Let L denote antilog_32 0.6 and M denote the number of positive integers which have the characteristic 4, when the base of log is 5, and N denote the value of $49^{(1-(\log)_7 2)}+5^{-(\log)_5 4}$. Find the value of $\frac{LM}{N}$.

Watch Video Solution

Example 1 1

1. Find the number of solution of $2^x+3^x+4^x-5^x=0$

Watch Video Solution

Example 1 2

1. Let a, b, c, d be positive integers such that $(\log)_a b = \frac{3}{2} and (\log)_c d = \frac{5}{4}$. If $(a - c) = 9$, then find the value of $(b - d)$.

Watch Video Solution

Example 1 3

1. If $a \geq b > 1$, then find the largest possible value of the expression $\log_a(a/b) + \log_a(b/a)$.

Watch Video Solution

Example 1 4

1. If $y = a^{\frac{1}{1-\log_a x}}$ and $z = a^{\frac{1}{1-\log_a y}}$, then prove that $x = a^{\frac{1}{1-\log_a z}}$

Watch Video Solution

Example 1 5

1. Solve $\sqrt{\log(-x)} = \log\sqrt{x^2}$(base is 10).

Watch Video Solution

Example 1 6

1. Solve$3^{(\log_9 x)^2 - \frac{9}{2}\log_9 x + 5} = 3\sqrt{3}$.

Watch Video Solution

Example 1 7

1. Solve for $x : (2x)^{\log_b 2} = (3x)^{\log_b 3}$.

Watch Video Solution

Example 1 8

1. Solve the equations for x and y: $(3x)^{\log 3} = (4y)^{\log 4}$, $4^{\log x} = 3^{\log y}$.

Watch Video Solution

Example 1 9

1. Solve $(\log)_{2x} 2 + (\log)_4 2x = -3/2$.

Watch Video Solution

Example 1 10

1. Solve:

$(\log)_{(2x+3)}\left(6x^2 + 23 + 21\right) + (\log)_{(3x+7)}\left(4x^2 + 12x + 9\right) = 4$

Watch Video Solution

Exercise 11

1. For $x \leq 2$, solve $x^3 \cdot 3^{|x-2|} + 3^{x+1} = x^3 \cdot 3^{x-2} + 3^{|x-2|+3}$

Watch Video Solution

2. Solve $\left(\frac{1}{2}\right)^{x^6 - 2x^4} < 2^{(x)^2}$.

Watch Video Solution

3. Solve for x and y: $y^x = x^y, x = 2y$.

Watch Video Solution

4. Solve $2^{x+2} - 2^{x+3} - 2^{x+4} > 5^{x+1} - 5^{x+2}$.

Watch Video Solution

5. Solve $\left(\frac{3}{4}\right)^{6x+10-x^2} < \frac{27}{64}$.

Watch Video Solution

6. Find the number of solutions of $|x| \cdot 3^{|x|} = 1$.

Watch Video Solution

Exercise 1 2

1. Find the value of $3^{2\log_9 3}$.

Watch Video Solution

2. Find the value of $\sqrt{(\log_{0.5} 4)^2}$.

Watch Video Solution

3. If $\log_{\sqrt{8}} b = 3\frac{1}{3}$, then find the value of b.

Watch Video Solution

4. Find the value of $\log_5 \log_2 \log_3 \log_2 512$.

Watch Video Solution

5. If $\log_5 x = a$ and $\log_2 y = a$, find 100^{2a-1} in terms of x and y .

Watch Video Solution

6. Find the value of $\log_{1/3} \sqrt[4]{729 \cdot \sqrt[3]{9^{-1} \cdot 27^{-4/3}}}$.

Watch Video Solution

7. Solve for $x : \log_4 \log_3 \log_2 x = 0.$

Watch Video Solution

8. Prove that $\log_{10} 2$lies between $\frac{1}{3}$ and $\frac{1}{4}$.

Watch Video Solution

9. Find number of roots of the equation $x^3 - \log_{0.5} x = 0.$

Watch Video Solution

Exercise 1 3

1. Write each of the following as single logarithm:

$(a) 1 + \log_2 5 \qquad (b) 2 - \log_3 7$

$(c) 2 \log_{10} x + 3 \log_{10} y - 5 \log_{10} z$

Watch Video Solution

2. Prove that $\frac{2}{5} < \log_{10} 3 < \frac{1}{2}$.

Watch Video Solution

3. Prove that $\log_7 \log_7 \sqrt{7\sqrt{(7\sqrt{7})}} = 1 - 3\log_7 2$.

Watch Video Solution

4. If $\log_{10} x = y$, then find $\log_{1000} x^2$ in terms of y.

Watch Video Solution

5. If $\log_7 2 = m$, then find $\log_{49} 28$ in terms of m.

Watch Video Solution

6. Find the value of $\log_2\left(\frac{1}{7^{\log_7 0.125}}\right)$.

Watch Video Solution

7. Find the value of $\left(\frac{4}{\log_2\left(2\sqrt{3}\right)}+\frac{2}{\log_3\left(2\sqrt{3}\right)}\right)^2$.

Watch Video Solution

8. If x and y are positive real numbers such that $2\log(2y-3x)=\log x+\log y$, then find the value of $\frac{x}{y}$.

Watch Video Solution

9. If $a^2+b^2=7ab$, prove that $\log\left(\frac{a+b}{3}\right)=\frac{1}{2}(\log a+\log b)$.

Watch Video Solution

10. If $\log_b n = 2$ and $\log_n 2b = 2$, then find the value of b.

Watch Video Solution

11. If $\log_2 x \times \log_3 x = \log_2 x + \log_3 x$, then find x .

Watch Video Solution

12. If $y^2 = xzandа^x = b^y = c^z$, then prove that $(\log)_6 a = (\log)_c b$.

Watch Video Solution

13. Prove the following identities:

(a) $\frac{\log_a n}{\log_{ab} n} = 1 + \log_a b$ $(b)\log_{ab} x = \frac{\log_a x \log_b x}{\log_a x + \log_b x}$.

