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## MATHS

## BOOKS - ICSE

## RECTILINEAR FIGURES

## Questions

1. The sum of the interior angles of a polygon
is five times the sum of its exterior angles.

Find the number of sides in the polygon.
2. One angle of an eight-sided polygon is $100^{\circ}$ and the other angles are equal. Find the measure of each equal angle.

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3. In a pentagon $A B C D E, A B$ is parallel to $E D$
and angle $B=140^{\circ}$. Find the angles C and D ,
if $\angle C: \angle D=5: 6$
4. In the pentagon $\operatorname{ABCDE}$, angle $A=110^{\circ}$, angle $B=140^{\circ}$ and angle $D=$ angle $E$. The sides
$A B$ and $D C$, when produced, meet at right angle. Calculate angles BCD and E.

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5. By dividing into triangles, find the sum of the angles of the doubly re-entrant heptagon

ABCDEFG as shown alongside. Does the
general value of $(2 n-4)$ right-angles hold for
re-entrant polygon?


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6. Each interior angle of a regular polygon is
$160^{\circ}$. Find the interior angle of another regular polygon whose number of sides is twothirds the number of sides of the given polygon.

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7. If the difference between an exterior angle of a regular polygon of ' $n$ ' sides and an exterior angle of another regular polygon of
' $(n+1)^{\prime}$ sides is equal to $5^{\circ}$, find the value of ' $n$ '.

## D Watch Video Solution

8. In the given figure, $A B C D$ is a parallelogram.

Find the values of $x, y$ and $z$

9. The given figure shows a rhombus $A B C D$.

Find $x$ and $y$


## D Watch Video Solution

10. $A B C D$ is a parallelogram and $A P$ and $C Q$ are perpendiculars from vertices $A$ and $C$ on
diagonal BD. Show that(i) $\triangle A P B \cong \triangle C Q D$
(ii) $A P=C Q$

## D Watch Video Solution

11. $A B C D$ is a parallelogram and $A P$ and $C Q$ are perpendiculars from vertices $A$ and $C$ on diagonal BD. Show that(i) $\triangle A P B \cong \triangle C Q D$
(ii) $A P=C Q$
12. In the adjoining figure, $A B C D$ and $P B C Q$ are parallelogram. Prove that:


APQD is a parallelogram

## D Watch Video Solution

13. In the adjoining figure, $A B C D$ and $P B C Q$ are parallelogram. Prove that:

$A P=D Q$

## D Watch Video Solution

14. In the adjoining figure, $A B C D$ and $P B C Q$ are parallelogram. Prove that:

$\triangle A B P \cong \triangle D C Q$

Watch Video Solution
15. A transversal cuts two parallel lines $P Q$ and

RS at points $A$ and $B$ respectively. The two interior angles at $A$ are bisected and so are the two interior angles at $B$, the four bisectors form a quadrilateral ACBD. Prove that:

ACBD is a rectangle

## D Watch Video Solution

16. $A B C D$ is a rhombus, $E A B F$ is a straight
line such that $E A=A B=B F$. Prove that
$E D$ and $F C$ when produced meet at right angles.

## D Watch Video Solution

17. $A B C D$ is a parallelogram $E$ is mid-point of $A B$ and DE bisects angle D. Prove that

$B C=B E$
18. $A B C D$ is a parallelogram $E$ is mid-point of
$A B$ and $D E$ bisects angle $D$. Prove that


CE bisects angle C

## D Watch Video Solution

19. $A B C D$ is a parallelogram $E$ is mid-point of
$A B$ and $D E$ bisects angle $D$. Prove that

$\angle D E C=90^{\circ}$

- Watch Video Solution

20. The figure, given alongside, shows a trapezium $A B C D$ in which $A B / D C$ and $A D=B C$.

## Prove that:


$\angle A=\angle B$

## D Watch Video Solution

21. The figure, given alongside, shows a trapezium $A B C D$ in which $A B / D C$ and $A D=B C$.

Prove that:

$\angle C=\angle D$

## - Watch Video Solution

22. The figure, given alongside, shows a trapezium $A B C D$ in which $A B / D C$ and $A D=B C$. Prove that:


## $\triangle A B C \cong \triangle B A D$

## - Watch Video Solution

23. The figure, given alongside, shows a trapezium $A B C D$ in which $A B / D C$ and $A D=B C$. Prove that:


## Diagonal $A C=$ diagonal $B D$

## ( Watch Video Solution

Exercise 14 A

1. The sum of the interior angles of a polygon
is four times the sum of its exterior angles.

Find the number of sides in the polygon.

