



# MATHS

# **BOOKS - NCERT EXEMPLAR**

# **RATIONAL NUMBERS**

**Solved Examples** 

1. In Examples 1 to 4, there are four options,

out of which one is correct.

Choose the correct one.

Which of the following rational numbers is

equivalent to  $\frac{2}{3}$ ?

A. 
$$\frac{3}{2}$$
  
B.  $\frac{4}{9}$   
C.  $\frac{4}{6}$   
D.  $\frac{9}{4}$ 

Answer: C

**2.** there are four options, out of which one is correct.

Choose the correct one.

Which of the following rational numbers is in

standard form?

A. 
$$\frac{20}{30}$$
  
B.  $\frac{10}{4}$   
C.  $\frac{1}{2}$   
D.  $\frac{1}{-3}$ 

Answer: C



3. In Examples 1 to 4, there are four options,

out of which one is correct.

Choose the correct one.

The sum of 
$$\frac{-3}{2}$$
 and  $\frac{1}{2}$  is

A.-1

- $\mathsf{B.}-2$
- C.4

#### Answer: A



**4.** In Examples 1 to 4, there are four options, out of which one is correct.

Choose the correct one.

The value of 
$$-rac{4}{3}-rac{-1}{3}$$
 is

A.-2

B.-3

 $\mathsf{D}.-1$ 

#### Answer: D

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**5.** In Examples 5 and 6, fill in the blanks to make the statements true.

There are \_\_\_\_\_ number of rational numbers

between two rational numbers.

6. In Examples 5 and 6, fill in the blanks to make the statements true.The rational number \_\_\_\_\_ is neither

positive nor negative.

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7. state whether the statements are True or

False.

In any rational number  $\frac{p}{q}$ , denominator is

always a nonzero integer.

**8.** state whether the statements are True or False.

"To reduce the rational number to its standard

form, we divide its numerator and

denominator by their HCF".

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9. state whether the statements are True or

False.

"All rational numbers are integers".



11. Which of the following pairs represent

equivalent rational numbers ?

 $\frac{7}{12}$  and  $\frac{28}{48}$ 



complete the pattern:

$$\frac{-1}{3}, \frac{-2}{6}, \frac{-3}{9}, \dots, \dots, \dots, \dots$$

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**14.** Find the sum of 
$$-4\frac{5}{6}$$
 and  $-7\frac{3}{4}$ .

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**15.** Find the product of 
$$-2\frac{3}{4}$$
 and  $5\frac{6}{7}$ .

**16.** Match column I to column II in the following:

Column I Column II  $(i)\frac{3}{4} \div \frac{3}{4}$  (a) - 1  $(ii)\frac{1}{2} \div \frac{4}{4}$   $(b)\frac{-2}{3}$   $(iii)\frac{2}{3} \div (-1)$   $(c)\frac{3}{2}$   $(iv)\frac{3}{4} \div \frac{1}{2}$   $(d)\frac{3}{8}$  $(v)\frac{5}{7} \div (\frac{-5}{7})$  (e)1

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17. Find the reciprocal of 
$$rac{2}{11}+-rac{5}{55}.$$

## Exercise

**1.** A rational number is defined as a number that can be expressed in the form  $\frac{p}{q}$ , where p and q are integers and

A. 
$$q = 0$$

$$\mathsf{B.}\,q=1$$

 $\mathsf{C}.\,q\neq 1$ 

D. 
$$q 
eq 0$$



# **2.** Which of the following rational numbers is positive?

A. 
$$\frac{-8}{7}$$
  
B.  $\frac{19}{-13}$   
C.  $\frac{-3}{-4}$   
D.  $\frac{-21}{13}$ 



**3.** Which of the following rational numbers is negative?

A. 
$$-\left(\frac{-3}{7}\right)$$
  
B.  $\frac{-5}{-3}$   
C.  $\frac{9}{8}$   
D.  $\frac{3}{-7}$ 



**4.** In the standard form of a rational number, the common factor of numerator and denominator is always:

A. 0

B. 1

#### $\mathsf{C}.-2$

D. 2





# **5.** Which of the following rational numbers is equal to its reciprocal?

A. 1

B. 2 C.  $\frac{1}{2}$ D. 0



**6.** The reciprocal of 
$$\frac{1}{2}$$
 is

A. 3

B. 2

 $\mathsf{C}.-1$ 

D. 0

#### **Answer:**



# — ;

#### Answer:



**8.** Which of the following is equivalent to  $\frac{4}{5}$ ?

A. 
$$\frac{5}{4}$$
  
B.  $\frac{16}{25}$   
C.  $\frac{16}{20}$   
D.  $\frac{15}{25}$ 

#### **Answer:**

**9.** How many rational numbers are there between two rational numbers?

A. 1

B. 0

C. unlimited

D. 100

#### Answer:

10. In the standard form of a rational number,

the denominator is always a

A. 0

B. negative integer

C. positive integer

D. 1

Answer: C

**11.** To reduce a rational number to its standard we divide its numerator form, and denominator by their A. LCM B. HCF C. product D. multiple

