# ©゙doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - NAND LAL PUBLICATION

## UNDERSTANDING QUADRILATERALS

## Try These

1. Match the following (caution !A figure may match to more
than one type)

| Figure |  | Type |
| :--- | :--- | :--- |
| 1. |  | (a) Simple closed curve |
| 2. | a | (b) A closed curve that is not simple |
| 3. |  | (c) Simple curve that is not closed |
| 4. |  | (d) Not a simple curve. |

## - Watch Video Solution

2. Try to give few more examples and non -example for a polygon.

## D Watch Video Solution

3. Take any quadrilateral , say $A B C D$.Divide it into two triangles by drawing a diagonal. You get six angles 1,2,3, 4,5 and 6 . Use the angles sum property of a triangle and argue
how the sum of the measures of $\angle A, \angle B, \angle C \angle D$ amounts to $180^{\circ}+180^{\circ}=360^{\circ}$.


- Watch Video Solution

4. Take four congruent card board colpes of any quadrilateral

ABCD, with angles as shown (fig i) Arrange the copies as shown in the figure, where angles $\angle 1, \angle 2, \angle 3, \angle 4$, meet at a point (fig .ii)


What can you say about the sum of the angles $\angle 1, \angle 2, \angle 3 \angle 4$ ?

## ( Watch Video Solution

5. As before consider quadrilateral $A B C D$ Let $P$. Be any point in its interior .Join $P$ to vertices $A, B, C$ and $D$. In the figure
,consider $\triangle P A B$.
From this we see $x=180^{\circ}-m \angle 2-m \angle 3$.
Similarly from $\triangle P B C, y=180^{\circ}-m \angle 4-m \angle 5$, from

## $\triangle P C D$

$z=180^{\circ}-m \angle 6-m \angle 7$ and from $\triangle P D A$
$w=180^{\circ}-m \angle 8-m \angle 1$
Use this to find the total measure $m \angle 1+\angle 2+\ldots \ldots . . m \angle 8$, does it help you to arive at the result ?

Remember $\angle x+\angle y+\angle z+\angle w=360^{\circ}$

6. Consider quadrilateral $A B C D$.Split it into two triangles to find the sum of the interior angles of quadrilateral $A B C D$


## - Watch Video Solution

7. In a regular hexagon.

What is the sum of the measures of its exterior angles $x$
$y, z, p, q, r ?$


## - Watch Video Solution

8. If $x^{p}$. $y^{q}=(x+y)^{p+q}$, show that $\frac{d y}{d x}=\frac{y}{x}$;

- Watch Video Solution

9. What is the measure of each ?
(i) exterior angle
(ii) Interior angle.

## (D) Watch Video Solution

10. Take a regular hexagon. Repeat this activity for the cases
of octagon

## (D) Watch Video Solution

11. What is the sum of the measure of its exterior angles a ,b,c,d,e,f,g,h.
12. Is a $=b=c=d=e=f=g=h$ ? why ? . where a,b,c,d,e,f,g,h are the sides of octagon

## - Watch Video Solution

13. What is the measure of each
(i)exterior angle
(ii) interior angle

## (D) Watch Video Solution

14. What is the sum of the measures of its exterior angles?

## (D) Watch Video Solution

$a=b=c=d=e=f=g=h=, m=n=o=p=q=r$
? Why ? where a,b,c,d,e,f,g and $h$ are the sides of octagon and $m, n, o, p, q, r$ are the sides of hexagon .

## D Watch Video Solution

16. What is the measure of each
(i)exterior angle
(ii) interior angle

## D Watch Video Solution

17. Take two identical set squares with angles $30^{\circ}-60^{\circ}-90^{\circ}$ and place these adjacently to form a
parallelogram as shwon in the fig .

Does this help you to verify the above property
property: The opposite sides of a parallelogram are of equal length.


