# ©゙" doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - NAND LAL PUBLICATION

## THE TRIANGLE AND ITS PROPERTIES

## Try These

1. Can you name the angle opposite to the sides $A B$ in a triangle $A B C$ ?
2. Write the six elements (i.e., the 3 sides and the 3 angles ) of $\triangle A B C$

## D Watch Video Solution

## 3. Write the:

Side opposite to the vertex Q of $\triangle P Q R$
4. Write the :

Angle opposite to the side LM of $\triangle L M N$

D Watch Video Solution
5. Write the :

Vertex opposite to the side RT of $\triangle R S T$
( Watch Video Solution
6. Look at fig and classify each of the triangles
according to its

Sides

Angles


- Watch Video Solution

7. An exterior angle of a triangle is of measure
$70^{\circ}$ and one of its interior opposite angles is of measure $25^{\circ}$. Find the measure of interior opposite angle.

## - Watch Video Solution

8. The two interior opposite angles of an exterior angles of a triangle are $60^{\circ}$ and $80^{\circ}$.

Find the measure of the exterior angle.
9. Is something wrong in this diagram (fig
6.12)? Comment


D Watch Video Solution
10. Two angles of a triangle are $30^{\circ}$ and $80^{\circ}$.

Find the third angle.

- Watch Video Solution

11. One of the angles of a trianlge is $80^{\circ}$ and
the other two angles are equal. Find the measure of each of the equal angles.

## D Watch Video Solution

12. The three angles of a triangle are in the ratio $1: 2: 1$. Find all the angles of the triangle.

Classify the triangle in two different ways.

## D Watch Video Solution

13. Find angle $x$ in each figure


## 14. Find angle $x$ in each figure



- Watch Video Solution


## 15. Find angle $x$ in each figure



## 16. Find angle $x$ in each figure


(D) Watch Video Solution
17. Find angle $x$ in each figure


- Watch Video Solution


## 18. Find angle $x$ in each figure


( Watch Video Solution

## 19. Find angle $x$ in each figure



## D Watch Video Solution

20. Find angle $x$ in each figure


- Watch Video Solution


## 21. Find angle $x$ in each figure



- Watch Video Solution

22. Find angles $x$ and $y$ in each figure


## 23. Find angles $x$ and $y$ in each figure



- Watch Video Solution


## 24. Find angles $x$ and $y$ in each figure



## - Watch Video Solution

25. Draw any three triangles, say
$\triangle A B C, \triangle P Q R$ and $\triangle X Y Z$ in your
notebook. (fig. 6.22)


## - Watch Video Solution

26. Find the unknown length $x$ in the following
figure (fig.6.29)


## - Watch Video Solution

27. Find the unknown length $x$ in the following
figure (fig.6.29)
28. Find the unknown length $x$ in the following
figure (fig.6.29)
15 cm

29. Find the unknown length $x$ in the following
figure (fig.6.29)


## - Watch Video Solution

30. Find the unknown length $x$ in the following
figure (fig.6.29)


## D Watch Video Solution

31. Find the unknown length $x$ in the following
figure (fig.6.29)


## D Watch Video Solution

## Think Discus And Write

## 1. How many medians can a triangle have ?



- Watch Video Solution

2. Does a median lie wholly in the interior of the triangle? (If you think that this is not true,
draw a figure to show such a case).

## - Watch Video Solution

## 3. How many altitudes can a triangle have?

## D Watch Video Solution

4. Draw rough sketches of altitudes from $A$ to
$\overline{B C}$ for the following triangles


## Acute-angled

## D Watch Video Solution

## 5. Draw rough sketches of altitudes from $A$ to

$\overline{B C}$ for the following triangles


Right-angled

- Watch Video Solution

6. Draw the rough sketches of altitudes from A to $\overline{B C}$ for the following triangles (Fig 6.6)

7. Will an altitude always lie in the interior of a triangle? If you think that this need not be true, draw a rough sketch to show such a case.

## - Watch Video Solution

8. Can you think of a triangle in which two altitudes of the triangle are two of its sides?
9. Can the altitude and median be same for a triangle?

## D Watch Video Solution

10. Exterior angles can be formed for a triangle
in many ways. Three of them are shown here
(fig. 6.10)

11. Are the exterior angles formed at each vertex of a triangle equal?

## D Watch Video Solution

12. What can you say about the sum of an exterior angle of a triangle and its adjacent interior angle?
13. What can you say about each of the interior opposite angles, when the exterior angle is
a right angle?

## - Watch Video Solution

14. What can you say about each of the interior opposite angles, when the exterior angle is
an obtuse angle?
15. What can you say about each of the interior opposite angles, when the exterior angle is an acute angle?

