





MATHS

BOOKS - NAND LAL PUBLICATION

UNDERSTANDING QUADRILATERALS



1. Match the following (caution !A figure may match to more

than one type)

	Figure	Туре	
1.	\sim	(a) Simple closed curve	
2.	· 7	(b) A closed curve that is not simple	
3.	0	(c) Simple curve that is not closed	
4.	\square	(d) Not a simple curve.	

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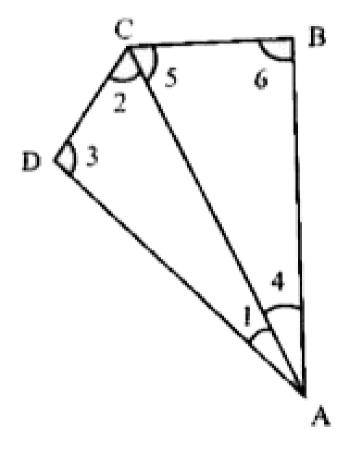
2. Try to give few more examples and non -example for a polygon .

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3. Take any quadrilateral , say ABCD .Divide it into two triangles by drawing a diagonal . You get six angles 1,2,3 ,4,5 and 6 . Use the angles sum property of a triangle and argue

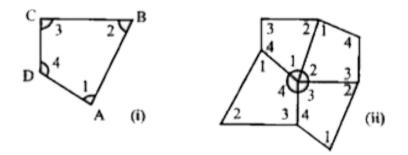
how the sum of the measures of $\angle A, \angle B, \angle C \angle D$ amounts

to 180° + 180° = 360° .





4. Take four congruent card board colpes of any quadrilateral ABCD , with angles as shown (fig i) Arrange the copies as shown in the figure , where angles $\angle 1$, $\angle 2$, $\angle 3$, $\angle 4$,meet at a point (fig .ii)



What can you say about the sum of the angles $\angle 1, \angle 2, \angle 3 \angle 4$

?



5. As before consider quadrilateral ABCD Let P . Be any point in its interior .Join P to vertices A,B,C and D . In the figure

,consider ΔPAB .

From this we see $x=180^{\circ}-m\angle 2-m\angle 3$.

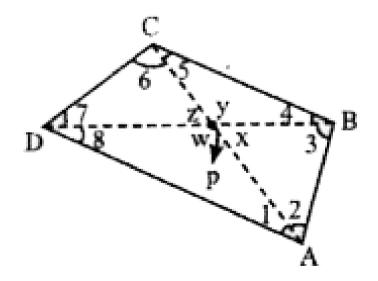
Similarly from $\Delta PBC, y = 180^\circ - m \measuredangle 4 - m \measuredangle 5$, from ΔPCD

 $z = 180^\circ - m \measuredangle 6 - m \measuredangle 7 \, ext{ and } \, ext{ from } \Delta PDA$

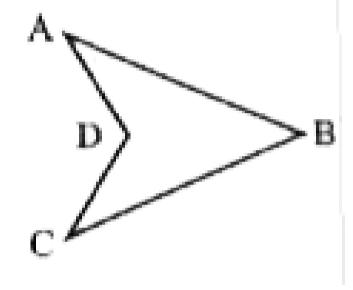
 $w = 180^\circ - m \measuredangle 8 - m \measuredangle 1$

Use this to find the total measure $m \angle 1 + \angle 2 + \dots + m \angle 8$, does it help you to arive at the result ?

Remember $\angle x + \angle y + \angle z + \angle w = 360^\circ$



6. Consider quadrilateral ABCD .Split it into two triangles to find the sum of the interior angles of quadrilateral ABCD

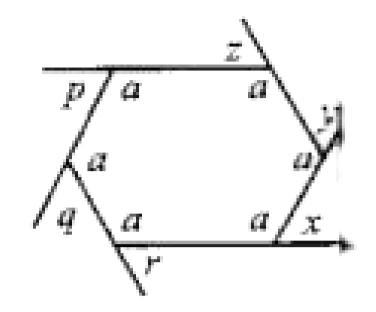




7. In a regular hexagon.

What is the sum of the measures of its exterior angles x

y,z,p,q,r?