## D Watch Video Solution

18. Find $x+y+z$

## Think Discuss And Write

1. $a, b, c$ and $d$ are the angle of any quadrilater if $\angle a=45, \angle b=60, \angle c=100$. Find $\angle d$

## (D) Watch Video Solution

2. A mason has made a concrete slab . He needs it to be rectangular. In what different ways can he make sure that it is rectangular?

## - Watch Video Solution

3. A square was defined as a rectangle with all sides equal .

Can we define it as rhobus with equal angles ? Explain this
idea.

## ( Watch Video Solution

4. Can a trapezium have all angles equal ? Can it have all sides equal ? Explain.

## D Watch Video Solution

## Do This

1. Take identical cut outs of congruent triangles of sides 3 cm
, $4 \mathrm{~cm}, 5 \mathrm{~cm}$ Arrange them as shown .


You get a trapezium (check if) which are the parallel sides here ?
should the non -parallel sides be equal ?

You can get two more trapeziums using the same set of triangles. Find them out and discuss their shapes.

## D Watch Video Solution

## Exercise 31

1. Give here are some figures .

(1)

(2)

(3)

(5)

(6)

(7)

(4)

(8)

Classify each of them on the basis of the following
(a) Simple curve
(b) Simple closed curve ,
(c) Polygon
(d) Convex polygon
(e) Concave polygon

## - Watch Video Solution

2. How many diagonals does each of the following have ?

A convex quadrailateral

## - Watch Video Solution

3. How many diagonals does each of the following have ?

A Triangle
4. How many diagonals does each of the following have?

A Triangle

## D Watch Video Solution

5. What is the sum of the measures of the angles of a convex quadrilateral? Will this property hold if the quadrilateral is not convex? (Make a non-convex quadrilateral and try!)

## (D) Watch Video Solution

6. Examine the table .(Each figure is divided into triangles
and the angles deduced from that.)

| Figure | Side | 3 | 4 |
| :---: | :---: | :---: | :---: |

What can you say about the angle sum of a convex polygon with number of sides?

7 Sides

## D Watch Video Solution

7. Examine the table. (Each figure is divided into triangles and the sum of the angles deduced from that.)

| Figure | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: |

What can
you say about the angle sum of a convex polygon with number of sides? 8

## - Watch Video Solution

8. Examine the table .(Each figure is divided into triangles and the angles deduced from that.)

| Figure | Side | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: |
| Angle sum | $180^{\circ}$ | $2 \times 180^{\circ}$ <br> $=(4-2) \times 180^{\circ}$ | $3 \times 180^{\circ}$ <br> $=(5-2) \times 180^{\circ}$ | $4 \times 180^{\circ}$ <br> $=(6-2) \times 180^{\circ}$ |

What can you say about the angle sum of a convex polygon with number of sides ?

10 sides
9. Examine the table .(Each figure is divided into triangles and the angles deduced from that.)

| Figure | Side | 3 | 4 |
| :---: | :---: | :---: | :---: |
| Angle sum | $180^{\circ}$ | $2 \times 180^{\circ}$ <br> $=(4-2) \times 180^{\circ}$ | $3 \times 180^{\circ}$ <br> $=(5-2) \times 180^{\circ}$ |
| $4-180^{\circ}$ <br> $=(6-2) \times 180^{\circ}$ |  |  |  |

What can you say about the angle sum of a convex polygon with number of sides?
n sides

## - Watch Video Solution

10. What is a regular polygon ? State the name of regular polygon of
(i) 3 sides, (ii) 4 sides, (iii) 6 sides
11. Find the angle measure $x$ in the following figures.


> (a)

- Watch Video Solution

12. Find the angle measure $x$ in the following figures. Des.


## (b)

- Watch Video Solution

13. Find the angle measure x in the following figures.

(c)
14. Find the angle measure $x$ in the following figures.


## (d)

D Watch Video Solution

## 15. Find $x+y+z$

16. 

Find $x+y+z+w$.

