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## MATHS

## BOOKS - VK GLOBAL PUBLICATION

## MATHS (HINGLISH)

## COORDINATE GEOMETRY

## Very Short Answer Answer Questions

1. What is the area of the triangle formed by
the points $O(0,0), A(-3,0)$ and $B(5,0)$ ?
2. If the centroid of the triangle formed by points $P(a, b), Q(b, c)$ and $R(c, a)$ is at the origin, what is the value of $a+b+c$ ?

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3. If $A O B C$ is a rectangle whose three vertices are $A(0,3), O(0,0)$ and $B(5,0)$, then the length of its diagonal is

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4. Find the value ofa, so that the point $(8, a)$ lie on the line $2 x-3 y=5$.

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5. Find distance between the points $(0,5)$ and
$(-5,0)$

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6. The distance of the point $P(-6,8)$ from the origin is

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7. If the points $A(1,2), B(0,0)$ and $C(a, b)$ are collinear , then

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8. Find the ratio in which the line segment
joining the points $(-3,10)$ and $(6,-8)$ is
divided by $(-1,6)$.

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9. The coordinates of the points $P$ and $Q$ are respectively ( $4,-3$ ) and ( $-1,7$ ). Find the abscissa of a point $R$ on the line segment $P Q$ such that $\frac{P R}{P Q}=\frac{3}{5}$.

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10. The length of a line segment is of 10 units
and the coordinates of one end-point are
$(2,-3)$. If the abscissa of the other end is 10 ,
find the ordinate of the other end.

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Short Answer Questions I

1. Write the coordinates of a point on $X$-axis which is equidistant from the points ( $-3,4$ )
and $(2,5)$.

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2. Find the values of $x$ for which the distance between the point $P(2,-3)$ and $Q(x, 5)$ is 10.

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3. What is the distance between the points
$\left(10 \cos 30^{\circ}, 0\right)$ and $\left(0,10 \cos 60^{\circ}\right) ?$

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4. If $A(-1,3), B(1,-1)$ and $C(5,1)$ are the vertices of a triangle $A B C$, what is the length of the median through vertex $A$ ?

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5. Write the ratio in which the line segment joining the points $A(3,-6)$ and $B(5,3)$ is divided by $X$-axis.

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6. The point $P(5,-3)$ is one of the two points of trisection of line segment joining the points
$A(7,-2)$ and $B(1,-5)$.

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7. $\triangle A B C$ with vertices $A(0-2,0), B(2,0)$ and
$C(0,2)$ is similar to $\triangle$ DEF with vertices
$D(-4,0), E(4,0)$ and $F(0,4)$.
8. Point $P(0,2)$ is the point of intersection of $Y$ axis and perpendicular bisector of line segment joining the points $A(-1,1)$ and $B(3,3)$.

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9. 

Check
whether
$(5, \backslash 2), \backslash(6, \backslash 4) \backslash$ and $\backslash(7, \backslash 2)$ are
the vertices of an isosceles triangle.

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10. If $(1,2),(4, y),(x, 6)$ and $(3,5)$ are the vertices of a parallelogram taken in order, find $x$ and $y$.

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11. Find the ratio in which the $y$-axis divides the
line segment joining the points $(5,-6)$ and
$(-1,-4)$. Also, find the coordinates of the point of division.
12. . Let $P$ and $Q$ be the points of trisection of
the line segment joining the points $A(2,-2)$
and $B(-7,4)$ such that $P$ is nearer to $A$. Find the coordinates of P and Q .

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13. Find the ratio in which the point $(-3, p)$
divides the line segment joining the points
$(-5,-4)$ and $(-2,3)$. Hence, find the
value of $p$.

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14. The $x$-coordinate of a point $P$ is twice its $y$ coordinate. If $P$ is equidistant from
$Q(2,-5) \operatorname{and} R(-3,6), \quad$ then find the coordinates of P .

