

### **MATHS**

**BOOKS - ICSE** 

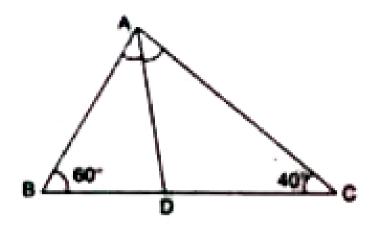
# **INEQUALITIES**

Example

**1.** In the adjoining figure, AD bisects  $\angle A$ .

Arrange AB, BD and DC in the descending

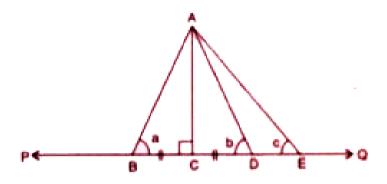
order of their lengths.





2. In the given figure, AC is perpendicular to line PQ and BC = CD. Show that AE is greater

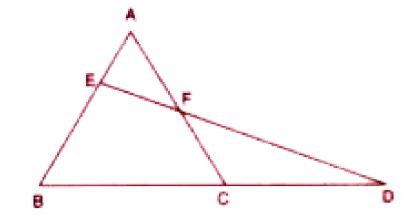
than AB.





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**3.** In the given figure, AB = AC. Prove that AF is greater than AE.

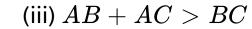


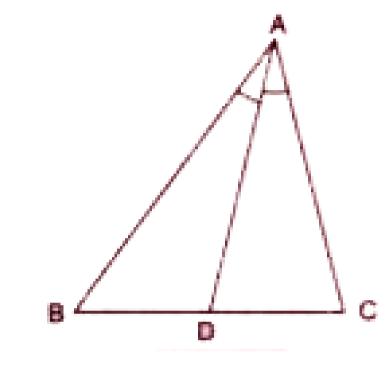


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**4.** In the figure, given alongside, AD bisects angle BAC. Prove that :

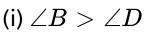
- (i) AB>BD
- (ii) AC > CD



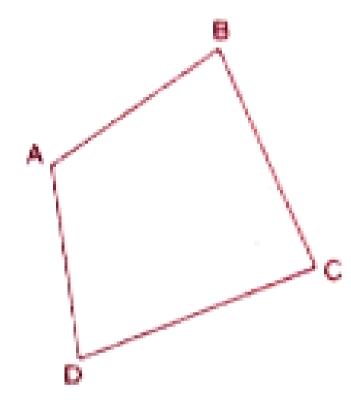




**5.** In quadrilateral ABCD, AB is the shortest side and DC is the longest side. Prove that :



(ii) 
$$\angle A > \angle C$$





6. AD is a median of triangle ABC. Prove that:

$$AB + AC > 2AD$$



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**7.** P is any point in the interior of a triangle

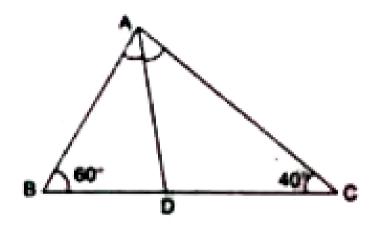
ABC.

Prove that : PA + PB < AC + BC



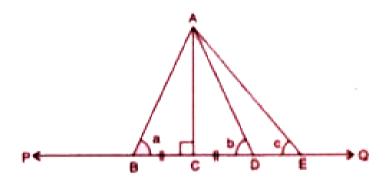
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**8.** In the adjoining figure, AD bisects  $\angle A$ . Arrange AB, BD and DC in the descending order of their lengths.





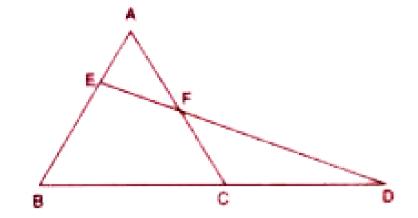
**9.** In the given figure, AC is perpendicular to line PQ and BC = CD. Show that AE is greater than AB.





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**10.** In the given figure, AB = AC. Prove that AF is greater than AE.



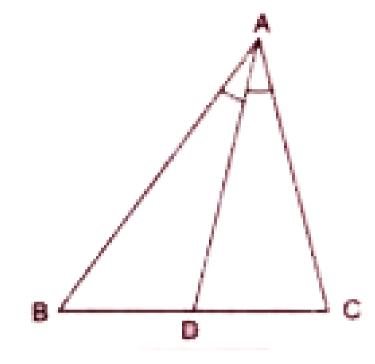


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**11.** In the figure, given alongside, AD bisects angle BAC. Prove that :