8. If
$$x^p. \ y^q = \left(x+y
ight)^{p+q}$$
 , show that $\displaystyle rac{dy}{dx} = \displaystyle rac{y}{x};$

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9. What is the measure of each ?

- (i) exterior angle
- (ii) Interior angle.

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10. Take a regular hexagon. Repeat this activity for the cases

of octagon

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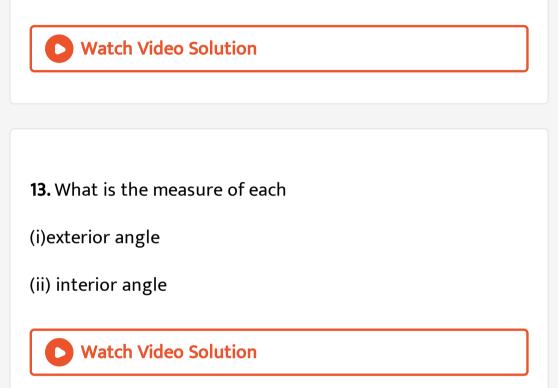
11. What is the sum of the measure of its exterior angles a

,b,c,d,e,f,g,h.



12. Is a =b=c=d=e=f=g=h ? why ? . where

a,b,c,d,e,f,g,h are the sides of octagon



14. What is the sum of the measures of its exterior angles?

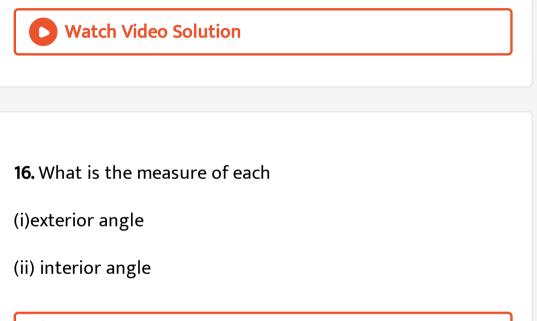


15.

$$a=b=c=d=e=f=g=h=$$
 , $m=n=o=p=q=r$

? Why ? where a,b,c,d,e,f,g and h are the sides of octagon and

m,n,o,p,q,r are the sides of hexagon .



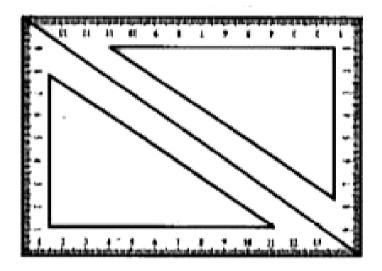
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17. Take two identical set squares with angles $30^{\circ}-60^{\circ}-90^{\circ}$ and place these adjacently to form a

parallelogram as shwon in the fig .

Does this help you to verify the above property

property: The opposite sides of a parallelogram are of equal length.



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18. Find x+y+z



1. a,b,c and d are the angle of any quadrilater .if $\angle a = 45, \angle b = 60, \angle c = 100.$ Find $\angle d$

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2. A mason has made a concrete slab .He needs it to be rectangular . In what different ways can he make sure that it is rectangular ?



3. A square was defined as a rectangle with all sides equal .

Can we define it as rhobus with equal angles ? Explain this

idea .
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4. Can a trapezium have all angles equal ? Can it have all
sides equal ? Explain .
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Do This
1. Take identical cut outs of congruent triangles of sides 3 cm ,4cm , 5cm Arrange them as shown .
$A \qquad 5 \text{ cm} \qquad E \qquad 5 \text{ cm} \qquad B$

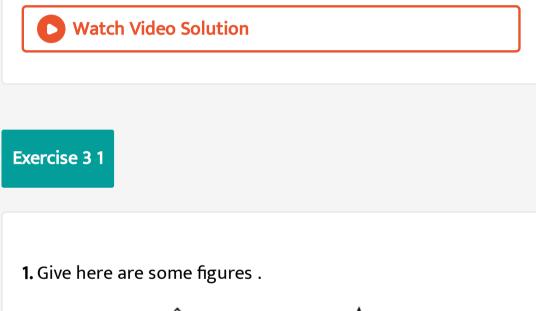
You get a trapezium (check if) which are the parallel sides

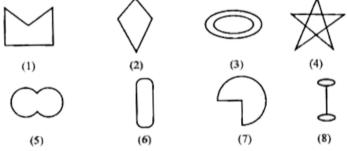
here ?

should the non -parallel sides be equal ?

