



## MATHS

### BOOKS - PEARSON IIT JEE FOUNDATION

#### POLYNOMIALS, LCM AND HCF OF POLYNOMIALS

##### Example 4 1

1. Find the product of  $(a + b + c) \left[ (a - b)^2 + (b - c)^2 + (c - a)^2 \right]$



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##### Example 4 2

1. Factorize  $a^3 + (b - a)^3 - b^3$ .



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### Example 4 3

1. If  $abc = 8$  and  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \frac{3}{2}$ , then find the value of  $ab + bc + ac$ .

A. 10

B. 11

C. 12

D. 13

**Answer: C**



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### Example 4 4

1. The HCF of the polynomials  $(x - 2)(2x^2 + x + a)$  and  $(2x - 1)(x^2 - 5x + b)$  is  $(x - 2)(2x - 1)$ . Find the relation between a and b.



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### Example 4 5

1.

If

$f(x) = (x^2 + 3x + a)$ ,  $g(x) = (x^2 + 5x + b)$ ,  $h(x) = (x^2 + 4x + c)$  and LCM of  $[f(x), g(x)]$  and  $h(x)$  is  $(x + 1)(x + 2)(x + 3)$ , then find  $(a - b + c)$ .



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### Test Your Concepts Very Short Answer Type Questions

1. The degree of the polynomial  $9x^4 - 7x^2 + 8x^3$  is \_\_\_\_\_.



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2. The numerical coefficient of the term  $17x^2$  is \_\_\_\_\_.



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3. The algebraic identity that can be used in evaluating the value of  $(98)^2$  is \_\_\_\_\_.



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4. 
$$\frac{37^3 - 28^3}{37^2 + 37 \cdot 28 + 28^2} =$$



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5. The literal coefficient of the term  $\frac{17}{3}x^3$  \_\_\_\_\_.

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6. The appropriate formula that can be used to find the value of  $\left(50\left(\frac{1}{4}\right) \times 49\left(\frac{3}{4}\right)\right)$  is

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7. If  $(a - b)^2 + (b - c)^2 + (c - a)^2 = 0$ , then the values of a, b, and c are \_\_\_\_\_.

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8. If  $a + \frac{1}{a} = -2$ , then  $a^2 + \frac{1}{a^2} =$  \_\_\_\_\_.

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## Test Your Concepts Factorise The Following

1. factorise  $x^4y - 2x^3y^2$



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2.  $\frac{x^3 + 8}{x + 2} = x^2 + 2x + 4$ . Is the given statement true?



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3. Simplify:  $(-3ab) - (11ab) - (-20ab) - (14ab)$



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$$4. (m+n)(m+n)(m+n)(m-n)(m-n)(m-n) = m^6 - n^6.$$

(True/False)



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$$5. \text{Divide } (4x^3 + 2x - 11) \text{ by } 2x^2.$$



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$$6. \frac{a^3 + b^3 - c^3 + 3abc}{a + b - c} =$$



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$$7. \text{factorise } ax^2y + axy^2 + a^2xy + 2axy.$$



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## Test Your Concepts Simplify The Following

1.  $(x^3 - 2x^2 - 3) \times (-x)$



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2. The HCF of  $(x^2 - 1)^2$ ,  $(x + 1)$  and  $(x^2 - 1)$  is



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3. factorise  $ax - bx + a^2 - ab$



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4. The HCF of  $xy + x^2$ ,  $xy - x^2$  and  $x^4 - x^2y^2$  is



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5. simplify  $(x + 11)^2$



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6. The HCF and LCM of  $36x^2y^3$  and  $32x^3y^2$  are \_\_\_\_\_ and \_\_\_\_\_ respectively.



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7.  $(5a + 2b)^3$  simplify



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8.  $\left(\frac{x}{4} + \frac{2y}{5}\right)^3$  simplify



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9. The LCM of  $27a^5$  and  $81a^{10}$  is  $3^4 a^{10}$ . If the given statement true?



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10. Find the products of the following by using the appropriate identity:

$$(x - 2)(x + 3)$$



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11. Find the products of the following by using the appropriate identity:

$$(x + 5)(x - 11)$$



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12. Find the products of the following by using the appropriate identity:

$$(x - 9)(x - 7)$$



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13. The HCF of  $36xy$  and  $k$  is 6, then the least value of  $k$  is



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14. The LCM of  $(x + a)^2$  and  $(x^2 - a^2)$  is \_\_\_\_\_.