## D Watch Video Solution

16. Can the exterior angle of a triangle be a straight angle?
17. Can you have a triangle with two right angles?

## D Watch Video Solution

18. Can you have a triangle with two obtuse angles?

D Watch Video Solution
19. Can you have a triangle with two acute angles?

- Watch Video Solution

20. Can you have a triangle with all the three angles greater than $60^{\circ}$ ?

D Watch Video Solution
21. Can you have a triangle with all the angles equal to $60^{\circ}$ ?

D Watch Video Solution
22. Can you have a triangle with all the three angles less than $60^{\circ}$ ?
23. Is the sum of any two angles of a triangle always greater than the third angle?

D Watch Video Solution
24. Which is the longest side in the triangle $P Q R$, right-angled at $P$ ?

- Watch Video Solution

25. Which is the longest side in the triangle $A B C$, right-angled at $B$ ?

D Watch Video Solution
26. Which is the longest side of a right triangle?

D Watch Video Solution
27. 'The diagonal of a rectangle produce by
itself the same area as produced by its length
and breadth'- This is Baudhayan Theorem.

Compare it with the Pythagoras property.

## - Watch Video Solution

## Do This

1. Take several cut outs of (i) an equilateral
triangle, (ii) an isosceles triangle and (iii) a

## scalene triangle.

Find their altitudes and medians. Do you find any thing special about them? Discuss it with your friends.

## D Watch Video Solution

Exercise 1

1. In $\Delta P Q R, \mathrm{D}$ is the mid point of $\overline{Q R}$
$\overline{P M}$ is
$\overline{P D}$ is

## Is $\mathrm{QM}=\mathrm{MR}$ ?



## - Watch Video Solution

## 2. Draw rough sketches for the following:

In $\triangle A B C$, BE is a median.

D Watch Video Solution
3. Draw rough sketches for the following:

In $\triangle P Q R, \mathrm{PQ}$ and PR are altitude of the triangle.

## D Watch Video Solution

4. Draw rough sketches for the following:

In `triangleXYZ, YL is an altitude in the exterior of the triangle.
5. Verify by drawing a diagram if the median and altitude of an isosceles triangle can be same.

## D Watch Video Solution

## Exercise 2

1. Find the value of the unknown exterior angle $x$ in the following diagrams


## - Watch Video Solution

2. Find the value of the unknown exterior angle $x$ in the following diagrams


## - Watch Video Solution

3. Find the value of the unknown exterior angle $x$ in the following diagrams


## - Watch Video Solution

4. Find the value of the unknown exterior angle $x$ in the following diagrams


## D Watch Video Solution

5. Find the value of the unknown exterior angle $x$ in the following diagrams


## ( Watch Video Solution

6. Find the value of the unknown exterior angle $x$ in the following diagrams


## - Watch Video Solution

## 7. Find the value of the unknown interior angle

 $x$ in the following figure

## - Watch Video Solution

8. Find the value of the unknown interior angle
$x$ in the following figure


## - Watch Video Solution

9. Find the value of the unknown interior angle $x$ in the following figure

## D Watch Video Solution

10. Find the value of the unknown interior angle x in the following figure


## - Watch Video Solution

11. Find the value of the unknown interior angle x in the following figure


## - Watch Video Solution

12. Find the value of the unknown interior angle x in the following figure


## ( Watch Video Solution

Exercise 3

1. Find the value of the unknown $x$ in the following diagrams


## D Watch Video Solution

2. Find the value of the unknown $x$ in the following diagrams


## D Watch Video Solution

3. Find the value of the unknown $x$ in the following diagrams


## D Watch Video Solution

4. Find the value of the unknown $x$ in the following diagrams


- Watch Video Solution

5. Find the value of the unknown $x$ in the following diagrams


## - Watch Video Solution

6. Find the value of the unknown $x$ in the following diagrams

## - Watch Video Solution

7. Find the value of unknown $x$ and $y$ in the following diagrams


- Watch Video Solution

8. Find the value of unknown $x$ and $y$ in the
following diagrams


## D Watch Video Solution

9. Find the value of unknown $x$ and $y$ in the following diagrams


D Watch Video Solution
10. Find the value of unknown $x$ and $y$ in the
following diagrams


- Watch Video Solution

11. Find the value of unknown $x$ and $y$ in the following diagrams


## D Watch Video Solution

12. Find the value of unknown $x$ and $y$ in the
following diagrams


- Watch Video Solution

1. Is it possible to have a triangle with the following sides?
$2 \mathrm{~cm}, 3 \mathrm{~cm}, 5 \mathrm{~cm}$

## D Watch Video Solution

2. Is it possible to have a triangle with the following sides?
$3 \mathrm{~cm}, 6 \mathrm{~cm}, 7 \mathrm{~cm}$
3. Is it possible to have a triangle with the following sides?
$6 \mathrm{~cm}, 3 \mathrm{~cm}, 2 \mathrm{~cm}$

## - Watch Video Solution

4. Take any point $O$ in the interior of a triangle

PQR. Is

$O P+O Q>P Q ?$

- Watch Video Solution

5. Take any point $O$ in the interior of a triangle PQR. Is
$O Q+O R>Q R ?$


## - Watch Video Solution

6. Take any point $O$ in the interior of a triangle PQR. Is

$\mathrm{OR}+\mathrm{OP}>\mathrm{RP}$ ?
7. $A M$ is a median of a triangle $A B C$.

