# ©゙" doubtnut 

## India's Number 1 Education App

## MATHS

## BOOKS - S CHAND IIT JEE FOUNDATION

## SOME APPLICATIONS OF TRIGONOMETRY

## Solved Examples

1. The angle of elevation of the top of a tower from a point at a distance of 100 metres from its foot on a horizontal plane is found to be $60^{\circ}$. Find the height of the tower
2. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle and by the rope with ground leave is $30^{\circ}$

## - Watch Video Solution

3. A kite if flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. If the length of the string is $40 \sqrt{3}$. find the inclination of the string with the ground

## D Watch Video Solution

4. The angle of depression of a boat $B$ from the top $K$ of a cliff HK, 300 metres high is $30^{\circ}$. Find the distance of the boat from the foot H of the cliff.

## - Watch Video Solution

5. Two men on either side of a temple 126 m high observe the angle of elevation of the top of the temple to be $30^{\circ}$ and $60^{\circ}$ respectively. Find the distance between the two men?

## - Watch Video Solution

6. A tower is 120 m high. Its shadow is s m shorter, when the sun's altitude is $60^{\circ}$ than when it was $45^{\circ}$. Find x correct to
nearest metre .

## - Watch Video Solution

7. The angular elevation of a tower from a point is 30 . As we more 100 m nearer to the base of the tower, the angle of elevation become $60^{\circ}$. Find the height of the tower and the distance of the first point fromt he base of the tower .

## ( Watch Video Solution

8. Two pillars of equal height and on either side of a road, which is 100 m wide. The angles of elevation of the top of the pillars are $60 o$ and $30 o$ at a point on the road between the
pillars. Find the position of the point between the pillars and the height of each pillar.

## - Watch Video Solution

9. A 10 m long flagstaff is fixed on the top of a tower from a point on the ground, the angles of elevations of the top and bottom of flagstaff are $45^{\circ}$ and $30^{\circ}$ respectively. Find the height of the tower

## - Watch Video Solution

10. The angle of depression of 47 m high building form the top of a tower 137 m high is $30^{\circ}$. Calculate the distance between the building and the tower .

Question Bank 34

1. If the angle of elevation of sun is $\theta$ and the length of the shadow of a pole of length $p$ is $s$, then
A. $p=s \cos \theta$
B. $p=s \sin \theta$
C. $p=\frac{s}{\cot \theta}$
D. $p=s \cot \theta$

Answer: C
2. The foot of a ladder leaning against a wall of length 5 metres rests on a level ground $5 \sqrt{3}$ metres from the base of the wall. The angle of inclination of the ladder with the ground is
A. $60^{\circ}$
B. $50^{\circ}$
C. $40^{\circ}$
D. $30^{\circ}$

Answer: D
3. From the top of a light house 60 metre high, with its base at the sea leave, the angel of depression of a boat is $30^{\circ}$. The distance of the boat from the foot of the light - house is
A. $60 \sqrt{3}$ metres
B. $\frac{60}{\sqrt{3}}$ metres
C. 60 metres
D. $30 \sqrt{2}$ metres

## Answer: A

## ( Watch Video Solution

4. A pole is standing erect on the ground which is horizontal.

The tip of the poke is tied tight with a rope of length $\sqrt{12} \mathrm{~m}$
to a point on the ground. If the rope is making $30^{\circ}$ angle with the horizontal , then the height of the pole is
A. $2 \sqrt{3} m$
B. $3 \sqrt{2} \mathrm{~m}$
C. 3 m
D. $\sqrt{3} \mathrm{~m}$

## Answer: D

## - Watch Video Solution

5. Two observers are stationed due north of a tower at a distance of 20 m from each other. If the elevations of the tower observed by them are $30^{\circ}$ and $45^{\circ}$ respectively, then the height of the tower is
A. 10 m
B. 16.32
C. $10(\sqrt{3}+1) m$
D. 30 m

## Answer: C

## D Watch Video Solution

6. Two ships are sailing in the sea on either side of a light house. The angle of depression of the two ships are $45^{\circ}$ each. If the height of the light-house is 300 metres, then the distance between the ships is
A. 600 m
B. $600 / \sqrt{3} m$
C. $300 \sqrt{3} m$
D. 300 m

Answer: A

## - Watch Video Solution

7. Two posts are k metres apart. If from the middle point of the line joining their feet, an observer finds the angles of elevations of their tops to be $60^{\circ}$ and $30^{\circ}$ respectively, then the ratio of heiht of the posts respectively is
A. 3
B. $\frac{1}{3}$
C. $\sqrt{3}$
D. $\frac{1}{\sqrt{3}}$

## Answer: A

## - Watch Video Solution

8. A person standing on the bank of a river observes that the angle subtended by a tree on the opposite of bank is $60^{\circ}$.

