



## MATHS

# **BOOKS - ICSE**

# **RECTILINEAR FIGURES**



 The sum of the interior angles of a polygon is five times the sum of its exterior angles.
 Find the number of sides in the polygon.



**2.** One angle of an eight-sided polygon is  $100^{\circ}$ 

and the other angles are equal. Find the measure of each equal angle.



3. In a pentagon ABCDE, AB is parallel to ED and angle  $B=140^\circ.$  Find the angles C and D, if  $\angle C: \angle D=5:6$ 



4. In the pentagon ABCDE, angle  $A = 110^{\circ}$ , angle B=  $140^{\circ}$  and angle D= angle E. The sides AB and DC, when produced, meet at right angle. Calculate angles BCD and E.



5. By dividing into triangles, find the sum of the angles of the doubly re-entrant heptagon ABCDEFG as shown alongside. Does the general value of (2n-4) right-angles hold for

re-entrant polygon?



**6.** Each interior angle of a regular polygon is  $160^{\circ}$ . Find the interior angle of another regular polygon whose number of sides is two-thirds the number of sides of the given polygon.

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**7.** If the difference between an exterior angle of a regular polygon of 'n' sides and an exterior angle of another regular polygon of ' (n+1) ' sides is equal to  $5^{\circ}$  , find the value

of 'n'.



**9.** The given figure shows a rhombus ABCD. Find x and y



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10. ABCD is a parallelogram and AP and CQ are

perpendiculars from vertices A and C on

diagonal BD . Show that(i)  $\Delta APB\cong \ \Delta CQD$ 

(ii) AP = CQ

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**11.** ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on diagonal BD . Show that(i)  $\Delta APB \cong \Delta CQD$ 

(ii) AP = CQ

### 12. In the adjoining figure, ABCD and PBCQ are

parallelogram. Prove that:



APQD is a parallelogram



### 13. In the adjoining figure, ABCD and PBCQ are

parallelogram. Prove that:



AP= DQ

### 14. In the adjoining figure, ABCD and PBCQ are

parallelogram. Prove that:



 $\Delta ABP\cong \Delta DCQ$ 

**15.** A transversal cuts two parallel lines PQ and RS at points A and B respectively. The two interior angles at A are bisected and so are the two interior angles at B, the four bisectors form a quadrilateral ACBD. Prove that:

ACBD is a rectangle

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**16.** ABCD is a rhombus, EABF is a straight line such that EA = AB = BF . Prove that

ED and FC when produced meet at right

angles.



17. ABCD is a parallelogram E is mid-point of AB

and DE bisects angle D. Prove that









18. ABCD is a parallelogram E is mid-point of

AB and DE bisects angle D. Prove that



CE bisects angle C

**19.** ABCD is a parallelogram E is mid-point of

AB and DE bisects angle D. Prove that



 $\angle DEC = 90^{\circ}$ 



**20.** The figure, given alongside, shows a trapezium ABCD in which AB/DC and AD= BC.

#### Prove that:



 $\angle A = \angle B$ 



**21.** The figure, given alongside, shows a trapezium ABCD in which AB/DC and AD= BC. Prove that:



**22.** The figure, given alongside, shows a trapezium ABCD in which AB/DC and AD= BC. Prove that:



**23.** The figure, given alongside, shows a trapezium ABCD in which AB/DC and AD= BC. Prove that:



is four times the sum of its exterior angles.

Find the number of sides in the polygon.

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2. The angles of a pentagon are in the ratio

4:8:6:4:5. Find each angle of the pentagon.

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**3.** One angle of a six-sided polygon is  $140^{\circ}$  and the other angles are equal. Find the measure of each equal angle.



**4.** In a polygon, there are 5 right angles and the remaining angles are equal to  $195^{\circ}$  each. Find the number of sides in the polygon.



5. Three angles of a seven sided polygon are  $132^{\circ}$  each and the remaining four angles are

equal . Find the value of each equal angle.



**6.** Two angles of an eight sided polygon are  $142^{\circ}$  and  $176^{\circ}$ . If the remaining angles are equal to each other, find the magnitude of each of the equal angles.



7. In a pentagon ABCDE, AB is parallel to DC

and  $\angle A : \angle E : \angle D = 3 : 4 : 5$ . Find angle E.

8. AB, BC and CD are the three consecutive sides of a regular polygon. If  $\angle BAC = 15^{\circ}$ , find,

each exterior angle of the polygon

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9. AB, BC and CD are the three consecutive sides of a regular polygon. If  $\angle BAC = 15^{\circ}$ ,

find,

each exterior angle of the polygon



10. AB, BC and CD are the three consecutive

sides of a regular polygon. If  $\angle BAC = 15^{\circ}$  ,

find,

number of sides of the polygon

11. The ratio between an exterior angle and an

interior angle of a regular polygon is 2 : 3. Find

the number of sides in the polygon.



12. The difference between an exterior angle of (n-1) sided regular polygon and an exterior angle of (n+2) sided regular polygon is  $6^{\circ}$ . Find the value of n

13. Two alternate sides of a regular polygon, when produced, meet at right angle. Find: the value of each exterior angle of the polygon.