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Short Answer Questions li

1. Determine if the points $(1,5),(2,3)$ and $(-2$,
-11) are collinear.

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2. Find the distance between the following pairs of points:
(i) $(5,7),(-1,3)$ (ii) (a,b), (-a,-b)

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3. Name the type of quadrilateral formed, if any, by the following points, and give reasons for your answer:'(i)<br>(1,\2),<br>(1,\0),<br>(1,\2),<br>(3,\0)
$(i i) \backslash(3, \backslash 5),(3, \backslash 1),(0, \backslash 3),(1, \backslash 4)(i \operatorname{i}) \backslash(4, \backslash 5), \backslash(7, \backslash$ 6),

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4. Find the values of $y$ for which the distance between the points $P(2,3)$ and $Q(10, y)$ is 10 units.
5. If $Q(0,1)$ is equidistant from $P(5,-3)$ and $R(x, 6)$, find the values of $x$. Also, find the distances $Q R$ and $P R$.

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6. Find the point on the $x$-axis which is equidistant from $(2,-5)$ and $(-2,9)$.
7. Find a relation between $x$ and $y$ if the points
$(x, y),(1,2)$ and $(7,0)$ are collinear.

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8. Find a relation between $x$ and $y$ such that
the point $(x, y)$ is equidistant from the points $(3,6)$ and $(-3,4)$

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9. Find the coordinates of the point which
divides the line joining of $(-1,7)$ and $(4,-3)$ in
the ratio 2:3.

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10. Find the co - ordinates of the points of trisection of the line segment joining $(4,-1)$
and $(-2,-3)$.
11. Find the ratio in which [the line segment joining $A(1,5)$ and $B(4,5)$ is divided by the xaxis. Also find the coordinates of the point of division.

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12. If $(1,2),(4, y),(x, 6)$ and $(3,5)$ are the vertices
of a parallelogram taken in order, find x and y .
13. Find the coordinates of a point $A$, here $A B$ is a diameter of the circle whose centre is $(2,-3)$ and $B(1,4)$.

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14. If A and B are $(2,2)$ and $(2,4)$, respectively, find the coordinates of $P$ such that $A P=\frac{3}{7} A B$ and P lies on the line segment $A B$.

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15. Find the coordinates of the points which divide the line segment joining
$A(2, \backslash 2) \backslash$ and $\backslash B(2,8)$ into four equal parts.

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16. Find the area of a rhombus if its vertices
$(3,0),(4,5),(-1,4)$ and $(-2,-1)$ are taken in order.
17. Find the area of the triangle whose vertices are: $(-5,-1),(3,-5),(5,2)$

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18. If the point $A(0,2)$ is equidistant from the points $B(3, p)$ and $C(p, 5)$, find $p$.

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19. If the points $A(-2,1), B(a, b)$ and $C(4,-1)$ are collinear and $a-b=1$, find the values of $a$ and $b$.
20. If the point $P(k-1,2)$ is equidistant from the points $A(3, k)$ and $B(k, 5)$, find the values of $k$.

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21. Find the ratio in which the line segment
joining the points $A(3,-3)$ and $B(-2,7)$
is divided by x-axis. Also, find the coordinates of the point of division.

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22. Find the values of $k$, if the points $A(k+1,2 k)$
, $B(3 k, 2 k+3)$ and $C(5 k-1,5 k)$ are collinear.

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23. If the point $\mathrm{P}(\mathrm{x}, \mathrm{y})$ is equidistant from the
points $A(a+b, b-a)$ and $B(a-b, a+b)$. Prove that $b x=a y$.
24. If the point $C(-1,2)$ divides internally the
line segment joining the points $A(2,5)$ and $B$
$(x, y)$ in the ratio of $3: 4$, find the value of $x^{2}+y^{2}$.

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## Long Answer Questions

1. Find the value of ' $k$ ', for which the points are collinear: (7,-2), (5, 1), (3, k).
2. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are
$(0,-1),(2,1)$ and $(0,3)$. Find the ratio of this area to the area of the given triangle.

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3. Find the area of the quadrilateral whose vertices taken in order are $(-4,-2),(-3,5),(3,-2)$

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4. You have studied in Class IX, (Chapter 9.

