



MATHS

BOOKS - KALYANI PUBLICATION

LOGARITHMS

Example

1. Determine logarithm of 1728 to the base $2\sqrt{3}$

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2. Prove that $\log_2 \log_3 \log_2 512 = 1$.

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3. Show that $7\log\left(\frac{10}{9}\right) - 2\log\left(\frac{25}{24}\right) + 3\log\left(\frac{81}{80}\right) = \log 2$

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4. If $a^2 + b^2 - 7ab = 0$, prove that $(\log a + \log b) = 2\log\left(\frac{a+b}{3}\right)$

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5. Show that $2\log(a+b) = 2\log a + \log\left\{1 + \frac{2b}{a} + \frac{b^2}{a^2}\right\}$

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6. Prove that $\log_a x + \log_{\frac{1}{a^2}} x = \log_a \sqrt{x}$

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7. Prove that $\frac{2}{3} < \log_{10} 5 < \frac{3}{4}$



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8. Solve the equation $\log_3 x + \log_9 x + \log_{27} x = 5.5$



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9. If $\frac{xy \log(xy)}{x+y} = \frac{yz \log(yz)}{y+z} = \frac{zx \log(zx)}{z+x}$ then show that $x^x = y^y = z^z$



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Exercise

1. Express the following in the form of $x = \log_a y$:

$$3^4 = 81$$



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2. Express the following in the form of $x = \log_a y$:

$$2^5 = 32$$



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3. Express the following in the form of $x = \log_a y$:

$$5^3 = 125$$



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4. Express the following in the form of $x = \log_a y$:

$$\sqrt{8} = 2^{\frac{3}{2}}$$



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5. Express the following in the form of $x = \log_a y$:

$$3^{-3} = \frac{1}{27}$$



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6. Express the following in the form of $x = \log_a y$:

$$\left(\frac{3}{2}\right)^5 = \frac{243}{32}$$



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7. Express the following in the form of $x = \log_a y$:

$$10^{-4} = .0001$$



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8. Express the following in index form :

$$\log_{10} 1000 = 3$$



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9. Express the following in index form :

$$\log_5 125 = 3$$



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10. Express the following in index form :

$$\log_{2\sqrt{2}} 64 = 4$$



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11. Express the following in index form :

$$\log_{25} (.04) = -1$$



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12. Express the following in index form :

$$\log_{11} \left(\frac{1}{121} \right) = -2$$



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13. Express the following in index form :

$$\log_4 \left(\frac{1}{8} \right) = -\frac{3}{2}$$



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14. Evaluate the following :

$$\log_6 216$$



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15. Evaluate the following :

$$\log_{5\sqrt{5}} 125$$



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16. Evaluate the following :

$$\log_{2\sqrt{3}} 144$$



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17. Evaluate the following :

$$\log_{\sqrt{5}} .008$$



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18. Evaluate the following :

$$\log_5 3125$$



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19. Evaluate the following :

$$\log_{3\sqrt{2}} 324$$



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20. Evaluate the following :

$$\log_{.001} 100$$



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21. Evaluate the following :

$$\log_{7\sqrt{7}} 2401$$



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22. Evaluate the following :

$$\log_{3\sqrt{2}} 5832$$



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23. Evaluate the following :