You can get two more trapeziums using the same set of

triangles. Find them out and discuss their shapes.





Classify each of them on the basis of the following

(a) Simple curve

- (b) Simple closed curve,
- (c) Polygon
- (d) Convex polygon
- (e) Concave polygon

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2. How many diagonals does each of the following have ?

A convex quadrailateral

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3. How many diagonals does each of the following have ?

A Triangle





4. How many diagonals does each of the following have ?

A Triangle

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5. What is the sum of the measures of the angles of a convex quadrilateral? Will this property hold if the quadrilateral is not convex? (Make a non-convex quadrilateral and try!)



6. Examine the table .(Each figure is divided into triangles and the angles deduced from that.)

Figure	\triangle	\bigtriangleup		\bigcirc
Side	3	4	5	6
Angle sum	180°	2 × 180° = (4 - 2) × 180°	3 × 180° = (5 - 2) × 180°	$4 \times 180^{\circ}$ = (6 - 2) × 180°

What can you say about the angle sum of a convex polygon

with number of sides ?

7 Sides

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7. Examine the table. (Each figure is divided into triangles and

the sum of the angles deduced from that.)

Figure	$ \land $	\bigcirc	\bigcirc	
Side	3	4	5	6
Angle sum	180°	$2 \times 180^{\circ}$ = (4 - 2) × 180°	$3 \times 180^{\circ}$ = $(5-2) \times 180^{\circ}$	$4 \times 180^{\circ}$ = (6 - 2) × 180°

What can

you say about the angle sum of a convex polygon with

number of sides? 8

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8. Examine the table .(Each figure is divided into triangles and the angles deduced from that.)

Figure	\triangle	\triangle	\bigcirc	
Side	3	4	5	6
Angle sum	180°	2 × 180° = (4 - 2) × 180°	3 × 180° = (5 - 2) × 180°	$4 \times 180^{\circ}$ = (6 - 2) × 180°

What can you say about the angle sum of a convex polygon

with number of sides ?

10 sides



9. Examine the table .(Each figure is divided into triangles

and the angles deduced from that.)

Figure	\triangle	\bigtriangleup	\bigcirc	
Side	3	4	5	6
Angle sum	180°	2 × 180° = (4 - 2) × 180°	3 × 180° = (5 - 2) × 180°	$4 \times 180^{\circ}$ = (6 - 2) × 180°

What can you say about the angle sum of a convex polygon

with number of sides ?

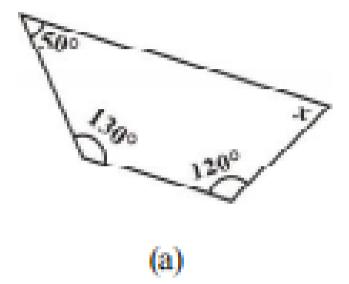
n sides

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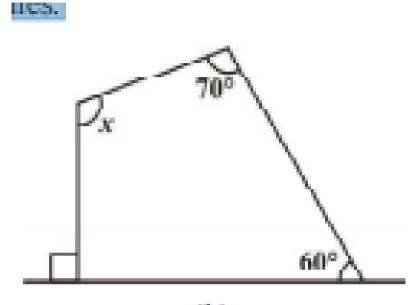
10. What is a regular polygon ? State the name of regular

polygon of

(i) 3 sides , (ii) 4 sides , (iii) 6 sides

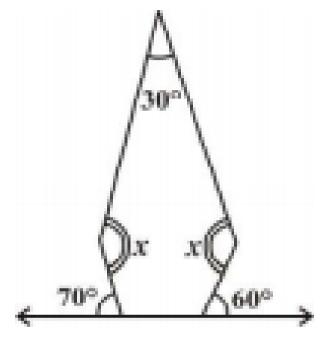






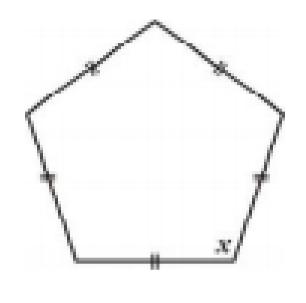
(b)