Example 3), that a median of a triangle divides it into two triangles of equal areas. Verify this result for $A$ $A B C$ whose vertices are
$A(4,6), B(3,2)$ and $C(5,2)$.

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5. Find the ratio in which the point $P(x, 2)$
divides the line segment joining the points
$A(12,5)$ and $B(4,-3)$. Also find the value of $x$.

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6. If $A(4,2), B(7,6)$ and $C(1,4)$ are the vertices of a $\triangle A B C$ and AD is its median, prove that the median AD divides $\triangle A B C$ into two triangles of equal areas.
7. If the points $A(2,4)$ is equidistant from $P(3,8)$ and $\mathrm{Q}(-10, y)$, then find the value of y . Also , find distance PQ .

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8. The base $B C$ of an equilateral triangle $A B C$
lies on $y$-axis. The coordinates of point $C$ are
$(0,-3)$. The origin is the midpoint of the base.

Find the coordinates of the points $A$ and $B$.

Also, find the coordinates of another point $D$ such that $A B C D$ is a rhombus.

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9. Prove that the area of a triangle with vertices $(\mathrm{t}, \mathrm{t}-2)$, $(\mathrm{t}+2, \mathrm{t}+2)$ and $(\mathrm{t}+3, \mathrm{t})$ is independent of $t$.

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10. The coordinates of $A, B, C$ are $(6,3)$,
$(-3,5),(4,-2)$ respectively and $P$ is any point $(x, y)$. Show that the ratio of the areas of the triangles $\triangle P B C$ and $\triangle A B C$ is $\left|\frac{x+y-2}{7}\right|$.

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11. The vertices of a
$\Delta A B C a r e A(4,6), B(1,5)$ and $C(7,2)$. A
line is drawn to intersect side $A B$ and $A C$ at $D$
and E respectively, such that $\frac{A D}{A B}=\frac{A E}{A C}=\frac{1}{4}$. Calculate the area of
$\triangle A D E$ and compare it with the area of $\triangle A B C$.
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Hots Higher Order Thinking SkIlls

1. The line joining the points $(2,1)$ and
$(5,-8)$ is trisected at the points $P$ and $Q$. If
point $P$ lies on the line $2 x-y+k=0$. Find the value of $k$.

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2. Prove that the diagonals of a rectangle bisect each other and are equal.

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3. In what ratio does the $y$-axis divide the line
segment joining the point $P(-4,5)$ and
$Q(3,-7)$ ? Also, find the coordinates of the point of intersection.

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4. Find the centre of a circle passing through
the points $(6,6),(3,7)$ and $(3,3)$.

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5. If the coordinates of the mid-points of the sides of a triangle are
$(1,1),(2,-3) \operatorname{and}(3,4)$. Find its (i) centroid
(ii) in-centre.

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6. Determine the ratio in which the line $2 x+y-$
$4=0$ divides the line segment joining the
points $A(2,-2)$ and $B(3,7)$.


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7. Show that $\Delta A B C$ with vertices $\mathrm{A}(-2,0), \mathrm{B}(0$,
2) and $\mathrm{C}(2,0)$ is similar to $\triangle D E F$ with vertices $\mathrm{D}(-4,0), \mathrm{F}(4,0)$ and $\mathrm{E}(0,4)$.

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Proficiency Exercise Very Short Answer Questions

1. The point which divides the line segment
joining the points $(7,-6)$ and $(3,4)$ in ration $1: 2$ internally lies in the
2. If $\mathrm{P}\left(\frac{a}{3}, 4\right)$ is the mid - point of the line segment joining the points $Q(-6,5)$ and $R(-2,3)$, then the value of $a$ is

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3. A line intersects the $y$-axis and $x$-axis at the points $P$ and $Q$ respectively. If $(2,-5)$ is the midpoint of $P Q$ then find the coordinates of $P$ and Q.