## D Watch Video Solution

2. The angles of a pentagon are in the ratio
$4: 8: 6: 4: 5$. Find each angle of the pentagon.

## D Watch Video Solution

3. One angle of a six-sided polygon is $140^{\circ}$ and
the other angles are equal. Find the measure of each equal angle.

## - Watch Video Solution

4. In a polygon, there are 5 right angles and the remaining angles are equal to $195^{\circ}$ each.

Find the number of sides in the polygon.

## D Watch Video Solution

5. Three angles of a seven sided polygon are
$132^{\circ}$ each and the remaining four angles are equal. Find the value of each equal angle.

## Watch Video Solution

6. Two angles of an eight sided polygon are $142^{\circ}$ and $176^{\circ}$. If the remaining angles are equal to each other, find the magnitude of each of the equal angles.

## - Watch Video Solution

7. In a pentagon $A B C D E, A B$ is parallel to $D C$ and $\angle A: \angle E: \angle D=3: 4: 5$. Find angle E .
8. $A B, B C$ and $C D$ are the three consecutive sides of a regular polygon. If $\angle B A C=15^{\circ}$, find, each exterior angle of the polygon

## D Watch Video Solution

9. $A B, B C$ and $C D$ are the three consecutive sides of a regular polygon. If $\angle B A C=15^{\circ}$,
find,
each exterior angle of the polygon

## D Watch Video Solution

10. $A B, B C$ and $C D$ are the three consecutive sides of a regular polygon. If $\angle B A C=15^{\circ}$, find, number of sides of the polygon
11. The ratio between an exterior angle and an interior angle of a regular polygon is $2: 3$. Find the number of sides in the polygon.

## D Watch Video Solution

12. The difference between an exterior angle of
( $n-1$ ) sided regular polygon and an exterior angle of $(n+2)$ sided regular polygon is $6^{\circ}$.

Find the value of $n$
13. Two alternate sides of a regular polygon, when produced, meet at right angle. Find:
the value of each exterior angle of the polygon.

## - Watch Video Solution

14. Two alternate sides of a regular polygon, when produced, meet at right angle. Calculate the number of sides in the polygon.

Exercise 14 B True False

1. The diagonals of a rectangle bisect each other

## D Watch Video Solution

2. State 'True' or 'False'

The diagonals of a quadrilateral bisect each other

## - Watch Video Solution

3. The diagonals of a parallelogram bisect each other.

## ( Watch Video Solution

4. Each diagonal of a rhombus bisects it.
( Watch Video Solution
5. The quadrilateral, whose four sides are equal, is a square

- Watch Video Solution

6. Which of the following statements are true and which are false?

Every rhombus is a parallelogram.

D Watch Video Solution

## 7. State True or False

## Every parallelogram is a rhombus

## D Watch Video Solution

8. Diagonals of a rhombus are equal.

## D Watch Video Solution

## 9. State True or False

If two adjacent sides of a parallelogram are
equal, it is a rhombus

## - Watch Video Solution

10. State True or False

If the diagonals of a quadrilateral bisect each other at right angle, the quadrilateral is a square.