(c)









15. Find x+y+z





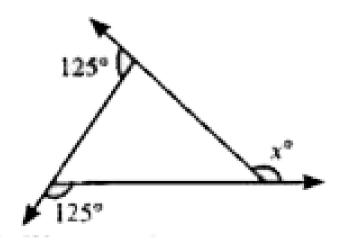


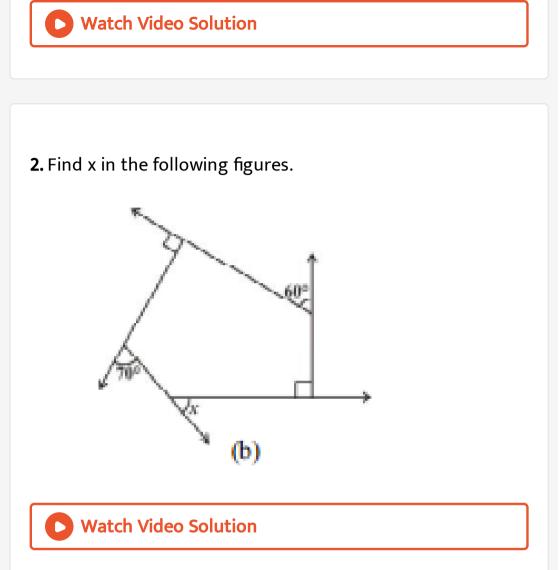
Find x+y+z+w.

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1. Find x in the following figures .





3. Find the measure of each exterior angle of a regular polygon of

9 sides



4. Find the measure of each exterior angle of a regular

polygon of

15 sides



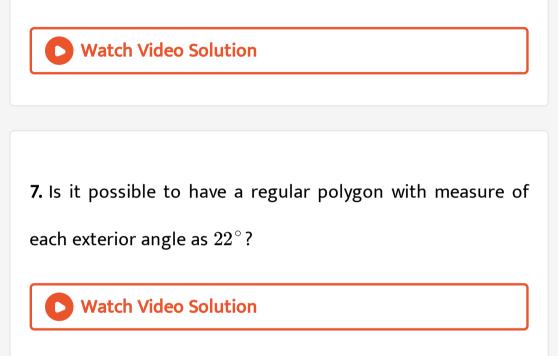
5. How many sides does a regular polygon have if the

measure of an exterior angle is 24° ?



6. How many sides does a regular polygon have if each of its

interior angles is 165° ?

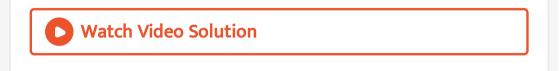


8. Can 22° be an interior angle of a regular polygon ? Why ?

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9. What is the minimum interior angle possible for a regular

polygon? Why?

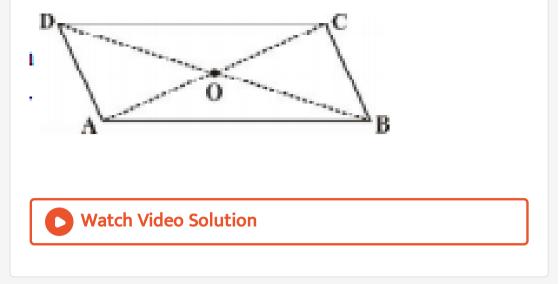


10. What is the maximum exterior angle possible for a regular polygon?

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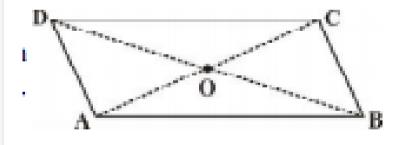
Exercise 3 3