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4. The perpendicular bisector of the line segment joining the points $A(1,5)$ and $B(4,6)$ cuts the $Y$-axis at

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5. if a line / passes through $(k, 2 k),(3 k, 3 k)$
and $(3,1), k \neq 0$ and the distance from the origin to the line / is $\frac{1}{\sqrt{m}}$ then $m=\ldots$
6. If $\mathrm{A}(5,2), \mathrm{B}(2,-2)$ and $\mathrm{C}(-2, \mathrm{t})$ are the vertices of a right triangle with $\angle B=90^{\circ}$ then find the value of $t$.

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7. If the area of a triangle formed by the points
$(k, 2 k),(-2,6)$ and $(3,1)$ is 20 square units, then
find $k$.
8. Prove that the points $\mathrm{A}(\mathrm{a}, \mathrm{O}), \mathrm{B}(\mathrm{O}, \mathrm{b})$ and $\mathrm{C}(1$,
1) are collinear, if $\frac{1}{a}+\frac{1}{b}=1$.

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9. Find the ratio in which the $x$-axis divides the segment joining $(-3,-5)$ and $(-1,1)$.
10. If the centroid of the triangle formed by
the points $(a, b),(b, c)$ and $(c, a)$ is at the origin, then find the value of $a^{3}+b^{3}+c^{3}$.

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11. Two vertices of a triangle are at $(-3,1)$ and
$(0,2)$ and the centroid is at the origin. Find its third vertex.
12. What is the ratio in which the point $P\left(\frac{-2}{5}, 6\right)$ divides the line joining of $A(-4,3)$ and $B(2,8)$ ?

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## Proficiency Exercise Short Answer Questions I

1. What is the distance between the points
$A(c, 0)$ and $B(0,-c) ?$
2. If $A(1,2), B(4,3)$ and $C(6,6)$ are the three vertices of a parallelogram $A B C D$, find the coordinates of the fourth vertex D .

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3. If $(2, p)$ is the midpoint of the line segment
joining the points $A(6,-5)$ and $B(-2,11)$, find the value of $p$.
4. If $A(2,2), B(-4,-4) \operatorname{and} C(5,-8)$ are the vertices of a triangle, then the lengthof the median through vertex $C$ is.

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5. What is the distance between the points $A$
$(5 \cos \theta, 0)$ and $\mathrm{B}(0,5 \sin \theta)$ ?

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6. Write the ratio in which the line segment joining points $(2,3)$ and $(3,-2)$ is divided by $X$ axis.

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7. If the distance between points $(x, 0)$ and $(0,3)$ is 5 , what are the values of $x$ ?

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8. Write the coordinates ot the point dividing
line segment joining the points $(1,5)$ and $(-5,1)$ internally in the ratio $1: 4$.

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9. What is the area of the triangle formed by
the points $O(0,0), A(4,0)$ and $B(0,3)$ ?

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10. In Q. No. 169, what is the value of $\frac{a^{2}}{b c}+\frac{b^{2}}{c a}+\frac{c^{2}}{a b} ?$

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11. If the mid-point of a segment joining
$A\left(\frac{x}{2}, \frac{y+1}{2}\right)$ and $\mathrm{B}(\mathrm{x}+1, \mathrm{y}-3)$ is $\mathrm{C}(5,-2)$,
find $x, y$.

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12. Find the distance between the points $\left(\frac{-8}{5}, 2\right) \operatorname{and}\left(\frac{2}{5}, 2\right)$

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13. Find the value of $c$ so that the point $(3, c)$
lies on the line represented by $2 x-3 y+5=0$.
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14. Prove that the points $(3,0),(6,4)$ and $(-1,3)$ are the vertices of a right angled isosceles triangle.

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15. Prove that the points $(2,-2),(-2,1)$ and $(5,2)$
are the vertices of a right angled triangle. Also
find the area of this triangle.
16. Point $A(2,-3)$ lies on the line segment joining the points $P(-4,-3)$ and $Q(1,-3)$.

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17. The points $A(3,1)$, $B(12,-2)$ and $C(0,2)$ cannot be vertices of a triangle.

