

MATHS

BOOKS - NAND LAL PUBLICATION

THE TRIANGLE AND ITS PROPERTIES

Try These

1. Can you name the angle opposite to the sides AB in a triangle ABC?



2. Write the six elements (i.e., the 3 sides and the 3 angles) of \triangle ABC



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3. Write the:

Side opposite to the vertex Q of $\ riangle \ PQR$



4. Write the:

Angle opposite to the side LM of $\ riangle \ LMN$



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5. Write the:

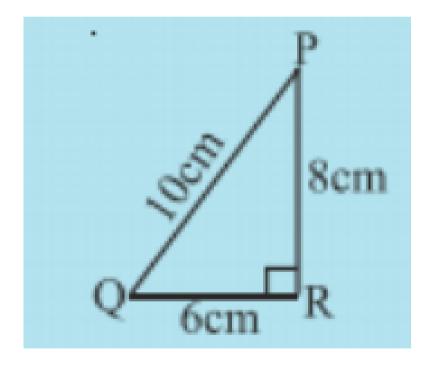
Vertex opposite to the side RT of $\ \triangle \ RST$



6. Look at fig and classify each of the triangles according to its

Sides

Angles





7. An exterior angle of a triangle is of measure 70° and one of its interior opposite angles is of measure 25° . Find the measure of interior opposite angle.

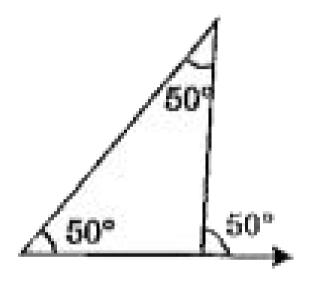


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8. The two interior opposite angles of an exterior angles of a triangle are 60° and 80° . Find the measure of the exterior angle.



9. Is something wrong in this diagram (fig 6.12)? Comment





10. Two angles of a triangle are 30° and 80° . Find the third angle.



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11. One of the angles of a triangge is 80° and the other two angles are equal. Find the measure of each of the equal angles.



12. The three angles of a triangle are in the ratio 1:2:1. Find all the angles of the triangle. Classify the triangle in two different ways.

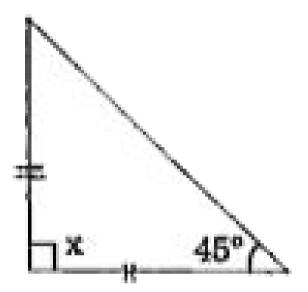


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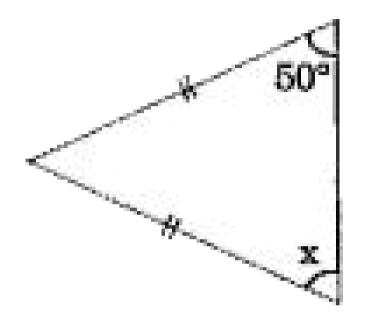
13. Find angle x in each figure



