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## MATHS

## BOOKS - ICSE

## INEQUALITIES

Example

1. In the adjoining figure, AD bisects $\angle A$.

Arrange $A B, B D$ and $D C$ in the descending
order of their lengths.


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2. In the given figure, $A C$ is perpendicular to
line $P Q$ and $B C=C D$. Show that $A E$ is greater
than $A B$.


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3. In the given figure, $A B=A C$. Prove that $A F$ is greater than AE .


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4. In the figure, given alongside, AD bisects angle BAC. Prove that :
(i) $A B>B D$
(ii) $A C>C D$
(iii) $A B+A C>B C$


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5. In quadrilateral $A B C D, A B$ is the shortest side
and DC is the longest side. Prove that :
(i) $\angle B>\angle D$
(ii) $\angle A>\angle C$


D

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6. $A D$ is a median of triangle $A B C$. Prove that :
$A B+A C>2 A D$

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7. $P$ is any point in the interior of a triangle

ABC.

Prove that : $P A+P B<A C+B C$

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8. In the adjoining figure, AD bisects $\angle A$.

Arrange $A B, B D$ and $D C$ in the descending order of their lengths.


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9. In the given figure, $A C$ is perpendicular to
line $P Q$ and $B C=C D$. Show that $A E$ is greater than $A B$.


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10. In the given figure, $A B=A C$. Prove that $A F$ is greater than AE.


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11. In the figure, given alongside, AD bisects angle BAC. Prove that :
(i) $A B>B D$
(ii) $A C>C D$
(iii) $A B+A C>B C$


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12. In quadrilateral $A B C D, A B$ is the shortest
side and DC is the longest side. Prove that :
(i) $\angle B>\angle D$
(ii) $\angle A>\angle C$


D

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13. $A D$ is a median of triangle $A B C$. Prove that :
$A B+B C+A C>2 A D$

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14. $P$ is any point in the interior of a triangle

ABC.

Prove that : $P A+P B<A C+B C$

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1. From the following figure, prove that :
$A B>C D$


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2. In a triangle $\mathrm{PQR}, \mathrm{QR}=\mathrm{PR}$ and $\angle P=36^{\circ}$.

Which is the largest side of the triangle ?
3. If two sides of a triangle are 8 cm and 13 cm ,
then the length of the third side is between a cm and bcm . Find the values of a and b such that $a$ is less than $b$.

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4. In each of following figures, write $B C, A C$ and
$C D$ in ascending order of their lengths.

(i)

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5. Arrange the sides of $\triangle B O C$ in descending order of their lengths. BO and CO are
bisectors of angles $A B C$ and $A C B$ respectively.


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6. $D$ is a point in side $B C$ of triangle $A B C$. If
$A D>A C$, show that $A B>A C$.
7. In the following figure,
$\angle B A C=60^{\circ}$ and $\angle A B C=65^{\circ}$.

Prove that :
(i) $C F>A F \quad$ (ii) $D C>D F$


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8. In the following figure,
$\mathrm{AC}=\mathrm{CD}, \angle B A D=110^{\circ}$ and $\angle A C B=74^{\circ}$.

Prove that : $B C>C D$.


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9. From the following figure, prove that :
(i) $A B>B D$
(ii) $A C>C D$
(iii) $A B+A C>B C$


## - Watch Video Solution

10. In a quadrilateral $A B C D$, prove that :
(i) $A B+B C+C D>D A$
(ii) $A B+B C+C D+D A>2 A C$
(iii) $A B+B C+C D+D A>2 B D$

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11. In the following figure, $A B C$ is an equilateral triangle and $P$ is any point in $A C$, prove that :
(i) $B P>P A$
(ii) $B P>P C$


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12. $P$ is any point inside the triangle $A B C$. Prove that: $\angle B P C>\angle B A C$.
13. Prove that the straight line joining the vertex of an isosceles triangle to any point in the base is smaller than either of the equal sides of the triangle.

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14. In the following diagram, $A D=A B$ and $A E$ bisects angle A. Prove that:
(i) $\mathrm{BE}=\mathrm{DE}$ (ii) $\angle A B D>\angle C$


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15. The sides $A B$ and $A C$ of a triangle $A B C$ are produced, and the bisectors of the external
angles at $B$ and $C$ meet at $P$. Prove that if $A B>A C$, then $P C>P B$.

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16. In the following figure, $A B$ is the largest side and $B C$ is the smallest side of the triangle ABC.


Write the angles $x^{\circ}, y^{\circ}$ and $z^{\circ}$ in
ascending order of their values.