Watch Video Solution

14. Compute $\log_{ab}\left(\sqrt[3]{a}/\sqrt{b}\right)$ if $\log_{ab} a = 4$.

Watch Video Solution

15. If $a^x = b^y = c^z = d^w$, show that $\log_a(bcd) = x\left(\frac{1}{y} + \frac{1}{z} + \frac{1}{w}\right)$.

Watch Video Solution

16. Find the value of $\left(\frac{1}{49}\right)^{1+\log_7 2} + 5^{-\log_{(1/5)}(7)}$.

Watch Video Solution

Exercise 1 4

1. Solve $\log_2\left(25^{x+3} - 1\right) = 2 + \log_2\left(5^{x+3} + 1\right)$.

Watch Video Solution

2. Solve $\log_4\left(2 \times 4^{x-2} - 1\right) + 4 = 2x$.

Watch Video Solution

3. Solve: $27^{\log_3 \sqrt[3]{x^2-3x+1}} = \dfrac{\log_2(x-1)}{|\log_2(x-1)|}$.

Watch Video Solution

4. Solve $\log_4(x-1) = \log_2(x-3)$.

Watch Video Solution

5. Solve $\log_6 9 - \log_9 27 + \log_8 x = \log_{64} x - \log_6 4$..

Watch Video Solution

6. Solve $\log_2\left(2\sqrt{17-2x}\right) = 1 - \log_{1/2}(x-1)$.

Watch Video Solution

7. Solve : $3\log_x(4) + 2\log_{4x} 4 + 3\log_{16x} 4 = 0$

Watch Video Solution

8. Solve$(\log_3 x)(\log_5 9) - \log_x 25 + \log_3 2 = \log_3 54.$

Watch Video Solution

9. Solve $\left(x^{\log_{10} 3}\right)^2 - \left(3^{\log_{10} x}\right) - 2 = 0.$

Watch Video Solution

10. Solve $x^{\log_4 x} = 2^{3(\log_4 x + 3)}$.

Watch Video Solution

11. Find the sum of the squares of all the real solution of the equation $2\log_{\left(2+\sqrt{3}\right)}\left(\sqrt{x^2+1}+x\right)+\log_{\left(2-\sqrt{3}\right)}\left(\sqrt{x^2+1}-x\right)=3$

Watch Video Solution

12. Prove that the equation $x^{\log_{\sqrt{x}}2x}=4$ has no solution.

Watch Video Solution

Exercise 1 5

1. Solve $\log_3|x|>2$.

Watch Video Solution

2. Solve $\log_{\cdot}\frac{x-4}{2x+5}<1$.

Watch Video Solution

3. Solve $\log_{10}\left(x^2-2x-2\right)\leq 0$.

Watch Video Solution

4. Let $f(x)=\sqrt{\log_{10}x^2}$.Find the set of all values of x for which f (x) is real.

Watch Video Solution

5. Solve $2^{\log_2(x-1)}>x+5$.

Watch Video Solution

6. Solve $\log_2|4-5x|>2$.

Watch Video Solution

7. Solve $\log_{0.2}\cdot\dfrac{x+2}{x}\leq 1.$

Watch Video Solution

8. Solve $\log_{1/2}\left(x^2-6x+12\right)\geq -2.$

Watch Video Solution

9. Solve $(0.5)^{\log_3\log_{(1/5)}\left(x^2-\frac{4}{5}\right)}>1.$

Watch Video Solution

10. Find the values of x which the function $f(x)=\sqrt{\log_{1/2}\left(\dfrac{x-1}{x+5}\right)}$ is defined.

Watch Video Solution

11. Solve $\log_{1-x}(x-2) \geq -1$.

Watch Video Solution

12. Solve $\log_3(x+2)(x+4) + \log_{1/3}(x+2) < \frac{1}{2}\log_{\sqrt{3}} 7$.

Watch Video Solution

13. Solve $\log_x\left(x^2-1\right) \leq 0$.

Watch Video Solution

Exercise 1 6

1. If $\log_{10} 2 = 0.3010$ and $\log_{10} 3 = 0.477$, then find the number of digits in the following numbers:

(a) 3^{40} $(b) 2^{32} \times 5^{25}$ $(c) 24^{24}$

Watch Video Solution

2. If characteristic of three numbers a, b and c and 5, -3 and 2, respectively, then find the maximum number of digits in N = abc.

Watch Video Solution

3. There are 3 number a, b and c such that $\log_{10} a = 5.71, \log_{10} b = 6.23$ and $\log_{10} c = 7.89$. Find the number of digits before dicimal in $\frac{ab^2}{c}$.

Watch Video Solution

4. Rupees 10,000 is invested at 6% interest compounded annually. How long will it take to accumulate Rs. 20, 000 in the account?