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**14.** Two alternate sides of a regular polygon, when produced, meet at right angle. Calculate the number of sides in the polygon.

Exercise 14 B True False

1. The diagonals of a rectangle bisect each

other

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2. State 'True' or 'False'

The diagonals of a quadrilateral bisect each

other



3. The diagonals of a parallelogram bisect each

other.

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## **4.** Each diagonal of a rhombus bisects it.





6. Which of the following statements are true

and which are false ?

Every rhombus is a parallelogram.



7. State True or False

Every parallelogram is a rhombus



9. State True or False

If two adjacent sides of a parallelogram are



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10. State True or False

If the diagonals of a quadrilateral bisect each

other at right angle, the quadrilateral is a

square.



### Exercise 14 B

**1.** In the figure, given below, AM bisects angle A and DM bisects angle D of parallelogram ABCD. Prove that:  $\angle AMD = 90^{\circ}$ 





2. In the following figure, AE and BC are equal and parallel and the three sides AB, CD and DE are equal to one another. If angle A is  $102^{\circ}$ . Find angles AEC and BCD





3. In a square ABCD, diagonals meet at O. P is a

point on BC, such that OB= BP. Show that:

$$egin{array}{l} \angle POC = \left(22rac{1}{2}
ight)^\circ \end{array}$$

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#### 4. In a square ABCD, diagonals meet at O. P is a

point on BC, such that OB= BP. Show that:

 $\angle BDC = 2 \angle POC$ 

5. In a square ABCD, diagonals meet at O. P is a

point on BC, such that OB= BP. Show that:

 $\angle BOP = 3 \angle COP$ 

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**6.** The given figure shows a square ABCD and an equilateral triangle ABP. Calculate:



**7.** The given figure shows a square ABCD and an equilateral triangle ABP. Calculate:


**8.** The given figure shows a square ABCD and an equilateral triangle ABP. Calculate:



#### $\angle PCD$

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**9.** The given figure shows a square ABCD and an equilateral triangle ABP. Calculate:



 $\mathsf{reflex}\,\angle APC$ 

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10. In the given figure, ABCD is a rhombus with

angle  $A=67^\circ$ 



If DEC is an equilateral triangle, calculate:

 $\angle CBE$ 



11. In the given figure, ABCD is a rhombus with

angle  $A=67^\circ$ 



If DEC is an equilateral triangle, calculate:

 $\angle DBE$ 



12. In each of the following figures, ABCD is a

parallelogram



In each case, given above, find the values of x and y



**13.** In each of the following figures, ABCD is a

parallelogram

D 6x + 3y - 8°  $4x + 20^{\circ}$ 

In each case, given above, find the values of x

and y



**14.** The angles of a quadrilateral are in the ratio 3:4:5:6. Show that the quadrilateral is a trapezium.

**15.** In a parallelogram ABCD, AB= 20 cm and

AD= 12cm. The bisector of angle A meets DC at

E and BC produced at F. Find the length of CF.

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16. In parallelogram ABCD, AP and AQ are perpendiculars from vertex of obtuse angle A as shown. If  $\angle x : \angle y = 2:1$ , find the angles of

#### the parallelogram.



Exercise 14 C

**1.** E is the mid-point of side AB and F is the mid point of side DC of parallelogram ABCD . Prove

that AEFD is a parallelogram.



**2.** The diagonal BD of a parallelogram ABCD bisects angles B and D. Prove that ABCD is a rhombus.

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**3.** The alongside figure shows a parallelogram ABCD in which AE= EF= FC.



Prove that:

DE is parallel to FB

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**4.** The alongside figure shows a parallelogram ABCD in which AE= EF= FC.



Prove that:

DE= FB



**5.** The alongside figure shows a parallelogram ABCD in which AE= EF= FC.



Prove that:

DEBF is a parallelogram



6. In the alongside figure, ABCD is a parallelogram in which AP bisects angle A and BQ bisects angel B. Prove that:



ABPQ is a parallelogram



7. In the alongside figure, ABCD is a parallelogram in which AP bisects angle A and BQ bisects angel B. Prove that:



ABPQ is a parallelogram

**8.** In the alongside figure, ABCD is a parallelogram in which AP bisects angle A and BQ bisects angel B. Prove that:



ABPQ is a parallelogram

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9. In the given figure, ABCD is a parallelogram.

Prove that: AB= 2BC



10. Prove that the bisectors of opposite angles

of a parallelogram are parallel.

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**11.** The bisectors of the angle of a parallelogram enclose a parallelogram (b) rhombus rectangle (d) square

12. Prove that the bisectors of the interior

angles of a rectangle form a square.

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**13.** In parallelogram ABCD, the bisector of angle A meets DC at P and AB= 2AD. Prove that: BP bisects angle B

14. In parallelogram ABCD, the bisector of angle A meets DC at P and AB= 2AD. Prove that: Angle APB=  $90^{\circ}$ 



15. Points M and N are taken on the diagonal

AC of a parallelogram ABCD such that AM= CN.

Prove that BMDN is a parallelogram.



