



# MATHS

## BOOKS - ICSE

## EXPANSIONS

Questions

1. Evaluate:  $(a + 2b)^2$



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**2.** Evaluate:  $(2a - 3b)^2$



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**3.** If  $a + b = 9$  and  $ab = -22$ , find :  $a - b$



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**4.** If  $a + b = 9$  and  $ab = -22$ , find :  $a^2 - b^2$



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5. If  $x \neq 0$  and  $x = 2$ , find  $x^2 + \frac{1}{x^2}$



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6. If  $x \neq 0$  and  $x = 2$ , find  $x^4 + \frac{1}{x^4}$



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7. Given:  $a^2 + \frac{1}{a^2} = 7$  and  $a \neq 0$ , find  
 $a + \frac{1}{a}$



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8. Given:  $a^2 + \frac{1}{a^2} = 7$  and  $a \neq 0$ , find

$$a - \frac{1}{a}$$



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9. Given:  $a^2 + \frac{1}{a^2} = 7$  and  $a \neq 0$ , find

$$a^2 - \frac{1}{a^2}$$



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10. If  $a^2 - 5a + 1 = 0$  and  $a \neq 0$ , find :

$$a + \frac{1}{a}$$



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11. If  $a^2 - 5a + 1 = 0$  and  $a \neq 0$ , find :

$$a^2 + \frac{1}{a^2}$$



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12. Evaluate:  $(2a + 3b)^3$



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13. Evaluate:  $(4a - 5b)^3$



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14. If  $a^2 + \frac{1}{a^2} = 23$  and  $a \neq 0$ , find the value of  $a^3 + \frac{1}{a^3}$



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15. If  $a + b + c = 0$ , show that :

$$a^3 + b^3 + c^3 = 3abc$$



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16. Use property to evaluate:

$$8^3 + (-5)^3 + (-3)^3$$



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17. Use property to evaluate:  $2^3 + 4^3 + (-6)^3$



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18. Expand:  $(3x - 2y + 4)(3x - 2y - 4)$



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19. Expand:  $(5x - 3y + 2)(5x + 3y + 2)$



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20. Expand:  $(2x + 3y - 4z)^2$



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21. Expand:  $(3x - 2y + 5z)^2$



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22. Expand:  $(4a - 5b - 2c)^2$



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**23.** If  $a^2 + b^2 + c^2 = 29$  and  $a + b + c = 9$ ,  
find:  $ab + bc + ca$



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**24.** If  $a + b - c = 4$  and  $a^2 + b^2 + c^2 = 38$ ,  
find  $ab - bc - ca$



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**25.** If  $a - b - c = 3$  and  $a^2 + b^2 + c^2 = 77$ ,

find:  $ab - bc + ca$



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**26.**

If  $x^3 + y^3 + z^3 = 3xyz$  and  $x + y + z = 0$ ,

find the value of :

$$\frac{(x+y)^2}{xy} + \frac{(y+z)^2}{yz} + \frac{(z+x)^2}{zx}$$



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**27.** Find  $(2x + 3y)^2$



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**28.** In the expansion of  $(5x - 3)(x + 2)^2$ , find

:

coefficients of  $x^2$  and x



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**29.** In the expansion of  $(5x - 3)(x + 2)^2$ , find

:

constant term



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**30.** If each of  $a$ ,  $b$  and  $c$  is a non-zero number

and  $\frac{a}{b} = \frac{b}{c}$ , show that:

$$(a + b + c)(a - b + c) = a^2 + b^2 + c^2$$



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**31.** If the sum of two numbers is 5 and the sum of their cubes is 35, find the sum of their squares



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**32.** If  $a= 2$ ,  $b= 3$  and  $c= 4$ , find the value of :  
$$\frac{ab + bc + ca - a^2 - b^2 - c^2}{3abc - a^3 - b^3 - c^3}$$
, using suitable identity