Watch Video Solution

5. An initial number of bacteria presented in a culture is 10000. This number doubles every 30 minutes. How long will it take to bacteria to reach the number 100000 ?

Watch Video Solution

6. Charles Richter defined the magnitude of an earthquake to be $M = \log_{10}\left(\frac{I}{S}\right)$, where I is the intensity of the earthquake (measured by the amplitude of a seismograph reading taken 100 km from the epicentre of the earthquake) and S is the intensity of a "standed earthquake" (whose amplitude is 1 micron $= 10^{-1}$ cm).

Each number increase on the Richter scale indicates an intensity ten times stronger. For example. an earthquake of magnitude 5. An earthquake of magnitude 7 is 100 times stronger then an earthquake of magnitude 5. An earthquake of magnitude 8 is 1000 times stronger than an earthquake of magnitude 5.

The earthquake in city A registered 8.3 on the Richter scale. In the same year, another earthquake was recorded in city B that was four times stronger. What was the magnitude of the earthquake in city B ?

Watch Video Solution

Exercises Single Correct Answer Type

1. $\log_4 18$ is

A. a rational number

B. an irrational number

C. a prime number

D. none of these

Answer: B

Watch Video Solution

2. The number $N = 6\log_{10} 2 + \log_{10} 31$ lies between two successive integers whose sum is equal to

A. 5

B. 7

C. 9

D. 10

Answer: B

Watch Video Solution

3. Given that $\log(2) = 0.3010,$ the number of digits in the number 2000^{2000} is 6601 (b) 6602 (c) 6603 (d) 6604

A. 6601

B. 6602

C. 6603

D. 6604

Answer: C

Watch Video Solution

4. If $(21.4)^a = (0.00214)^b = 100$, then the value of $\frac{1}{a} - \frac{1}{b}$ is 0 (b) 1 (c) 2 (d) 4

A. 0

B. 1

C. 2

D. 4

Answer: C

Watch Video Solution

5. The value of $\log ab - \log|b| =$

A. log a

B. $\log|a|$

C. $-\log a$

D. none of these

Answer: B

Watch Video Solution

6. If a, b, c are consecutive positive integers and log (1+ac) = 2K, then the value of K is

A. log b

B. log a

C. 2

D. 1

Answer: A

Watch Video Solution

7. if $\frac{a+\log_4 3}{a+\log_2 3} = \frac{a+\log_8 3}{a+\log_4 3} = b$ then find the value of b

A. $\frac{1}{2}$

B. $\frac{2}{3}$

C. $\frac{1}{3}$

D. $\frac{3}{2}$

Answer: C

Watch Video Solution

8. If $p > 1 and q > 1$ are such that $\log(p+q) = \log p + \log q,$ then the value of $\log(p-1) + \log(q-1)$ is equal to 0 (b) 1 (c) 2 (d) none of these

A. 0

B. 1

C. 2

D. none of these

Answer: A

Watch Video Solution

9. The value of $\left(1+2\frac{\log_3 2}{\left(1+(\log)_3 2\right)^2}+\left((\log)_6 2\right)^2\right.$ is 2 (b) 3 (c) 4 (d) 1

A. 2

B. 3

C. 4

D. 1

Answer: D

Watch Video Solution

10. If $(\log)_4 5 = a and (\log)_5 6 = b,$ then $(\log)_3 2$ is equal to $\frac{1}{2a+1}$ (b) $\frac{1}{2b+1}$ (c) $2ab+1$ (d) $\frac{1}{2ab-1}$

A. $\frac{1}{2a+1}$

B. $\frac{1}{2b+1}$

C. $2ab+1$

D. $\frac{1}{2ab-1}$

Answer: D

Watch Video Solution

11. If $\log_{10} 2 = a, \log_{10} 3 = b$ then $\log_{0.72}(9.6)$ in terms of a and b is equal to

A. $\frac{2a+3b-1}{5a+b-2}$

B. $\frac{5a+b-1}{3a+2b-2}$

C. $\frac{3a+b-2}{2a+3b-1}$

D. $\frac{2a+5b-2}{3a+b-1}$

Answer: B

Watch Video Solution

12. There exists a natural number N which is 50 times its own logarithm to the base 10, then N is divisible by 5 (b) 7 (c) 9 (d) 11

A. 5

B. 7

C. 9

D. 11

Answer: A

Watch Video Solution

13. The value of $\frac{(\log)_2 24}{(\log)_{96} 2} - \frac{(\log)_2 192}{(\log)_{12} 2}$ is 3 (b) 0 (c) 2 (d) 1

A. 3

B. 0

C. 2

D. 1

Answer: A

Watch Video Solution

14. $\log_{x-1} x \cdot \log_{x-2}(x-1) \cdot \ldots \cdot \log_{x-12}(x-11) = 2$,x is equal to