1. Given a parallelogram ABCD. Complete each statement along with the definition or property used AD =



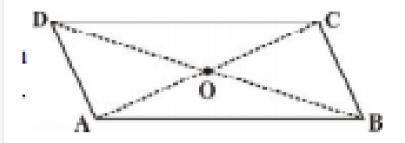
2. Given a parallelogram ABCD. Complete each statement

along with the definition or property used OC =



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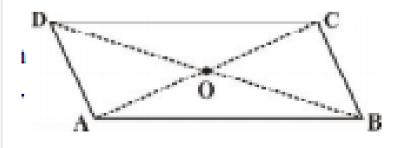
3. Given a parallelogram ABCD. Complete each statement along with the definition or property used OC =



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4. Given a parallelogram ABCD. Complete each statement

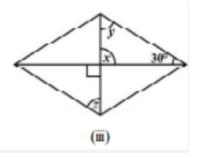
along with the definition or property used OC =





5. Consider the following parallelograms. Find the values of

the unknowns x, y, z.





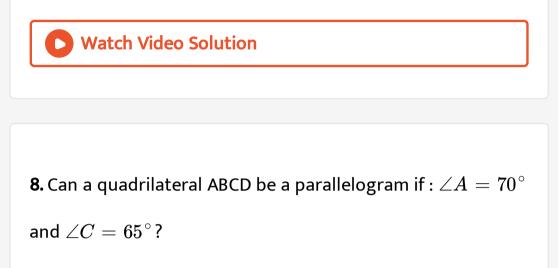
6. Can a quadrilateral ABCD be a parallelogram if :

 $\angle D + \angle B = 180^{\circ}$?

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7. Can a quadrilateral ABCD be a parallelogram if

:AB=DC=8cm,AD=4cm and BC =4.4cm?



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9. Draw a rough figure of a quadrilateral that is not a parallelogram but has exactly two opposite angles of equal measure.



10. The measures of two adjacent angles of a parallelogram are in the ratio 3 : 2. Find the measure of each of the angles of the parallelogram.

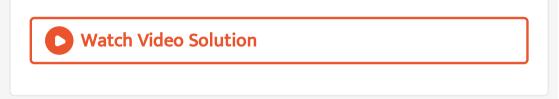


11. Two adjacent angles of a parallelogram have equal measure. Find the measure of each of the angles of the parallelogram.

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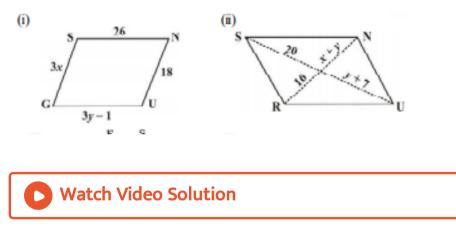
12. The adjacent figure HOPE is a parallelogram.Find the angle measures x,y and z.State the properties you use to find



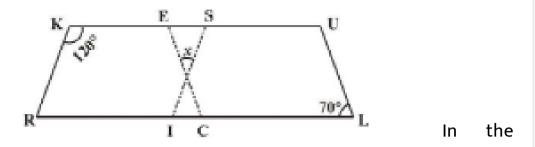


13. The following figures GUNS and RUNS are parallelograms.

Find x and y. (Lengths are in cm)



14.



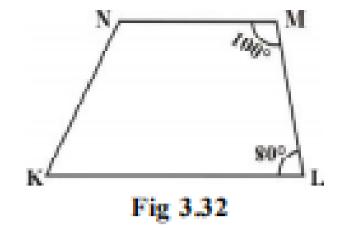
above figure both RISK and CLUE are parallelograms. Find the

value of x.