Is $A B+B C+C A>2 A M$ ? (Consider the sides of triangles $\triangle A B M$ triangleAMC.)

## - Watch Video Solution

8. $A B C D$ is a quadrilateral.
$A B+B C+C D+D A>A C+B D ?$


## - Watch Video Solution

9. $A B C D$ is quadrilateral. Is
$A B+B C+C D+D A<2(A C+B D) ?$

D Watch Video Solution
10. The lengths of two sides of a triangle are 12 cm and 15 cm . Between what two measures should the length of the third side fall?

## - Watch Video Solution

Exercose 5

1. $P Q R$ is a triangle, right angled at $P$. If $P Q=$ 10 cm and $P R=24 \mathrm{~cm}$. Find $Q R$.
2. $A B C$ is a triangle, right angled at $C$. If $A B=25 \mathrm{~cm}$ and $A C=7 \mathrm{~cm}$. Find $B C$ ?

## - Watch Video Solution

3. A 15 m long ladder reached a window 12 m
high from the ground on placing it against a wall at a distance $a$. Find the distance of the foot of the ladder from the wall.
4. Which of the following can be the sides of a right triangle? In case of right angled triangle, identify the right angles.
$2.5 \mathrm{~cm}, 6.5 \mathrm{~cm} 6 \mathrm{~cm}$

## - Watch Video Solution

5. Which of the following can be the sides of a right triangle? In case of right angled triangle,
identify the right angles.

## $2 \mathrm{~cm}, 2 \mathrm{~cm}, 5 \mathrm{~cm}$

## D Watch Video Solution

6. Which of the following can be the sides of a right triangle? In case of right angled triangle, identify the right angles.
$1.5 \mathrm{~cm}, 2 \mathrm{~cm}, 2.5 \mathrm{~cm}$
7. A tree is broken at a height of 5 m from the ground and its top touches the ground at a distance of 12 m from the base of the tree.

Find the original height of the tree.

## - Watch Video Solution

8. Angle Q and R of a $\triangle P Q R$ are $25^{\circ}$ and $65^{\circ}$. Write which of the following is true

(i) $P Q^{3}+Q R^{2}=R P^{2}$
(ii) $P Q^{2}+R P^{2}=Q R^{2}$
(iii) $R P^{2}+Q R^{2}=P Q^{2}$

## - Watch Video Solution

9. Find the perimeter of the rectangle whose length is 40 cm and a diagonal is 41 cm .
10. The diagonals of a rhombus measure 16 cm and 30 cm . Find its perimeter.

D Watch Video Solution

Additional Questions For Practice Objective Type Questions Fill In The Blanks

1. If two angle of the triangle are $50^{\circ}, 70^{\circ}$,
then the measure of the third angle is -----

## - Watch Video Solution

2. In $\triangle A B C$, right angled at $C$. If $A C=8 \mathrm{~cm}$, $B C=15 \mathrm{~cm}$, then length of $A B=----$

## - Watch Video Solution

3. An isosceles right angled triangle has two acute angles, then measure of each of them is
4. If a triangle holds pythagoras property, it must be a ........ Triangle

- Watch Video Solution

5. If the angles of a triangle are $25^{\circ}, 25^{\circ}, 130^{\circ}$, then the triangle is a triangle

## 6. Match the following

(a) Centroid divides each median

- Exterior angle of the triangle
(b) In $\triangle \mathrm{PQR}$, angle opposite to
- are equal to each other. side QR
(c) A triangle has
- in the ratio $2: 1$
(d) Sum of two interior opposite angles - angle P
(e) In isosceles triangle sides - Three altitudes. opposite to equal angles


## - Watch Video Solution

## 7. State whether true or false

## Sum of the three exterior angles of a triangle

is $180^{\circ}$

## D Watch Video Solution

8. State whether true or false

Medians of a triangle always lie in the interior of triangle.

## D Watch Video Solution

9. State whether true or false

A triangle can have its three angle measures
as $68^{\circ}, 71^{\circ}, 39^{\circ}$.
(D) Watch Video Solution
10. State whether true or false

If the angles of $\triangle P Q R$ are in the ratio $1: 2: 3$,
then the triangle formed is a scalene triangle.