A. 9

B. 16

C. 25

D. none of these

Answer: B

Watch Video Solution

15. If $f.\ (x) = \log\left(\frac{1+x}{1-x}\right)$, then

A. $f(x_1) \cdot f(x_2) = f(x_1 + x_2)$

B. $f(x+2) - 2f(x+1) + f(x) = 0$

C. $f(x) + f(x+1) = f\left(x^2 + x\right)$

D. $f(x_1) + f(x_2) = f\left(\frac{x_1 + x_2}{1 + x_1 x_2}\right)$

Answer: D

Watch Video Solution

16. If $a^4 b^5 = 1$ then the value of $\log_a\left(a^5 b^4\right)$ equals

A. $9/5$

B. 4

C. 5

D. $8/5$

Answer: A

Watch Video Solution

17. The value of $3^{(\log)_4 5} - 5^{(\log)_4 3}$ is 0 (b) 1 (c) 2 (d) none of these

A. 0

B. 1

C. 2

D. none of these

Answer: A

Watch Video Solution

18. If $2^{x+y} = 6^y$ and $3^{x-1} = 2^{y+1}$, then the value of $(\log 3 - \log 2)/(x - y)$ is

A. 1

B. $\log_2 3 - \log_3 2$

C. $\log(3/2)$

D. none of these

Answer: C

Watch Video Solution

19. The value of x satisfying $\sqrt{3}^{-4+2\log_{\sqrt{5}} x} = 1/9$ is

A. 2

B. 3

C. 4

D. none of these

Answer: D

Watch Video Solution

20. The value of x satisfying the equation

$\sqrt[3]{5}^{\log_5 5^{\log_5 5^{\log_5 5^{\log_5\left(\frac{x}{2}\right)}}}}$ = 3, is

A. 1

B. 3

C. 18

D. 54

Answer: D

Watch Video Solution

21. If $\sqrt{(\log)_2 x} - 0.5 = (\log)_2 \sqrt{x,}$ then x equals odd integer (b) prime number composite number (d) irrational

A. odd integer

B. prime number

C. composite number

D. irrational

Answer: B

Watch Video Solution

22. If $\log_y x + \log_x y = 2, x^2 + y = 12$, then the value of xy is

A. 9

B. 12

C. 15

D. 21

Answer: A

Watch Video Solution

23. $4^{\log_9 3} + 9^{\log_2 4} = 10^{\log_x 83}$, then x is equal to

A. 2

B. 3

C. 10

D. 30

Answer: C

Watch Video Solution

24. Solve $(x+1)^{\log_{10}(x+1)} = 100(x+1)$

A. all the roots are positive real numbers.

B. all the roots lie in the interval (0, 100)

C. all the roots lie in the interval [-1, 99]

D. none of these

Answer: C

Watch Video Solution

25. If $\log_2 x + \log_x 2 = \frac{10}{3} = \log_2 y + \log_y 2$ and $x \neq y$,then $x + y =$

A. 2

B. $65/8$

C. $37/6$

D. none of these

Answer: D

Watch Video Solution

26. If $(\log)_{10}\left[\frac{1}{2^x + x - 1}\right] = x\left[(\log)_{10}5 - 1\right]$, then $x =$ 4 (b) 3 (c) 2 (d) 1

A. 4

B. 3

C. 2

D. 1

Answer: D

Watch Video Solution

27. If $(\log)_3\{5+4(\log)_3(x-1)\}=2,$ then x is equal to 4 (b) 3 (c) 8 (d) $(\log)_2 16$

A. 2

B. 4

C. 8

D. 16

Answer: B

Watch Video Solution

28. If $2x^{\log_4 3} + 3^{\log_4 x} = 27$, then x is equal to

A. 2

B. 4

C. 8

D. 16

Answer: D

Watch Video Solution

29. The equation $\log_4(2-x) + \log_{0.25}(2+x) = \log_4(1-x) + \log_{0.25}(2x+1)$ has

A. only one prime solution

B. two real solutions

C. no real solution

D. none of these

Answer: D

Watch Video Solution

30. The values of b for which the equation $2\log_{\frac{1}{25}}(bx+28) = 1\log_5\left(12-4x-x^2\right)$ has coincident roots is/are

A. b = - 12

B. b = 4

C. b = 4 or b =- 12

D. b =- 4 or b = 12

Answer: C

Watch Video Solution

31. If the equation $2^x(1-2^x)+4^y=2^y$ is solved for y in terms of x where $x<0$, then the sum of the solution is $x(\log)_2(1-2^x)$ (b) $x+(\log)_2(1-2^x)$ $(\log)_2(1-2^x)$ (d) $x(\log)_2(2^x+1)$

A. $x\log_2(1-2^x)$

B. $x+\log_2(1-2^x)$

C. $\log_2(1-2^x)$

D. $x\log_2(2^x+1)$

Answer: B

Watch Video Solution

32. The number of solution of $x^{\log_x(x+3)^2}=16$is

A. 0

B. 1

C. 2

D. ∞

Answer: A

Watch Video Solution

33. The product of roots of the equation $\frac{\log_8\left(8/x^2\right)}{\left(\log_8 x\right)^2} = 3$ is

A. 1

B. $1/2$

C. $1/3$

D. $1/4$

Answer: D

Watch Video Solution

34. Let $a > 1$ be a real number . If S is the set of real number x that are solutions to the equation $a^{2\log_2 x} = 5 + 4x^{\log_2 a}$, then

A. 2

B. infinite

C. 0

D. 1

Answer: D

Watch Video Solution

35. the number of roots of the equation $\log_{3\sqrt{x}} x + \log_{3x}\left(\sqrt{x}\right) = 0$ is

A. 1

B. 2

C. 3

D. 0

Answer: B

Watch Video Solution

36. The set of all x satisfying the equation $x^{\log}\_3x^2+\left((\log)_3x\right)^{2-10}=\frac{1}{x^2}is$ 1 (b) 2 (c) 3 (d) 0