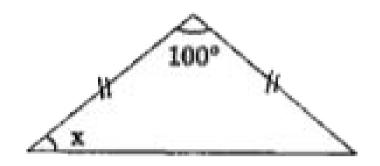




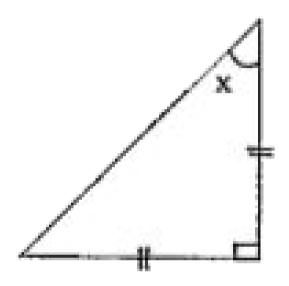




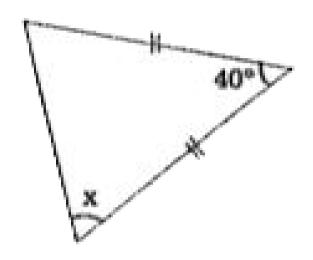








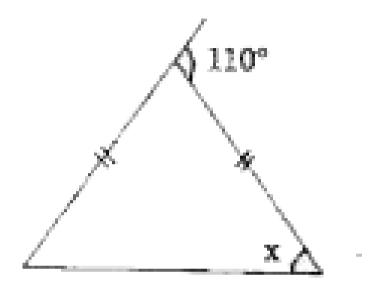




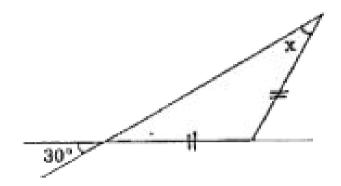








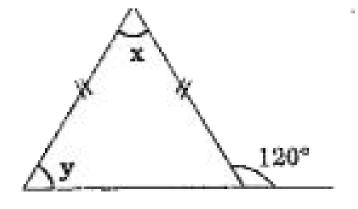






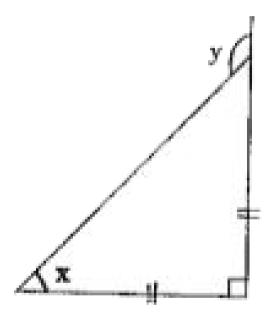
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22. Find angles x and y in each figure



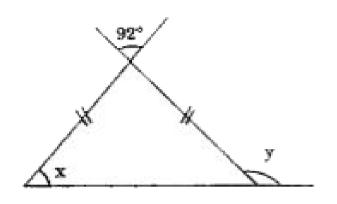


23. Find angles x and y in each figure





24. Find angles x and y in each figure

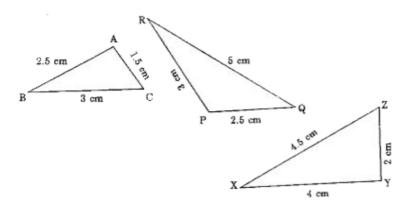




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25. Draw any three triangles, say $\Delta ABC, \Delta PQR \text{ and } \Delta XYZ$ in your

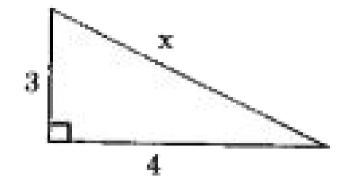
notebook. (fig. 6.22)





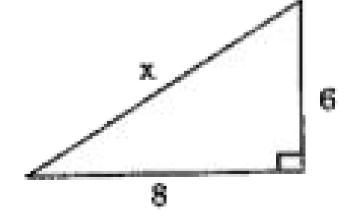
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26. Find the unknown length x in the following figure (fig.6.29)





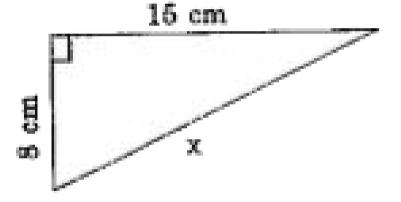
27. Find the unknown length x in the following figure (fig.6.29)





28. Find the unknown length x in the following

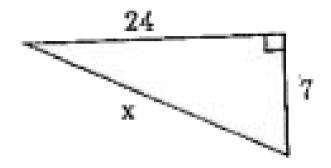
figure (fig.6.29)





29. Find the unknown length x in the following

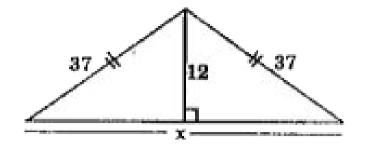
figure (fig.6.29)





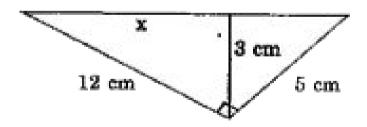
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30. Find the unknown length x in the following figure (fig.6.29)





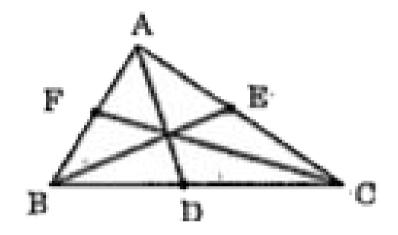
31. Find the unknown length x in the following figure (fig.6.29)





Think Discus And Write

1. How many medians can a triangle have?





2. Does a median lie wholly in the interior of the triangle? (If you think that this is not true,

draw a figure to show such a case).