## D Watch Video Solution

## Exercise 32

1. Find x in the following figures .


## (D) Watch Video Solution

2. Find $x$ in the following figures.


## - Watch Video Solution

3. Find the measure of each exterior angle of a regular polygon of

9 sides
4. Find the measure of each exterior angle of a regular polygon of

15 sides

## (D) Watch Video Solution

5. How many sides does a regular polygon have if the measure of an exterior angle is $24^{\circ}$ ?
6. How many sides does a regular polygon have if each of its interior angles is $165^{\circ}$ ?

## - Watch Video Solution

7. Is it possible to have a regular polygon with measure of each exterior angle as $22^{\circ}$ ?

## (D) Watch Video Solution

8. Can $22^{\circ}$ be an interior angle of a regular polygon? Why ?
9. What is the minimum interior angle possible for a regular polygon? Why?

## - Watch Video Solution

10. What is the maximum exterior angle possible for a regular polygon?

## D Watch Video Solution

## Exercise 33

1. Given a parallelogram $A B C D$. Complete each statement along with the definition or property used $A D=$


## - Watch Video Solution

2. Given a parallelogram $A B C D$. Complete each statement along with the definition or property used $\mathrm{OC}=$


- Watch Video Solution

3. Given a parallelogram $A B C D$. Complete each statement along with the definition or property used $\mathrm{OC}=. . . .$.


## - Watch Video Solution

4. Given a parallelogram $A B C D$. Complete each statement along with the definition or property used OC = $\qquad$

5. Consider the following parallelograms. Find the values of the unknowns $x, y, z$.

(iii)

## - Watch Video Solution

6. Can a quadrilateral $A B C D$ be a parallelogram if :
$\angle D+\angle B=180^{\circ} ?$

Watch Video Solution
7. Can a quadrilateral $A B C D$ be a parallelogram if
$: A B=D C=8 \mathrm{~cm}, A D=4 \mathrm{~cm}$ and $B C=4.4 \mathrm{~cm}$ ?

## D Watch Video Solution

8. Can a quadrilateral ABCD be a parallelogram if : $\angle A=70^{\circ}$ and $\angle C=65^{\circ}$ ?

## ( Watch Video Solution

9. Draw a rough figure of a quadrilateral that is not a parallelogram but has exactly two opposite angles of equal measure.
10. The measures of two adjacent angles of a parallelogram are in the ratio $3: 2$. Find the measure of each of the angles of the parallelogram.

## - Watch Video Solution

11. Two adjacent angles of a parallelogram have equal measure. Find the measure of each of the angles of the parallelogram.

## - Watch Video Solution

12. The adjacent figure HOPE is a parallelogram.Find the angle measures $x, y$ and $z$.State the properties you use to find
them.

## - Watch Video Solution

13. The following figures GUNS and RUNS are parallelograms.

Find x and y . (Lengths are in cm )
(i)

(ii)

14.

above figure both RISK and CLUE are parallelograms. Find the value of $x$.

## ( Watch Video Solution

15. Explain how this figure is a trapezium. Which of its two sides are parallel? (Fig 3.32)


Fig 3.32

- Watch Video Solution

16. Find $m \angle C$ in the figure if $\overline{A B}|\mid D C$


- Watch Video Solution

17. Find the measure of $\angle P$ and $\angle S$ if $\overline{S P}|\mid \overline{R Q}$


- Watch Video Solution

1. State whether True or False. All rectangles are squares

## D Watch Video Solution

2. State whether True or False. All rhombuses are parallelograms

## (D) Watch Video Solution

3. State whether True or False. All squares are rhombuses and also rectangles
4. State whether True or False. All squares are not parallelograms.