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**33.**

Evaluate:

$$\frac{0.6 \times 0.6 \times 0.6 - 0.3 \times 0.3 \times 0.3}{0.6 \times 0.6 + 0.6 \times 0.3 + 0.3 \times 0.3},$$

using

suitable identity



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**34.** If  $x^2 + y^2 + z^2 - xy - yz - zx = 0$ ,

prove that :  $x = y = z$



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**Exercise 4 A**

**1. Find the square of:**

$$2a + b$$



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**2. Find the square of:**

$$3a + 7b$$



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**3.** Find the square of:

$$3a - 4b$$



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**4.** Find the square of:

$$\frac{3a}{2b} - \frac{2b}{3a}$$



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**5.** Use identities to evaluate:  $(101)^2$



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6. Use identities to evaluate:  $(502)^2$



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7. Use identities to evaluate:  $(97)^2$



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8. Use identities to evaluate:  $(998)^2$



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9. Evaluate:

$$\left(\frac{7}{8}x + \frac{4}{5}y\right)^2$$



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10. Evaluate:

$$\left(\frac{2x}{7} - \frac{7y}{4}\right)^2$$



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**11.**

Evaluate:

$$\left(\frac{a}{2b} + \frac{2b}{a}\right)^2 - \left(\frac{a}{2b} - \frac{2b}{a}\right)^2 - 4$$



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**12.** Evaluate:  $(4a + 3b)^2 - (4a - 3b)^2 + 48ab$



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**13.** If  $a + b = 7$  and  $ab = 10$ , find  $a - b$



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**14.** If  $a - b = 7$  and  $ab = 18$ , find  $a + b$



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**15.** If  $x + y = \frac{7}{2}$  and  $xy = \frac{5}{2}$ , find

$x - y$



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**16.** If  $x + y = \frac{7}{2}$  and  $xy = \frac{5}{2}$ , find

$$x^2 - y^2$$



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**17.** If  $a - b = 0.9$  and  $ab = 0.36$  find:

$$a + b$$



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**18.** If  $a - b = 0.9$  and  $ab = 0.36$  find:

$$a^2 - b^2$$



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**19.** If  $a - b = 4$  and  $a + b = 6$ , find:

$$a^2 + b^2$$



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**20.** If  $a - b = 4$  and  $a + b = 6$ , find:

$ab$



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**21.** If  $a + \frac{1}{a} = 6$  and  $a \neq 0$ , find

$$a - \frac{1}{a}$$



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**22.** If  $a + \frac{1}{a} = 6$  and  $a \neq 0$ , find

$$a^2 - \frac{1}{a^2}$$



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**23.** If  $a - \frac{1}{a} = 8$  and  $a \neq 0$ , find:

$$a + \frac{1}{a}$$



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**24.** If  $a - \frac{1}{a} = 8$  and  $a \neq 0$ , find:

$$a^2 - \frac{1}{a^2}$$



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**25.** If  $a^2 - 3a + 1 = 0$  and  $a \neq 0$ , find :

$$a + \frac{1}{a}$$



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**26.** If  $a^2 - 3a + 1 = 0$  and  $a \neq 0$ , find :

$$a^2 + \frac{1}{a^2}$$



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**27.** If  $a^2 - 5a - 1 = 0$  and  $a \neq 0$ , find :

$$a - \frac{1}{a}$$



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**28.** If  $a^2 - 5a - 1 = 0$  and  $a \neq 0$ , find :

$$a - \frac{1}{a}$$



**Watch Video Solution**

**29.** If  $a^2 - 5a - 1 = 0$  and  $a \neq 0$ , find :

$$a^2 - \frac{1}{a^2}$$



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**30.** If  $3x + 4y = 16$  and  $xy = 4$ , find the value of  $9x^2 + 16y^2$



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**31.** The number  $x$  is 2 more than the number  $y$ .

If the sum of the squares of  $x$  and  $y$  is 34, find the product of  $x$  and  $y$ .

Given :  $x - y = 2$  and  $x^2 + y^2 = 34$

To find the value of  $xy$ .



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32. The difference between two positive numbers is 5 and the sum of their squares is 73. Find the product of these numbers.