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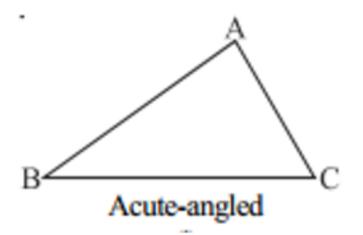
3. How many altitudes can a triangle have?



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4. Draw rough sketches of altitudes from A to

 \overline{BC} for the following triangles

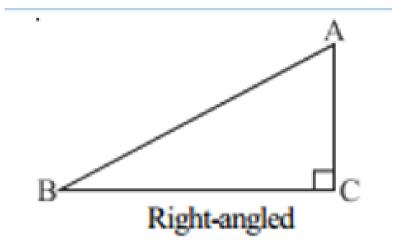




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5. Draw rough sketches of altitudes from A to

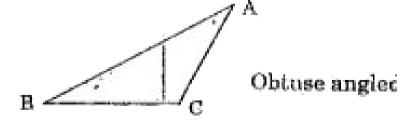
 \overline{BC} for the following triangles





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6. Draw the rough sketches of altitudes from A to \overline{BC} for the following triangles (Fig 6.6)



7. Will an altitude always lie in the interior of a triangle? If you think that this need not be true, draw a rough sketch to show such a case.



8. Can you think of a triangle in which two altitudes of the triangle are two of its sides?

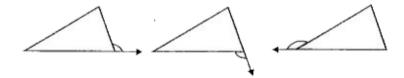


9. Can the altitude and median be same for a triangle?



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10. Exterior angles can be formed for a triangle in many ways. Three of them are shown here (fig. 6.10)





11. Are the exterior angles formed at each vertex of a triangle equal?



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12. What can you say about the sum of an exterior angle of a triangle and its adjacent interior angle?



13. What can you say about each of the interior opposite angles, when the exterior angle is a right angle?



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14. What can you say about each of the interior opposite angles, when the exterior angle is an obtuse angle?



15. What can you say about each of the interior opposite angles, when the exterior angle is an acute angle?



16. Can the exterior angle of a triangle be a straight angle?



17. Can you have a triangle with two right angles?



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18. Can you have a triangle with two obtuse angles?



19. Can you have a triangle with two acute angles?



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20. Can you have a triangle with all the three angles greater than 60° ?



21. Can you have a triangle with all the angles equal to 60° ?



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22. Can you have a triangle with all the three angles less than 60° ?



23. Is the sum of any two angles of a triangle always greater than the third angle?



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24. Which is the longest side in the triangle PQR, right-angled at P?



25. Which is the longest side in the triangle ABC, right-angled at B?



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26. Which is the longest side of a right triangle?



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27. 'The diagonal of a rectangle produce by itself the same area as produced by its length and breadth' – This is Baudhayan Theorem. Compare it with the Pythagoras property.



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Do This

1. Take several cut outs of (i) an equilateral triangle, (ii) an isosceles triangle and (iii) a

scalene triangle.

Find their altitudes and medians. Do you find any thing special about them? Discuss it with your friends.



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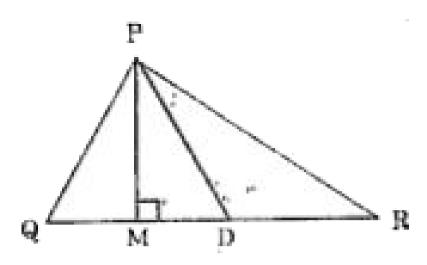
Exercise 1

1. In ΔPQR , D is the mid point of \overline{QR}

 \overline{PM} is

 \overline{PD} is

Is QM= MR?





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2. Draw rough sketches for the following:

In $\triangle ABC$,BE is a median.



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3. Draw rough sketches for the following:

In $\triangle PQR$,PQ and PR are altitude of the triangle.