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15. Find the following products using the appropriate identity:

$$(x + 11)(x - 11)$$



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16. Find the following products using the appropriate identity:

$$\left( \frac{x}{3} + \frac{1}{2} \right) \left( \frac{x}{3} - \frac{1}{2} \right)$$



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17. Find the following products using the appropriate identity:

$$(ab + cd)(ab - cd)$$



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18. Find the values of the following by using suitable identity:

$$(55)^2$$



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**19.** Find the values of the following by using suitable identity:

$$(26)^2$$



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**20.** Find the values of the following by using suitable identity:

$$105 \times 95$$



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**21.** Find the values of the following by using suitable identity:

$$52.5 \times 47.5$$



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**22.** Find the values of the following by using suitable identity:

$$(206)^3$$



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**23.** Find the values of the following by using suitable identity:

$$(396)^3$$



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**24.** Factorize

$$x^5y - xy^5$$



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**25. Factorize**

$$x^2 + 5x - 6$$



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**26.**  $(3x^2 + x - 11) \times (7x^3 + 12)$



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**27.** Using the factor method, simplify  $(x^2y + 2xy + x + 2) \div (xy + 1)$ .



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**28.** What must be subtracted from  $2x^2 - 1$  in order to get  $x^3 + x^2 + x + 1$ ?



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**29. Factorize**

$$1 + 6ab + 9a^2b^2$$



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**30. Factorize**

$$8l^3 - 36l^2m + 54lm^2 - 27m^3$$



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**Test Your Concepts Short Answer Type Questions**

**1.** If  $A = 5x^3 - 11$ ,

$B = 9x^3 - 2x^2 + 7$ , and

$C = x^2 + 9$ , then find

$A + C$ .



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**2.** If  $A = 5x^3 - 11$ ,

$B = 9x^3 - 2x^2 + 7$ , and

$C = x^2 + 9$ , then find

$A + (B + C)$ .



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**3.** What must be added to  $7x^3 - 3x^2 + 5x + 4$  in order to get

$9x^3 + x^2 - x - 1$ ?



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## Test Your Concepts Expand The Following By Using Appropriate Identity

1.  $(x + 2y + 3z)^2$



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2.  $(3a - 2b + 5c)^2$



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3. Expand the following by using the identity

$$(a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

$$(2x - 3y)^3$$



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**4.** Expand the following by using the identity

$$(a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

$$\left(\frac{a}{11} - 1\right)^3$$



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**5.** Find the following products.

$$(cx + by)(cx - by) \left( (cx)^2 + (by)^2 \right)$$



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**6.** Find the following products.

$$(a + 1)(a - 1)(a^2 + 1)$$



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**7.** If  $a^2 + b^2 = 40$  and  $ab = 12$ , find  $a + b$  and  $a - b$ .



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**8.** Factorize :

$$64a^3 - 1$$



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**9.** Simplify:

$$(2x + 3y)^2 + (2x - 3y)^2$$



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**10.** Simplify:

$$(1 - ab)^2 - (1 + ab)^2$$



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11. Simplify:

$$(2a - 3b + 1)^2 + (2a - 3b - 1)^2$$



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12. Simplify:

$$(5x + 3y + 2)^2 + (5x + 3y - 2)^2$$



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13. Simplify:

$$(ax + by)^3 - (ax - by)^3$$



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**14. Simplify:**

$$(4x + 7)^3 + (4x - 7)^3$$



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**15.** If  $a - b = 5$  and  $ab = -4$ , then find  $a^3 - b^3$ .



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**16.** If  $a^2 - 2a - 1 = 0$ , then find  $a - \frac{1}{a}$ ,  $a + \frac{1}{a}$ ,  $a^2 + \frac{1}{a^2}$  and  $a^2 - \frac{1}{a^2}$ .



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**Test Your Concepts Essay Type Questions**

1. If  $a^2 + b^2 + c^2 = 24$  and  $ab + bc + ca = -4$ , then find  $a + b + c$ .



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2. Find the LCM and the HCF of the polynomials  $(x^2 - 1)(x^2 + x - 2)$  and  $(x^2 + 2x + 1)(x^2 + 2x - 3)5$ . Verify if the product of the L.C.M and the HCF is equal to the product of polynomials.