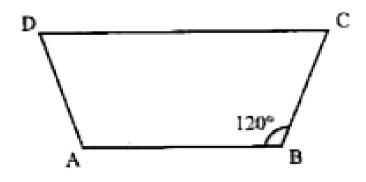
15. Explain how this figure is a trapezium. Which of its two

sides are parallel? (Fig 3.32)

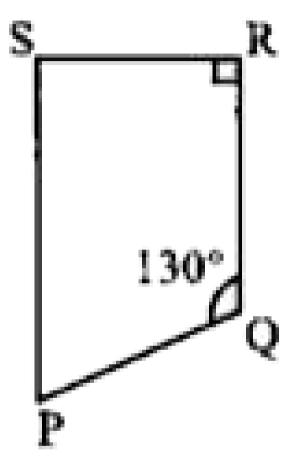




16. Find $m \angle C$ in the figure if $\overline{AB} \mid \ \mid DC$



17. Find the measure of $\angle P$ and $\angle S$ if $\overline{SP} \mid | \overline{RQ}$





1. State whether True or False. All rectangles are squares

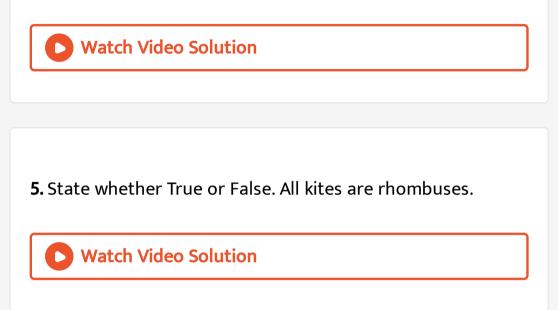
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2. State whether True or False. All rhombuses are	
parallelograms	
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3. State whether True or False. All squares are rhombuses

and also rectangles



4. State whether True or False. All squares are not parallelograms.



6. State whether True or False. All parallelograms are trapeziums.

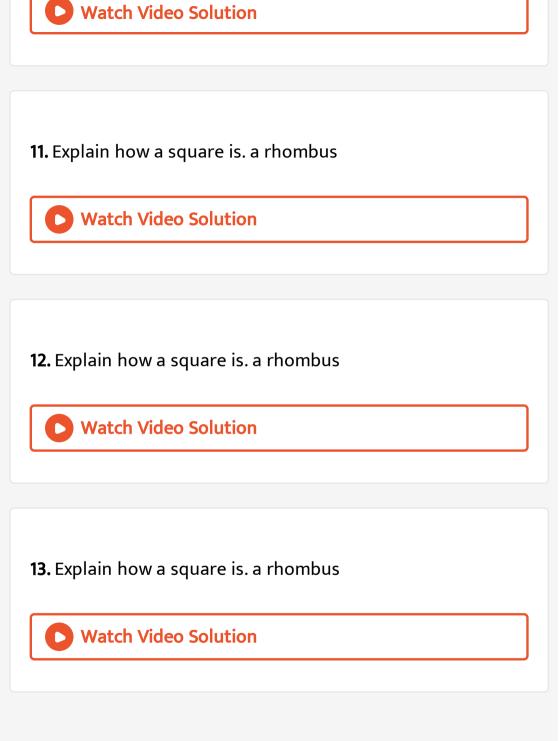


7. State whether True or False. All squares are trapeziums.

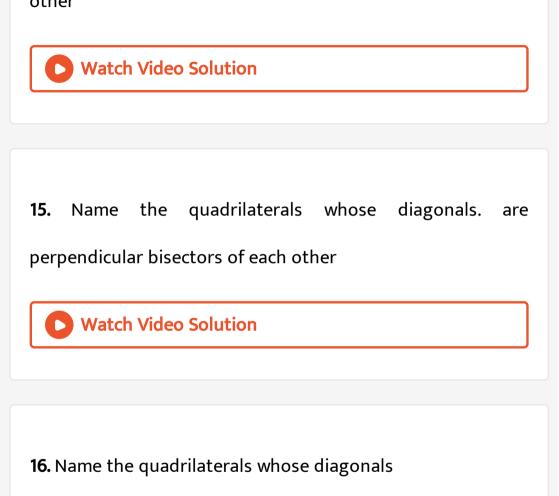
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8. Identify all the quadrilaterals that have. four sides of equal length
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9. Identify all the quadrilaterals that have. four right angles
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10. Explain how a square is. a quadrilateral





14. Name the quadrilaterals whose diagonals. bisect each other



(i) bisect each other .