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4. Draw rough sketches for the following:

In `triangleXYZ,YL is an altitude in the exterior of the triangle.



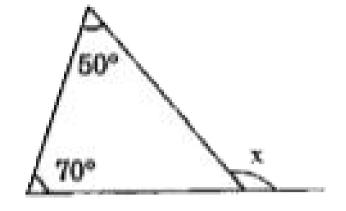
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5. Verify by drawing a diagram if the median and altitude of an isosceles triangle can be same.

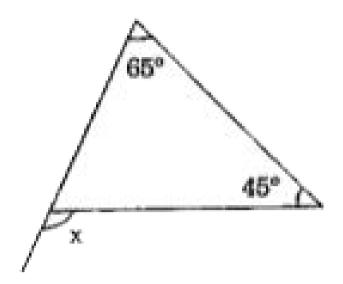


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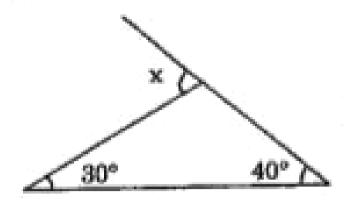
Exercise 2



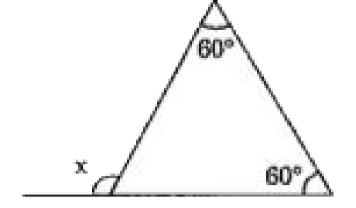




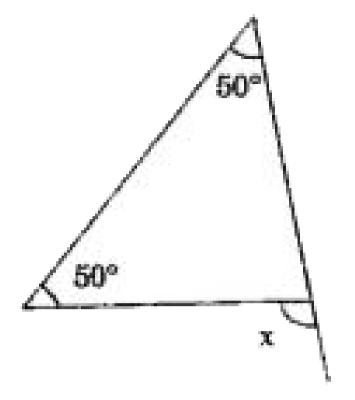




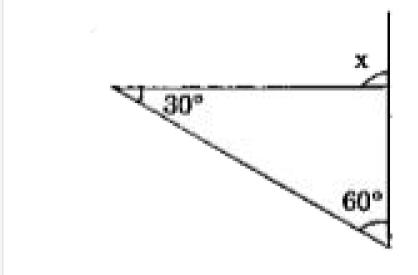




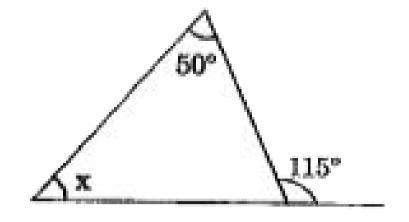




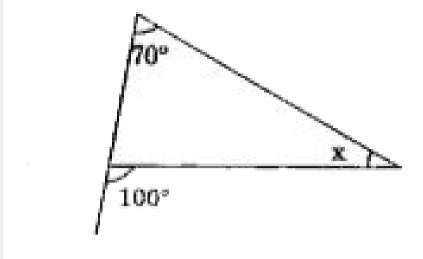




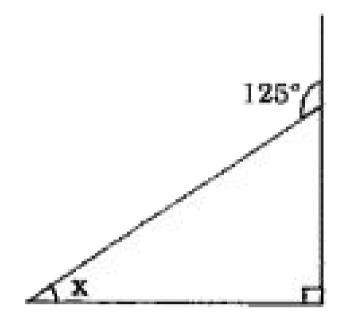




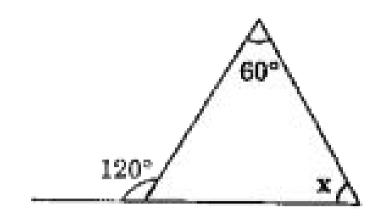




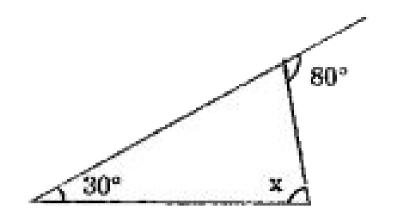




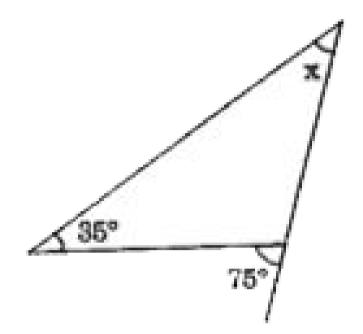








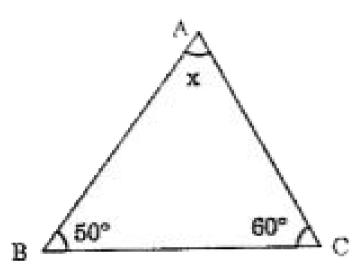




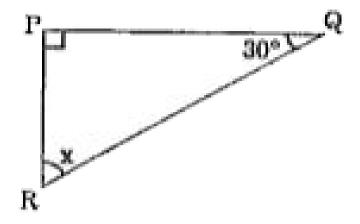


Exercise 3

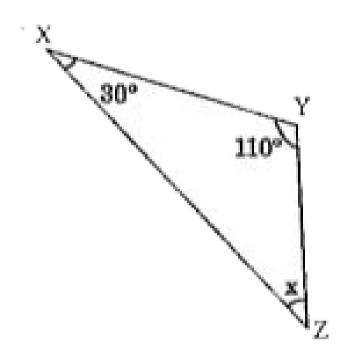
1. Find the value of the unknown x in the following diagrams