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### Exercise 4 B

1. Find the cube of:  $3a - 2b$



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2. Find the cube of:  $5a + 3b$



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3. Find the cube of:  $2a + \frac{1}{2a}$  ( $a \neq 0$ )



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4. Find the cube of:  $3a - \frac{1}{a}$  ( $a \neq 0$ )



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5. If  $a^2 + \frac{1}{a^2} = 47$  and  $a \neq 0$ , find:

$$a + \frac{1}{a}$$



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6. If  $a^2 + \frac{1}{a^2} = 47$  and  $a \neq 0$ , find:

$$a^3 + \frac{1}{a^3}$$



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7. If  $a^2 + \frac{1}{a^2} = 18$  and  $a \neq 0$ , find:

$$a - \frac{1}{a}$$



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8. If  $a^2 + \frac{1}{a^2} = 18$  and  $a \neq 0$ , find:

$$a^3 - \frac{1}{a^3}$$



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9. If  $a + \frac{1}{a} = p$  and  $a \neq 0$ , then show that:

$$a^3 + \frac{1}{a^3} = p(p^2 - 3)$$



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10. If  $a + 2b = 5$ , then show that:

$$a^3 + 8b^3 + 30ab = 125$$



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11. If  $\left(a + \frac{1}{a}\right)^2 = 3$  and  $a \neq 0$ , then show that:  $a^3 + \frac{1}{a^3} = 0$



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12. If  $a + 2b + c = 0$ , then show that:

$$a^3 + 8b^3 + c^3 = 6abc$$



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**13.** Use property to evaluate:

$$13^3 + (-8)^3 + (-5)^3$$



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**14.** Use property to evaluate:

$$7^3 + 3^3 + (-10)^3$$



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**15.** Use property to evaluate:

$$9^3 - 5^3 - 4^3$$



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**16.** Use property to evaluate:

$$38^3 + (-26)^3 + (-12)^3$$



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**17.** If  $a \neq 0$  and  $a - \frac{1}{a} = 3$ , find :

$$a^2 + \frac{1}{a^2}$$



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**18.** If  $a \neq 0$  and  $a - \frac{1}{a} = 3$ , find :

$$a^3 - \frac{1}{a^3}$$



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**19.** If  $a \neq 0$  and  $a - \frac{1}{a} = 4$ , find

$$a^2 + \frac{1}{a^2}$$



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**20.** If  $a \neq 0$  and  $a - \frac{1}{a} = 4$ , find

$$a^4 + \frac{1}{a^4}$$



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**21.** If  $a \neq 0$  and  $a - \frac{1}{a} = 4$ , find

$$a^3 - \frac{1}{a^3}$$



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**22.** If  $x \neq 0$  and  $x + \frac{1}{x} = 2$ , then show that:

$$x^2 + \frac{1}{x^2} = x^3 + \frac{1}{x^3} = x^4 + \frac{1}{x^4}$$



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**23.** If  $2x - 3y = 10$  and  $xy = 16$ , find the value of  $8x^3 - 27y^3$



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**24.** Expand:  $(3x + 5y + 2z)(3x - 5y + 2z)$



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**25.** Expand:  $(3x - 5y - 2z)(3x - 5y + 2z)$



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**26.** The sum of two numbers is 9 and their product is 20. Find the sum of their:  
squares



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**27.** The sum of two numbers is 9 and their product is 20. Find the sum of their:  
cubes



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**28.** Two positive numbers  $x$  and  $y$  are such that  $x > y$ . If the difference of these numbers is 5 and their product is 24, find:

sum of these numbers



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**29.** Two positive numbers  $x$  and  $y$  are such that  $x > y$ . If the difference of these numbers is 5 and their product is 24, find:

difference of their cubes



**Watch Video Solution**

**30.** Two positive numbers  $x$  and  $y$  are such that  $x > y$ . If the difference of these numbers is 5 and their product is 24, find:

sum of their cubes



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**31.** If  $4x^2 + y^2 = a$  and  $xy = b$ , find the value of  $2x + y$



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## Exercise 4 C

1. Expand:  $(x + 8)(x + 10)$



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2. Expand:  $(x + 8)(x - 10)$



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3. Expand:  $(x - 8)(x + 10)$



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4. Expand:  $(x - 8)(x - 10)$



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5. Expand:  $\left(2x - \frac{1}{x}\right)\left(3x + \frac{2}{x}\right)$