$$\log_{3\sqrt{9}} 81$$

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24. Prove that

$$\log_2 \log_3 9 = 1$$

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25. Prove that

$$\log_3 \log_2 8 = 1$$

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26. Prove that

$$\log_4 \log_{\sqrt{2}} 256 = 2$$



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27. Prove that

$$\log_2 \log_{\sqrt{2}} \log_3 81 = 2$$



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28. Prove that

$$\log_2 \log_{\sqrt{2}} \log_3^9 = 1$$



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29. Prove that

$$\log_4 \log_4 \log_4 256 = 0$$



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30. Prove that

$$\log_2 \log_2 \log_2 16 = 1$$

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31. Evaluate

$$\log_4 \log_{\sqrt{3}} \log_4 64 =$$

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32. Prove that

$$\log_8 \log_4 \log_{\sqrt{2}} 256 = \frac{1}{3}$$

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33. Prove that

$$\log_5 \log_2 \log_3 \log_2 512 = 0$$



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34. Prove that

$$\log_2 \log_2 \log_3 \log_3 19683 = 0$$



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35. Determine x if

$$\log_{10}(\log_{10} x) = 1$$



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36. Determine x if

$$\log_2(\log_2 x) = 1$$



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37. Determine x if

$$\log_2(\log_9 x) = -1$$

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38. Determine x if

$$\log_2(\log_{\sqrt{3}} x) = 2$$

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39. Determine x if

$$\log_{36}(\log_2 x) = \frac{1}{2}$$

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40. Determine x if

$$\log_{25}(\log_3 x) = \frac{1}{2}$$



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41. Determine x if

$$\log_5 \{ \log_3 (\log_2 x) \} = 0$$



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42. Determine x if

$$\log_3 \{ \log_2 (\log_2 x) \} = 1$$



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43. Prove that

$$\log_a \frac{51}{16} + \log_a \frac{44}{85} - \log_a \frac{33}{40} = \log_a 2$$



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44. Prove that

$$\log_x \frac{9}{14} + \log_x \frac{35}{24} - \log_x \frac{15}{48} = \log_x 3$$



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45. Prove that

$$\log_a \frac{p^2}{qr} + \log_a \frac{q^2}{rp} + \log_a \frac{r^2}{pq} = 0$$



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46. Prove that

$$\log(x^2) + \log(y^2) + \log(z^2) = \log xy + \log yz + \log zx$$



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47. Prove that

$$(\log a)^2 - (\log b)^2 = \log(ab) \log\left(\frac{a}{b}\right)$$



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48. Prove that

$$\log_a \frac{25}{21} + \log_a \frac{9}{35} + \log_a \frac{49}{15} = 0$$



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49. Prove that

$$\log \frac{75}{16} - 2 \log \frac{5}{9} + \log \frac{32}{243} = \log 2$$



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50. Show that $7 \log \left(\frac{10}{9} \right) - 2 \log \left(\frac{25}{24} \right) + 3 \log \left(\frac{81}{80} \right) = \log 2$



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51. Prove that

$$7 \log \frac{16}{15} + 5 \log \frac{25}{24} + 3 \log \frac{81}{80} = \log 2$$

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52. Prove that

$$16 \log \frac{16}{15} + 12 \log \frac{25}{24} + 7 \log \frac{81}{80} = \log 5$$

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53. Prove that

$$7 \log \frac{15}{16} + 6 \log \frac{8}{3} + 5 \log \frac{2}{5} + \log \frac{32}{25} = \log 3$$

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54. Prove that

$$\log \frac{384}{5} + \log \frac{513}{32} + \log \frac{5}{27} - \log \frac{57}{25} = 2$$



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55. Prove that

$$\log\left\{a + \sqrt{a^2 + 1}\right\} = -\log\left\{\sqrt{a^2 + 1} - a\right\}$$



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56. Assuming the base as 10, prove that

$$\log \frac{81}{8} - 2 \log \frac{3}{2} + 3 \log \frac{2}{3} + \log \frac{3}{4} = 0$$



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57. Assuming the base as 10, prove that

$$\log 2 + 16 \log \frac{16}{15} + 12 \log \frac{25}{24} + 7 \log \frac{80}{81} = 1$$



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58. Assuming the base as 10, prove that

$$\log 20 + 7 \log \frac{15}{16} + 5 \log \frac{24}{25} + 3 \log \frac{80}{81} = 1$$