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3. If  $x + y + z = 0$ , then find  $(x + y)^3 + (y + z)^3 + (z + x)^3$ .



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4. If  $x + y = 3$  and  $xy = 2$ , then find  $x^4 + y^4$ .



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5. If  $x - y = 3$  and  $xy = 10$ , then find  $x^4 + y^4$ .



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6. If  $x^2 + \frac{1}{x^2} = \frac{17}{4}$ , then find  $x - \frac{1}{x}, x + \frac{1}{x}, x^3 - \frac{1}{x^3}$  and  $x^3 + \frac{1}{x^3}$



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### Concept Application Level 1

1. If  $a + \frac{1}{a} = 3$ , then the value of  $a^2 + \frac{1}{a^2}$  is \_\_\_\_\_.

A. 9

B. 6

C. 7

D. 8

**Answer:** C



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2. If  $a^2 + \frac{1}{a^2} = 27$ , then the value of  $a - \frac{1}{a}$  is \_\_\_\_\_.

A.  $\pm 5$

B.  $\pm 6$

C.  $\pm 7$

D.  $\pm 8$

**Answer:** A



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3. The expansion of  $(x^2 + 4)(x^2 - 4)(x^4 + 16)$  is \_\_\_\_\_.

A.  $x^8 - 128$

B.  $x^4 - 16^2$

C.  $x^6 - 256$

D.  $x^8 - 256$

Answer: D



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4. If the value of  $a^2 + \frac{1}{a^2}$  is 786, then the value of  $a - \frac{1}{a}$  is \_\_\_\_\_.

A.  $\pm 23$

B.  $\pm 25$

C.  $\pm 17$

D.  $\pm 28$

**Answer: D**



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5. Which of the following is the factor of  $4a^2 + b^2 - 4ab + 2b - 4a + 1$ ?

A.  $(a - b)$

B.  $(a + b - 2)$

C.  $(a - b + 2)$

D.  $(2a - b - 1)$

**Answer: D**



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6. Expand  $\left(\frac{x}{3} - \frac{y}{2}\right)^2$

A.  $\frac{x^2}{9} + \frac{y^2}{4}$

B.  $\frac{x^2}{9} - \frac{y^2}{4}$

C.  $\frac{x^2}{9} + \frac{y^2}{4} - \frac{xy}{9}$

D.  $\frac{x^2}{9} + \frac{y^2}{4} + \frac{xy}{9}$

Answer: C



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7. Simplest form of  $\left(\frac{2a}{5} + \frac{3q}{5}\right)^3 - \left(\frac{2a}{5} - \frac{3q}{5}\right)^3$  is

A.  $\frac{1}{125}(54q^3 - 72a^2q)$

B.  $\frac{1}{125}(54q^3 + 72a^2q)$

C.  $\frac{1}{125}(16q^3 + 108aq^2)$

D.  $\frac{1}{125}(16q^3 - 108aq^2)$

**Answer:** B



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8. Factorize the polynomial  $-r^2 + p^2 + q^2 - 2pq$ .

A.  $(p - q - r)(p - q + r)$

B.  $(p + q + r)(p - q - r)$

C.  $(p - q)(q - r)$

D.  $(p - r)(q - r)$

**Answer:** A



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9.  $\left(a + \frac{1}{a} + 2\right)^2 = 4$  then find  $a^2 + \frac{1}{a^2}$  given that  $a^2 + \frac{1}{a^2}$  can not be negative

A. 12

B. 13

C. 14

D. -14

**Answer:** C



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10. The product of the polynomials  $(x^2 - x + 2)$  and  $(x - 1)$  is \_\_\_\_\_.

A.  $x^3 - 2x^2 + 3x - 2$

B.  $x^3 + 3x^2 - 3x + 2$

C.  $x^3 - 2x + 4x^2 - 6$

D.  $x^3 - 2x^2 + 3x + 2$

**Answer: A**



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11. Simplify the equation  $\left(\frac{a}{2} - \frac{b}{3}\right)^3 + \left(\frac{a}{2} + \frac{b}{3}\right)^3$ .