Answer: B



**12.** Which is greater number in the following:

A. 
$$\frac{-1}{2}$$
  
B. 0  
C.  $\frac{1}{2}$ 

D. -2



13. fill in the blanks to make the statements



**14.** fill in the blanks to make the statements true.

1 is a \_\_\_\_\_ rational number.

15. fill in the blanks to make the statements

٠

true.

The standard form of 
$$rac{-8}{-36}$$
 is \_\_\_\_\_

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# 16. fill in the blanks to make the statements

true.

The standard form of 
$$rac{18}{-24}$$
 is \_\_\_\_ .

**17.** fill in the blanks to make the statements true.

On a number line,  $\frac{-1}{2}$  is to the \_\_\_\_ of zero (0).



18. fill in the blanks to make the statements

true.

On a number line, 
$$rac{4}{3}$$
 is to the \_\_\_ of zero (0).

19. fill in the blanks to make the statements

true.

$$-rac{1}{2}$$
 is \_\_\_\_ than  $rac{1}{5}$ 



20. fill in the blanks to make the statements

true.

$$-rac{3}{5}$$
 is \_\_\_ than 0.

21. fill in the blanks to make the statements

true.

 $\frac{-16}{24}$  and  $\frac{20}{-16}$  represent \_\_\_\_ rational

numbers.



22. fill in the blanks to make the statements

true.

$$\frac{-27}{45}$$
 and  $\frac{-3}{5}$  represent \_\_\_\_ rational

numbers.

**23.** fill in the blanks to make the statements true.

Additive inverse of  $\frac{2}{3}$  is \_\_\_\_\_.

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24. fill in the blanks to make the statements

true.

$$rac{-3}{5} + rac{2}{5} = ----.$$

#### 25. fill in the blanks to make the statements

true.

$$\frac{-5}{6} + \frac{-1}{6} = -----.$$

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26. fill in the blanks to make the statements

true.

$$rac{3}{4} imes \left(rac{-2}{3}
ight)=$$
 \_\_\_\_\_.

27. fill in the blanks to make the statements

true.

$$rac{-5}{3} imes \left(rac{-3}{5}
ight) = ----$$



#### 28. fill in the blanks to make the statements

true.

$$\frac{-6}{7} = \frac{-}{42}$$



**29.** fill in the blanks to make the statements true.  $\frac{1}{2} = \frac{6}{-}$ 

## 30. fill in the blanks to make the statements

true.

$$\frac{-2}{9} - \frac{7}{9} =$$
\_\_\_\_\_

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31. fill in the boxes with the correct symbol >,<





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# **32.** fill in the boxes with the correct symbol >,<

or =.

$$rac{3}{7}$$
  $\Box$   $rac{-5}{6}$ 

33. fill in the boxes with the correct symbol >,<



$$\frac{5}{6}$$
  $\Box$   $\frac{8}{4}$ 



# 34. fill in the boxes with the correct symbol >,<

$$rac{-9}{7}$$
  $\Box$   $rac{4}{-7}$ 



# **35.** fill in the boxes with the correct symbol >,<



$$\frac{8}{8}$$
  $\Box$   $\frac{2}{2}$ 



**36.** The reciprocal of \_\_\_\_\_ does not exist.



**37.** The reciprocal of 1 is \_\_\_\_\_.




**38.** 
$$\frac{-3}{7} \div \left(\frac{-7}{3}\right) =$$
\_\_\_\_\_.

**39.** 
$$0 \div \left(\frac{-5}{6}\right) =$$
\_\_\_\_\_

**40.** 
$$0 \times \left(\frac{-5}{6}\right) =$$
\_\_\_\_\_.

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41. \_\_\_\_ 
$$\times \left(\frac{-2}{5}\right) = 1.$$
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#### 42. The standard form of rational number -1

is \_\_\_\_\_.

**43.** If m is a common divisor of a and b, then





**45.** Two rational numbers are said to be equivalent or equal, if they have the same \_\_\_\_\_ form.



**46.** If 
$$\frac{p}{q}$$
 is a rational number, then q cannot be

**47.** State whether the statements given are True or False.

Every natural number is a rational number but

every rational number need not be a natural

number.