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59. Assuming the base as 10, prove that

$$24 \log \frac{9}{10} - 8 \log \frac{24}{25} + 10 \log \frac{160}{81} = 2$$



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60. Assuming the base as 10, prove that

$$\log 768 + \log \frac{81}{32} + 3 \log \frac{5}{3} + \log \frac{1}{9} = 3$$



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61. Assuming the base as 10, prove that

$$23 \log \frac{16}{15} + 17 \log \frac{25}{24} + 10 \log \frac{81}{80} = 1$$



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62. Assuming the base as 10, prove that

$$20 \log 8 + 45 \log 16 - 18 \log 32 = 30(5 - 5 \log 5)$$



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63. Assuming the base as 10, prove that

$$\log 12.5 = 2 - 3 \log 2$$



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64. Assuming the base as 10, prove that

$$\log 800 = 2 + 3 \log 2$$



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65. Assuming the base as 10, prove that

$$\log\left(1 + \frac{1}{2}\right) + \log\left(1 + \frac{1}{3}\right) + \log\left(1 + \frac{1}{4}\right) + \dots + \log\left(1 + \frac{1}{19}\right) = 1$$

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66. Assuming the base as 10, prove that

$$\frac{\log 3\sqrt{3} + \log 2\sqrt{2} - \log 5\sqrt{5}}{\log 1.2} = \frac{3}{2}$$

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67. If $\frac{\log p}{b - c} = \frac{\log q}{c - a} = \frac{\log r}{a - b}$, then prove that

$$p^a \cdot q^b \cdot r^c = 1$$

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68. If $\frac{\log x}{a + b - 2c} = \frac{\log y}{b + c - 2a} = \frac{\log z}{a + c - 2b}$, then prove that $xyz = 1$

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69. If $\frac{xy \log(xy)}{x+y} = \frac{yz \log(yz)}{y+z} = \frac{zx \log(zx)}{z+x}$ then show that $x^x = y^y = z^z$

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70. If $\frac{\log x}{y-z} = \frac{\log y}{z-x} = \frac{\log z}{x-y}$ prove that $xyz = 1$

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71. If $(3.7)^x = (.37)^y = 1000$, then prove that $\frac{1}{x} - \frac{1}{y} = \frac{1}{3}$

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72. If $a^2 + b^2 = 23ab$, then prove that $\log\left(\frac{a+b}{5}\right) = \frac{1}{2}(\log a + \log b)$

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73. If $x^2 + y^2 = 7xy$, then prove that
$$\log(x + y) = \log 3 + \frac{1}{2}(\log x + \log y)$$

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74. If $x^2 + y^2 = 11xy$, then prove that
$$\log\left(\frac{x + y}{13}\right) = \frac{1}{2}(\log x + \log y)$$

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75. If $a^2 + b^2 = 18ab$, then prove that $\log\left(\frac{a - b}{4}\right) = \frac{1}{2}(\log a + \log b)$

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76. If $4a^4 + 9b^4 = 37a^2b^2$, then prove that $\log(2a^2 + 3b^2) = \log a + \log b + \log 7$

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77. If $2\log(a + b) = \log a + \log b + \log 8$, then prove that $(a + b)^2 = 8ab$

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78. If $\log\left(\frac{x + y}{3}\right) = \frac{1}{2}(\log x + \log y)$, then prove that $\frac{x}{y} + \frac{y}{x} = 7$

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79. If $\log\left(\frac{a + 2b}{4}\right) = \frac{1}{2}(\log a + \log b)$, then prove that $a^2 + 4b^2 = 12ab$

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80. If $\log\left(\frac{x+y}{2}\right) = \frac{1}{2}(\log x + \log y)$, then prove that $x = y$



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81. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_2 6 = 2.5854$



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82. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771,$ find the value of $\log_{10} 12$



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83. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_6 5 = .8982$

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84. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_4 9 = 1.5848$

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85. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771,$ then find the value of
 $\log_{10} \left((24)^{\frac{1}{2}} \right)$

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86. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_6 30 = 1.898$