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18. Point $P(0,-7)$ is the point of intersection of
$y$-axis and perpendicular bisector of line segment joining the points $A(-1,0)$ and $B(7$, $-6)$.

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19. The points $A(4,3), B(6,4), C(5,-6)$ and $D(-3,5)$ are vertices of a parallelogram.
20. The points $P(-2,4)$ lies on a circle of radius

6 and centre $(3,5)$.

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21. The points $(1,1),(13,1)$ and $(13,6)$ are the vertices of a right triangle.
22. A circle has its centre at the origin and a point $P(5,0)$ lies on it . The point $Q(6,8)$ lies outside the circle.

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23. The points $A(-6,10), B(-4,6)$ and $C(3,-8)$ are
collinear such that
$\mathrm{AB}=-\frac{2}{9} A C$.
24. In Fig. $A B C$ is a triangle co-ordinates of whose vertex $A$ are $(0,-1)$. $D$ and $E$ respectively are the mid-points of sides $A B$ and AC their co-ordinates are $(1,0)$ and $(0,1)$ respectively. If $F$ is the mid-point of $B C$ find the areas of $\triangle A B C$ and $\triangle D E F$

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25. If the points $A(4,3) \operatorname{and} B(x, 5)$ are on the circle with centre $O(2,3)$, find the value of $x$.
26. Find a point which is equidistant from the points $A(-5,4)$ and $B(-1,6)$. How many such points are there?

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27. Find the points on the $X$-axis which are at distance of $2 \sqrt{5}$ from the point $(7,-4)$. How many such points are there?
28. What type of quadrilateral do the points $A$ $(2,-2), B(7,3) C(11,-1)$ and $D(6,-6)$ taken in that order from?

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29. Find the point on $x$-axis which is equidistant from the points $(-2,5)$ and $(2,-3)$.
30. Find the coordinates of the point $Q$ on the

X- axis which lies on the perpendicular bisector of the line segment joining the points
$A(-5,-2)$ and $B(4,-2)$. Name the type of triangle formed by the points $\mathrm{Q}, \mathrm{A}$ and B .

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31. Show that four points (1, -2$),(3,6),(5,10)$
and $(3,2)$ are the vertices of a parallelogram.
32. Name the type of triangle formed by the points $A(-5,6), B(-4,-2)$ and $C(7,5)$.

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33. In the following examples, can the segment joining the given points from a triangle ? If triangle is formed, state the type of the triangle considering sides of the triangle.
(iii)
$(\sqrt{2}, \sqrt{2}), B(-\sqrt{2},-\sqrt{2}), C(-\sqrt{6}, \sqrt{6})$

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34. Do the points $A(3,2), B(-2,-3)$
and $C(2,3)$ form a triangle? If so, name the
type of triangle formed.

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35. The line segment joining the points (3, -4) and $(1,2)$ is trisected at the points $P$ and $Q$. If the co-ordinates of P and Q are $(p,-2)$ and $\left(\frac{5}{3}, q\right)$ respectively, find the values of $p$ and $q$.

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36. If the point $P(m, 3)$ lies on the line segment joining the points $A\left(-\frac{2}{5}, 6\right)$ and $B(2,8)$, find the value of $m$.

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37. Point $P$ divides the line segment joining the points $\mathrm{A}(-1,3)$ and
$\mathrm{B}(9,8)$ such that $\frac{A P}{B P}=\frac{k}{1}$. If P lies on the line $x-y+2=0$, find k.

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38. Point $A$ lies on the line segment $P Q$ joining $P(6,-6)$ and $Q(-4,-1)$ in such a way that
$P A$
$\frac{P A}{P Q}=\frac{2}{5}$. If the point A also lies on the line $3 x+k(y+1)=0$, find the value of $k$.

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39. If $R(x, y)$ is a point on the line segment joining the points $P(a, b) a n d Q(b, a)$, then prove that $x+y=a+b$
40. Find the ratio in which the line $x+3 y-14=$

0 divides the line segment joining the points $A$
$(-2,4)$ and $B(3.7)$.