A.  $\frac{a^3}{4} + ab^2$

B.  $\frac{a^3}{4} + \frac{ab^2}{3}$

C.  $\frac{2b^3}{27} + \frac{a^2b}{2}$

D.  $\frac{2b^3}{27} + a^2b$

**Answer: B**



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**12. Factorize :**  $(x - y)^3 + (y - z)^3 + (z - x)^3$

- A.  $2x^3 + 2y^3 + 2z^3$
- B.  $(x - y)(y - z)(z - x)$
- C. 0
- D.  $3(x - y)(y - z)(z - x)$

**Answer:** D



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**13. If**  $x + y = 3$  **and**  $xy = 2$ , **then find**  $x^4 + y^4$ .

- A. 16
- B. 14

C. 18

D. 17

**Answer: D**



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**14.** The HCF of the polynomials  $10(a - 1)(a - 2)^3$ ,  $120(a - 3)(a - 2)^3$ , and  $135(a + 3)(a - 2)^3$  is \_\_\_\_\_.

A.  $25(a - 3)(a - 2)$

B.  $5(a - 3)(a + 2)$

C.  $5(a - 2)^3$

D.  $5(a - 3)(a - 2)(a + 3)$

**Answer: C**



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15. The LCM of the polynomials  $12(x^4 + x^3 + x^2)$  and  $18(x^4 - x)$  is

- A.  $36x^2(x^3 - 1)$
- B.  $36x(x^3 - 1)$
- C.  $36(x^4 + x^3 + x^2)(x^4 - x)$
- D.  $36(x^4 + x^3 + x^2)(x + 1)$

**Answer:** A



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16. The polynomials  $a^2 - b + ab - a$ , on factorization, reduces to \_\_\_\_\_.

A.  $(a + b)(a^2 + b^2)$

B.  $(a + b)(a + 1)$

C.  $(a - b)(a + b)$

D.  $(a + b)(a - 1)$

**Answer:** D



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17. find value  $(8x^3 + 11x) \div 3x$

A.  $\frac{8}{3}x^2 + \frac{11}{3}$

B.  $\frac{8}{3}x^3 + 11x$

C.  $\frac{8}{3}x^2 + \frac{11}{3}x$

D.  $24x^4 + 33x^2$

**Answer:** A



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18. The HCF of polynomials  $x^3 - 1$  and  $x^2 - 1$  is \_\_\_\_\_.

A.  $x - 1$

B.  $x + 1$

C.  $x^2 - x + 1$

D. 1

**Answer:** A



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19. The factorized form of the polynomial  $y^2 + (x - 1)y - x$  is

A.  $(y + x - 1)(x + 1)$

B.  $(y + 1)(x - 1)$

C.  $(y - 1)(y + x)$

D.  $(x - 1)(x + y)$

**Answer: C**



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**20.** if  $a + b = 3$  and  $ab = 2$ , then find  $a^3 + b^3$ .

A. 6

B. 4

C. 9

D. 12

**Answer: C**



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**21.** The value of  $51^3 + 49^3$  is

A.  $5^6 2^4 - 300$

B.  $5^6 2^4 + 300$

C. 250, 000

D.  $5^6 2^4 + 299$

**Answer:** B



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**22.** If  $x + y + z = 5$  and  $xy + yz + zx = 7$ , then  
 $x^3 + y^3 + z^3 - 3xyz = \underline{\hspace{2cm}}$ .



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**23.** Factorization of the polynomial

$(x - y)^2 a^2 + 2(x - y)(x + y)ab + b^2(x + y)^2$  gives

- A.  $(ax - by)(ax + by)$
- B.  $(ax + by)(bx + ay)$
- C.  $(ax - ay + bx + by)^2$
- D.  $(ax + ay + bx + by)^2$

**Answer:** C



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**24.** The factors of the expression  $x^2 - 2x - 63$  are \_\_\_\_\_.