- Watch Video Solution

1. In the figure, given below, $A M$ bisects angle $A$ and $D M$ bisects angle $D$ of parallelogram $A B C D$.

Prove that: $\angle A M D=90^{\circ}$


## D Watch Video Solution

2. In the following figure, $A E$ and $B C$ are equal
and parallel and the three sides $A B, C D$ and $D E$
are equal to one another. If angle $A$ is $102^{\circ}$.
Find angles AEC and BCD


## D Watch Video Solution

3. In a square $A B C D$, diagonals meet at $O$. $P$ is a point on $B C$, such that $O B=B P$. Show that:
$\angle P O C=\left(22 \frac{1}{2}\right)^{\circ}$

- Watch Video Solution

4. In a square $A B C D$, diagonals meet at $\mathrm{O} . \mathrm{P}$ is a point on $B C$, such that $O B=B P$. Show that:
$\angle B D C=2 \angle P O C$

- Watch Video Solution

5. In a square $A B C D$, diagonals meet at $O$. $P$ is a point on $B C$, such that $O B=B P$. Show that:
$\angle B O P=3 \angle C O P$

D Watch Video Solution
6. The given figure shows a square $A B C D$ and an equilateral triangle ABP. Calculate:

$\angle A O B$
(D) Watch Video Solution
7. The given figure shows a square $A B C D$ and an equilateral triangle $A B P$. Calculate:

$\angle B P C$

## D Watch Video Solution

8. The given figure shows a square $A B C D$ and an equilateral triangle ABP. Calculate:

$\angle P C D$

- Watch Video Solution

9. The given figure shows a square $A B C D$ and an equilateral triangle ABP. Calculate:

reflex $\angle A P C$

D Watch Video Solution
10. In the given figure, $A B C D$ is a rhombus with
angle $A=67^{\circ}$


If DEC is an equilateral triangle, calculate:
$\angle C B E$

## - Watch Video Solution

11. In the given figure, $A B C D$ is a rhombus with
angle $A=67^{\circ}$


If $D E C$ is an equilateral triangle, calculate:
$\angle D B E$

## D Watch Video Solution

12. In each of the following figures, $A B C D$ is a parallelogram


In each case, given above, find the values of $x$ and $y$

## - Watch Video Solution

13. In each of the following figures, $A B C D$ is a
parallelogram


In each case, given above, find the values of $x$ and $y$

## D Watch Video Solution

14. The angles of a quadrilateral are in the
ratio 3:4:5: Show that the quadrilateral is a trapezium.
15. In a parallelogram $A B C D, A B=20 \mathrm{~cm}$ and
$A D=12 \mathrm{~cm}$. The bisector of angle A meets $D C$ at
$E$ and $B C$ produced at $F$. Find the length of $C F$.

## D Watch Video Solution

16. In parallelogram $A B C D, A P$ and $A Q$ are perpendiculars from vertex of obtuse angle $A$ as shown. If $\angle x: \angle y=2: 1$, find the angles of
the parallelogram.


## - Watch Video Solution

Exercise 14 C

1. $E$ is the mid-point of side $A B$ and $F$ is the mid
point of side DC of parallelogram ABCD . Prove
that AEFD is a parallelogram.

## - Watch Video Solution

2. The diagonal $B D$ of a parallelogram $A B C D$
bisects angles $B$ and $D$. Prove that $A B C D$ is a rhombus.

## D Watch Video Solution

3. The alongside figure shows a parallelogram
$A B C D$ in which $A E=E F=F C$.

Prove that:

DE is parallel to $F B$

D Watch Video Solution
4. The alongside figure shows a parallelogram
$A B C D$ in which $A E=E F=F C$.

Prove that:
$D E=F B$

- Watch Video Solution

5. The alongside figure shows a parallelogram $A B C D$ in which $A E=E F=F C$.

Prove that:

DEBF is a parallelogram

## D Watch Video Solution

6. In the alongside figure, $A B C D$ is $a$ parallelogram in which AP bisects angle A and $B Q$ bisects angel $B$. Prove that:

ABPQ is a parallelogram

## - Watch Video Solution

7. In the alongside figure, $A B C D$ is a parallelogram in which AP bisects angle $A$ and BQ bisects angel B. Prove that:
$A B P Q$ is a parallelogram

## D Watch Video Solution

8. In the alongside figure, $A B C D$ is a parallelogram in which AP bisects angle A and BQ bisects angel B. Prove that:

ABPQ is a parallelogram

## D Watch Video Solution

9. In the given figure, $A B C D$ is a parallelogram.

Prove that: $A B=2 B C$
10. Prove that the bisectors of opposite angles of a parallelogram are parallel.