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41. If the points $(p, q),(m, n)$ and
$(p-m, q-n)$ are collinear, show that $p n=q m$.
42. Prove that the points
$(a, b+c),(b, c+a)$ and $(c, a+b) \quad$ are collinear.

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43. If the mid-point of the line segment joining
the points $A(3,4)$ and $B(k, 6)$ is $P(x, y)$ and
Plies on the line $x+y-10=0$, find the value of
k.

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44. If $(1,2),(4, y),(x, 6)$ and $(3,5)$ are the vertices of a parallelogram taken in order, find $x$ and $y$.

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45. If $P(9 a-2,-b)$ divides line segment joining $A$
$(3 a+1,-3)$ and $B(8 a, 5)$ in the ratio $3: 1$, then find the values of $a$ and $b$.
46. In what ratio does the $x$-axis divide the line segment joining the points $(-4,-6)$ and $(-1,7)$ ?

Find the co-ordinates of the point of division.

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47. Find the area of the triangle whose vertices
are $(-4,8),(6,-6)$ and $(-3,-2)$.

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48. If $\mathrm{D}\left(-\frac{1}{2}, \frac{5}{2}\right), \mathrm{E}(7,3)$ and $\mathrm{F}\left(\frac{7}{2}, \frac{7}{2}\right)$ are
the mid - points of sides of $\triangle A B C$, then find the area of the $\triangle A B C$.

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49. Find the area of the triangle $A B C$ with
$A(1,-4)$ and mid-points of sides through A being $(2,-1) \operatorname{and}(0,-1)$.
50. If $(a, b)$ is the mid - point of the line segment joining the points $A(10,-6), B(k, 4)$ and $a-2 b=18$, then find the value of $k$ and the distance $A B$.

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51. If $(a, b)$ is the mid - point of the line segment joining the points $A(10,-6), B(k, 4)$ and $a-2 b=18$, then find the value of $k$ and the distance $A B$.
52. Find the ratio in which the line
$2 x+3 y-5=0$ divides the line segment joining the points $(8,-9)$ and $(2,1)$. Also find the coordinates of the points of division.

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53. If the centre of a circle is (2a,a-7) ,then Find the value of a , if the ciecle passes through the point (11,-9) and has diameter $10 \sqrt{2}$ units .

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54. Find the coordinates of points which divide the line segment joining $A(5,-6)$ and $B(-1,8)$ into four equal parts.

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55. Find the value of $k$ for which the points
$A(k+1,2 k), B(3 k, 2 k+3)$ and $C(5 k-1,5 k)$ are collinear.
56. Find the coordinates of the point $R$ on the
line segment joining the points $P(-1,3)$ and $Q$
$(2,5)$ such that $\mathrm{PR}=\frac{3}{5} \mathrm{PQ}$.

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57. Find the third vertex of a triangle, if two of its vertices are at $(-3,1)$ and $(0,-2)$ and the centroid is at the origin.
58. Find the area of the quadrilateral whose vertices taken in order are (-4, -2$),(-3,5),(3,-2)$ and (2,3)

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59. The area of a triangle is 5 square unit. Two of its vertices are $(2,1),(3,-2)$ and the third vertex lies on the line $y=x+3$. The third vertex can be
60. If the points $A(2,9), B(a, 5)$ and $C(5,5)$ are the vertices of a $\triangle A B C$. Right angled at B , then find the values of a and hence the area of $\triangle A B C$.

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61. The vertices of a triangle are ( $a, b-c$ ), (b, c-
a) and (c, a-b). Prove that its centroid lies on $x$-axis.
62. The base PQ of two equilateral triangles $P Q R$ and $P Q R$ with side $2 a$ lies along $y$-axis such that the mid-point of $P Q$ is at the origin.

Find the coordinates of the vertices $R$ and $R$ of the triangles.

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63. If the points $(a, b),\left(a^{\prime}, b^{\prime}\right)$ and ( $\left.a-a^{\prime}, b-b^{\prime}\right)$ are collinear, show that $a b^{\prime}=a^{\prime} b$.

