



# MATHS

## **BOOKS - NAGEEN PRAKASHAN ENGLISH**

## TRIANGLES

**Solved Examples** 

**1.** In the given figure, prove that AC = BD.

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2. In the adjoining figure, AB = CD and AB||CD prove that

(i)  $\Delta AOB\cong \Delta DOC$ 

(ii) AD and BC bisect each other at the point O.



the sides PQ and QR and the median PM of triangle PQR respectively.

Prove that the triangles ABC and PQR are congruent.



4. In the adjoining figure, BD = CE and  $\angle ADB = \angle AEC = 90^{\circ}$ , prove

that

(i)  $\Delta ABD \cong \Delta ACE$  (ii) ABC is an isosceles triangle.



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**5.** In the adjoining figure, D is the mid-point of BC. If BM and CN are perpendiculars from B and C respectively on AD and AD produced, then prove that BM = CN.



6. Use the information marked to prove :

(i)  $\Delta EAC\cong \Delta DBC$  (ii) EC=DC

Also state the Euclid's axiom used in proving the congruency of two





7. In the adjoining figure ABCD is a parallelogram, ABM is a line segment

and E is the mid-point of BC. Prove that :

(i)  $\Delta DCE\cong\Delta MBe$  (ii) AB=BM

(iii) AM = 2DC



8. In the given figure, D and E are the points on the base BC of  $\Delta ABC$ such that BD = CE, AD = AE and  $\angle ADE = \angle AED$ , prove that





9. In the given figure,  $PS=PR, \angle TPS=\angle QPR.$  Prove that PT=PQ.



10. In right triangle ABC, right angle at C, M is the mid-point of the hydrotenuse AB. C is joined to M and produced to a point D such that DM = CM. Point D is joined to point B. Show that

(i)  $\Delta AMC\cong \Delta BMD$  (ii)  $\angle DBC= \angle ACB$ 





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**11.** In the given figure, AC = AE, AB = AD and  $\angle BAD = \angle EAC$ . Prove that BC = DE.



12. If the bisector of the vertical angle of a triangle bisects the base of the triangle. then the triangle is isosceles. GIVEN : triangle A B C in which A D is the bisector of angle A meeting B C in D such that BD = DCTOPROVE: triangleA B C is an isosceles triangle.

**13.** ABC is an isosceles triangle with AB = AC. Side BA is produced to

D such that AB = AD. Prove that  $\angle BCD$  is a right angle.

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**14.** If  $\Delta ABC$  is an isosceles triangle with AB = AC. Prove that the perpendiculars from the vertices B and C to their opposite sides are equal.

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**15.** BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles



**16.** In the adjoining figure, find the measure of angle FEB, if the lengths of sides AD, DF and FE are equal and  $\angle ACB = 65^{\circ}$ .



**17.** ABC is a triangle in which  $\angle B = 2 \angle CD$  is a point on BC such that

AD bisects ot BAC and AB=CD . Prove that  $ot BAC=72^0$  .



18. In  $\Delta ABC,$   $ar{A}=100^\circ,$   $ar{C}=30^\circ.$  Find (i) largest side, (ii) smallest

side of  $\Delta ABC$ .



**19.** In  $\Delta ABC, D$  is any point on side BC. Prove that

AB + BC + CA > 2AD

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20. In the adjoining figure, ABCD is a quadrilateral. Its diagonals AC and

BD intersect at point 'O'. Prove that :

(a) AB + BC + CD + DA < 2(AC + BD)

(b) AB + BC + CD + DA > (AC + BD)



21. Show that the difference of any two sides of a triangle is less than the

third side.



22. In  $\Delta ABC, BC = CA$  and  $\angle A = 40^{\circ}$ . Find the largest side of

 $\Delta ABD.$ 

**23.** In the adjoining figure, AD bisects  $\angle A$ . Arrange AB, BD and DC in the descending order of their lengths.



24. In quadrilateral ABCD, AB is the shortest side and DC is the longest

side. Prove that :

(i)  $\angle B > \angle D$ 



**25.** If D any point on the BC of an isosceles triangle ABC then prove that

AB > AD and AC > AD.



26. In isosceles triangle ABC, D is a point on the base BC produced. Prove





27. In the adjoining figure, ABC is a triangle and D is any point in its interior. Show that BD + DC < AB + AC.



28. Prove that the perimeter of a triangle is greater than the sum of its

altitudes.



