



## MATHS

### BOOKS - CENGAGE MATHS (HINGLISH)

#### BINOMIAL THEOREM

#### Question Bank

1. Let  $P$  be the  $7^{\text{th}}$  term from the beginning and  $Q$  be the  $7^{\text{th}}$  term from

the end in the expansion of  $\left( \left( \sqrt[3]{3} + \frac{1}{\sqrt[3]{4}} \right)^n \right)$  where  $n \in N$ . If  $12P = Q$ ,

then find the value of  $n$ .



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2. In the expansion of  $(2 - 3x)^{19}$  if  $r^{\text{th}}$  term has algebraically least coefficient then  $r$  is

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3. The value of  $\sum_{0 \leq i \leq j \leq 5} \binom{5}{j} \binom{j}{i}$  is equal to

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4. Let coefficient of  $x^2$  and  $x^3$  in the expansion of  $(3 + ax)^9$  are equal. If  $a$  lies between the roots of the equation  $49x^2 + 7px - 9 = 0$ , then the range of  $p$  is  $(-\infty, -\lambda)$ . Find the value of  $\lambda$ .

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5. The sum of the series

$$\frac{\binom{101}{C_1}}{\binom{101}{C_0}} + \frac{2 \cdot \binom{101}{C_2}}{\binom{101}{C_1}} + 3 \cdot \frac{\binom{101}{C_3}}{\binom{101}{C_2}} \text{ equals}$$

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6. Number of terms in the expansion of  $\left(\frac{x^1}{3} + \frac{x^2}{5}\right)^{40}$  with integral power of  $x$  is equal to

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7. If fifth term is numerically greatest term in expansion of  $\left(5 + \frac{x}{2}\right)^{11}$  then total number of possible integral values of  $x$  is

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8. If  $N = (6 + \sqrt{34})^7$ , then digit at unit's place of  $(N(1 - \{N\}))^{10}$ , (where  $\{ \}$  denotes fractional part function), is equal to

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9. If  ${}^6C_0 + {}^7C_0 + {}^8C_0 + \dots + {}^{13}C_0 = m$  (where  $m < 20$ ) then the value of  $(m-r)$  is equal to .

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10. If  $T = \sum_{r=1}^{18} \frac{(-1)^{r-1} \cdot r^{18} \cdot {}^{18}C_r}{r+1}$  then  $(1/T) - 10$  is equal to

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11. If  $T = \sum_{k=2006}^{2013} {}^k C_{2006}$  simplifies  ${}^n C_p$  where  $o$  is prime, then  $(n+p)$  is

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12. If  $(7 + x + x^2)^{25} = a_0 + a_1x + a_1x^2 + \dots + a_{50+x^{50}}$ , then  $(a_0 + a_1 + a_2 + \dots + a_{50})$  is

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13. Let number of dissimilar terms in the expansion of  $(x + y + z)^{25}$  is  $\lambda$ , then  $|\lambda - u|$  is (where  $u > 5$ ).

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14. Coefficient of  $t^{12}$  in  $(1 + t^2)^6(1 + t^6)(1 + t^{12})$  is

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15. Coefficient of  $x^{12}$  in  $(1 + x^3)^5(1 + x^4)^8(1 + x^5)^{11}$  is

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16. If  $l, m, n$  are in A.P., then the sum of coefficients of  $(1 + (lx^2 - 2m...x + n)^{2014})^{2015}$  when expanded in powers of  $x$  is

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17. If

$1 \binom{2014}{1} \binom{2013}{2013} + 2 \binom{2014}{2} \binom{2013}{2012} + 3 \binom{2014}{3} \binom{2013}{2011} + \dots + 2014 \binom{2014}{2014} \binom{2013}{0} =$   
 $2014 \binom{4026}{\lambda}$  then  $\sum$  of all digits of  $\lambda$  is.

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18. Number of terms containing integral powers of 'x' is expansion of  $(1 + 2\sqrt{x})^{40}$  is

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19. Let  $(1+x^2)^2(1+x)^n = A_0 + A_1 x + A_2 x^2 + \dots$ . If  $A_0, A_1, A_2$  are in A.P. then the value of  $n$  is

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20. If the second term of the expansion  $\left[ \frac{a^1}{13} + \frac{a}{\sqrt{a^{-1}}} \right]^n$  is  $14 \frac{a^5}{2}$  then the value of  ${}^n C_3$  is

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21. The sum of the roots (real or complex) of the equation  $x^{2001} + \left( \frac{1}{2} - x \right)^{2001} = 0$  is

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22. The last two digits of the number  $3^{400}$  are

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23. Sum of all the rational terms in the expansion of  $\left(\frac{3^1}{4} + \frac{4^1}{3}\right)^2$ , is

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24. The sum of rational terms in the binomial expansion of  $\left(\sqrt{2} + \sqrt[3]{5}\right)^{10}$  is

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25. If  $1 + x^4 + x^5 = \sum_{I=0}^5 a_i(1+x)^i$ , for all  $x \in R$ , then absolute value of  $a_2$  is equal to

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26. If the coefficient of  $x^{100}$  in  $1 + (1 + x) + (1 + x)^2 + \dots + (1+x)^n$ , ( $n \geq 100$ ) is  ${}^{(201)}C_{101}$ , then  $n$  is equal to

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27. The digit at unit place in the coefficient of  $x^{50}$  in the product  $(1 - x)^{50} (1 - (1 - x)^2)^{50}$  is

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28. The total number of terms in the product  $\left( {}^{101}C_0 - {}^{101}C_1x + {}^{101}C_2x^2 - \dots - {}^{(101)}C_{101}x^{101} \right) (1 + x + x^2 + \dots)$

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29. If the constant term in the binomial expansion of  $\left(x^2 - \frac{1}{x}\right)^n$ ,  $n \in N$  is 15 then the value of  $n$  is equal to

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30. Consider a sequence of 1001 terms as  $\frac{{}^{1001}C_0}{1.2.3.4}$ ,  $\frac{{}^{1001}C_1}{2.3.4.5}$ ,  $\frac{{}^{100}C_2}{3.4.5.6}$ ,  $\dots$ ,  $\frac{{}^{1001}C_{1000}}{1001.1002.1003.1004}$  If  $n^{\text{th}}$  term is greatest term of sequence then  $n$  is equal to-

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31. Coefficient of  $x^6$  in  $(1+x)(1+x^2)^2(1+x^3)^3 \dots (1+x^n)^n$  is

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