A. $\{1,9\}$

B. $\{1,9,1/81\}$

C. $\{1,4,1/81\}$

D. $\{9,1/81\}$

Answer: D

Watch Video Solution

37. Number of real values of x satisfying the equation $(\log)_2\left(x^2-x\right)(\log)_2\left(\frac{x-1}{x}\right)+\left((\log)_2x\right)^2=4, is$ 0 (b) 2 (c) 3 (d) 7

A. 0

B. 2

C. 3

D. 7

Answer: B

Watch Video Solution

38. If $xy^2 = 4$ and $\log_3(\log_2 x) + \log_{1/3}\left(\log_{1/2} y\right) = 1$, then x equals

A. 4

B. 8

C. 16

D. 64

Answer: D

Watch Video Solution

39. If $x_1 and x_2$ are the roots of the equation $e^2 x^{\ln x} = x^3$ with $x_1 > x_2$, then $x_1 = 2x_2$ (b) $x_1 = x22\ 2x_1 = x22$ (d) $x12 = x23$

A. $x_1 = 2x_2$

B. $x_1 = x_2^2$

C. $2x_1 = x_2^2$

D. $x_1^2 = x_2^3$

Answer: B

Watch Video Solution

40. The number of real values of the parameter k for which $(\log_{16} x)^2 - (\log)_{16} x + (\log)_{16} k = 0$ with real coefficients will have exactly one solution is 2 (b) 1 (c) 4 (d) none of these

A. 2

B. 1

C. 4

D. none of these

Answer: A

Watch Video Solution

41. $x^{(\log)_5 x} > 5$ implies $x \in (0, \infty)$ (b) (0,1/5)U(5,∞) (c) (2,2.5) (d) (0,2.5)

A. $x \in (0, \infty)$

B. $x \in (0, 1/5) \cup (5, \infty)$

C. $x \in (1, \infty)$

D. $x \in (1, 2)$

Answer: B

Watch Video Solution

42. If $S=\left\{x \in N: 2+(\log)_2 \sqrt{x+1}>1-(\log)_{\frac{1}{2}} \sqrt{4-x^2}\right\}$, then $(a) S=\{1\}$ (b) $S=Z$ (c) $S=N$ (d) none of these

A. $S=\{1\}$

B. S = Z

C. S = N

D. none of these

Answer: A

Watch Video Solution

43. If $S=\left\{x \in R: \left((\log)_{0.6} 0.216\right)(\log)_5(5-2x) \leq 0\right\}$, then S is equal to $(2.5, \infty)$ (b) $(2, 2.5)$ (c) $(2, 2.5)$ (d) $(0, 2.5)$

A. $[2.5, \infty)$

B. $[2, 2.5)$

C. $(2, 2.5)$

D. $(0, 2.5)$

Answer: B

Watch Video Solution

44. The solution set of inequality

$\frac{1}{2^x - 1} > \frac{1}{1 - 2^{x-1}}$ is

A. $(1, \infty)$

B. $(0, \log_2(4/3))$

C. $(-1, \infty)$

D. $(0, \log_2(4/3)) \cup (1, \infty)$

Answer: D

Watch Video Solution

45. if $\log_2 x + \log_2 y \geq 6$ then the least value of $x + y$

A. 4

B. 8

C. 16

D. 32

Answer: C

Watch Video Solution

46. Which of the following is not the solution $\log_x\left(\frac{5}{2} - \frac{1}{x}\right) > \left(\frac{5}{2} - \frac{1}{x}\right)$?

A. $\left(\frac{2}{5}, \frac{1}{2}\right)$

B. $(1, 2)$

C. $\left(\frac{2}{5}, 1\right)$

D. none of these

Answer: A :: B

Watch Video Solution

47. The solution set of the inequality $(\log)_{10}\left(x^2-16\right) \leq (\log)_{10}(4x-11)$ is $4, \infty)$ (b) $(4,5)$ (c) $\left(\frac{11}{4}, \infty\right)$ (d) $\left(\frac{11}{4}, 5\right)$

A. $(4, \infty)$

B. $(4,5]$

C. $(11/4, \infty)$

D. $\left(\frac{11}{4}, 5\right)$

Answer: B

Watch Video Solution

48. Solution set of the inequality $(\log)_{0.8}\left((\log)_6 \frac{x^2+x}{x+4}\right)<0$ is $(-4,-3)$ (b) $(-3,4)\cup(8,\infty)$ $(-3,\infty)$ (d) $(-4,-3)\cup(8,\infty)$

A. $(-4,-3)$

B. $(-3,4)\cup(8,\infty)$

C. $(-3,\infty)$

D. $(-4,-3)\cup(8,\infty)$

Answer: D

Watch Video Solution

49. Which of the following is not the solution of $(\log)_3\left(x^2-2\right)<(\log)_3\left(\frac{3}{2}|x|-1\right)$ is $(\sqrt{2},2)$ (b) $(-2,-\sqrt{2})$ $(-\sqrt{2},2$ (d) none of these

A. $(-\sqrt{2},2)$

B. $(-2,-\sqrt{2})$

C. $\left(-\sqrt{2}, 2\right)$

D. none of these

Answer: C

Watch Video Solution

50. The true solution set of inequality $\log_{x+1}\left(x^2-4\right) > 1$ is equal to

A. $(2, \infty)$

B. $\left(2, \frac{1+\sqrt{21}}{2}\right)$

C. $\left(\frac{1-\sqrt{21}}{2}, \frac{1+\sqrt{21}}{2}\right)$

D. $\left(\frac{1+\sqrt{21}}{2}, \infty\right)$

Answer: D

Watch Video Solution

Multiple Correct Answers Type

1. For $a > 0, \neq 1,$ the roots of the equation $(\log)_{ax} a + (\log)_x a^2 + (\log)_{a^2 a} a^3 = 0$ are given $a^{-\frac{4}{3}}$ (b) $a^{-\frac{3}{4}}$ (c) a (d) $a^{-\frac{1}{2}}$