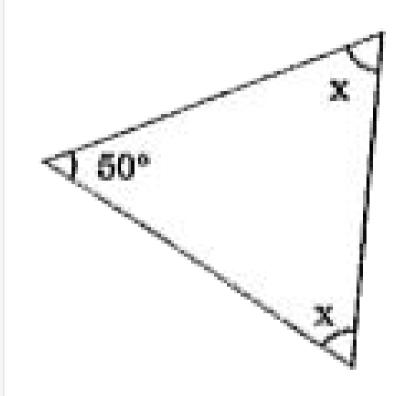




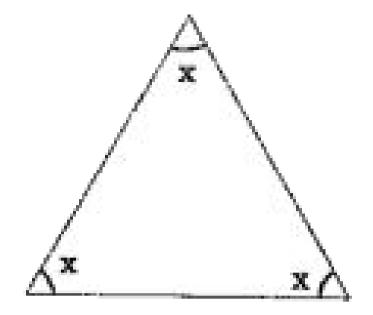




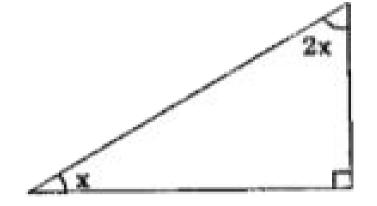




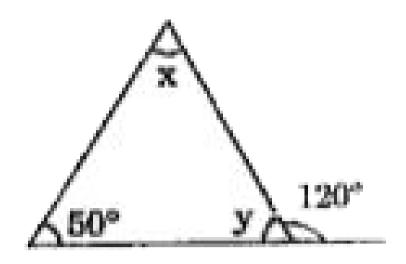




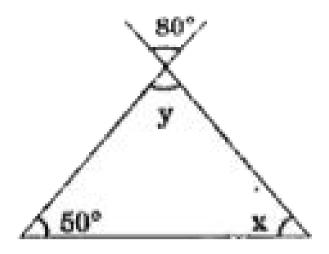




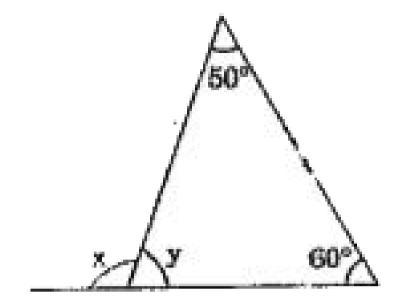




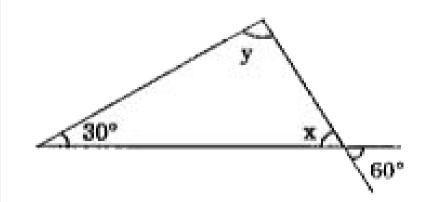




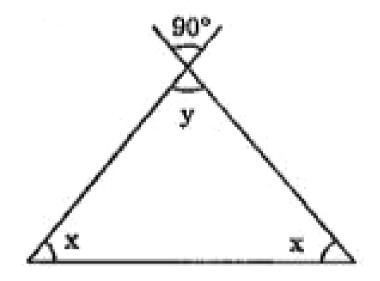




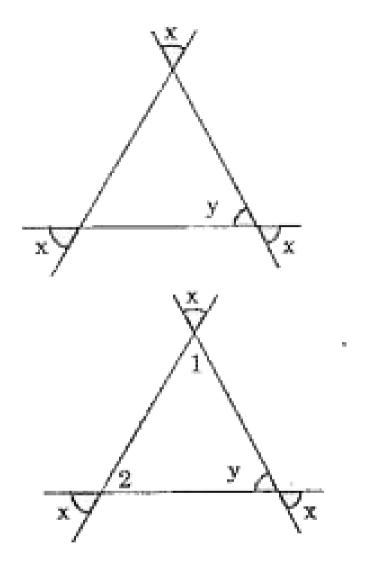














Exercise 4

1. Is it possible to have a triangle with the following sides?

2 cm, 3 cm, 5 cm



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2. Is it possible to have a triangle with the following sides?

3 cm, 6 cm, 7 cm



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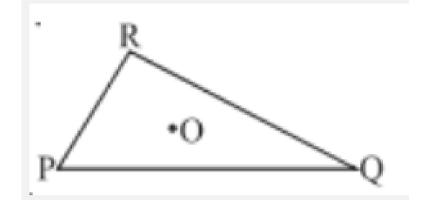
3. Is it possible to have a triangle with the following sides?

6 cm, 3 cm, 2 cm



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4. Take any point O in the interior of a triangle PQR. Is

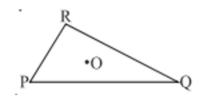


OP+OQ>PQ?



5. Take any point O in the interior of a triangle PQR. Is

OQ+OR>QR?