- A.  $x - 7, x - 9$
- B.  $x + 7, x + 9$

C.  $x + 7, x - 9$

D.  $x - 7, x + 9$

**Answer: C**



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25. If  $ab + bc + ca = 4$  and  $abc = 2$ , then find the value of

$$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \text{_____}.$$

A. 2

B. 1

C. 0

D. -1

**Answer: A**



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**26.** Factorize  $x^2 - y^2 + z^2 - a^2 + 2(xz + ay)$

A.  $(x + y + z - a)(x - y + z - a)$

B.  $(x + z - y + a)(x + y + z - a)$

C.  $(x - y + z + a)(x + y - z + a)$

D.  $(x - y - z - a)(x + y + z + a)$

**Answer:** B



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**27.** If  $x + \frac{1}{x} = 7$  then  $x^3 - \frac{1}{x^3}$  is

A.  $9\sqrt{5}$

B.  $144\sqrt{5}$

C.  $135\sqrt{5}$

D.  $\sqrt{5}$

**Answer: B**



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28. If  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 1$  and  $abc = 2$  then find  $ab^2c^2 + a^2bc^2 + a^2b^2c$  is

A. 4

B. -4

C. 2

D. -2

**Answer: A**



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**29.** If  $a^3 + b^3 = 5$  and  $a + b = 1$ , then find the value of ab.



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**30.** Simplify  $\left(x^{\frac{2}{3}} - y^{\frac{2}{3}}\right)\left(x^{\frac{4}{3}} + x^{\frac{2}{3}}y^{\frac{2}{3}} + y^{\frac{4}{3}}\right)$



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**31.** If  $x^3 + \frac{1}{x^3} = 62$ , then find the value of  $\sqrt{x^3} + \frac{1}{\sqrt{x^3}}$ .

The following steps are involved in solving the above problem.

Arrange them in sequential order.

(A)  $\therefore \left(\sqrt{x^3} + \frac{1}{\sqrt{x^3}}\right)^2 = 62 + 2 = 64$

(B)  $\Rightarrow \left(\sqrt{x^3} + \frac{1}{\sqrt{x^3}}\right) = \sqrt{64} = 8$

(C)  $\therefore \left(\sqrt{x^3} + \frac{1}{\sqrt{x^3}}\right)^2 = x^3 + \frac{1}{x^3} + 2$

(D) But  $x^3 + \frac{1}{x^3} = 62$

A. CABD

B. ABCD

C. ACDB

D. CDAB

**Answer:** D



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32. The square of binomial is a \_\_\_\_\_.

A. Monomial

B. Binomial

C. Trinomial

D. None of these

**Answer:** C



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33. Which of the following is a binomial?

A.  $ax$

B.  $(x - y)^2$

C.  $(x + y)^2$

D.  $(x + y)(x - y)$

Answer: D



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Concept Application Level 2

1. If  $x^2 + y^2 + xy = 1$  and  $x + y = 2$ , then find  $xy$ .

A. -3

B. 3

C.  $-\frac{3}{2}$

D.  $-\frac{2}{3}$

**Answer:** B



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2.35. Factorization of the polynomial,  $11x^2 - 10\sqrt{3}x - 3$  gives

A.  $(x + \sqrt{3})(11x - \sqrt{3})$

B.  $(x + 3\sqrt{3})(11x - \sqrt{3})$

C.  $(x - \sqrt{3})(11x + \sqrt{3})$

D.  $(x + \sqrt{3})(11x + \sqrt{3})$

**Answer:** C



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3. If  $h(y) = y^2$  and  $g(z) = z^3$ , then the HCF of  $h(b) - h(a)$  and  $g(b) - g(a)$  is \_\_\_\_\_.

A.  $a + b$

B.  $a^2 - b^2$

C.  $b - a$

D.  $a - b$

**Answer: C**



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4. The HCF of the polynomials  $(x^3 - 9^3)(x + 3)$  and  $(x^2 - 9)(x^2 - 3)$  is \_\_\_\_\_.

A.  $x + \sqrt{3}$

B.  $x - 9$

C.  $x + 3$

D.  $x - 3$

**Answer:** C



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5.  $x^2 + y^2 - z^2 - 2xy$

A.  $(x - y - z)(x - y + z)$

B.  $(x + y + z)(x - y + z)$

C.  $(x + y + z)(x - y - z)$

D.  $(x - y + z)(x + y - z)$

**Answer:** A



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6. The polynomial  $x^3 + 8y^3 + 27z^3 - 18xyz$  on factorization gives \_\_\_\_\_.