**29.**  $\Delta ABC$  and  $\Delta DBC$  are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC (see Fig. 7.39). If AD is extended to intersect BC at P, show that (i)  $\Delta ABD \cong \Delta ACD$ (ii) `DeltaA B P~=Delta

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**30.** In figure,  $\angle B < \angle A$  and  $\angle C < \angle D$ . Show that AD < BC.

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**31.** PQR is a triangle. S is a point on the side QR of  $\Delta PQR$  such that

 $\angle PSR = \angle QPR$ . Given QP = 8 cm, PR = 6 cm and SR = 3 cm.



Find the lengths of QR and PS.



**33.** Prove that sum of any two sides of a triangle is greater than twice the median with respect to the third side

median with respect to the third side.

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**34.** Show that in a quadrilateral ABCDAB + BC + CD + DA < 2(BD + AC) $\bigcirc$  Watch Video Solution

**1.** If 3 sides of a triangle are 35 cm, 16 cm and 12 cm, then which type of

triangle is this ?

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2. If 3 sides of a triangle are of lengths12 cm, 8 cm and 17 cm. then which

type of triangle is this ?

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3. If 3 sides of a triangle are of length 16 cm, 12 cm and 13 cm, then which

type of triangle is this ?



4. If 3 sides of a triangle are 63 cm, 16 cm, and 65 cm, then which type of

triangle is this ?

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5. If 3 sides are of lengths 24 cm, 10 cm and 12 cm, then which type of

triangle is this ?

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**1.** Which of the following pairs of triangles are congruent ? Also state the condition of congruency in each case :



(iv) In  $\triangle ABC$  and  $\triangle DEF$ , AB = EF, BC = DF and  $\angle B = \angle F$ (v) In  $\triangle ABC$  and  $\triangle PQR$ , AB = QR, AC = PR and  $\angle B = \angle R$ (vi) In  $\triangle ABC$  and  $\triangle PQR$ ,  $\angle A = \angle P$ , AC = PR and AB = PQ(vi) In  $\triangle ABC$  and  $\triangle PQR$ , AB = QR,  $\angle A = \angle Q$  and AC = QP.

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2. In a  $\Delta ABC, D$  in mid-point of BC, AD is produced upto E so that

DE = AD, prove that :

(i)  $\Delta ABD$  and  $\Delta ECD$  are congruent (ii) AB = EC

(iii) AB is parallel to EC.

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**3.** In the given figure, AB = DB and AC = DC. If  $\angle ABD = 58^\circ, \angle DBC = (2x - 4)^\circ, \angle ACB = y + 15^\circ \text{ and } \angle DCB = 63$ , find the values of x and y.



**4.** BD is the disector of angle ABC. From a point P in BD, perpendiculars PE and PF are drawn to AB and BC respectively, prove that :

(i) Triangle BEP is conguent to triangle BFP (ii) PE=PF.

5. Given a  $\triangle ABD$  in which AB = AD and AC bisects BD. Prove that :  $\triangle ABC \cong \triangle ADC$ .

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6. In a tringle ABC, AB = AC and bisector of angle A meets BC at D. Prove

that :

(i)  $\Delta ABD \cong \Delta ACD$  (ii) AD is perpendicular to BC.

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7. In quadrilateral ABCD, AB=DC and AD=BC. Prove that the sides AB and DC

are parallel to each other.

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8. In  $\Delta ABC, AB = AC$  and the bisectors of  $\angle B$  and  $\angle C$  meet AC and

AB at point D and E respectively. Prove that BD = CE.



**9.** In  $\Delta ABC, \angle B = \angle C$ . Prove the perpendiculars from the mid-point of

BC to AB and AC are equal.

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10. Find the value of x and y in each of the following figures containing

two congruent triangles :





**11.** In the adjoining figure,  $\angle BAC = \angle BDC$  and  $\angle ABC = \angle BCD$ . Prove that :

(i)  $\Delta ABC \cong \Delta DCB$ 

(ii)  $\Delta ABE \cong \Delta DCF$ .



**12.** In the adjoining figure, ABCD is a quadrilateral. M and N are the points on AD and CD respectively such that AB = BC,  $\angle ABM = \angle CBN$  and  $\angle MBD = \angle NBD$ . Prove that BM = BN.





**13.** Given AD = DC and DB biscets  $\angle ADC$ .

(i) Prove that,  $\Delta ADB \cong \Delta CDB$ 

(ii) If  $\angle ABD = 48^{\circ}$ , find  $\angle CBD$ .