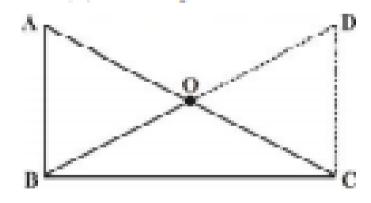
(ii) are equal



17. Explain why a rectangle is a convex quadrilateral.



18. ABC is a right-angled triangle and O is the mid point of the side opposite to the right angle. Explain why O is equidistant from A, B and C. (The dotted lines are drawn additionally to help you).



1. Diagonals of which figure bisect each other at right angles

(i) parallelogram

(ii) rectangle

(iii) rhombus

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2. The four angles quadrilaterals add upto

 $180^{\,\circ}$

(ii) 360°

(iii) 54

3. Number of diagonals in a hexagon are

(i) 6

(ii) 5

(iii) <u>9</u>



4. Sum of all the interior angles of a pentagon are

(i) 540°

(ii) 720°

(iii) 360°

5. Which of the following cannot be the angles of a quadrilateral ?

 $70^{\,\circ}\,,\,80^{\,\circ}\,,\,90^{\,\circ}\,,\,120^{\,\circ}$

(ii) $102^\circ, 88^\circ, 92^\circ, 78^\circ$

(iii) $80^\circ, 85^\circ, 90^\circ, 78^\circ$

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6. Adjacent sides of the polygon are

(i) Any 2 sides of the polygon

(ii) Any 2 sides with common vertex

(iii) any two sides connecting non - consecutive vertices

- 7. Which is not correct ?
- (i) Equilateral Δ is a regular polygon
- (ii) Square is a regular polygon
- (iii) Rhombus is a regular polygon

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8. Fill in the blanks .

Every _ is a rectangle .



9. Isosceles trapezium is a trapezium in which base angles

are ____





10. Adjacent angles of a paralleogram are supplementary .

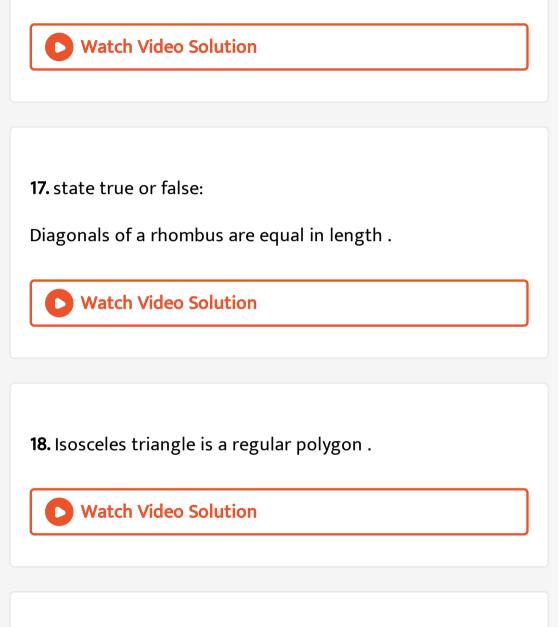
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11. Sum of interior angles of a 9 sided polygon are
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12. Number of diagonals in a octagen are 20 .



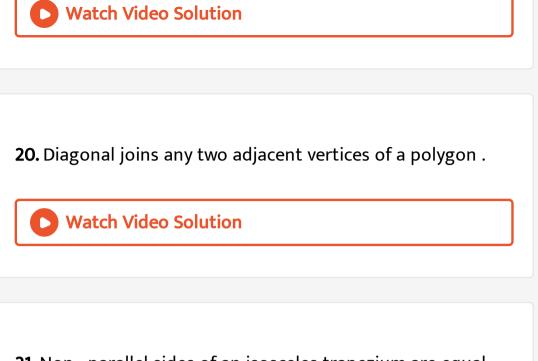
13. If an angle of a parallelogram is a right angle then it is
called a
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14. If two adjacent sides of a rectangle are equal then it is
called a
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15. State whether True or False .
Diagonals bisect in a trapezium .