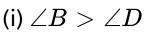
- (i) AB>BD
- (ii) AC > CD

(iii) 
$$AB + AC > BC$$

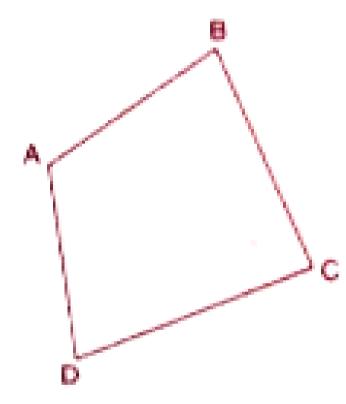




**12.** In quadrilateral ABCD, AB is the shortest side and DC is the longest side. Prove that:



(ii) 
$$\angle A > \angle C$$





**13.** AD is a median of triangle ABC. Prove that:

$$AB + BC + AC > 2AD$$



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14. P is any point in the interior of a triangle

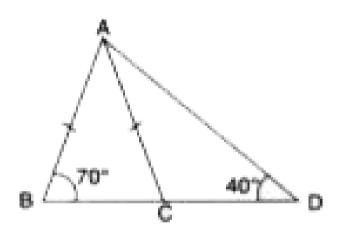
ABC.

Prove that : PA + PB < AC + BC



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1. From the following figure, prove that :





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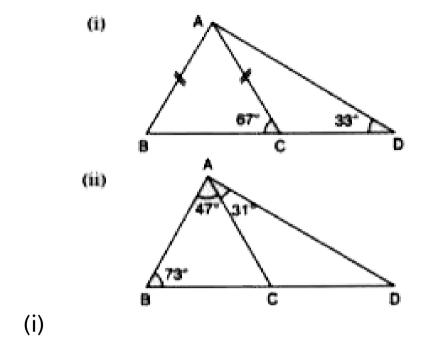
**2.** In a triangle PQR, QR = PR and  $\angle P = 36^{\circ}$ .

Which is the largest side of the triangle?

3. If two sides of a triangle are 8 cm and 13 cm, then the length of the third side is between a cm and b cm. Find the values of a and b such that a is less than b.



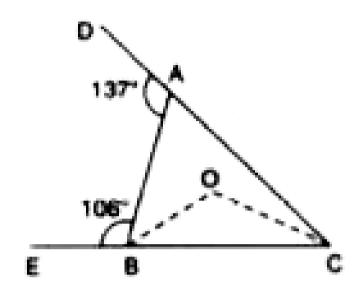
**4.** In each of following figures, write BC, AC and CD in ascending order of their lengths.





5. Arrange the sides of  $\Delta BOC$  in descending order of their lengths. BO and CO are

bisectors of angles ABC and ACB respectively.





6. D is a point in side BC of triangle ABC. If

AD>AC, show that AB>AC.

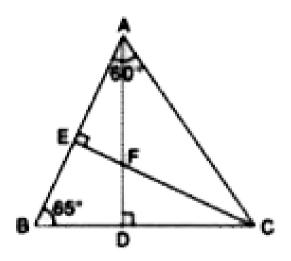


7. In the following figure,

$$\angle BAC = 60^{\circ}$$
 and  $\angle ABC = 65^{\circ}$ .

Prove that:

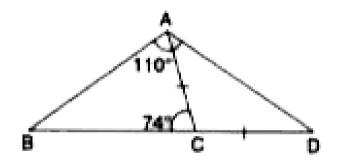
(i) 
$$CF > AF$$
 (ii)  $DC > DF$ 



**8.** In the following figure,

AC = CD, 
$$\angle BAD = 110^{\circ}$$
 and  $\angle ACB = 74^{\circ}$ .

Prove that : BC > CD.



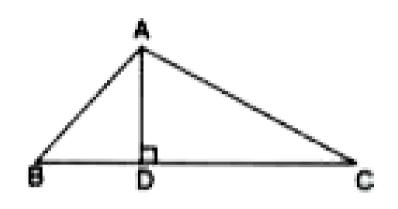
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- 9. From the following figure, prove that:
- (i) AB > BD

(ii) AC > CD

(iii) 
$$AB + AC > BC$$





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#### 10. In a quadrilateral ABCD, prove that:

(i) 
$$AB + BC + CD > DA$$

(ii) 
$$AB+BC+CD+DA>2AC$$

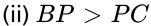
(iii) 
$$AB+BC+CD+DA>2BD$$

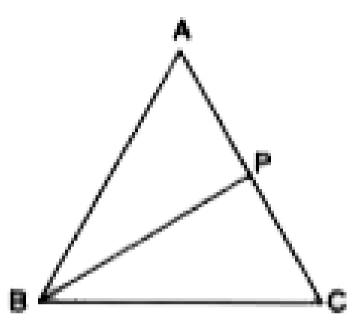


(i) BP > PA

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11. In the following figure, ABC is an equilateral triangle and P is any point in AC, prove that:







**12.** P is any point inside the triangle ABC. Prove

that :  $\angle BPC > \angle BAC$ .



