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India's Number 1 Education App

## MATHS

## BOOKS - ICSE

## MID-POINT AND ITS

## CONVERSE(INCLUDING INTERCEPT THEOREM)

## Questions

1. The figure formed by joining the mid-points of the adjacent sides of a quadrilateral is a (a) parallelogram (b) rectangle (c)square
rhombus

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2. In parallelogram PQRS. L is mid-point of side SR and $S N$ is drawn parallel to $L Q$ which meets RQ produced prove that :

$S P=\frac{1}{2} R N$

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3. In parallelogram PQRS. L is mid-point of side Sr and SN is drawn parallel to $L Q$ which meets RQ produced prove that :

$S N=2 L Q$

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4. The adjoining figure shows a parallelogram
$A B C D$ in which $P$ is mid-point of $A B$ and $Q$ is
mid-point of CD. Prove that $A E=E F=F C$.


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5. 

In
a
right-angled
triangle
$A B C, \angle A B C=90^{\circ}$ and D is mid-point of AC .
Prove that $B D=\frac{1}{2} A C$.

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6. In triangle $A B C, B E$ ad CF are median $M$ is a point on $B E$ produced such that $B E=E M$ and $N$ is point on CF produced such that CF=FN.

Prove that
NAM is a straight line

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7. In triangle $A B C, B E$ ad $C F$ are median $M$ is a point on $B E$ produced such that $B E=E M$ and $N$
is point on CF produced such that $C F=F N$.

Prove that

A is the mid-point of MN

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8. $E$ is the mid-point of the side $A D$ of the tarapezium ABCD with $A B|\mid D C$. A line through E drawn parallel to $A B$ intersects $B C$ at $F$. Show that $F$ is the mid-points of $B C$.

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9. In a trapezium $A B C D, A B / D C, E$ is mid-point of $a D$. $A$ line through $E$ and parallel to $A B$ intersects BC at point F. Show that:
$2 E F=A B+D C$

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10. Prove by vector method that the line segment joining the mid-points of the diagonals of a trapezium is parallel to the parallel sides and equal to half of their difference.
11. Use the intercept Theorem to prove that the converse of the Mid-point Theorem

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12. $A B C D$ is a parallelogram. $E$ is the mid-point of $A B$ and $F$ is the mid-point of $C D . G H$ is any
line that intersects $A D, E F$ and $B C$ at $G, P$ and $H$
respectively. Prove that : GP=PH


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13. Use the information, given in the adjoining figure, to show that $A B=A C$


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Exercise 12 A

1. In triangle $A B C, M$ is mid-point of $A B$ and $a$
straight line through $M$ and parallel to $B C$ cuts
$A C$ at $N$. Find the lengths of $A N$ and $M N$, if $B C=$

7 cm and $\mathrm{AC}=5 \mathrm{~cm}$.

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2. Prove that the figure obtained by joining the mid-points of the adjacent sides of a rectangle is a rhombus.

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3. $D, E$ and $F$ are the mid-points of the sides $A B$,
$B C$ and CA of an isosceles triangle $A B C$ in which $\mathrm{AB}=\mathrm{BC}$. Prove that $\triangle D E F$ is also isosceles.

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4. The following figure shows a trapezium
$A B C D$ in which $A B / / D C . P$ is the mid-point of
AD and PR // AB. Prove that:
$P R=\frac{1}{2}(A B+C D)$


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5. The figure, given below, shows a trapezium

ABCD. $M$ and $N$ are the mid-points of the nonparallel sides $A D$ and $B C$ respectively. Find:

$M N$, if $A B=11 \mathrm{~cm}$ and $D C=8 \mathrm{~cm}$.

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6. The figure, given below, shows a trapezium
$A B C D . M$ and $N$ are the mid-points of the nonparallel sides $A D$ and $B C$ respectively. Find:

$A B$, if $D C=20 \mathrm{~cm}$ and $M N=27 \mathrm{~cm}$

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7. The figure, given below, shows a trapezium
$A B C D . M$ and $N$ are the mid-points of the nonparallel sides $A D$ and $B C$ respectively. Find:


## $D C$, if $M N=15 \mathrm{~cm}$ and $A B=23 \mathrm{~cm}$.

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8. The diagonals of a quadrilateral intersect at
right angles. Prove that the figure obtained by
joining the mid-points of the adjacent sides of
the quadrilateral is a rectangle.
9. $L$ and $M$ are the mid-points of sides $A B$ and DC respectively of parallelogram $A B C D$. Prove that segments $D L$ and $B M$ trisect diagonal $A C$.