When he retires 40 m.from the bank, he finds the angle to be $30^{\circ}$. What is the breadth of the river ?
A. 20 m
B. 24 m
C. 40 m
D. 64 m

Answer: A

## ( Watch Video Solution

9. The horizontal distance between two trees of different heights is 60 m . The angle of depression of the top of the first tree when seen from the top of the second tree is $45 o$. If the height of the second tree is 80 m , find the height of the first tree.
A. $\frac{k}{2 \sqrt{2}}$
B. $\frac{k}{4}$
C. $k \sqrt{2}$
D. $\frac{k}{\sqrt{2}}$

Answer: A

## D Watch Video Solution

10. Two persons are a metres apart and the height of one is double that of the other. If from the middle point of the line joining their feet, an observer finds the angular elevation of their tops to be complementary, then the height of the shorter post is $\frac{a}{4}$ (b) $\frac{a}{\sqrt{2}}$ (c) $a \sqrt{2}$ (d) $\frac{a}{2 \sqrt{2}}$
A. 20 m
B. $10(1+\sqrt{2}) \mathrm{m}$
C. $10 \sqrt{2} \mathrm{~m}$
D. $20 \sqrt{2} \mathrm{~m}$

Answer: A

## - Watch Video Solution

11. A tree $A c$ is broken over by wind from $B$. $D$ is the point where the top of the broken tree touches the ground and BD makes an angle of $45^{\circ}$ with the ground. If the distance between the base of the tree and the point $\mathrm{D}=10 \mathrm{~m}$ What is the height of the tree ?
A. $20 \sqrt{3} m$
B. 60 m
C. $20(\sqrt{3}-1) m$
D. $40 \sqrt{3} m$

Answer: B

## - Watch Video Solution

12. From a point on the ground the angles of elevation of the bottom and top of transmission tower fixed at the top of 20 m high building are $45^{\circ}$ and $60^{\circ}$ respectively. Find the height of the tower ?
A. 43.3 m
B. 57.66 m
C. 86.6 m
D. 100 m

## Answer: C

## - View Text Solution

13. A straight highway leads to the foot of a tower of height

50 m . From the top of the tower, angles of depressions of two cars standing on the highway are $30^{\circ}$ and $60^{\circ}$, What is the distance between the cars ?
A. 100 m
B. 125 m
C. $50 \sqrt{3} m$
D. 150 m
14. The angle of elevation of the top of a hill at the foot of a tower is $60^{\circ}$ and hte angle of elevation of the top of the tower form the foot of the hill is $30^{\circ}$. If the tower is 50 m high, what is the hight of the hill
A. 1350 m
B. 1268 m
C. 1000 m
D. 1160 m

## Answer: D

15. An aeroplane when 3000 m high passes vertically above another aeroplane at an instance when their angles of elevation at the same observation point are $60^{\circ}$ and $45^{\circ}$.. How many metres higher is hits one than the other

## - View Text Solution

## Self Assessment Sheet 33

1. The angle of elevation of the top of a tree of height 18 metres is $30^{\circ}$ when measured form a point $P$ in the plane of its base. The distance of the base of the tree from $P$ is
A. 6 m
B. $6 \sqrt{3} m$
C. 19 m
D. $18 \sqrt{3} \mathrm{~m}$

## Answer: D

## - View Text Solution

2. If the shadow of a pole 3 metre high is $3 \sqrt{3}$ metre long then the angle of elevation of the sun is
A. $30^{\circ}$
B. $45^{\circ}$
C. $60^{\circ}$
D. $75^{\circ}$

Answer: A

## D View Text Solution

3. The angle of depression of two posts $P$ and $Q$ at a distance of 2 metres on the same side of a road from a ballowm (B) vertically over the road are observed to be $45^{\circ}$ and $60^{\circ}$. What is the height of the balloon ?

A. $3-\sqrt{3}$
B. $\sqrt{3}-1$
C. $3+\sqrt{3}$
D. $\sqrt{3}+1$

## Answer: C

## - Watch Video Solution

4. The height of a tower is $h$ and the angle of elevation of the top of the tower is $\alpha$. On moving a distance $\mathrm{h} / 2$ towards the tower, the angle of elevation becomes $\beta$. What is the value of $\cot \alpha-\cot \beta$
A. $\frac{1}{2}$
B. $\frac{2}{3}$
C. 1
D. 2

Answer: A

## - Watch Video Solution

5. Two houses are collinear with the base of a tower and are
at distance 3 m and 12 m (on the same side) from the base of the tower. The angles of elevation from these two houses of the top of the tower are complementary. What is the height of the tower?
A. 4 m
B. 6 m
C. 7.5 m
D. 36 m

Answer: B

## - Watch Video Solution

6. The shadow of a flagstaff is three times as long as the shadow of the flagstaff when the sun rays meet the ground at $60^{\circ}$. Find the angle between the sun rays and the ground at the time of longer shadow
A. $45^{\circ}$
B. $30^{\circ}$
C. $15^{\circ}$
D. $90^{\circ}$

## Answer: B

## - Watch Video Solution

7. From a point $A$ on the ground, the angles of elevation of the top of a 10 m tall building and a helicopter hovering at some height of the building are $30^{\circ}$ and $60^{\circ}$ respectively.