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6. Expand:  $\left(3a + \frac{2}{b}\right)\left(2a - \frac{3}{b}\right)$



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7. Expand:  $(x + y - z)^2$



**Watch Video Solution**

8. Expand:  $(x - 2y + 2)^2$



**Watch Video Solution**

**9.** Expand:  $(5a - 3b + c)^2$



**Watch Video Solution**

**10.** Expand:  $(5x - 3y - 2)^2$



**Watch Video Solution**

**11.** Expand:  $\left(x - \frac{1}{x} + 5\right)^2$



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**12.** If  $a + b + c = 12$  and  $a^2 + b^2 + c^2 = 50$ ,  
find  $ab + bc + ca$



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**13.** If  
 $a^2 + b^2 + c^2 = 35$  and  $ab + bc + ca = 23$ ,  
find  $a + b + c$



**Watch Video Solution**

**14.** If  $a + b + c = p$  and  $ab + bc + ca = q$ ,  
find  $a^2 + b^2 + c^2$



**Watch Video Solution**

**15.** If  
 $a^2 + b^2 + c^2 = 50$  and  $ab + bc + ca = 47$ ,  
find  $a + b + c$



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**16.** If  $x + y - z = 4$  and  $x^2 + y^2 + z^2 = 30$ ,

then find the value of  $xy - yz - zx$



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### Exercise 4 D

**1.** If

$x + 2y + 3z = 0$  and  $x^3 + 4y^3 + 9z^3 = 18xyz$

, evaluate:

$$\frac{(x + 2y)^2}{xy} + \frac{(2y + 3z)^2}{yz} + \frac{(3z + x)^2}{zx}$$



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2. If  $a = \frac{1}{a} = m$  and  $a \neq 0$ , find in terms of 'm', the value of :

$$a - \frac{1}{a}$$



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3. If  $a = \frac{1}{a} = m$  and  $a \neq 0$ , find in terms of 'm', the value of :

$$a^2 - \frac{1}{a^2}$$



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4. In the expansion of  $(2x^2 - 8)(x - 4)^2$ , find  
the value of  
coefficient of  $x^3$



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5. In the expansion of  $(2x^2 - 8)(x - 4)^2$ , find  
the value of  
coefficient of  $x^2$



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6. In the expansion of  $(2x^2 - 8)(x - 4)^2$ , find  
the value of  
constant term



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7. If  $x > 0$  and  $x^2 + \frac{1}{9x^2} = \frac{25}{36}$ , find  
 $x^3 + \frac{1}{27x^3}$



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**8.** If  $2(x^2 + 1) = 5x$ , find

$$x - \frac{1}{x}$$



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**9.** If  $2(x^2 + 1) = 5x$ , find

$$x^3 - \frac{1}{x^3}$$



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**10.** If  $a^2 + b^2 = 34$  and  $ab = 12$ , find:

$$3(a + b)^2 + 5(a - b)^2$$



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**11.** If  $a^2 + b^2 = 34$  and  $ab = 12$ , find:

$$7(a - b)^2 - 2(a + b)^2$$



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12. If  $3x - \frac{4}{x} = 4$  and  $x \neq 0$ , find

$$27x^3 - \frac{64}{x^3}$$



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13. If  $x^2 + \frac{1}{x^2} = 7$  and  $x \neq 0$ , find the value

$$\text{of: } 7x^3 + 8x - \frac{7}{x^3} - \frac{8}{x}$$



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14. If  $x = \frac{1}{x} - 5$  and  $x \neq 5$ , find  $x^2 - \frac{1}{x^2}$



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15. If  $x = \frac{1}{5-x}$  and  $x \neq 5$ , find  $x^3 + \frac{1}{x^3}$



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16. If  $3a + 5b + 4c = 0$ , show that:

$$27a^3 + 125b^3 + 64c^3 = 180abc$$



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**17.** The sum of two numbers is 7 and the sum of their cubes is 133. Find the sum of their squares