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10. $A B C D$ is a quadrilateral in which $A D=B C . E$,
$F, G$ and $H$ are the mid-points of $A B, B D, C D$ and
$A C$ respectively. Prove that EFGH is a rhombus.


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11. A parallelogram $A B C D$ has $P$ the mid-point of $D C$ and $Q$ a midpoint of $A C$ such that $C Q=\frac{1}{4} A C . P Q$ produced meets $B C$ at R . Prove that:

$R$ is the mid-point of $B C$

D Watch Video Solution
12. A parallelogram $A B C D$ has $P$ the mid-point
of $D C$ and $Q$ a point of $A C$ such that
$C Q=\frac{1}{4} A C . P Q$ produced meets $B C$ at R . Prove that:
$P R=\frac{1}{2} D B$.

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13. D, E and F are the mid-points of the sides
$A B, B C$ and $C A$ respectively of $A B C$. $A E$ meets
DF at $O$. $P$ and $Q$ are the mid-points of $O B$ and
OC respectively. Prove that DPOF is a parallelogram.
14. In triangle $A B C, P$ is the mid-point of side BC. A line through P and parallel to CA meets
$A B$ at point $Q$ and a line through $Q$ and parallel to $B C$ meets median $A P$ at point $R$.

Prove that :
$A P=2 A R$

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15. In triangle $A B C, P$ is the mid-point of side $B C$. A line through $P$ and parallel to CA meets
$A B$ at point $Q$ and a line through $Q$ and a line through $Q$ and parallel to $B C$ meets median AP at point R. Prove that :
$B C=4 Q R$.

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16. In trapezium $A B C D, A B$ is parallel to $D C . P$ and $Q$ are the mid-points of $A D$ and $B C$ respectively. BP product meets CD produced at point E. Prove that :

Point $P$ bisects $B E$,

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17. In trapezium $A B C D, A B$ is parallel to $D C . P$ and $Q$ are the mid-points of $A D$ and $B C$ respectively. BP produced meets CD produced at point E. Prove that : $P Q$ is parallel to $A B$.

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18. In a triangle $A B C, A D$ is a median and $E$ is mid-point of median AD. A line through $B$ and
$E$ meets $A C$ at point $E$. Prove that $: A C=3 A F$

Draw DG parallel to BF, which meets AC at point G.

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19. $D$ and $F$ are the mid-points of sides $A B$ and
$A C$ of a triangle $A B C$. A line through $F$ and parallel to $A B$ meets $B C$ at point $E$.

Prove that BDFE is a parallelogram

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20. $D$ and $F$ are the mid-points of sides $A B$ and $A C$ of a triangle $A B C$. A line through $F$ and parallel to $A B$ meets $B C$ at point $E$.

Find AB , if $E F=4.8 \mathrm{~cm}$.

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21. In $\Delta A B C, A D$ is the median and $D E$ is parallel to $B A$, where $E$ is a point in $A C$. Prove that BE is also a median.
22. In $A A B C, E$ is mid-point of the median $A D$ and $B E$ produced meets side $A C$ at point Q .

Show that $\mathrm{BE}: \mathrm{EQ}=3: 1$.

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23. In the given figure, $M$ is mid-point of $A B$ and $D E$, whereas $N$ is mid-point of $B C$ and $D F$.

Show that : EF = AC.


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Exercise 12 B

1. Use the following figure to find:

$B C$, if $A B=7.2 \mathrm{~cm}$.

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## 2. Use the following figure to find :


$G E$, if $F E=4 \mathrm{~cm} . \mathrm{B}$
( Watch Video Solution
3. Use the following figure to find :

$A E$, if $B D=4.1 \mathrm{~cm}$.

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4. Use the following figure to find :

$D F$, if CG = 11 cm .

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5. In the figure, given below, $2 \mathrm{AD}=\mathrm{AB}, \mathrm{P}$ is midpoint of $A B, Q$ is mid-point of $D R$ and $P R / / B S$.

Prove that:


AQ//BS

D Watch Video Solution
6. In the figure, given below, $2 A D=A B, P$ is midpoint of $A B, Q$ is mid-point of $D R$ and $P R / / B S$.