## ( Watch Video Solution

5. State whether True or False. All kites are rhombuses.

## D Watch Video Solution

6. State whether True or False. All parallelograms are trapeziums.

## Watch Video Solution

7. State whether True or False. All squares are trapeziums.

## ( Watch Video Solution

8. Identify all the quadrilaterals that have. four sides of equal length

## D Watch Video Solution

9. Identify all the quadrilaterals that have. four right angles

## D Watch Video Solution

10. Explain how a square is. a quadrilateral

## ( W) Watch Video Solution

11. Explain how a square is. a rhombus

## - Watch Video Solution

12. Explain how a square is. a rhombus

## (D) Watch Video Solution

13. Explain how a square is. a rhombus

## - Watch Video Solution

14. Name the quadrilaterals whose diagonals. bisect each other

## - Watch Video Solution

15. Name the quadrilaterals whose diagonals. are perpendicular bisectors of each other

## D Watch Video Solution

16. Name the quadrilaterals whose diagonals
(i) bisect each other .
(ii) are equal
17. Explain why a rectangle is a convex quadrilateral.

## D Watch Video Solution

18. $A B C$ is a right-angled triangle and $O$ is the mid point of the side opposite to the right angle. Explain why O is equidistant from A, B and C. (The dotted lines are drawn additionally to help you).


## Additional Questions For Practice Objective Type Questions

1. Diagonals of which figure bisect each other at right angles
(i) parallelogram
(ii) rectangle
(iii) rhombus

## D Watch Video Solution

2. The four angles quadrilaterals add upto
$180^{\circ}$
(ii) $360^{\circ}$
(iii) 54
3. Number of diagonals in a hexagon are
(i) 6
(ii) 5
(iii) $\underline{9}$

D Watch Video Solution
4. Sum of all the interior angles of a pentagon are
(i) $540^{\circ}$
(ii) $720^{\circ}$
(iii) $360^{\circ}$
5. Which of the folllowing cannot be the angles of a quadrilateral ?
$70^{\circ}, 80^{\circ}, 90^{\circ}, 120^{\circ}$
(ii) $102^{\circ}, 88^{\circ}, 92^{\circ}, 78^{\circ}$
(iii) $80^{\circ}, 85^{\circ}, 90^{\circ}, 78^{\circ}$

## ( Watch Video Solution

6. Adjacent sides of the polygon are
(i) Any 2 sides of the polygon
(ii) Any 2 sides with common vertex
(iii) any two sides connecting non - consecutive vertices

## D Watch Video Solution

7. Which is not correct ?
(i) Equilateral $\Delta$ is a regular polygon
(ii) Square is a regular polygon
(iii) Rhombus is a regular polygon

## D Watch Video Solution

8. Fill in the blanks .

Every _is a rectangle .

## D Watch Video Solution

9. Isosceles trapezium is a trapezium in which base angles are $\qquad$
10. Adjacent angles of a paralleogram are supplementary .

## - Watch Video Solution

11. Sum of interior angles of a 9 sided polygon are

## (D) Watch Video Solution

12. Number of diagonals in a octagen are $\underline{20}$.

## (D) Watch Video Solution

13. If an angle of a parallelogram is a right angle then it is called a $\qquad$

## (D) Watch Video Solution

14. If two adjacent sides of a rectangle are equal then it is
called a $\qquad$ .

## D Watch Video Solution

15. State whether True or False .

Diagonals bisect in a trapezium .

## D Watch Video Solution

16. At least one angle of a concave quadrilateral is greater than $180^{\circ}$.

## - Watch Video Solution

17. state true or false:

Diagonals of a rhombus are equal in length .

## (D) Watch Video Solution

18. Isosceles triangle is a regular polygon .

## - Watch Video Solution

19. Every curve is a closed curve .

## ( Watch Video Solution

20. Diagonal joins any two adjacent vertices of a polygon .

## (D) Watch Video Solution

21. Non - parallel sides of an isosceles trapezium are equal .

## D Watch Video Solution

## Additional Questions For Practice Short Answer Type Questions

1. Which of the following figure is a regular polygon?
A. (a) Any triangle
B. (b) Right angle triangle
C. (c) Equilater triangle
D. (d) none of these

## Answer:

## D Watch Video Solution

## Additional Questions For Practice Long Answer Type Questions

1. Ratio between the exterior angle and interior angle of a regular polygon is 2:7. Find the number of sides of the polygon.
2. Angles of the quadrilateral are $(2 x+1)^{\circ},(2 x+9)^{\circ},(3 x-4)^{\circ},(x+10)^{\circ}$.Find the measure of each of the angles of the quadrilateral.