### **48.** State whether the statements given are

True or False.

Zero is a rational number.



**49.** State whether the statements given are True or False.

Every integer is a rational number but every

rational number need not be an integer.

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**50.** State whether the statements given are True or False.

Every negative integer is not a negative

rational number.



51. State whether the statements given are

True or False.

If  $\frac{p}{q}$  is a rational number and m is a non-zero integer, then  $\frac{p}{q} = \frac{p \times m}{q \times m}$ 

52. State whether the statements give are True

or False.

If  $\frac{p}{q}$  is a rational number and m is a non-zero common divisor of p and q, then  $\frac{p}{q} = \frac{p \div m}{q \div m}$ 

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**53.** State whether the statements given are True or False.

In a rational number, denominator always has

to be a non-zero integer.



**54.** State whether the statements given are True or False.

If  $\frac{p}{q}$  is a rational number and m is a non-zero integer, then  $\frac{p \times m}{q \times m}$  is a rational number not equivalent to  $\frac{p}{q}$ .

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**55.** State whether the statements given are True or False.

Sum of two rational numbers is always a

rational number.



56. State whether the statements given are

True or False.

All decimal numbers are also rational numbers.

57. State whether the statements given are

True or False.

The quotient of two rationals is always a

rational number.

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58. State whether the statements given are

True or False.

Every fraction is a rational number.

**59.** State whether the statements given are True or False.

Two rationals with different numerators can never be equal.

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**60.** State whether the statements given are True or False.

8 can be written as a rational number with any

integer as denominator.



**62.** State whether the statements given are True or False.



63. State whether the statements given are

True or False.

The rational numbers 
$$\frac{-12}{-5}$$
 and  $\frac{-7}{17}$  are on

the opposite sides of zero on the number line.

64. State whether the statements given are

True or False.

Every rational number is a whole number.



65. State whether the statements given are

True or False.

Zero is the smallest rational number.

#### 66. Match the following:

Column I (i)  $\frac{a}{b} \div \frac{a}{b}$  (a)  $\frac{-a}{b}$ (ii)  $\frac{a}{b} \div \frac{c}{d}$  (b) - 1 (iii)  $\frac{a}{b} \div (-1)$  (c) 1 (iv)  $\frac{a}{b} \div \frac{-a}{b}$  (d)  $\frac{bc}{ad}$ (v)  $\frac{b}{a} \div \left(\frac{d}{c}\right)$  (e)  $\frac{ad}{bc}$ 

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**67.** Write each of the following rational numbers with positive denominators:  $\frac{5}{-18}, \frac{15}{-28}, \frac{-17}{-13}.$ 





-80

**70.** Reduce each of the following rational numbers in its lowest form:

 $\frac{-60}{72}$ 

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#### 71. Reduce each of the following rational

numbers in its lowest form:

- 91
- -364



## **72.** Express each of the following rational numbers in its standard form:

- -12
- -30



#### 73. Express each of the following rational

numbers in its standard form:

-49

#### 74. Express each of the following rational

numbers in its standard form:

$$\frac{-15}{35}$$



#### 75. Express each of the following rational

numbers in its standard form:

299

-161



78. Represent the following rational numbers

on a number line: 
$$\frac{3}{8}, \frac{-7}{3}, \frac{22}{-6}$$

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80. Give three rational numbers equivalent to:

$$\frac{-3}{4}$$



83. Write the next three rational numbers to

complete the pattern:

$$\frac{-8}{7}, \frac{-16}{14}, \frac{-24}{21}, \frac{-32}{28}, \dots, \dots, \dots$$

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## **84.** List four rational numbers between $\frac{5}{7}$ and $\frac{7}{8}$ .

85. Find the sum of

$$\frac{8}{13}$$
 and  $\frac{3}{11}$ 

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$$\frac{7}{3}$$
 and  $\frac{-4}{3}$ 

<b>87.</b> Solve:			
29		30	
4		7	

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**89.** Find the product of:

$$\frac{-4}{5}$$
 and  $\frac{-5}{12}$ 

90. Find the product of:

$$\frac{-22}{11}$$
 and  $\frac{-21}{11}$ 





$$\frac{3}{7} \div \left(\frac{21}{-55}\right)$$





96. Which is greater in the following?

$$-3rac{5}{7}, 3rac{1}{9}$$

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**97.** Write a rational number in which the numerator is less than -7 imes 11 and the denominator is greater than 12 + 4.