Find the height of the helicopter above the building
A. $10 \sqrt{3}$
B. $20(3+\sqrt{3}) \mathrm{m}$
C. 20 m
D. 30 m

## Answer: C

## D Watch Video Solution

8. From two points $A$ and $B$ on the same side of a building
the angles of elevation of the top of the building are $30^{\circ}$ and $60^{\circ}$ respectively. if the height of the building is 10 $m$ find the distances between $A$ and $B$ correct to two decimal places
A. 10.66 m
B. 13.43 m
C. 11.55 m

## Answer: C

## D Watch Video Solution

9. A man stands on the ground at a point $A$, which is on the same horizontal plane as $B$, the foot of a vertical pole $B C$.

The height of the pole is 10 m . The man's eye is 2 m above the ground. He observes the angle of elevation at C, The top of the pole as $x^{\circ}$ where $\tan x^{\circ}=\frac{2}{5}$. the distance AB (in metres) is
A. 15 m
B. 18 m
C. 20 m
D. 16 m

## Answer: C

## D Watch Video Solution

10. The angle of elevation of the top of an unfinished pillar at a point 150 m from its base is $30^{\circ}$. If the angle of elevation at the same point is to be $45^{\circ}$, then the pillar has to be raised to a height of how many metres?
A. 59.4 m
B. 61.4 m
C. 62.4 m
D. 63.4 m

## Answer: D

## ( Watch Video Solution

## Unit Test 6

1. If $\tan x=\frac{3}{4}, 0<x<90^{\circ}$, then what is value of $\sin \mathrm{x}$ $\cos x ?$
A. $\frac{3}{5}$
B. $\frac{4}{5}$
C. $\frac{12}{25}$
D. $\frac{13}{25}$
2. What is the expression $\frac{\tan x}{1+\sec x}-\frac{\tan x}{1-\sec x}$ equal to ?
A. $\operatorname{cosec} x$
B. $2 \operatorname{cosec} x$
C. $2 \sin x$
D. $2 \cos x$

## Answer: B

## (D) Watch Video Solution

3. If $\tan \theta=1$ and $\sin \phi=\frac{1}{\sqrt{2}}$, and $\theta, \phi \in\left[0, \frac{\pi}{2}\right]$, then the value of $\cos (\theta+\phi)$ is
A. -1
B. 0
C. 1
D. $\frac{\sqrt{3}}{2}$

Answer: B

## D Watch Video Solution

4. If $\cos \theta=\frac{3}{5}$, then the value of $\frac{\sin \theta-\tan \theta+1}{2 \tan ^{2} \theta}$ is
A. $\frac{13}{15}$
B. $\frac{91}{160}$
C. $\frac{14}{15}$
D. $\frac{92}{160}$

## Answer: C

## (D) Watch Video Solution

5. Given $x \cos \theta+y \sin \theta=2$ and $x \cos \theta-y \sin \theta=0$, then which of the following is correct
A. $x^{2}+y^{2}=1$
B. $\frac{1}{x^{2}}+\frac{1}{y^{2}}=1$
C. $x y=1$
D. $x^{2}-y^{2}=1$

Answer: B

D Watch Video Solution
6. Which of the following is /are the value (s) of the the
expression?
$\sin A(1+\tan A)+\cos A(1+\cot A)$

1. $\sec A+\operatorname{cosec} A$
2. $2 \operatorname{cosec} A(\sin a+\cos A)$
3. $\tan A+\cot A$

Select the correct answer using the code given below :
A. 1 only
B. 1 and 2 only
C. 2 only
D. 1 and 3 only

Answer: A
7. If $\sin A=\frac{2 m n}{m^{2}+n^{2}}$, What is the value of $\tan \mathrm{A}$ ?
A. $\frac{2 m n}{m^{2}+n^{2}}$
B. $\frac{2 m n}{m^{2}-n^{2}}$
C. $\frac{m^{2}-n^{2}}{2 m n}$
D. $\frac{m^{2}+n^{2}}{m^{2}-n^{2}}$