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64. Show that the points $\left(a^{2}, 0\right),\left(0, b^{2}\right)$ and
$(1,1)$ are collinear if $\frac{1}{a^{2}}+\frac{1}{b^{2}}=1$.

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65. The coordinates of $A, B, C$ are
$(6,3),(-3,5)$ and $(4,-2)$ respectively and $P$ is any point $(x, y)$. Show that the ratio of the areas of triangles $P B C$ and $A B C$ is $\left|\frac{x+y-2}{7}\right|$.

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66. Show that $(1,-1)$ is the centre of the circle circumscribing the triangle whose vertices are $(4,3),(-2,3)$ and (6, -1).
67. If the point $A(-2,1), B(a, b)$ and $C(4,-1)$ are collinear and $a-b=1$, find the values of $a$ and $b$.

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68. If the points $P(-3,9), Q(a, b)$ and $R(4,-5)$ are
collinera and $a+b=1$, find the values of $a$ and b.

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69. If the points $A(-1,-4), B(b, c)$ and
$C(5,-1)$ are collinear and $2 b+c=4$, find the values of $b$ and $c$.

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70. If the point $P(2,2)$ is equidistant from the points $A(-2, k)$ and $B(-2 k,-3)$, find $k$. Also, find the length of AP.
71. Points $A(-1, y)$ and $B(5,7)$ lie on a circle with centre $O(2,-3 y)$. Find the values of $y$. Hence, find the radius of the circle.

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72. the value of $k$ for which the points
$(3 k-1, k-2),(k, k-7)$
( $k-1,-k-2$ ) are collinear.
73. Points P, Q, R and S divide the line segment joining the points $A(1,2)$ and $B(6,7)$ in five equal parts. Find the coordinates of the point P.

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## Proficiency Exercise Long Answer Questions

1. If the points $A(1,2), B(2,3), C * a, 2)$ and $D$
$(-4-3)$ form a parallelogram, them find the
value of $a$ and height of the parallelogram taking $A B$ as base.

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2. $A(6,1), B(8,2)$ and $C(9,4)$ are the vertices of a parallelogram $A B C D$. If $E$ is the midpoint of $D C$, find the area of $\triangle A D E$.

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3. Find the area of the triangle formed by joining the mid-points of the sides of the triangle, whose vertices are (2,-4), $(6,2)$ and ($4,6)$. Find the ratio of this area to the area of the given triangle.

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4. The mid-points $D, E, F$ of the sides of a triangle $A B C$ are $(3,4),(8,9)$ and $(6,7)$. Find the coordinates of the vertices of the triangle.
5. Find the coordinates of the third vertex of an equilateral triangle, whose two vertices are
$(3,4)$ and $(-2,3)$.

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6. Show that the points $(a, a),(-a,-a)$
and $(-\sqrt{3} a, \sqrt{3} a)$ are the vertices of an equilateral triangle. Also, find its area.
7. If $A(3,4)$ and $C(1,-1)$ are two opposite angular points of square $A B C D$, find the coordinates of other two vertices.

## D View Text Solution

8. The points A
$\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$ and $C\left(x_{3}, y_{3}\right)$ are the vertices of $\triangle A B C$.
(i) The median from A Meets BC at D. Find the
coordinates of the points D.
(ii) Find the coordinates of the point $P$ on $A d$ such that $A P: P D=2: 1$.
(iii) Find the coordinates of points $Q$ and $R$ on medians $B E$ and $C F$, respectively such that $B Q: Q E=2: 1$ and $C R: R F=2: 1$.

What are the coordinates of the centroid of the $\triangle A B C$ ?

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9. 

$\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$ and $C\left(x_{3}, y_{3}\right)$ are the
vertices of $\triangle A B C$.
(i) The median from A Meets Bc at D. Find the coordinates of the points $D$.
(ii) Find the coordinates of the point $P$ on $A d$ such that $A P: P D=2: 1$.
(iii) Find the coordinates of points $Q$ and $R$ on medians $B E$ and $C F$, respectively such that
$B Q: Q E=2: 1$ and $C R: R F=2: 1$.