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**18.** In each of the following find the value of 'a'

$$4x^2 + ax + 9 = (2x + 3)^2$$



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**19.** In each of the following find the value of 'a'

$$4x^2 + ax + 9 = (2x - 3)^2$$



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**20.** In each of the following find the value of 'a'

$$9x^2 + (7a - 5)x + 25 = (3x + 5)^2$$



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**21.** If  $\frac{x^2 + 1}{x} = 3\frac{1}{3}$  and  $x > 1$ , find

$$x - \frac{1}{x}$$



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**22.** If  $\frac{x^2 + 1}{x} = 3\frac{1}{3}$  and  $x > 1$ , find

$$x^3 - \frac{1}{x^3}$$



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**23.** The difference between two positive numbers is 4 and the difference between their cubes is 316. Find:

their product



**Watch Video Solution**

**24.** The difference between two positive numbers is 4 and the difference between their cubes is 316. Find:

their product



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## Exercise 4 E

1. Simplify:  $(x + 6)(x + 4)(x - 2)$



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2. Simplify:  $(x - 6)(x - 4)(x + 2)$



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**3. Simplify:**  $(x - 6)(x - 4)(x - 2)$



**Watch Video Solution**

**4. Simplify:**  $(x + 6)(x - 4)(x - 2)$



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**5. Simplify using following identity:**

$$(a \pm b)(a^2 ab + b^2) = a^3 \pm b^3$$

$$(2x + 3y)(4x^2 - 6xy + 9y^2)$$



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**6.** Simplify using following identiy:

$$(a \pm b)(a^2 ab + b^2) = a^3 \pm b^3$$

$$\left(3x - \frac{5}{x}\right)\left(9x^2 + 15 + \frac{25}{x^2}\right)$$



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**7.** Simplify using following identiy:

$$(a \pm b)(a^2 ab + b^2) = a^3 \pm b^3$$

$$\left(\frac{a}{3} - 3b\right)\left(\frac{a^2}{9} + ab + 9b^2\right)$$



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**8. Using suitable identity, evaluate:**

$$(104)^3$$



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**9. Using suitable identity, evaluate:**

$$(97)^3$$



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10.

Simplify:

$$\frac{(x^2 - y^2)^3 + (y^2 - z^2)^3 + (z^2 - x^2)^3}{(x - y)^3 + (y - z)^3 + (z - x)^3}$$



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11.

Evaluate:

$$\frac{0.8 \times 0.8 \times 0.8 + 0.5 \times 0.5 \times 0.5}{0.8 \times 0.8 - 0.8 \times 0.5 + 0.5 \times 0.5}$$



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12.

Evaluate:

$$\frac{1.2 \times 1.2 + 1.2 \times 0.3 + 0.3 \times 0.3}{1.2 \times 1.2 \times 1.2 - 0.3 \times 0.3 \times 0.3}$$



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13. If  $a - 2b + 3c = 0$ , state the value of

$$a^3 - 8b^3 + 27c^3$$



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14. If  $x + 5y = 10$ , find the value of  
 $x^3 + 125y^3 + 150xy - 1000$



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15. If  $x = 3 + 2\sqrt{2}$ , find

$$\frac{1}{x}$$



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**16.** If  $x = 3 + 2\sqrt{2}$ , find

$$x - \frac{1}{x}$$



**Watch Video Solution**

**17.** If  $x = 3 + 2\sqrt{2}$ , find

$$\left(x - \frac{1}{x}\right)^3$$



**Watch Video Solution**

**18.** If  $x = 3 + 2\sqrt{2}$ , find

$$x^3 - \frac{1}{x^3}$$



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**19.** If  $a + b = 11$  and  $a^2 + b^2 = 65$ , find

$$a^3 + b^3$$



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**20.** If  $x, y$  and  $z$  are three different numbers,

then prove that :

$x^2 + y^2 + z^2 - xy - yz - zx$       is      always

positive



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**21.** Find:  $(a + b)(a + b)$



**Watch Video Solution**

**22.** Find :  $(a + b)(a + b)(a + b)$



**Watch Video Solution**

**23.**

Find :

- (i)  $(a + b)(a + b)$
- (ii)  $(a + b)(a + b)(a + b)$
- (iii)  $(a - b)(a - b)(a - b)$  by using the result  
of part (ii)



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**3 Marks Questions**

**1.** Use identities to evaluate :

$$(i) (101)^2 \quad (ii) (998)^2$$



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**2.** If  $x + y = \frac{7}{2}$  and  $xy = \frac{5}{2}$ , find

$$x - y$$



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**3.** The number  $x$  is 2 more than the number  $y$ .