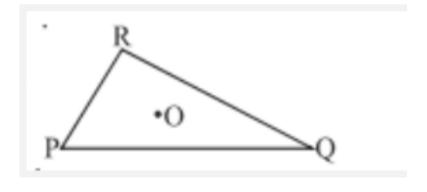




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6. Take any point O in the interior of a triangle

PQR. Is



OR+OP>RP?

7. AM is a median of a triangle ABC.

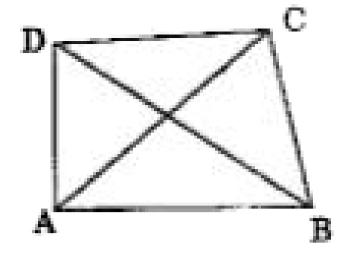
Is AB+BC+CA> 2 AM? (Consider the sides of triangles \triangle ABM triangleAMC`.)





8. ABCD is a quadrilateral. Is

AB + BC + CD + DA > AC + BD?





9. ABCD is quadrilateral. Is

AB + BC + CD + DA < 2 (AC + BD)?





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10. The lengths of two sides of a triangle are 12 cm and 15 cm. Between what two measures should the length of the third side fall?



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Exercose 5

1. PQR is a triangle, right angled at P. If PQ= 10cm and PR= 24cm. Find QR.

2. ABC is a triangle, right angled at C. If AB=25cm and AC=7cm. Find BC?



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3. A 15 m long ladder reached a window 12 m high from the ground on placing it against a wall at a distance a. Find the distance of the foot of the ladder from the wall.