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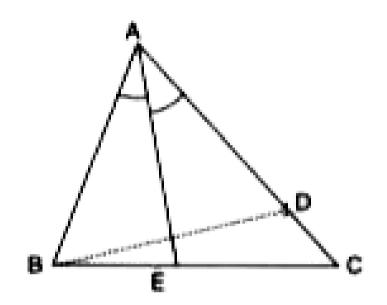
**13.** Prove that the straight line joining the vertex of an isosceles triangle to any point in the base is smaller than either of the equal sides of the triangle.



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**14.** In the following diagram, AD = AB and AE bisects angle A. Prove that :

(i) BE = DE (ii)  $\angle ABD > \angle C$ 





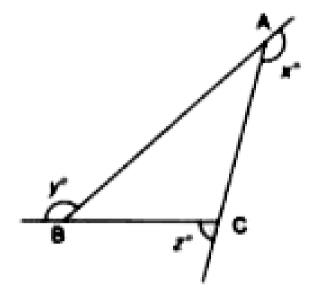
**15.** The sides AB and AC of a triangle ABC are produced, and the bisectors of the external

angles at B and C meet at P. Prove that if



AB > AC, then PC > PB.

**16.** In the following figure, AB is the largest side and BC is the smallest side of the triangle ABC.

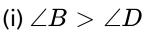


Write the angles  $x^\circ, y^\circ$  and  $z^\circ$  in ascending order of their values.

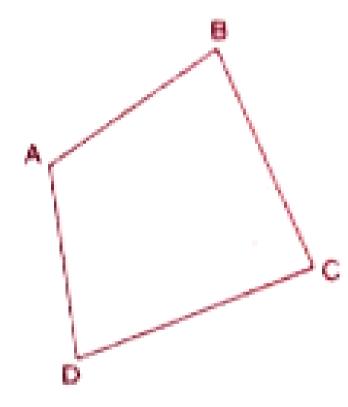


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**17.** In quadrilateral ABCD, AB is the shortest side and DC is the longest side. Prove that :



(ii) 
$$\angle A > \angle C$$





**18.** In triangle ABC, side AC is greater than side AB. If the internal bisector of angle A meets the opposite side at point D, prove that :  $\angle ADC$  is greater than  $\angle ADB$ .



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**19.** In isosceles triangle ABC, sides AB and AC are equal. If point D lies in base BC and point E lies on BC produced (BC being produced through vertex C), prove that:

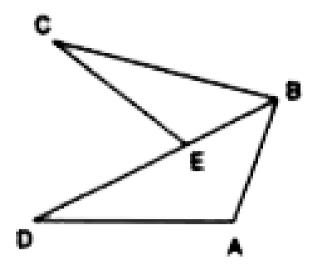
- (i) AC > AD
- (ii) AE > AC
- (iii) AE>AD



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**20.** Given : ED = EC

Prove : AB + AD > BC.

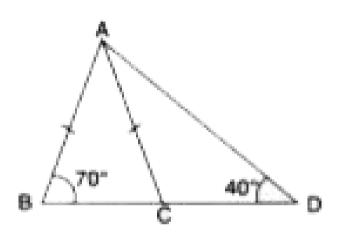




**21.** In triangle ABC, AB>AC and D is a point in side BC. Show that : AB>AD.



22. From the following figure, prove that :





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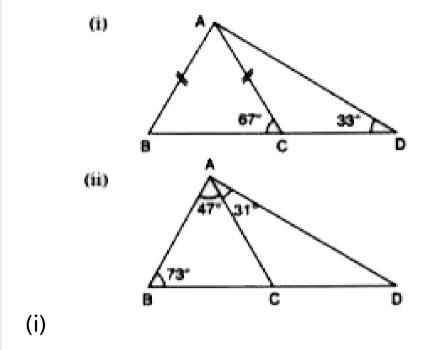
**23.** In a triangle PQR, QR = PR and  $\angle P = 36^{\circ}$  .

Which is the largest side of the triangle?

**24.** If two sides of a triangle are 8 cm and 13 cm, then the length of the third side is between a cm and b cm. Find the values of a and b such that a is less than b.



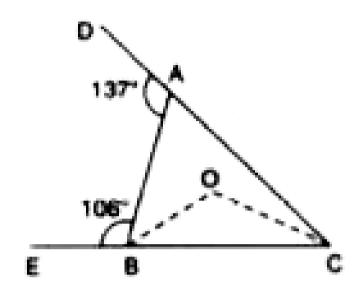
**25.** In each of following figures, write BC, AC and CD in ascending order of their lengths.





**26.** Arrange the sides of  $\Delta BOC$  in descending order of their lengths. BO and CO are

bisectors of angles ABC and ACB respectively.





27. D is a point in side BC of triangle ABC. If

AD>AC, show that AB>AC.