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87. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1,$ then prove that
 $\log_3 70 = 3.8673$

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88. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1,$ then prove that
 $\log_7 90 = 2.3124$

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89. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_6 45 = 2.1244$



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90. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_9 24 = 1.4465$



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91. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1,$ then prove that
 $\log_3 56 = 3.6642$



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92. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771$, then find the value of $\log_{10} 3.6$



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93. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1$, then prove that
 $\log_3 56 = 3.6642$



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94. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782$, then prove that
 $\log_5 72 = 2.6572$



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95. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 5 = .6990, \log_{10} 10 = .7782,$ then prove that
 $\log_9 96 = 2.0774$

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96. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1,$ then prove that
 $\log_7 120 = 2.4606$

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97. Given that $\log_{10} 2 = .3010, \log_{10} 3 = .4771, \log_{10} 4 = .6021,$
 $\log_{10} 7 = .8450, \log_{10} 10 = 1,$ then prove that
 $\log_8 140 = 2.3764$

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98. Prove that

$$\log_a x + \log_{\frac{1}{a}} x = 0$$

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99. Prove that

$$\log_3 2 = \log_9 4 = \log_{27} 8$$

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100. Prove that

$$\log_{a^2} x = \left(\frac{1}{2}\right) \log_a x$$

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101. Prove that

$$\log_a x = \log_{a^2} x^2 = \log_{a^n} x^n$$



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102. Prove that

$$\frac{1}{\log_6 24} + \frac{1}{\log_{12} 24} + \frac{1}{\log_8 24} = 2$$



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103. Prove that

$$\frac{1}{\log_a x} + \frac{1}{\log_b x} + \frac{1}{\log_c x} = 0$$



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104. Prove that

$$\frac{1}{\log_a P} + \frac{1}{\log_b P} + \frac{1}{\log_c P} = \frac{1}{\log_x P} \text{ where, } abc = x$$



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105. Prove that

$$\log_a m + \log_{a^2} m^2 + \log_{a^3} m^3 + \dots + \log_{a^p} m^p = p \log_a m$$



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106. Prove that

$$\log_a x \cdot \log_b a \cdot \log_c b \cdot \log_x c = 1$$



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107. Prove that

$$\log_a x \cdot \log_b y = \log_b x \cdot \log_a y$$



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108. Prove that

$$\frac{\log_a bx}{\log_a x} = 1 + \log_x b$$





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109. Prove that

$$\log_a(ab) + \log_b(ab) = \log_a(ab) \cdot \log_b(ab)$$



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110. Prove that

$$\frac{1}{4} < \log_{10} 2 < \frac{1}{3}$$



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111. Prove that

$$\frac{3}{10} < \log_{10} 2 < \frac{1}{3}$$



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112. Prove that

$$\frac{1}{3} < \log_{10} 3 < \frac{1}{2}$$

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113. Prove that $\frac{5}{6} < \log_{10} 7 < \frac{6}{7}$.

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114. Solve the following equation :

$$\log x + \log 3 + 3 \log 2 = 2 \log 4$$

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115. Solve the following equation :

$$\frac{\log x}{\log 4} = \frac{\log 64}{\log 16}$$

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116. Solve the following equation :

$$\log_x 2 + \log_x 4 + \log_x 8 + \log_x 16 = 10$$



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117. Solve the following equation :

$$\log_2 x + \log_4 x + \log_{16} x = \frac{21}{24}$$



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118. Solve the following equation :

$$\log_2 x + \log_{16} x = 15$$



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119. Solve the following equation :

$$\log_3 x + \log_9 (x^2) + \log_{27} (x^3) = 3$$

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120. Solve the following equation :

$$\log_8 x + \log_4 x + \log_2 x = 11$$

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121. Solve the following equation :

$$\log_4 x + \log_2 x = 6$$

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122. Solve the following equation :

$$\log_x 3 + \log_x 9 + \log_x 729 = 9$$



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