4. Which of the following can be the sides of a right triangle? In case of right angled triangle, identify the right angles.

2.5cm, 6.5cm 6cm



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5. Which of the following can be the sides of a right triangle? In case of right angled triangle,

identify the right angles.

2cm, 2cm, 5cm



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6. Which of the following can be the sides of a right triangle? In case of right angled triangle, identify the right angles.

1.5cm, 2cm, 2.5cm

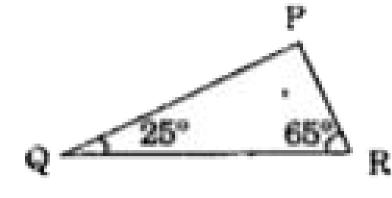


7. A tree is broken at a height of 5 m from the ground and its top touches the ground at a distance of 12 m from the base of the tree. Find the original height of the tree.



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8. Angle Q and R of a ΔPQR are 25° and 65° . Write which of the following is true



$$(i) PQ^3 + QR^2 = RP^2$$

(ii)
$$PQ^2+RP^2=QR^2$$

(iii)
$$RP^2+QR^2=PQ^2$$



9. Find the perimeter of the rectangle whose length is 40 cm and a diagonal is 41 cm.

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10. The diagonals of a rhombus measure 16 cm and 30 cm. Find its perimeter.



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Additional Questions For Practice Objective Type **Questions Fill In The Blanks**

1. If two angle of the triangle are 50° , 70° , then the measure of the third angle is ----



2. In ΔABC , right angled at C. If AC=8cm, BC=15cm, then length of AB= ----



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3. An isosceles right angled triangle has two acute angles, then measure of each of them is



4. If a triangle holds pythagoras property, it must be a Triangle



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5. If the angles of a triangle are $25^{\circ}, 25^{\circ}, 130^{\circ},$ then the triangle is a triangle



6. Match the following

- (a) Centroid divides each median Exterior angle of the triangle
- (b) In Δ PQR, angle opposite to are equal to each other.
 side QR
- (c) A triangle has in the ratio 2: 1
- (d) Sum of two interior opposite angles- angle P
- (e) In isosceles triangle sides Three altitudes. opposite to equal angles



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7. State whether true or false

Sum of the three exterior angles of a triangle

is 180°



8. State whether true or false

Medians of a triangle always lie in the interior of triangle.



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9. State whether true or false

A triangle can have its three angle measures

as $68^\circ, 71^\circ, 39^\circ.$



10. State whether true or false

If the angles of ΔPQR are in the ratio 1:2:3, then the triangle formed is a scalene triangle.



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11. State whether true or false

Sum of any two sides of the triangle is less
than the third side.



Additional Questions For Practice Short Answer Type

1. Answer the following

If a, b, c are three sides of a triangle, then write three conditions of a triangle to be formed.



2. Can the exterior angle of a triangle be a straight angle?



3. Can you have a triangle with two right angles?



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4. Answer the following

Two diagonals of the rhombus are x and y, then what is the length of each side of the rhombus?



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5. Answer the following

The lengths of two sides of a triangle are 5cm and 9cm. Between what measures should the third side fall.



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6. If $\angle PRS = \frac{5}{9}$ of straight angle in triangle PQR. Find the measure of equal interior opposite angles.

7. The square of the hypotenuse of right angled triangle is 72cm. If two legs of right angled triangle are equal, what is the length of each leg?



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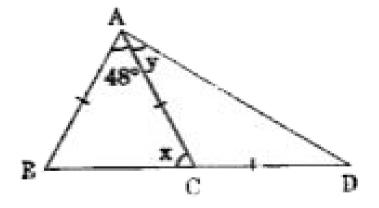
8. The angles of a triangle are $(3x-11)^{\circ}, (4x-7)^{\circ}, 2x^{\circ}.$ Find the

measures of angles.