- A.  $(x + 2y + 3z)(x^2 + 4y^2 + 9z^2 + 2xy + 6yz + 3zx)$
- B.  $(x + 2y + 3z)(x^2 + 4y^2 + 9z^2 + 4xy + 12yz + 6zx)$
- C.  $(x + 2y + 3z)(x^2 + 4y^2 + 9z^2 + 2xy - 6yz - 3zx)$
- D.  $(x + 2y + 3z)(x^2 + 4y^2 + 9z^2 - 2xy - 12yz - 6zx)$

**Answer: C**



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7. The polynomial  $x^4 + 12x^2 + 64$  on factorization gives \_\_\_\_\_.

- A.  $(x^2 - 2x + 8)(x^2 + 2x - 8)$

B.  $(x^2 - 2x - 8)(x^2 + 2x + 8)$

C.  $(x^2 + 2x - 8)(x^2 - 2x - 8)$

D.  $(x^2 - 2x + 8)(x^2 + 2x + 8)$

**Answer: D**



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8. The HCF of  $(x - 1)(x^2 - 4)$  and  $(x^2 - 1)(x + 2)$  is \_\_\_\_\_.

A.  $x - 2$

B.  $x + 1$

C.  $x - 1$

D.  $(x - 1)(x + 2)$

**Answer: D**



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9. The *HCF* and *LCM* of the polynomials  $p(x)$  and  $q(x)$  are  $(x^2 + 2x)(x^2 - 20x + 91)$  and  $2x^2(x^2 - 2x - 143)(x^2 - 5x - 14)$ . If  $p(x)$  is  $x(x - 13)(x - 7)(x^2 + 13x + 22)$ , then  $q(x)$  is

A.  $2x^2(x^2 - 20x + 91)(x - 2)$

B.  $2x^2(x - 9)^2(x - 11)$

C.  $2x^2(x^2 - 20x + 91)(x + 2)$

D.  $2x^2(x^2 + 20x - 91)(x + 2)$

**Answer: C**



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10. The LCM of the polynomials  $(x - 3)(x + 5)^2$ ,  $(x + 5)(x - 7)^2$  and  $(x - 7)(x - 3)^2$  is

-----.

A.  $(x - 3)(x - 7)(x - 5)$

B. 1

C.  $(x - 3)^2(x - 7)^2(x + 5)^2$

D.  $(x - 3)^2(x - 7)^2$

**Answer: C**



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**11.** The factors of the expression

$a + b + c + 2\sqrt{ab} - 2\sqrt{bc} - 2\sqrt{ca}$  are \_\_\_\_\_.

A.  $\sqrt{a} - \sqrt{b} + \sqrt{c}, \sqrt{a} - \sqrt{b} + \sqrt{c}$

B.  $\sqrt{a} + \sqrt{b} - \sqrt{c}, \sqrt{a} - \sqrt{b} + \sqrt{c}$

C.  $\sqrt{a} + \sqrt{b} - \sqrt{c}, \sqrt{a} + \sqrt{b} - \sqrt{c}$

D.  $\sqrt{a} + \sqrt{b} - \sqrt{c}$ ,  $\sqrt{a} + b - c$

**Answer: C**



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12. The HCF of two polynomials A and B using longdivision method was found to be  $2x + 1$  after twosteps. The first two quotients obtained are  $x$  and  $(x + 1)$ . Find A and B. Given that degree of  $A >$  degree of B.

A.  $A = 2x^3 + 3x^2 + x - 1$ ,  $B = 2x^2 - 3x + 1$

B.  $A = 2x^3 - 3x^2 + x - 1$ ,  $B = 2x^2 - 3x - 1$

C.  $A = 2x^3 + 3x^2 - 3x - 1$ ,  $B = 2x^2 - 3x + 1$

D.  $A = 2x^3 + 3x^2 + 3x + 1$ ,  $B = 2x^2 + 3x + 1$

**Answer: D**

13. The polynomial,  $x^6 + 64y^6$  on factorization gives \_\_\_\_\_.

- A.  $(x^2 + 4y^2)(x^4 - 4y^4)$
- B.  $(x^2 + 4y^2)(x^4 - 4x^2y^2 + 16y^4)$
- C.  $(x^2 - 4y^2)(x^4 + 4y^4)$
- D.  $(x^2 + 4y^2)(x^4 + 4x^2y^2 + 16y^4)$

**Answer: B**



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14. If the LCM of the polynomials  $(x - 3)(x - p)$  and  $(x + 3)(x + 5)$  is  $(x - 3)(x + 3)(x - p)$ , then p is \_\_\_\_\_.