Answer: B

## D Watch Video Solution

8. If $\sec ^{2} \theta+\tan ^{2} \theta=\frac{5}{3}$ and $0 \leq \theta \leq \frac{\pi}{2}$ then the value of $\theta$ is equal to
A. $15^{\circ}$
B. $30^{\circ}$
C. $45^{\circ}$
D. $60^{\circ}$

Answer: B

## D Watch Video Solution

9. Evaluate $: \frac{5 \sin ^{2} 30^{\circ}+\cos ^{2} 45^{\circ}+4 \tan ^{2} 60^{\circ}}{2 \sin 30^{\circ} \cos 60^{\circ}+\tan 45^{\circ}}$
A. 1
B. $9 \frac{1}{6}$
C. $7 \frac{3}{7}$
D. $\frac{47}{12}$

Answer: B

## ( Watch Video Solution

10. Evaluate $: \frac{5 \cos ^{2} 60^{\circ}+4 \sec ^{2} 30^{\circ}-\tan ^{2} 45^{\circ}}{\sin ^{2} 30^{\circ}+\cos ^{2} 30^{\circ}}$
A. $2 \frac{5}{16}$
B. $\frac{67}{12}$
C. 0
D. 1

Answer: B
11.
The
value
$\sin ^{2} 1^{\circ}+\sin ^{2} 2^{\circ}+\sin ^{2} 3^{\circ}+\ldots+\sin ^{2} 89^{\circ}+\sin ^{2} 90^{\circ}$
is
A. 1
B. 0
C. 45.5
D. 44

## Answer: C

D Watch Video Solution
12. If $\tan 2 A=\cot \left(A-60^{\circ}\right)$, where 2 A is an acute angle then the value of $A$ is
A. $30^{\circ}$
B. $60^{\circ}$
C. $50^{\circ}$
D. $24^{\circ}$

## Answer: C

## - Watch Video Solution

13. Evaluate $: \frac{2 \cos 53^{\circ} \operatorname{cosec} 37^{\circ}}{\left(\cos ^{2} 29^{\circ}+\cos ^{2} 61^{2}\right)}-3 \tan ^{2} 45^{\circ}$
A. 1
B. 3
C. 6
D. -1

Answer: D

## D Watch Video Solution

14. 

Evaluate
$\sin \theta \cos \theta-\frac{\sin \theta \cos \left(90^{\circ}-\theta\right) \cos \theta}{\sec \left(90^{\circ}-\theta\right)}-\frac{\cos \theta \sin \left(90^{\circ}-\theta\right) \sin \theta}{\operatorname{cosec}\left(90^{\circ}-\theta\right)}$
A. -1
B. 2
C. 0
D. 1

## Answer: C

## (D) Watch Video Solution

15. Using trigonometric identities $5 \operatorname{cosec}^{2} \theta-5 \cot ^{2} \theta$ expressed as an integer is
A. 5
B. 3
C. 2
D. 0

Answer: C
16. The angle of elevation of the top of a tower at $a$ horizontal distance equal to the height of the tower from the base of the tower is
A. $30^{\circ}$
B. $45^{\circ}$
C. $60^{\circ}$
D. any acute angle

## Answer: B

## - Watch Video Solution

17. a person aims at a bird on top of a 5 metre high pole with an elevation of $30^{\circ}$. If the bullet is fired, it will travel k metre
before reaching the bird. The value of $k$ (in meters) is
A. $5 \sqrt{3} / 2$
B. 10
C. $5 \sqrt{3}$
D. $10 \sqrt{3}$

## Answer: B

## - Watch Video Solution

18. Horizontal distance between two pillars of different heights is 60 m . It was observed that the angular elevation from the top of the shorter pillar is $45^{\circ}$. If the height of taller pillar is 130 m , the height of the shorter pillar is
A. 45 m
B. 70 m
C. 80 m
D. 60 m

Answer: B

## D Watch Video Solution

19. The angles of elevation of the top of a tower $h$ metre tall
from two different points ont he same horizontal line are $x$ and $\mathrm{y}(x>y)$. What is the distance between the points
A. $h(\tan x-\tan y)$
B. $\frac{h}{\tan x \tan y}$
C. $\frac{h(\tan x-\tan y)}{\tan x \tan y}$
D. $\frac{h(\tan x \tan y)}{\tan x-\tan y}$

## Answer: C

## - Watch Video Solution

20. A radio transmitter antenna of height 100 m stands at the top of a tall building. At a point on the ground, the angle of elevationof the bottom of the antenna is $45^{\circ}$ and that of the the top of the antenna is $60^{\circ}$. What is the height of the building ?
A. 100 m
B. 50 m
C. $50(\sqrt{3}+1) m$
D. $50(\sqrt{3}-1) m$

## Answer: D

- Watch Video Solution