## ( Watch Video Solution

3. $A B C D E F$ is a regular hexagon with line I passing through side AF . Find the measure of $\angle x$ and $\angle y$.

## D View Text Solution

4. Find the measure of each angle of the parallelogram if the larger angle is $60^{\circ}$ less than twice of smaller angles.
5. PQRS is a rhombus. $\angle Q R P=55^{\circ}$. Find $\angle P S R$

## (D) Watch Video Solution

6. Sum of all the interior angles of a regular polygon is twice sum of its exterior angles. Find the number of sides of the polygon.

## (D) Watch Video Solution

7. One of the sides of the parallelogram is 6 cm more than the other. If its perimeted is 36 cm . Find the sides of the parallelogram.

# Additional Questions For Practice Hots High Order Thinking 

 Skill1. If the length of the side of a rhombus is equal to the length of one diagonal Find the angles of the rhombus .

## - Watch Video Solution

## Sample Paper For Practice

1. Correct the statements given below .

Parallel sides of the isosceles trapezium are equal .

## - Watch Video Solution

2. Sum of all the interior angles of a quadrilateral is $180^{\circ}$ ?.

## D Watch Video Solution

3. Diagonals of the parallelogram bisect each other at right angles .

## D Watch Video Solution

4. Minimum number of sides in a polygon is 2 .

## (D) Watch Video Solution

5. Fill in the blank spaces .

A regular polygon each of whose angle is $\qquad$ a regular polygon at 5 sides.

## (D) Watch Video Solution

6. Measure of each interior angle of a polygon is equal to 8 times the measure of each exterior angle. Then the number of sides of polygon has

## (D) Watch Video Solution

7. Diagonals of the rhombus bisect each other at $\qquad$ .
8. Sum of all interior angles of a $n$ sided polygon is $\qquad$ .

## D Watch Video Solution

9. Number of diagonals in a hexagon are
(i) 6
(ii) 5
(iii) $\underline{9}$

- Watch Video Solution

10. Which letter of English alphabet form simple closed curve?

D Watch Video Solution
11. Maximum exterior angle possible for a regular polygon
(i) $60^{\circ}$
(ii) $120^{\circ}$
(iii) $180^{\circ}$

## (D) Watch Video Solution

12. Quadrilateral in which measure of each angle is less than
$180^{\circ}$ is a
(i) Concave quadrilateral
(ii) Convex quadrilateral
(iii) Both
13. Identify the type of quadrilateral in the following .

A quadrilateral which is equiangular but not equilateral .

## D Watch Video Solution

14. Identify the type of quadrilateral in the following .

A quadrilateral which is equilateral but not equiangular .

## (D) Watch Video Solution

15. Identify the type of quadrilateral in the following .

A quadrilateral which is equiangular but not equilateral.

## D Watch Video Solution

16. Identify the type of quadrilateral in the following .

A quadrilateral whose diagonals bisect each other at right angles .

## ( Watch Video Solution

17. One side of the square is 36 cm and the side opposite to it is $5 x-4$. Find the value of $x$.

## - Watch Video Solution

18. Each interior angle of a polygon is double the exterior angle . Find the number of sides of the polygon .

## D Watch Video Solution

19. One of angles of a parallelogram is $26^{\circ}$ more than its adjacent angle. What is the measure of each angle ?

## - Watch Video Solution

20. PQRS is a parallelogram and $O$ is the point of intersection of the diagonals. $\mathrm{OR}=4 \mathrm{~cm}$ and QS is 3 more than PR . Find OS .

## (D) Watch Video Solution

21. ABCD is a quadrilateral such that $\angle A=\angle B, \angle C=\angle D$.

If $\angle A=2 \angle C$. Find the angles of the quadrilateral .