A. -5

B. -4

C. -2

D. -1

**Answer: A**



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**15.** The number of terms which contain variables in the expansion of

$$\left(x + \frac{1}{x} + 1\right)^2 \quad (\text{A})\ 6 \ (\text{B})\ 5 \ (\text{C})\ 4 \ (\text{D})\ 3$$

A. 6

B. 5

C. 4

D. 3

**Answer: C**



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- 16.** If  $(a + b + c)^2 = 36$ ,  $ab + bc + ca = 11$  and  $a, b, c \in N$ , then find  $a^2 + b^2 + c^2$ .

A. 17

B. 22

C. 14

D. 6

**Answer: C**



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- 17.** If  $2x + \frac{y}{3} = 12$  and  $xy = 30$ , then find  $8x^3 + \frac{y^3}{27}$ .

A. 1008

B. 168

C. 106

D. 108

**Answer: A**



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**18.** Find the LCM of the polynomials  $5(x^3 - y^3)$  and  $35(x^6 - y^6)$ .

A.  $(x - y)$

B.  $5(x^3 - y^3)$

C.  $35(x^3 - y^3)$

D.  $35(x^6 - y^6)$

**Answer: D**



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19. Find the HCF of the polynomials  $6(x^2 - 36)$  and  $36(x + 6)$ .

A.  $6(x + 6)$

B.  $6(x - 6)$

C.  $(x + 6)$

D.  $(x - 6)$

**Answer: A**



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20. If  $a^2 + b^2 + c^2 = 29$ ,  $ab + bc + ca = 26$  and  $a, b, c \in N$ , then

find  $a + b + c$ .

A. 9

B. 6

C. 7

D. 10

**Answer: A**



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**21.** If  $3x - \frac{y}{5} = 10$  and  $xy = 5$ , then find  $27x^3 - \frac{y^3}{125}$

A. 1060

B. 1150

C. 112

D. 1000

**Answer: B**



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## Concept Application Level 3

1. If  $a + b + c = 6$  and  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \frac{3}{2}$ , then find  $\frac{a}{b} + \frac{a}{c} + \frac{b}{a} + \frac{b}{c} + \frac{c}{a} + \frac{c}{b}$ .

A. 6

B. 4

C. 9

D. 12

**Answer: A**



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2. If  $\left(\frac{a}{b}\right) + \left(\frac{b}{a}\right) = 2$ , then find  $\left(\frac{a}{b}\right)^{100} - \left(\frac{b}{a}\right)^{100}$

A.  $\frac{2^{20} - 1}{2^{10}}$

B. 2

C. 0

D.  $\frac{2^{20} + 1}{2^{10}}$

**Answer: C**



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3. factors of  $x^4 + y^4 - x^2y^2 = \underline{\hspace{2cm}}$ .

A.  $(x^2 + y^2 + \sqrt{3}xy)(x^2 + y^2 - \sqrt{3}xy)$

B.  $(x^2 - y^2 + \sqrt{3}xy)(x^2 - y^2 - \sqrt{3}xy)$

C.  $(x^2 - y^2 + \sqrt{3}xy)(y^2 - x^2 - \sqrt{3}xy)$

D.  $(x^2 + y^2 - \sqrt{3}xy)(x^2 + y^2 - \sqrt{3}xy)$

**Answer: A**



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4. If  $p(x) = (x - 4)^p(x + 6)^5$ ,  $q(x) = (x + 6)^q(x - 4)^6$  and LCM of  $p(x)$  and  $q(x)$  is  $(x - 4)^6(x + 6)^q$ , then find the maximum value of  $(p - q)$

A. -1

B. 0

C. 1

D. 11

**Answer: C**



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5. If  $x^2 + y^2 - xy = 3$  and  $y - x = 1$ , then find  $\frac{xy}{x^2 - y^2}$ .

- A.  $\frac{2}{5}$
- B.  $\frac{5}{2}$
- C.  $\frac{3}{5}$
- D.  $\frac{5}{3}$

**Answer:** A



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6. If  $abc = 6$  and  $a + b + c = 6$ , then find the value of  $\frac{1}{ac} + \frac{1}{ab} + \frac{1}{bc}$ .

- A. 2
- B. 1
- C. 3
- D. 0

**Answer: B**



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