If the sum of the squares of  $x$  and  $y$  is 34, find the product of  $x$  and  $y$ .

Given :  $x - y = 2$  and  $x^2 + y^2 = 34$

To find the value of  $xy$ .



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**4.** If  $a^2 + \frac{1}{a^2} = 47$  and  $a \neq 0$ , find:

$$a + \frac{1}{a}$$



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5. If  $a + 2b + c = 0$ , then show that:

$$a^3 + 8b^3 + c^3 = 6abc$$



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6. Use property to evaluate :

$$(i) 13^3 + (-8)^3 + (-5)^3$$

$$(ii) 9^3 - 5^3 - 4^3$$



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7. If  $x + y - z = 4$  and  $x^2 + y^2 + z^2 = 30$ ,  
then find the value of  $xy - yz - zx$



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8. If  $x^2 + \frac{1}{x^2} = 7$  and  $x \neq 0$ , find the value  
of :  $7x^3 + 8x - \frac{7}{x^3} - \frac{8}{x}$



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9. In each of the following find the value of 'a' :  
(i)  $4x^2 + ax + 9 = (2x + 3)^2$

$$(ii) 9x^2 + (7a - 5)x + 25 = (3x + 5)^2$$



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**10.** If  $x - \frac{1}{x} = 3$ , find the value of  $x^3 - \frac{1}{x^3}$



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**11.** If  $x - \frac{1}{x} = 3$ , find the value of  $x^3 - \frac{1}{x^3}$



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## 4 Marks Questions

1. Evaluate :

$$(i) \left( \frac{a}{2b} + \frac{2b}{a} \right)^2 - \left( \frac{a}{2b} - \frac{2b}{a} \right)^2 - 4$$

$$(ii) (4a + 3b)^2 - (4a - 3b)^2 + 48ab$$



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2. If  $a^2 - 5a - 1 = 0$  and  $a \neq 0$ , find :

$$a^2 - \frac{1}{a^2}$$



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**3.** If  $x \neq 0$  and  $x + \frac{1}{x} = 2$ , then show that:

$$x^2 + \frac{1}{x^2} = x^3 + \frac{1}{x^3} = x^4 + \frac{1}{x^4}$$



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**4.** Two positive numbers  $x$  and  $y$  are such that

$x > y$ . If the difference of these numbers is 5

and their product is 24 find :

(i) sum of these number

(ii) difference of their cubes

(iii) Sum of their cubes



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5. Expand :

$$(i) (5 - 3y - 2)^2 \quad (ii) \left( x - \frac{1}{x} + 5 \right)^2$$



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6.

If

$$x + 2y + 3z = 0 \text{ and } x^3 + 4y^3 + 9z^3 = 18xyz$$

,

evaluate:

$$\frac{(x + 2y)^2}{xy} + \frac{(2y + 3z)^2}{yz} + \frac{(3z + x)^2}{zx}$$



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7. In the expansion of  $(2x^2 - 8)(x - 4)^2$ , find the value of :

- (i) coefficient of  $x^3$  (ii) Coefficient of  $x^2$
- (iii) Constant term



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8. If  $2(x^2 + 1) = 5x$ , find :

$$(i) x - \frac{1}{x} \quad (ii) x^3 - \frac{1}{x^3}$$



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9.

Simplify:

$$\frac{(x^2 - y^2)^3 + (y^2 - z^2)^3 + (z^2 - x^2)^3}{(x - y)^3 + (y - z)^3 + (z - x)^3}$$



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10. If  $x = 3 + 2\sqrt{2}$ , find :

(i)  $\frac{1}{x}$  (ii)  $x - \frac{1}{x}$

(iii)  $\left(x - \frac{1}{x}\right)^3$  (iv)  $x^3 - \frac{1}{x^3}$



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