A. $a^{-4/3}$

B. $a^{-3/4}$

C. a

D. $a^{-1/2}$

Answer: A::D

Watch Video Solution

2. 6/ The real solutions of the equation $2^{x+2}.5^{6-x} = 10^{x^2}$ is

A. 1

B. 2

C. $-\log_{10}(250)$

D. $\log_{10} 4 - 3$

Answer: B::C::D

Watch Video Solution

3. If $\frac{\log x}{b-c} = \frac{\log y}{c-a} = \frac{\log z}{a-b}$, then which of the following is/are true?

$zyz = 1$ (b) $x^a y^b z^c = 1$ $x^{b+c} y^{c+b} = 1$ (d) $xyz = x^a y^b z^c$

A. $xyz = 1$

B. $x^a y^b z^c = 1$

C. $x^{b+c} y^{c+a} z^{a+b} = 1$

D. $xyz = x^a y^b z^c$

Answer: A::B::C::D

Watch Video Solution

4. If $(\log)_k x \log_5 k = (\log)_x 5, k \neq 1, k > 0,$ then x is equal to k (b) 1/5 (c) 5 (d) none of these

A. k

B. $1/5$

C. 5

D. none of these

Answer: B::C

Watch Video Solution

5. If $p, q \in N$ satisfy the equation $x^{\sqrt{x}} = \left(\sqrt{x}\right)^x$, then

A. p+q=5

B. $|p - q| = 4$

C. pq=4

D. if $\log_q p$ is defined, then $\log_p q$ is not and vice versa

Answer: A::C::D

Watch Video Solution

6. Which of the following, when simplified, reduces to unity? $(\log)_{10}5\log_{10}20+\left((\log)_{10}2\right)^2$. (c) $-(\log)_5(\log)_3\sqrt{5\sqrt{9}}\,\frac{1}{6}(\log)_{\frac{\sqrt{3}}{2}}\left(\frac{64}{27}\right)$

A. $\log_{10}5\cdot\log_{10}20+(\log_{10}2)^2$

B. $\dfrac{2\log 2+\log 3}{\log 48-\log 4}$

C. $-\log_5\log_3\sqrt{\sqrt[5]{9}}$

D. $\dfrac{1}{6}\log_{\sqrt{3}/2}\left(\dfrac{64}{27}\right)$

Answer: A::B::C

Watch Video Solution

7. If $(\log)_a x = b$ for permissible values of $aandx$, then identify the statement(s) which can be correct. If $aandb$ are two irrational numbers, then x can be rational. If a is rational and b is irrational, then x can be rational. If a is irrational and b is rational, then x can be rational. If $aandb$ are rational, then x can be rational.

A. If a and b are two irrational numbers, then x can be retional.

B. If a is rational and b is irrational, then x can be rational.

C. If a is irrational and b is rational, then x can be rational.

D. If a and b are rational, then x can be rational.

Answer: A::B::C::D

Watch Video Solution

8. The number of solutions of the equation $\log_{x+1}(x-0.5) = \log_{x-0.5}(x+1)$ is

A. two real solutions

B. no prime solution

C. one integral solution

D. no irrational solution

Answer: B::C::D

Watch Video Solution

9. The equation $\sqrt{1+\log_x \sqrt{27}\log_3 x}+1=0$ has

A. no integral solution

B. one irrational solution

C. two real solutions

D. no prime solution

Answer: A::D

Watch Video Solution

10. If $\log_{1/2}(4-x) \geq \log_{1/2} 2 - \log_{1/2}(x-1)$,then x belongs to

A. $(1, 2]$

B. $[3, 4)$

C. $(1, 3]$

D. $[1, 4)$

Answer: A::B

Watch Video Solution

11. If the equation $x^{\log_a x^2} = \frac{x^{k-2}}{a^k}, a \neq 0$has exactly one solution for x, then the value of k is/are

A. $6 + 4\sqrt{2}$

B. $2 + 6\sqrt{3})$

C. $6 - 4\sqrt{2}$

D. $2-6\sqrt{3}$

Answer: A::C

Watch Video Solution

12. The set of real values of x satisfying the equation $|x-1|^{\log_3(x^2)-2\log_x(9)}=(x-1)^7$

A. $\frac{1}{\sqrt{3}}$

B. 1

C. 2

D. 81

Answer: C::D

Watch Video Solution

13. If x = 9 is one of the solutions of $\log_e\left(x^2+15a^2\right)-\log_e(a-2)=\log_e\left(\frac{8ax}{a-2}\right)$,then

A. $a=\frac{3}{5}$

B. a = 3

C. x = 15

D. x = 2

Answer: B

Watch Video Solution

14. In which of the following, $m>n(m,n\in R)$?

A. $m=(\log_2 5)^2$ and $n=\log_2 20$

B. $m=\log_{10}2$ and $n=\log_{10}\sqrt[3]{10}$

C. $m=\log_{10}5\cdot\log_{10}20$ and $n=1$

D. $m = \log_{1/2}\left(\frac{1}{3}\right)$ and $n = \log_{1/3}\left(\frac{1}{2}\right)$

Answer: A::D

Watch Video Solution

15. if $\log_{10} 5 = a$ and $\log_{10} 3 = b$ then:

A. $\log_{30} 8 = \frac{3(1-a)}{b+1}$

B. $\log_{40} 15 = \frac{a+b}{3-2a}$

C. $\log_{243} 32 = \frac{1-a}{b}$

D. none of these

Answer: A::B::C

Watch Video Solution

16. The value of $\frac{6a^{\log_e b}(\log_{a^2} b)(\log_{b^2} a)}{e^{\log_e a \cdot \log_e b}}$ is

A. independent of a

B. independent of b

C. dependent on a

D. dependent on b

Answer: A::B

Watch Video Solution

17. The inequality $\sqrt{x^{(\log)_2\sqrt{x}}} \geq 2$ is satisfied (a) by only one value of x (b) $x \in \left(0, \left(\frac{1}{4}\right)\right)$ (c)$x \in [4, \infty)$ (d) $x \in (1, 2)$

A. only one value of x

B. $x \in \left(0, \frac{1}{4}\right]$

C. $x \in [4, \infty)$

D. $x \in (1, 2)$

Answer: B::C

Watch Video Solution

18. If $3^x = 4^{x-1}$, then x = a. $\frac{2\log_3 2}{2\log_3 2 - 1}$ b. $\frac{2}{2 - \log_2 3}$ c. $\frac{1}{1 - \log_4 3}$ d. $\frac{2\log_2 3}{2\log_2 3 - 1}$

A. $\frac{2\log_3 2}{2\log_3 2 - 1}$

B. $\frac{2}{2 - \log_2 3}$

C. $\frac{1}{1 - \log_4 3}$

D. $\frac{2\log_2 3}{2\log_2 3 - 1}$

Answer: A::B::C

Watch Video Solution

Linked Comprehension Type

1. Consider the system of equations

$$\log_3(\log_2 x) + \log_{1/3}\left(\log_{1/2} y\right) = 1 \text{ and } xy^2 = 9.$$

The value of x in the interval

A. $(200, 300)$

B. $(400, 500)$

C. $(700, 800)$

D. none of these

Answer: C

Watch Video Solution

2. Consider the system of equations

$$\log_3(\log_2 x) + \log_{1/3}\left(\log_{1/2} y\right) = 1 \text{ and } xy^2 = 9.$$

The value of 1/y lies in the interval

A. $(5, 7)$

B. $(7, 10)$

C. $(11, 15)$

D. $(25, 30)$

Answer: B

Watch Video Solution

3. Consider equations $x^{\log_y x} = 2$ and $y^{\log_x y} = 16$.

The value of x is

A. $2^{\sqrt[3]{2}}$

B. $2^{\sqrt[3]{4}}$

C. $2^{\sqrt[3]{64}}$

D. $2\sqrt[3]{256})$

Answer: B

Watch Video Solution

4. Solve $x^{(\log)_y x} = 2 and y^{(\log)_x y} = 16$

A. $2^{\sqrt[3]{2}}$

B. $2^{\sqrt[3]{4}}$

C. $2^{\sqrt[3]{128}}$

D. $2^{\sqrt[3]{16}}$

Answer: D

Watch Video Solution

5. $2\left(\sqrt{\log_a(ab)^{1/4}+\log_b(ab)^{1/4}}-\sqrt{\log_a\left(\frac{b}{a}\right)^{1/4}+\log_b\left(\frac{a}{b}\right)^{1/4}}\right)\sqrt{\log_a(b)}$ =

A. 1

B. 2

C. $2^{\log_a b}$

D. $2^{\log_b a}$

Answer: B

Watch Video Solution

6. $2\left(\sqrt{\log_a(ab)^{\frac{1}{4}}+\log_b(ab)^{\frac{1}{4}}}-\sqrt{\log_a\left(\frac{b}{a}\right)^{\frac{1}{4}}+\log_b\left(\frac{a}{b}\right)^{\frac{1}{4}}}\right)\sqrt{\log_a(b)}=$

A. 1

B. 2

C. $2^{\log_a b}$

D. $2^{\log_b a}$

Answer: C

Watch Video Solution

Matrix Match Type

1. Match the following List I to List II

List I	List II
a. The smallest integer greater than $\frac{1}{\log_3 \pi} + \frac{1}{\log_4 \pi}$ is	p. 10
b. Let $3^a = 4$, $4^b = 5$, $5^c = 6$, $6^d = 7$, $7^e = 8$, and $8^f = 9$. Then the value of the product $(abcdef)$ is	q. 3
c. Characteristic of the logarithm of 2008 to the base 2 is	r. 1
d. If $\log_2(\log_2(\log_3 x)) = \log_2(\log_3(\log_2 y)) = 0$, then the value of $(x - y)$ is	s. 2

Watch Video Solution

2. Match the following List I to List II

List I	LIst II
a. $2^{\log_{(2\sqrt{2})} 15}$ is	p. rational
b. $\sqrt[3]{\left(5^{1/\log_7 5} + \frac{1}{\sqrt{(-\log_{10} 0.1)}}\right)}$ is	q. irrational
c. $\log_3 5 \cdot \log_{25} 27$ is	r. composite
d. Product of roots of equation $x^{\log_{10} x} = 100x$ is	s. prime

Watch Video Solution

3.