14. The adjoining figure shows a square ABCD and an equilateral triangle

DEC. Prove that :

(i)  $\angle ADE = \angle BCE = 30^{\circ}$ 

#### (ii) $\Delta ADE\cong \Delta BCE$



**15.** Equilateral triangles ABD and ACE are drawn on sides AB and AC respectively of a  $\Delta ABC$  outside it. Prove that :

(i)  $\angle DAC = \angle EAB$  (ii) DC = BE

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16. The following figure shows a square ABCD and an equilateral triangle

DCE. Prove that :

- (i)  $\angle ADE = \angle BCE = 150^{\circ}$
- (ii)  $\Delta ADE \cong \Delta BCE$
- (iii) AE = BE





**17.** The given figure shows a parallelogram ABCD. Squares ABPQ and ADRS are drawn on sides AB and AD of the parallelogram ABCD. Prove that :

(i)  $\angle SAQ = \angle ABC$ 

#### (ii) SQ = AC



18. In a  $\Delta ABC$ , BD is the median to the side AC, BD is produced to E such

that BD = DE. Prove that : AE is parallel to BC.



**19.** In the given figure,  $\angle BDC = \angle BEA$  and AB = BC. Show that





**20.** If the diagonals of a quadrilateral bisect each other at right angle, prove that the quadrilateral is a rhombus.

### A rhombus has all its four sides equal.



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**21.** In the adjoining figure, BM and DN are the perpendiculars from B and

D respectively to AC such that BM = DN. Prove that BO = OD.







**23.** In the adjoining figure, ABCD is a parallelogram. If  $\angle MBC = \angle NDA$ ,

prove that AM = NC.


**24.** In the adjoining figure, QX and RX are the bisectors of the angles Q and R respectively of the angles Q and R respectively of the triangle PQR. If  $XS \perp PQ$ . Prove that :

(i)  $\Delta XTQ\cong\Delta XSQ$ 





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**25.** In the following figure, OA = OC and AB = BC. Prove that :

(i)  $\angle AOB = 90^{\circ}$ 

(ii)  $\Delta AOD \cong \Delta COD$ 

(iii) AD = CD



**26.** In the adjoining figure, ABCD is a paralogram. The side AB is produced

to P such that AB=BP and the side AD is produced to Q such that AD = DQ.

Prove that CP = CQ.



27. In the following figures, AB = PQ, AC = PR and AM = PN. Prove that  $\Delta ABC \cong \Delta PQR$ .



**28.** Prove that the medians of an equilateral triangle are equal.

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29. ABCD is a square EF is parallel to BD. R is the mid-point of EF. Prove

that :

(i) BE = DF

(ii) AR bisects angle BAD

(iii) If AR produced it will pass through C.



**30.** The following figure shows a triangle ABC in which AB = AC. M is a point on AB and N is a point on AC such that BM = CN. Prove that :

(i) AM = AN

(ii)  $\Delta AMC\cong\Delta ANB$ 

(iii) BN = CM

## (iv) $\Delta BMC\cong\Delta CNB$





**31.** In the given figure, AB||DC and  $\angle D = \angle C$ . Prove that :

(i) AD = BC

(ii) AC = BD



- **32.** In the given figure : AB//FD, AC//GE and BD = CE, prove that :
- (i) BG = DF
- (ii) CF = EG



**33.** In the adjoining figure,  $\angle AYZ = \angle BYX = 90^{\circ}, AY = YZ$  and XY = BY. Prove that AB = ZX.



**34.** In the adjoining figure, ABCD is a square and PAB is an equilateral triangle. Find :

(i)  $\angle APD$ 

(ii)  $\angle PDC$ 

(iii)  $\angle DPC$ 

(iv) Prove that DP = CP



**35.** In the adjoining figure,  $\Delta ABC$  is right angled at C and M is the midpoint of hypotenuse AB, If AC = 32 cm and BC = 60 cm, then find the length of CM.



## Exercise 7 B

1. In  $\Delta ABC, AB = 8$  cm, BC = 15 cm and AC = 17 cm. find the largest

angle.





3. In the adjoining figure, write the sides of  $\Delta ABC$  in descending order of their length.



- 4. In the adjoining figure, explain :
- (i) which side is the greatest side ?
- (ii) which of two sides are equal ?
- (iii) which is the smallest side of  $\Delta AQS$  ?



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5. In the adjoining figure,

(i) Which side is smallest?

(ii) In  $\Delta ABC$ , what is the nature of  $\angle BAC$  ?



7. In the adjoining figure, AB > AC and the angle bisectors of  $\angle B$  and

 $\angle C$  meet at point P. Prove that

PB > PC.



8. Prove that sum of any two sides of a triangle is greater than twice the

median with respect to the third side.