**98.** If  $x = \frac{1}{10}$  and  $y = \frac{-3}{8}$ . then evaluate

x+y, x-y, x imes y and  $x \div y$ .

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#### 99. Find the reciprocal of the following:

$$\left(rac{1}{2} imesrac{1}{4}
ight)+\left(rac{1}{2} imes 6
ight)$$

**100.** Find the reciprocal of the following:

 $\frac{20}{51}\times\frac{4}{91}$ 

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#### **101.** Find the reciprocal of the following:

$$\frac{3}{13} \div \frac{-4}{65}$$

**102.** Find the reciprocal of the following:

$$\left(\,-5 imesrac{12}{15}
ight)-\left(\,-3 imesrac{2}{9}
ight)$$

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### **103.** Complete the following table by finding the sums:

+	$-\frac{1}{9}$	$\frac{4}{11}$	$\frac{-5}{6}$
$\frac{2}{3}$			
$-\frac{5}{4}$		$\frac{-39}{44}$	
$-\frac{1}{3}$			. (

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# **104.** Write each of the following numbers in the form $\frac{p}{q}$ , where p and q are integers: six-eighths





**106.** Write each of the following numbers in the form  $\frac{p}{q}$ , where p and q are integers: opposite of 1







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**108.** Write each of the following numbers in the form  $\frac{p}{q}$ , where p and q are integers: zero


**109.** Write each of the following numbers in the form  $\frac{p}{q}$ , where p and q are integers: opposite of three-fifths





**111.** Given that  $\frac{p}{q}$  and  $\frac{r}{s}$  are two rational numbers with different denominators and both of them are in standard form. To compare these rational numbers we say that:  $rac{\Box}{\Box} \ < \ rac{\Box}{\Box}$  . If p imes s < r imes q**Watch Video Solution 112.** Given that  $\frac{p}{q}$  and  $\frac{r}{s}$  are two rational numbers with different denominators and both of them are in standard form. To compare these rational numbers we say that:

$$rac{p}{q}=rac{r}{s}$$
, if \_\_\_\_ = \_\_\_\_

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**113.** Given that  $\frac{p}{q}$  and  $\frac{r}{s}$  are two rational numbers with different denominators and both of them are in standard form. To compare these rational numbers we say that:  $\frac{\Box}{\Box} > \frac{\Box}{\Box}$ , if  $p \times s > r \times q$ 

114. In each of the following cases, write the rational number whose numerator and denominator are respectively as under: 5 - 39 and 54 - 6

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**115.** In each of the following cases, write the rational number whose numerator and denominator are respectively as under:

$$(-4) imes 6 ext{ and } 8 \div 2$$



**116.** In each of the following cases, write the rational number whose numerator and denominator are respectively as under:  $35 \div (-7)$  and 35 - 18

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**117.** In each of the following cases, write the rational number whose numerator and

denominator are respectively as under:

25 + 15 and  $81 \div 40$ 



118. Write the following as rational numbers in

their standard forms:

35%



119. Write the following as rational numbers in

their standard forms:

1.2



# 120. Write the following as rational numbers in

their standard forms:

$$-6\frac{3}{7}$$

121. Write the following as rational numbers in

their standard forms:

 $240 \div (-840)$ 

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# 122. Write the following as rational numbers in

their standard forms:

 $115 \div 207$ 

123. Find a rational number exactly halfway

between:

$$\frac{-1}{3}$$
 and  $\frac{1}{3}$ 

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# 124. Find a rational number exactly halfway

between:

 $\frac{1}{6}$  and  $\frac{1}{9}$ 

125. Find a rational number exactly halfway



$$\frac{5}{-13}$$
 and  $\frac{-7}{9}$ 



## 126. Find a rational number exactly halfway

between:

$$\frac{1}{15}$$
 and  $\frac{1}{12}$ 

**127.** Taking  $x = \frac{-4}{9}, y = \frac{5}{12}$  and  $z = \frac{7}{18}$ , find:

the rational number which when added to x gives y.



**128.** Taking 
$$x = \frac{-4}{9}, y = \frac{5}{12}$$
 and  $z = \frac{7}{18}$ ,

find:

the rational number which subtracted from y gives z.

**129.** Taking 
$$x = \frac{-4}{9}, y = \frac{5}{12}$$
 and  $z = \frac{7}{18}$ , find:

the rational number which when added to z

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gives us x.



the rational number which when multiplied by

y to get x.

**131.** Taking 
$$x = \frac{-4}{9}, y = \frac{5}{12}$$
 and  $z = \frac{7}{18}$ ,

find:

the reciprocal of x + y.