List I	List II
a. The value of $\log_2 \log_2 \log_4 256 - \log_{\sqrt{2}} 4$ is	p. 1
b. If $\log_3 (5x-2) - 2\log_3 \sqrt{3x+1} = 1 - \log_3 4$, then $x =$	q. 6
c. Product of roots of the equation $7^{\log_7 (x^2-4x-5)} = (x-1)$ is	r. 3
d. Number of integers satisfying $\log_2 \sqrt{x} - 2(\log_{\frac{1}{4}} x)^2 - 1 > 0$ are	s. 5

A. $\begin{matrix} a & b & c & d \\ s & p & q & r \end{matrix}$

B. $\begin{matrix} a & b & c & d \\ s & p & q & r \end{matrix}$

C. $\begin{matrix} a & b & c & d \\ q & r & p & s \end{matrix}$

D. $\begin{matrix} a & b & c & d \\ r & p & q & s \end{matrix}$

Answer: A

View Text Solution

Numerical Value Type

1. If $\log_a b = 2, \log_b c = 2,$ and $\log_3 c = 3 + \log_3$ a,then the value of c/(ab)is _____.

Watch Video Solution

2. The value of $(\log_{10} 2)^3 + \log_{10} 8 \cdot \log_{10} 5 + (\log_{10} 5)^3$ is _____.

Watch Video Solution

3. If $\log_4 A = \log_6 B = \log_9(A + B),$ then $[4(B/A)]$(where $[\cdot]$ represents the greatest integer function) equals _____.

Watch Video Solution

4. Integral value of x which satisfies the equation $= \log_6 54 + (\log)_x 16 = (\log)_{\sqrt{2}} x - (\log)_{36}\left(\frac{4}{9}\right) is..$

Watch Video Solution

5. If $a = \log_{245} 175$ and $b = \log_{1715} 875$, then the value of $\dfrac{1-ab}{a-b}$ is _____.

Watch Video Solution

6. The difference of roots of the equation $\left(\log_{27} x^3\right)^2 = \log_{27x^6}$ is _____.

Watch Video Solution

7. Sum of integral values of x satisfying the inequality $3^{\left(\frac{5}{2}\right)\log_3(12-3x)} - 3^{\log_2(x)} > 32$

Watch Video Solution

8. The least integer greater than $\log_2 15 \cdot \log_{1/62 \cdot \log_3 1/6}$ is _____.

Watch Video Solution

9. The reciprocal of $\frac{2}{\log_4 (2000)^6} + \frac{3}{\log_5 (2000)^6}$ is _____.

Watch Video Solution

10. Sum of integers satisfying $\sqrt{\log_2 x - 1} - 1/2 \log_2 \left(x^3\right) + 2 > 0$ is _____.

Watch Video Solution

11. Number of integers satisfying the inequality $\log_{1/2} |x - 3| > -1$ is _____.

Watch Video Solution

12. Number of integers ≤ 10 satisfying the inequality $2 \log_{1/2}(x - 1) \leq \frac{1}{3} - \frac{1}{\log_{x^2 - x} 8}$ is _____.

Watch Video Solution

13. The value of $\left(\sqrt{3+2\sqrt{2}}+\sqrt{3-2\sqrt{2}}\right)^{2^9}$ is _____.

Watch Video Solution

14. The value of $5^{(\log)_{\frac{1}{5}}\left(\frac{1}{2}\right)}+(\log)_{\sqrt{2}}\frac{4}{\sqrt{7}+\sqrt{3}}+(\log)_{\frac{1}{2}}\frac{1}{10+2\sqrt{21}}$ is.....

Watch Video Solution

15. The value of $N=\frac{(\log)_5 250}{(\log)_{50}5}-\frac{(\log)_5 10}{(\log)_{1250}5}$ is.....

Watch Video Solution

16. if $x+\log_{10}(1+2^x)=x\log_{10}5+\log_{10}6$ then x

Watch Video Solution

17. The x, y, z are positive real numbers such that $(\log)_{2x} z = 3, (\log)_{5y} z = 6, and (\log)_{xy} z = \frac{2}{3},$ then the value of $\left(\frac{1}{2z}\right)$ is .....

Watch Video Solution

18. If $a = (\log)_{12} 18, b = (\log)_{24} 54,$ then find the value of $ab + 5(a - b)$.

Watch Video Solution

19. The value of

$$6 + \log_{3/2}\left(\frac{1}{3\sqrt{2}}\sqrt{4 - \frac{1}{3\sqrt{2}}\sqrt{4 - \frac{1}{3\sqrt{2}}\sqrt{4 - \frac{1}{3\sqrt{2}}\ldots}}}\right)$$ is _____.

Watch Video Solution

20. The value of $\left((\log_2 9)^2\right)^{\frac{1}{\log_2(\log_2 9)}} \times (\sqrt{7})^{\frac{1}{\log_4 7}}$ is _____.

Watch Video Solution

Jee Main

1. the equation $e^{\sin x} - e^{-\sin x} - 4 = 0$ has.

A. infinite number of real roots

B. no real roots

C. exactly one real root

D. exactly four real roots

Answer: B

Watch Video Solution

Jee Advanced

1. Let (x_0, y_0) be the solution of the following equations In $(2x)^{In2} = (3y)^{\ln 3}$ and $3^{\ln x} = 2^{\ln y}$ Then x_0 is

A. $\frac{1}{6}$

B. $\frac{1}{3}$

C. $\frac{1}{2}$

D. 6

Answer: C

Watch Video Solution