Prove that:


DS $=3 R S$

D Watch Video Solution
7. The side $A C$ of a triangle $A B C$ is produced to point E so that $C E=\frac{1}{2} \mathrm{AC}$. D is the midpoint of $B C$ and $E D$ produced meets $A B$ at $F$. Lines through $D$ and $C$ are drawn parallel to $A B$ which meet $A C$ at point $P$ and $E F$ at point $R$ respectively. Prove that:
$3 D F=E F$

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8. The side $A C$ of a triangle $A B C$ is produced to point E so that $C E=\frac{1}{2} \mathrm{AC}$. D is the midpoint of $B C$ and $E D$ produced meets $A B$ at $F$. Lines through $D$ and $C$ are drawn parallel to $A B$ which meet $A C$ at point $P$ and $E F$ at point $R$ respectively. Prove that:
$4 C R=A B$

## D Watch Video Solution

9. In triangle $A B C$, the medians $B P$ and $C Q$ are produced upto points M and N respectively such that $\mathrm{BP}=\mathrm{PM}$ and $\mathrm{CQ}=\mathrm{QN}$. Prove that:
$\mathrm{M}, \mathrm{A}$ and N are collinear.

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10. In triangle $A B C$, the medians $B P$ and $C Q$ are produced upto points $M$ and $N$ respectively such that $B P=P M$ and $C Q=Q N$. Prove
that :

A is the mid-point of $M N$.

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11. In triangle $A B C$, angle $B$ is obtuse. $D$ and $E$ are mid-points of sides $A B$ and $B C$ respectively and $F$ is a point on side $A C$ such that $E F$ is parallel to $A B$. Show that BEFD is a parallelogram.
12. In parallelogram $A B C D, E$ and $F$ are midpoints of the sides $A B$ and $C D$ respectively. The lines segments $A F$ and $B F$ meet the line segments ED and EC at points $G$ and $H$ respectively. Prove that :
triangle HEB and FHC are congruent.

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13. In parallelogram $A B C D, E$ and $F$ are midpoints of the sides $A B$ and $C D$ respectively. The lines segments $A F$ and $B F$ meet the line
segments $E D$ and $E C$ at points $G$ and $H$ respectively. Prove that:

GEHF is a parallelogram.

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14. In triangle $A B C, D$ and $E$ are points on side
$A B$ such that $A D=D E=E B$. Through $D$ and $E$,
lines are drawn parallel to BC which meet side
$A C$ at points $F$ and $G$ respectively. Through $F$ and Glines are drawn parallel to $A B$ which
meet side $B C$ at points $M$ and $N$ respectively.

Prove that : $B M=M N=N C$.

## D Watch Video Solution

15. In triangle $A B C, M$ is mid-point of $A B, N$ is mid-point of $A C$ and $D$ is any point in base $B C$.

Use Intercept Theorem to show that MN bisects AD.
16. If the quadrilateral formed by joining the mid points of the adjacent sides of quadrilateral $A B C D$ is a rectangle, show that the diagonals $A C$ and $B D$ intersect at right angle.

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17. In triangle $A B C, D$ and $E$ are mid-points of the sides $A B$ and $A C$ respectively. Through $E$, a straight line is drawn parallel to $A B$ to meet $B C$
at $F$. Prove that $B D E F$ is a parallelogram. If $A B=$
$16 \mathrm{~cm}, \mathrm{AC}=12 \mathrm{~cm}$ and $\mathrm{BC}=18 \mathrm{~cm}$, find the perimeter of the parallelogram BDEF.

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18. In the given figure, $A D$ and $C E$ are medians
and $D F \| C E$. Prove that : $F b=\frac{1}{4} A B$.

19. In parallelogram $A B C D, E$ is the mid-point of
$A B$ and $A P$ is parallel to $E C$ which meets $D C$ at point O and BC produced at P. Prove that:

$P B=2 A D$
20. In parallelogram $A B C D, E$ is the mid-point of $A B$ and $A P$ is parallel to $E C$ which meets $D C$ at point O and BC produced at P. Prove that:


O is mid-point of AP.
21. In trapezium $A B C D$, sides $A B$ and $D C$ are parallel to each other. E is mid-point of AD and
$F$ is mid-point of $B C$.
Prove that : $A B+D C=2 E F$.

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22. In $\Delta A B C, A D$ is the median and $D E$ is parallel to $B A$, where $E$ is a point in $A C$. Prove
that $B E$ is also a median.

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23. Adjacent sides of a parallelgram are equal
and one of diagonls is equal to any one of the sides of this parallelgoram. Show that its diagonals are in the ratio $\sqrt{3}: 1$.

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