What are the coordinates of the centroid of the $\triangle A B C$ ?

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10. 

The points
$\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$ and $C\left(x_{3}, y_{3}\right)$ are the vertices of $\triangle A B C$.
(i) The median from A Meets Bc at D. Find the coordinates of the points D.
(ii) Find the coordinates of the point $P$ on Ad such that $A P: P D=2: 1$.
(iii) Find the coordinates of points $Q$ and $R$ on medians $B E$ and $C F$, respectively such that
$B Q: Q E=2: 1$ and $C R: R F=2: 1$.

What are the coordinates of the centroid of the $\triangle A B C$ ?

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11. The points $A\left(x_{1}, y_{1}\right), B\left(x_{2}, y_{2}\right)$ and
$C\left(x_{3}, y_{3}\right)$ are the vertices of $\triangle A B C$.

What are the coordinates of the centroid of the triangle $A B C$.
12.
$A(-3,5), B(-2,-7), C(1,-8) a n d D(6,3)$
are the vertices of a quadrilateral $A B C D$ find its
area.

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13. If $A(4,-6), B(3,-2)$ and $C(5,2)$ are
the vertices of a $\triangle A B C$ and $A D$ is its median, prove that the median $A D$ divides
$\Delta A B C$ into two triangles of equal areas.
14. The midpoint $P$ of the line segment joining the points $A(-10,4)$ and $B(-2,0)$ lies on the line segment joining the points $C(-9,-4)$ and $D(-4$, y). Find the ratio in which P divides $C D$. Also find the value of $y$.

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15. If $A(-4,8), B(-3,-4), C(0,-5)$ and $D(5,6)$ are the
vertices of a quadrilateral $A B C D$, find its area.
16. Find the values of k so that the area of the
triangle with vertices $(1,-1),(-4,2 k)$, and $(-k,-5)$
is 24 sq. units.

## D View Text Solution

17. The base $Q R$ of an equilateral triangle $P Q R$
lies on $x$-axis. The coordinates of the point $Q$ are $(-4,0)$ and origin is the midpoint of the
base. Find the coordinates of the points $P$ and R.

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18. Find the area of quadrilateral $A B C D$, the coordinates of whose vertices are $A(1,2), B(6,2)$,
$C(5,3)$ and $D(3,4)$.

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Self Assessment Test

1. Find the area of triangle with vertices ( 0,0 ),
$(4,0)$ and $(0,5)$.

## D View Text Solution

2. Which point lies on the perpendicular bisector of the line segment joining the points
$A(-3,4)$ andB $(3,-4)$ ?

D View Text Solution
3. If the points $(1, x),(5,2)$ and $(9,5)$ are collinear then find the value of x .

## - View Text Solution

4. In which quadrant, the point which divides
the line segment joining the points $(5,4)$ and $(-6,-7)$ in the ratio $1: 3$ internally lies?

- View Text Solution

5. $A(3,2)$ andB $(-2,1)$ are two vertices of a triangle $A B C$ whose centroid $G$ has the coordinates $\quad\left(\frac{5}{3},-\frac{1}{3}\right)$. Find the coordinates of the third vertex $C$ of the triangle.

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6. Find the point on $x$-axis which is equidistant from $(-2,5)$ and $(2,3)$.
7. Find the condition that the points $A(3,4)$, $B(-5,-6)$ and $C(x, y)$ may lie on the same straight line.

## - View Text Solution

8. In what ratio does the line $x-y-2=0$ divide the line segment joining the points $A(3,-1)$ and $B(8,9)$ ?
9. $A(3,2) \operatorname{and} B(-2,1)$ are two vertices of a triangle $A B C$ whose centroid $G$ has the coordinates $\quad\left(\frac{5}{3},-\frac{1}{3}\right) . \quad$ Find the coordinates of the third vertex $C$ of the triangle.

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10. If $A(-5,7), B(-4,-5), C(-1,-6)$ and $D(4,5)$ are vertices of a quadrilateral, find the area of the quadrilateral $A B C D$.