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17. In quadrilateral $A B C D, A B$ is the shortest side and DC is the longest side. Prove that :
(i) $\angle B>\angle D$
(ii) $\angle A>\angle C$


D

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18. In triangle $A B C$, side $A C$ is greater than side
$A B$. If the internal bisector of angle $A$ meets
the opposite side at point D , prove that :
$\angle A D C$ is greater than $\angle A D B$.

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19. In isosceles triangle $A B C$, sides $A B$ and $A C$ are equal. If point $D$ lies in base $B C$ and point $E$ lies on $B C$ produced ( $B C$ being produced through vertex C), prove that :
(i) $A C>A D$
(ii) $A E>A C$
(iii) $A E>A D$

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20. Given : ED = EC

Prove : $A B+A D>B C$.


## D Watch Video Solution

21. In triangle $\mathrm{ABC}, A B>A C$ and D is a point in side BC . Show that : $A B>A D$.

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22. From the following figure, prove that :
$A B>C D$


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23. In a triangle $\mathrm{PQR}, \mathrm{QR}=\mathrm{PR}$ and $\angle P=36^{\circ}$.

Which is the largest side of the triangle ?
24. If two sides of a triangle are 8 cm and 13
cm , then the length of the third side is between acm and bcm . Find the values of $a$ and $b$ such that $a$ is less than $b$.

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25. In each of following figures, write $B C, A C$ and $C D$ in ascending order of their lengths.

(i)

D Watch Video Solution
26. Arrange the sides of $\triangle B O C$ in descending order of their lengths. BO and CO are
bisectors of angles $A B C$ and $A C B$ respectively.


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27. $D$ is a point in side $B C$ of triangle $A B C$. If $A D>A C$, show that $A B>A C$.
28. 

In
the following
figure,
$\angle B A C=60^{\circ}$ and $\angle A B C=65^{\circ}$.

Prove that :
(i) $C F>A F$
(ii) $D C>D F$


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29. In the following figure,
$\mathrm{AC}=\mathrm{CD}, \angle B A D=110^{\circ}$ and $\angle A C B=74^{\circ}$.

Prove that : $B C>C D$.


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30. From the following figure, prove that :
(i) $A B>B D$
(ii) $A C>C D$
(iii) $A B+A C>B C$


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31. In a quadrilateral $A B C D$, prove that :
(i) $A B+B C+C D>D A$
(ii) $A B+B C+C D+D A>2 A C$
(iii) $A B+B C+C D+D A>2 B D$

## D Watch Video Solution

32. In the following figure, $A B C$ is an equilateral triangle and $P$ is any point in $A C$, prove that:
(i) $B P>P A$
(ii) $B P>P C$


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33. $P$ is any point inside the triangle $A B C$. Prove
that: $\angle B P C>\angle B A C$.
34. Prove that the straight line joining the vertex of an isosceles triangle to any point in the base is smaller than either of the equal sides of the triangle.

## D Watch Video Solution

35. In the following diagram, $A D=A B$ and $A E$ bisects angle A. Prove that:
(i) $\mathrm{BE}=\mathrm{DE}$ (ii) $\angle A B D>\angle C$


## - Watch Video Solution

36. The sides $A B$ and $A C$ of a triangle $A B C$ are produced, and the bisectors of the external
angles at $B$ and $C$ meet at $P$. Prove that if $A B>A C$, then $P C>P B$.

## D Watch Video Solution

37. In the following figure, $A B$ is the largest side and $B C$ is the smallest side of the triangle ABC.


Write the angles $x^{\circ}, y^{\circ}$ and $z^{\circ}$ in
ascending order of their values.

## D Watch Video Solution

38. In quadrilateral $A B C D$, side $A B$ is the longest and side DC is the shortest. Prove that
(i) $\angle C>\angle A \quad$ (ii) $\angle D>\angle B$

## D Watch Video Solution

39. In triangle $A B C$, side $A C$ is greater than side
$A B$. If the internal bisector of angle $A$ meets
the opposite side at point D , prove that :
$\angle A D C$ is greater than $\angle A D B$.
40. In isosceles triangle $A B C$, sides $A B$ and $A C$ are equal. If point $D$ lies in base $B C$ and point $E$
lies on $B C$ produced ( $B C$ being produced through vertex C ), prove that :
(i) $A C>A D$
(ii) $A E>A C$
(iii) $A E>A D$

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## 41. Given : ED = EC

Prove : $A B+A D>B C$.


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42. In triangle $\mathrm{ABC}, A B>A C$ and D is a point in side BC . Show that : $A B>A D$.

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