16. At least one angle of a concave quadrilateral is greater

than 180° .



19. Every curve is a closed curve .



21. Non - parallel sides of an isosceles trapezium are equal .

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Additional Questions For Practice Short Answer Type Questions

1. Which of the following figure is a regular polygon?

A. (a) Any triangle

B. (b) Right angle triangle

C. (c) Equilater triangle

D. (d) none of these

Answer:



Additional Questions For Practice Long Answer Type Questions

1. Ratio between the exterior angle and interior angle of a regular polygon is 2:7 .Find the number of sides of the polygon .



2. Angles of the quadrilateral are $(2x+1)^{\,\circ},\,(2x+9)^{\,\circ},\,(3x-4)^{\,\circ},\,(x+10)^{\,\circ}$.Find the

measure of each of the angles of the quadrilateral .



3. ABCDEF is a regular hexagon with line I passing through

side AF . Find the measure of $\angle x \; ext{and} \; \angle y$.



4. Find the measure of each angle of the parallelogram if the

larger angle is 60° less than twice of smaller angles .



5. PQRS is a rhombus . $\angle QRP = 55^{\,\circ}$. Find $\angle PSR$

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6. Sum of all the interior angles of a regular polygon is twice sum of its exterior angles .Find the number of sides of the polygon .



7. One of the sides of the parallelogram is 6 cm more than the other . If its perimeted is 36 cm . Find the sides of the parallelogram .



1. If the length of the side of a rhombus is equal to the

length of one diagonal Find the angles of the rhombus .



Sample Paper For Practice

1. Correct the statements given below .

Parallel sides of the isosceles trapezium are equal .

2. Sum of all the interior angles of a quadrilateral is 180° ?.

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3. Diagonals of the parallelogram bisect each other at right angles .
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4. Minimum number of sides in a polygon is 2.
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5. Fill in the blank spaces .

A regular polygon each of whose angle is ______ a regular

polygon at 5 sides .

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6. Measure of each interior angle of a polygon is equal to 8

times the measure of each exterior angle . Then the number

of sides of polygon has____

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7. Diagonals of the rhombus bisect each other at ______.

8. Sum of all interior angles of a n sided polygon is _____ .

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9. Number of diagonals in a hexagon are
(i) 6
(ii) 5
(iii) <u>9</u>
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10. Which letter of English alphabet form simple closed

curve?



11. Maximum exterior angle possible for a regular polygon

- (i) 60°
- (ii) 120°
- (iii) 180°

- 12. Quadrilateral in which measure of each angle is less than
- 180° is a
- (i) Concave quadrilateral
- (ii) Convex quadrilateral
- (iii) Both



13. Identify the type of quadrilateral in the following .

A quadrilateral which is equiangular but not equilateral .



14. Identify the type of quadrilateral in the following .

A quadrilateral which is equilateral but not equiangular.



15. Identify the type of quadrilateral in the following .

A quadrilateral which is equiangular but not equilateral.



16. Identify the type of quadrilateral in the following .

A quadrilateral whose diagonals bisect each other at right -

angles .

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17. One side of the square is 36 cm and the side opposite to

it is 5x-4. Find the value of x.



18. Each interior angle of a polygon is double the exterior

angle . Find the number of sides of the polygon .



19. One of angles of a parallelogram is 26° more than its adjacent angle . What is the measure of each angle ?



20. PQRS is a parallelogram and O is the point of intersection of the diagonals . OR =4 cm and QS is 3 more than PR .Find OS .



21. ABCD is a quadrilateral such that $\angle A = \angle B, \angle C = \angle D$.

If $ar{\angle}A=2ar{\angle}C$. Find the angles of the quadrilateral .