## D Watch Video Solution

11. State whether true or false

Sum of any two sides of the triangle is less
than the third side.

## D Watch Video Solution

Additional Questions For Practice Short Answer Type

1. Answer the following

If $a, b, c$ are three sides of a triangle, then
write three conditions of a triangle to be formed.

## (D) Watch Video Solution

2. Can the exterior angle of a triangle be a straight angle?

## - Watch Video Solution

3. Can you have a triangle with two right angles?

## D Watch Video Solution

4. Answer the following

Two diagonals of the rhombus are $x$ and $y$, then what is the length of each side of the rhombus?
5. Answer the following

The lengths of two sides of a triangle are 5 cm and 9 cm . Between what measures should the third side fall.

## D Watch Video Solution

6. If $\angle P R S=\frac{5}{9}$ of straight angle in triangle
$P Q R$. Find the measure of equal interior opposite angles.

## - View Text Solution

7. The square of the hypotenuse of right angled triangle is 72 cm . If two legs of right angled triangle are equal, what is the length of each leg?

## - Watch Video Solution

8. The angles of a triangle are
$(3 x-11)^{\circ},(4 x-7)^{\circ}, 2 x^{\circ}$. Find the
measures of angles.

## D Watch Video Solution

9. In the adjoining figure, find the value of $x$ and $y$


- Watch Video Solution

Additional Questions For Practice Long Answer Type Questions

1. The sides of the $\triangle A B C$ are produced. Find the sum of the exterior angles of the triangle


- Watch Video Solution

2. Find the perimeter of the shaded triangle.

Given $\angle P=\angle S=90^{\circ}$

## D Watch Video Solution

3. Find the angles of the $\triangle X Y Z$ having

$$
3 \angle Y=4 \angle Z
$$



## Additional Questions For Practice Hots

1. Find $x+y+z$


D Watch Video Solution

## Sample Paper For Practice Fill In The Blanks

1. Six elements of the triangle are ..........and.
(D) Watch Video Solution
2. Polygon with minimum number of sides is

D Watch Video Solution
3. .......is the longest side in right angled triangle

- Watch Video Solution

4. Sum of the interior angles of a triangle is equal to........

- Watch Video Solution

5. ........of a triangle always intersect at a point which lies inside the triangle.

## D Watch Video Solution

6. If two equal sides of right angled triangle are 9 cm then square of the hypotenuse is..........cm

- Watch Video Solution

Sample Paper For Practice True Or False

1. Altitudes of a triangle always lie in its exterior.

## D Watch Video Solution

2. Can you have a triangle with all the three angles less than $60^{\circ}$ ?
3. A median is a line segment that joins vertex and its perpendicular to the opposite side.

## - Watch Video Solution

4. Exterior angle of a triangle is equal to sum of any two interior angles.

## - Watch Video Solution

5. Side opposite to vertex L of $\Delta \mathrm{LMN}$ is LM .

## - Watch Video Solution

6. Triangle is possible with length of sides 6 cm , $4 \mathrm{~cm}, 10 \mathrm{~cm}$.
( Watch Video Solution

Sample Paper For Practice

1. Answer the following

If $\mathrm{PQ}=\mathrm{PR}$ in $\triangle P Q R$. Write the pair of equal

## D Watch Video Solution

## 2. Answer the following

Is it possible to have triangle with the measures in $\Delta P Q R$ as
$\angle P=105^{\circ}, \angle R=85^{\circ}, P Q=5 \mathrm{~cm} . \quad$ Give reason.
3. Answer the following

Are the number 6,8,10 form pythagorean triplet? How?

## D Watch Video Solution

4. Answer the following

If one of the exterior angle of a triangle is
$110^{\circ}$, what will be the sum of other interior opposite angles?
5. In an isosceles triangle the base angles are
$15^{\circ}$ more than the vertical angles. Find the angles of the triangle

## D Watch Video Solution

6. One of the exterior angles of a triangle is
$100^{\circ}$. The interior opposite angles are in the ratio $2: 3$. Find all the angles of the triangle.
7. In the adjoining figure PS perpendicular to
$Q$ R. Also, $P R=25 \mathrm{~cm} P S=15 \mathrm{~cm}$ and $Q R=28 \mathrm{~cm}$. Find

PQ


- Watch Video Solution

8. Two poles 22 m and 30 m high stand upright on a play ground. If their feet are 15 m apart,
find the distance between their tops


D Watch Video Solution
9.
$\Delta P Q R, \angle P=40^{\circ}, P Q| | S R, \angle S R T=70^{\circ}$
, then find $\angle P Q R$ and $\angle P R Q$


D Watch Video Solution