## D Watch Video Solution

11. The bisectors of the angle of a parallelogram enclose a parallelogram
rhombus rectangle (d) square
( Watch Video Solution
12. Prove that the bisectors of the interior angles of a rectangle form a square.

## - Watch Video Solution

13. In parallelogram $A B C D$, the bisector of angle $A$ meets $D C$ at $P$ and $A B=2 A D$. Prove that:
$B P$ bisects angle $B$
14. In parallelogram $A B C D$, the bisector of angle $A$ meets $D C$ at $P$ and $A B=2 A D$. Prove that:

Angle APB $=90^{\circ}$

## - Watch Video Solution

15. Points $M$ and $N$ are taken on the diagonal
$A C$ of a parallelogram $A B C D$ such that $A M=C N$.
Prove that BMDN is a parallelogram.
16. In the following figure, $A B C D$ is $a$ parallelogram. Prove that:

AP bisects angle A

## D Watch Video Solution

17. In the following figure, $A B C D$ is a parallelogram. Prove that:

$B P$ bisects angle $B$

## D Watch Video Solution

18. In the following figure, $A B C D$ is a parallelogram. Prove that:
$\angle D A P+\angle C B P=\angle A P B$

## D Watch Video Solution

19. $A B C D$ is a square. $A$ is joined to a point $P$ on $B C$ and $D$ is joined to a point $Q$ on $A B$. If $A P=$ $D Q$, prove that $A P$ and $D Q$ are perpendicular to each other.
20. In a quadrilateral $A B C D, A B=A D$ and $C B=C D$.

Prove that:

AC bisects angle BAD

- Watch Video Solution

21. In a quadrilateral $A B C D, A B=A D$ and $C B=C D$.

Prove that:
$A C$ is perpendicular bisector of $B D$
22. The following figure shows a trapezium
$A B C D$ in which $A B$ is parallel to $D C$ and $A D=B C$


Prove that:
$\angle D A B=\angle C B A$
23. The following figure shows a trapezium
$A B C D$ in which $A B$ is parallel to $D C$ and $A D=B C$


Prove that:
$\angle A D C=\angle B C D$

D Watch Video Solution
24. The following figure shows a trapezium
$A B C D$ in which $A B$ is parallel to $D C$ and $A D=B C$


Prove that:
$O A=O B$ and $O C=O D$
( Watch Video Solution
25. In a parallelogram, prove that the bisectors of any two consecutive angles intersect at right angle.

## D Watch Video Solution

26. Prove that the bisectors of opposite angles
of a parallelogram are parallel.

D Watch Video Solution

## 27. The diagonals of a rectangle intersect each

 other at right angles. Prove that the rectangle is a square.
## D Watch Video Solution

28. In the following figure, $A B C D$ and $P Q R S$ are two parallelogram such that
$\angle D=120^{\circ}$ and $\angle Q=70^{\circ}$. Find the value of $x$.

## Polygons 3 Marks Questions

1. The sum of interior angles of a regular polygon is twice the sum of its exterior angles.

Find the number of sides of the polygon.

## - Watch Video Solution

2. The interior angles of a pentagon are in the ratio 4:5:6:7:5. Find each angle of the
pentagon.

## D Watch Video Solution

3. In a polygon, there are 5 right angles and the remaining angles are equal to $195^{\circ}$ each.

Find the number of sides in the polygon.

## - Watch Video Solution

4. Two angles of an eight sided polygon are
$142^{\circ}$ and $176^{\circ}$. If the remaining angles are
equal to each other, find the magnitude of each of the equal angles.

## D Watch Video Solution

5. Each interior angle of a regular polygon is
$135^{\circ}$. Find :
(i) the measure of each exterior angle
(ii) number of sides of the polygon
(iii) name of polygon
6. In a pentagon $A B C D E, A B$ is parallel to $D C$ and $\angle A: \angle E: \angle D=3: 4: 5$. Find angle E .