**132.** Taking  $x = \frac{-4}{9}, y = \frac{5}{12}$  and  $z = \frac{7}{18}$ ,

find:

the sum of reciprocals of x and y.

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**133.** Taking  $x = \frac{-4}{9}, y = \frac{5}{12}$  and  $z = \frac{7}{18}$ , find:

 $(x \div y) imes z$ 

**134.** Taking  $x = \frac{-4}{9}, y = \frac{5}{12}$  and  $z = \frac{7}{18}$ , find: (x - y) + z

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**135.** Taking 
$$x = \frac{-4}{9}, y = \frac{5}{12}$$
 and  $z = \frac{7}{18}$ , find:

$$x + (y + z)$$

136. Taking  $x = \frac{-4}{9}, y = \frac{5}{12}$  and  $z = \frac{7}{18}$ , find:  $x \div (y \div z)$ 

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**137.** Taking 
$$x = \frac{-4}{9}, y = \frac{5}{12}$$
 and  $z = \frac{7}{18}$ , find:  
 $x - (y + z)$ 





**142.** From a rope 68 m long, pieces of equal size are cut. If length of one piece is  $4\frac{1}{4}$ m, find the number of such pieces.



#### 143. If 12 shirts of equal size can be prepared

from 27m cloth, what is length of cloth

required for each shirt?

144. Insert 3 equivalent rational numbers

between

$$\frac{-1}{2}$$
 and  $\frac{1}{5}$ 

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# 145. Insert 3 equivalent rational numbers

between

0 and -10

#### **146.** Put the (right tick), wherever applicable

Number	Natural Number	Whole Number	Integer	Fraction	Rational Number
(a) – 114					
(b) <sup>19</sup> / <sub>27</sub>		6		S	
(c) $\frac{623}{1}$	. (	$\langle \cdot \rangle$	5		
(d) -19 <mark>3</mark>		Ĭ,Õ	Z		
(e) $\frac{73}{71}$	0	2Ì			
(f) O	Q V				

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**147.** 'a' and 'b' are two different numbers taken from the numbers 1 – 50. What is the largest value that  $\frac{a-b}{a+b}$  can have? What is the largest value that  $\frac{a+b}{a-b}$  can have?





**148.** 150 students are studying English, Maths or both. 62 per cent of the students are studying English and 68 per cent are studying Maths. How many students are studying both?



**149.** A body floats  $\frac{2}{9}$  of its volume above the surface. What is the ratio of the body

submerged volume to its exposed volume? Re-

write it as a rational number.



150. Find the odd one out of the following and

give reason.

A. 
$$\frac{4}{3} \times \frac{3}{4}$$
  
B.  $\frac{-3}{2} \times \frac{-2}{3}$   
C.  $2 \times \frac{1}{2}$   
D.  $\frac{-1}{3} \times \frac{3}{1}$ 



**151.** Find the odd one out of the following and give reason.

A. 
$$\frac{4}{-9}$$
  
B.  $\frac{-16}{36}$   
C.  $\frac{-20}{-45}$   
D.  $\frac{28}{-63}$ 



**152.** Find the odd one out of the following and give reason.

A. 
$$\frac{-4}{3}$$
  
B.  $\frac{-7}{6}$   
C.  $\frac{-10}{3}$   
D.  $\frac{-8}{7}$ 



**153.** Find the odd one out of the following and give reason.

A. 
$$\frac{-3}{7}$$
  
B.  $\frac{-9}{15}$   
C.  $\frac{+24}{20}$   
D.  $\frac{+35}{25}$ 



**154.** What's the Error? Chhaya simplified a rational number in this manner  $\frac{-25}{-30} = \frac{-5}{6}$ .

What error did the student make?

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**Think And Discuss** 

**1.** Give an example of two or more rational numbers whose denominators with no common factors.

2. Tell if 
$$-2rac{1}{5}-\left(-2rac{3}{16}
ight)$$
 is positive or

negative. Explain.

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**3.** Explain how to add  $2\frac{2}{5} + 9\frac{1}{2}$ , without first

writing them as improper fractions.



4. Explain how you can be sure that a fraction

is simplified.



**5.** Give the sign of a rational number in which the numerator is negative and the denominator is negative.

A. negative

B. positive

C. can not determine

D. none of the above

Answer: B





1. Moving from start to finish by going from

smaller to bigger rational numbers.



**2.** Three monkeys are climbing upstairs. They can only move ahead if they eat a banana with

the common factor of their numerator and denominator on it. Which of the three monkeys will be able to reach till the end?