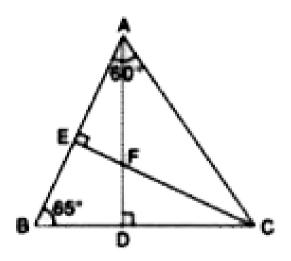


28. In the following figure,

$$\angle BAC = 60^{\circ}$$
 and  $\angle ABC = 65^{\circ}$ .

Prove that:

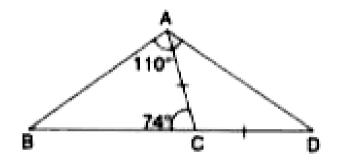
(i) 
$$CF > AF$$
 (ii)  $DC > DF$ 



**29.** In the following figure,

AC = CD, 
$$\angle BAD = 110^{\circ}$$
 and  $\angle ACB = 74^{\circ}$ .

Prove that : BC > CD.



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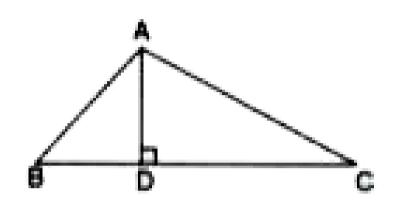
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**30.** From the following figure, prove that :

(i) AB > BD

(ii) AC > CD

(iii) 
$$AB + AC > BC$$





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#### 31. In a quadrilateral ABCD, prove that:

(i) 
$$AB + BC + CD > DA$$

(ii) 
$$AB+BC+CD+DA>2AC$$

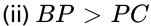
(iii) 
$$AB+BC+CD+DA>2BD$$

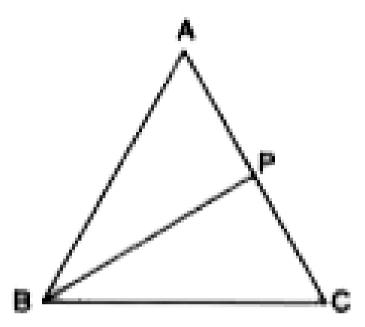


(i) BP > PA

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**32.** In the following figure, ABC is an equilateral triangle and P is any point in AC, prove that:







**33.** P is any point inside the triangle ABC. Prove

that :  $\angle BPC > \angle BAC$ .



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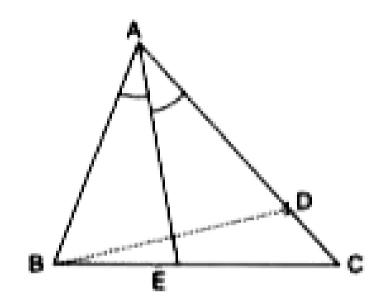
**34.** Prove that the straight line joining the vertex of an isosceles triangle to any point in the base is smaller than either of the equal sides of the triangle.



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**35.** In the following diagram, AD = AB and AE bisects angle A. Prove that :

(i) BE = DE (ii)  $\angle ABD > \angle C$ 





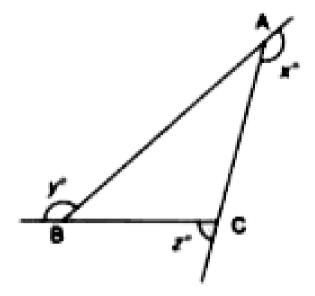
**36.** The sides AB and AC of a triangle ABC are produced, and the bisectors of the external

angles at B and C meet at P. Prove that if



AB > AC, then PC > PB.

**37.** In the following figure, AB is the largest side and BC is the smallest side of the triangle ABC.



Write the angles  $x^{\circ}, y^{\circ}$  and  $z^{\circ}$  in ascending order of their values.



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**38.** In quadrilateral ABCD, side AB is the longest and side DC is the shortest. Prove that

:

(i) 
$$\angle C > \angle A$$
 (ii)  $\angle D > \angle B$ 



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**39.** In triangle ABC, side AC is greater than side AB. If the internal bisector of angle A meets the opposite side at point D, prove that :  $\angle ADC$  is greater than  $\angle ADB$ .



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**40.** In isosceles triangle ABC, sides AB and AC are equal. If point D lies in base BC and point E lies on BC produced (BC being produced through vertex C), prove that:

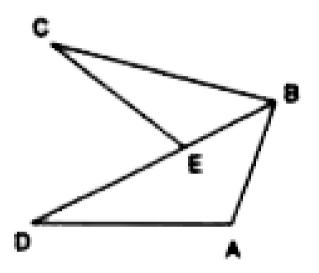
- (i) AC > AD
- (ii) AE > AC
- (iii) AE > AD



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**41.** Given : ED = EC

Prove : AB + AD > BC.





**42.** In triangle ABC, AB > AC and D is a point

in side BC. Show that : AB > AD.



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