## - Watch Video Solution

2. $A B, B C$ and $D C$ are the three consecutive sides of a regular polygon. If $\angle B A C=15^{\circ}$, find:
(i) each interior angle of the polygon.
(ii) each exterior angle of the polygon.
(iii) number of sides of the polygon.

## D Watch Video Solution

3. The ratio between an exterior angle and an interior angle of a regular polygon is $2: 3$. Find the number of sides in the polygon.

D Watch Video Solution
4. The difference between an exterior angle of
( $n-1$ ) sided regular polygon and an exterior angle of $(n+2)$ sided regular polygon is $6^{\circ}$. Find the value of $n$

## (D) Watch Video Solution

Quadrilaterals And Its Properties 3 Marks
Questions

1. In the following figure, $A E$ and $B C$ are equal and parallel and the three sides $A B, C D$ and $D E$
are equal to one another. If angle $A$ is $102^{\circ}$.

Find angles AEC and BCD


## D Watch Video Solution

2. The angles of a quadrilateral are in the ratio
$3: 4: 5: 6$. Show that the quadrilateral is a trapezium.
3. In parallelogram $A B C D, A P$ and $A Q$ are perpendiculars from vertex of obtuse angle $A$ as shown. If $\angle x: \angle y=2: 1$, find the angles of the parallelogram.


## D Watch Video Solution

4. The diagonal $B D$ of a parallelogram $A B C D$ bisects angles $B$ and $D$. Prove that $A B C D$ is a rhombus.

## D Watch Video Solution

5. Points $M$ and $N$ are taken on the diagonal
$A C$ of a parallelogram $A B C D$ such that $A M=C N$.

Prove that BMDN is a parallelogram.

## D Watch Video Solution

6. The diagonals of a rectangle intersect each other at right angles. Prove that the rectangle is a square.

## D Watch Video Solution

7. The opposite angles of a parallelogram are equal.

- Watch Video Solution

8. $A B C D$ is a parallelogram in which
$\angle D A B=80^{\circ}$. Bisector of $\angle A$ and $\angle B$
meets CD at P. Prove that :

(i) $A D=D P$
(ii) $\mathrm{CP}=\mathrm{CB}$
(iii) $D C=2 A D$

D Watch Video Solution

Quadrilaterals And Its Properties 4 Marks Questions

1. The given figure shows a square $A B C D$ and an equilateral triangle $A B P$.


Calculate :
(i) $\angle A O B$
(ii) $\angle B P C$
(iii) $\angle P C D$
(iv) reflex $\angle A P C$

## D Watch Video Solution

2. In the given figure, $A B C D$ is a rhombus with
angle $\mathrm{A}=67^{\circ}$.


If DEC is an equilateral triangle. Calculate :
(i) $\angle C B E$ (ii) $\angle D B E$
(D) Watch Video Solution
3. The along side figure shows a parallelogram
$A B C D$ in which $A E=E F=F C$.


Prove that :
(i) DE is parallel to FB
(ii) $\mathrm{DE}=\mathrm{FB}$
(iii) DEBF is a parallelogram

- Watch Video Solution

4. The bisectors of the angle of a parallelogram enclose a parallelogram rhombus rectangle (d) square

## D Watch Video Solution

5. In parallelogram $A B C D$, the bisector of angle
$A$ meets $D C$ at $P$ and $A B=2 A D$.

Prove that :
(i) BP bisects angle $B$.
(ii) Angle $\mathrm{APB}=90^{\circ}$
6. In a quadrilateral $A B C D, A B=A D$ and $C B=C D$.

Prove that :
(i) $A C$ bisects angle BAD
(ii) $A C$ is perpendicular bisector of $B D$.

## D Watch Video Solution

7. The following figure shows a trapezium
$A B C D$ in which $A B$ is parallel to $D C$ and $A D=B C$.


Prove that :
(i) $\angle D A B=\angle C B A$
(ii) $\angle A D C=\angle B C D$
(iii) $A C=B D$
(iv) $O A=O B$ and $O C=O D$
(D) Watch Video Solution