**9.** In the adjoining figure, PQ=PR. Show that PS > PQ.



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**10.** Prove that the perimeter of a triangle is greater than the sum of its

altitudes.



11. Prove that the sum of the sides of a quadrilateral is greater than twice

of one of its diagonal.



**12.** Prove that in a quadrilateral the sum of all the sides is greater than

the sum of its diagonals.

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**13.** Prove that the perimeter of a triangle is greater than the sum of its

three medians.

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**14.** In the adjoining figure, P is an interior point of  $\Delta ABC$ . Then prove that :





- 15. In  $\Delta ABC$ , if BC > AC > AB then :
- (i) What is the relation  $\angle A$  and  $\angle C$  ?
- (ii) What is the relation between the values of  $\left(AB+AC
  ight)$  and BC ?
- (iii) What is the relation between the values of (AC-BC) and AB ?
- (iv) What is the smallest angle in  $\Delta ABC$  ?

**16.** In the adjoining figure, line segment PA, PB and PC are drawn from point P to line XY. Here PB is perpendicular to XY.

(i) What is the nature of the angles formed by line segment PA and PC from XY ?

(ii) Which line segment is the smallest in the segment PA, PB and PC?



**17.** Show that in a right angled triangle, the hypotenuse is the longest side.



**Revision Exercise Very Short Answer Questions** 

**1.** In an isosceles  $\Delta ABC$  if  $\angle A = 90^{\circ}$  and AB = AC, find  $\angle B$  and  $\angle C$ .





5. In 
$$\Delta XYZ, \angle X = 45^{\circ}, \angle Y = 75^{\circ}$$
 in another triangle ABC,  
 $\angle A = 45^{\circ}, \angle C = 60^{\circ}$  and AC = 6 cm. find XZ, given that  
 $\Delta XYZ \cong \Delta ABC$ .

**6.** Find the greatest and the smallest side of  $\Delta ABC$  in the adjoining figure.



7. In the given figure whether  $\Delta ABC$  is congruent to  $\Delta PQR$ . Mention the condition for congruence.



**8.** In  $\Delta ABC, \angle A = \angle B = 30^{\circ}$  name the longest side.

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9. In  $\Delta ABC, AB = 2.5$  cm and BC = 6 cm. what is the possible length

of AC ?

**10.** In quadrilateral ABCD, AB is the shortest side and DC is the longest side. Prove that :

(i)  $\angle B > \angle D$ 

(ii)  $\angle A > \angle C$ 



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**Revision Exercise Short Answer Type Question** 

1. P is any point in the angle ABC such that the perpendicular drawn from

P on AB and BC are equal. Prove that BP bisects angle ABC.

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**2.** The given figure shows a circle with centre O. P is mid-point of chord AB. Show that OP is perpendicular to AB.





 $ot DCB=63\,^\circ$  , find the values of x and y.



4. In the adjoining figure,  $\angle ABD = 127^{\circ}$  and  $\angle ACE = 149^{\circ}.$  Prove that

AC > AB.





6. In the adjoining figure AB=CD and AB||CD prove that :

(i)  $\Delta AOB\cong \Delta DOG$ 

(ii) AD and BC bisect each other at point O.



7. In the adjoining figure,  $\angle DAB = \angle ABC$  and AD = BC prove that

BD = AC.



8. In the adjoining figure, AD=DC and DB bisects  $\angle ADC$ . Prove that

 $\Delta ADB \cong \Delta CDB.$ 



9. In  $\Delta ABC$ , AB = AC and D is a point in BC so that BD = CD. Prove

that AD bisects  $\angle BAC$ .

10. In PQR , S is any point on the side QR . Show that PQ+QR+RP>2PS

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Revision Exercise Long Answer Type Question

1. In the given figure, if x = y and AB = CB, then prove that AE = CD



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2. ABC is a triangle, right angled at B. If BCDE is a square on side BC and

ACFG is a square on AC, prove that AD = BF.

**3.** In the given figure, ABC is an equilibrium triangle, PQ||AC and AC is produced to R such that CR=BP. Prove that QR bisects PC.



4. The given figure shows a quadrilateral ABCD. Prove that :

AB + BC + CD + DA > AC + BD



5. In the adjoining figure, the diagonals AC and BD of a quadrilateral ABCD

intersect point O. Prove that :

AB + BC + CD + DA < 2(AC + BD)



7. In the adjoining figure BO and CO are the bisectors of  $\angle CBD$  and  $\angle BCE$  respectively. If AC > AB, prove that OB > OC.



**8.** In the following figure, if AD = DE. Prove that :

AB+BC>CE