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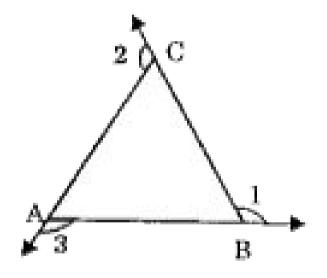
9. In the adjoining figure, find the value of x and y





Additional Questions For Practice Long Answer Type Questions

1. The sides of the ΔABC are produced. Find the sum of the exterior angles of the triangle





2. Find the perimeter of the shaded triangle.

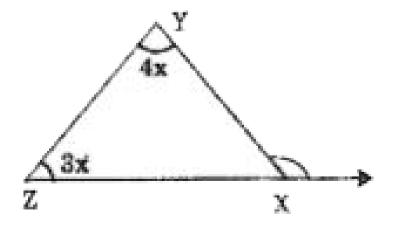
Given
$$\angle P = \angle S = 90^{\circ}$$



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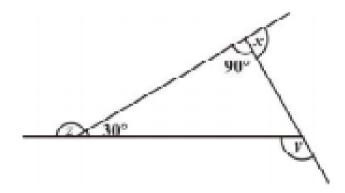
3. Find the angles of the ΔXYZ having

$$3\angle Y = 4\angle Z$$



Additional Questions For Practice Hots

1. Find x+y+z





Sample Paper For Practice Fill In The Blanks

1. Six elements of the triangle areand.......



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2. Polygon with minimum number of sides



3.is the longest side in right angled triangle



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4. Sum of the interior angles of a triangle is equal to......



5.of a triangle always intersect at a point which lies inside the triangle.



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6. If two equal sides of right angled triangle are 9cm then square of the hypotenuse

is.....cm



1. Altitudes of a triangle always lie in its exterior.



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2. Can you have a triangle with all the three angles less than 60° ?



3. A median is a line segment that joins vertex and its perpendicular to the opposite side.



4. Exterior angle of a triangle is equal to sum of any two interior angles.



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5. Side opposite to vertex L of Δ LMN is LM.



6. Triangle is possible with length of sides 6cm, 4cm, 10cm.



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Sample Paper For Practice

1. Answer the following

If PQ= PR in ΔPQR . Write the pair of equal

angles



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2. Answer the following

measures in ΔPQR as

Is it possible to have triangle with the

$$\angle P=105^{\circ}, \angle R=85^{\circ}, PQ=5cm.$$
 Give reason.



3. Answer the following

Are the number 6,8,10 form pythagorean triplet? How?



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4. Answer the following

If one of the exterior angle of a triangle is 110° , what will be the sum of other interior opposite angles?



5. In an isosceles triangle the base angles are 15° more than the vertical angles. Find the angles of the triangle

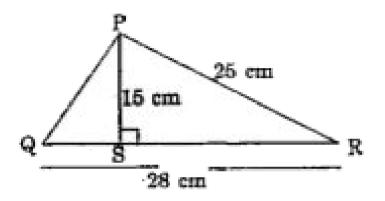


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6. One of the exterior angles of a triangle is 100° . The interior opposite angles are in the ratio 2:3. Find all the angles of the triangle.



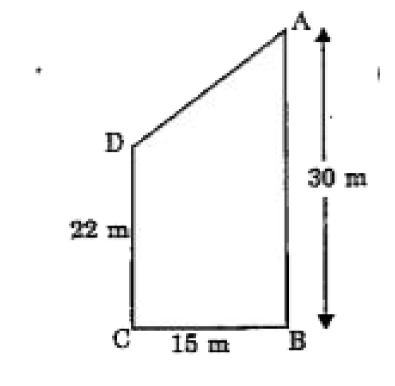
7. In the adjoining figure PS perpendicular to QR. Also, PR=25cm PS=15cm and QR=28cm. Find PQ





8. Two poles 22m and 30m high stand upright on a play ground. If their feet are 15m apart,

find the distance between their tops



$$\Delta PQR, \angle P = 40^{\circ}, PQ \mid \mid SR, \angle SRT = 70^{\circ}$$

, then find $\angle PQR$ and $\angle PRQ$