16. In the following figure, ABCD is a

parallelogram. Prove that:



AP bisects angle A

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# **17.** In the following figure, ABCD is a parallelogram. Prove that:



## **18.** In the following figure, ABCD is a parallelogram. Prove that:



#### $\angle DAP + \angle CBP = \angle APB$



19. ABCD is a square. A is joined to a point P on

BC and D is joined to a point Q on AB. If AP =

DQ, prove that AP and DQ are perpendicular to

each other.



**20.** In a quadrilateral ABCD, AB= AD and CB= CD.

Prove that:

AC bisects angle BAD

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**21.** In a quadrilateral ABCD, AB= AD and CB= CD.

Prove that:

AC is perpendicular bisector of BD

**22.** The following figure shows a trapezium ABCD in which AB is parallel to DC and AD= BC



Prove that:

 $\angle DAB = \angle CBA$ 

**23.** The following figure shows a trapezium ABCD in which AB is parallel to DC and AD= BC



Prove that:

 $\angle ADC = \angle BCD$ 



**24.** The following figure shows a trapezium ABCD in which AB is parallel to DC and AD= BC



Prove that:

OA = OB and OC= OD

**25.** In a parallelogram, prove that the bisectors of any two consecutive angles intersect at right angle.



26. Prove that the bisectors of opposite angles

of a parallelogram are parallel.



**27.** The diagonals of a rectangle intersect each other at right angles. Prove that the rectangle is a square.



#### 28. In the following figure, ABCD and PQRS are

two parallelogram such that

 ${{{\angle D}}=120^{\,\circ}}\,\,\,{
m and}\,\,{{{\angle Q}}=70^{\,\circ}}.$  Find the value

of x.







#### Polygons 3 Marks Questions

 The sum of interior angles of a regular polygon is twice the sum of its exterior angles.
 Find the number of sides of the polygon.

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2. The interior angles of a pentagon are in the

ratio 4:5:6:7:5. Find each angle of the



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**3.** In a polygon, there are 5 right angles and the remaining angles are equal to  $195^{\circ}$  each. Find the number of sides in the polygon.

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**4.** Two angles of an eight sided polygon are  $142^{\circ}$  and  $176^{\circ}$ . If the remaining angles are

equal to each other, find the magnitude of

each of the equal angles.



- 5. Each interior angle of a regular polygon is
- $135^{\,\circ}$  . Find :
- (i) the measure of each exterior angle
- (ii) number of sides of the polygon
- (iii) name of polygon



1. In a pentagon ABCDE, AB is parallel to DC

and  $\angle A : \angle E : \angle D = 3 : 4 : 5$ . Find angle E.

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2. AB, BC and DC are the three consecutive sides of a regular polygon. If  $\angle BAC = 15^{\circ}$ , find :

(i) each interior angle of the polygon.

(ii) each exterior angle of the polygon.

(iii) number of sides of the polygon.



3. The ratio between an exterior angle and an

interior angle of a regular polygon is 2 : 3. Find

the number of sides in the polygon.



**4.** The difference between an exterior angle of (n-1) sided regular polygon and an exterior angle of (n+2) sided regular polygon is  $6^{\circ}$ . Find the value of n



### Quadrilaterals And Its Properties 3 Marks Questions

**1.** In the following figure, AE and BC are equal and parallel and the three sides AB, CD and DE

are equal to one another. If angle A is  $102^{\,\circ}$  .

Find angles AEC and BCD



**2.** The angles of a quadrilateral are in the ratio 3:4:5:6. Show that the quadrilateral is a trapezium.



**3.** In parallelogram ABCD, AP and AQ are perpendiculars from vertex of obtuse angle A as shown. If  $\angle x : \angle y = 2:1$ , find the angles of the parallelogram.



**4.** The diagonal BD of a parallelogram ABCD bisects angles B and D. Prove that ABCD is a rhombus.

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5. Points M and N are taken on the diagonal

AC of a parallelogram ABCD such that AM= CN.

Prove that BMDN is a parallelogram.



**6.** The diagonals of a rectangle intersect each other at right angles. Prove that the rectangle is a square.



7. The opposite angles of a parallelogram are

equal.
8. ABCD is a parallelogram in which  $\angle DAB = 80^{\circ}$ . Bisector of  $\angle A$  and  $\angle B$ 

meets CD at P. Prove that :



(i) AD = DP

(ii) CP = CB

(iii) DC = 2AD

1. The given figure shows a square ABCD and

an equilateral triangle ABP.



Calculate :

(i)  $\angle AOB$ 

(ii)  $\angle BPC$ 

(iii)  $\angle PCD$ 

(iv) reflex  $\angle APC$ 

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**2.** In the given figure, ABCD is a rhombus with angle  $A = 67^{\circ}$ .



If DEC is an equilateral triangle. Calculate :

(i)  $\angle CBE$  (ii)  $\angle DBE$ 

3. The along side figure shows a parallelogram

ABCD in which AE = EF = FC.



Prove that :

- (i) DE is parallel to FB
- (ii) DE = FB

(iii) DEBF is a parallelogram

**4.** The bisectors of the angle of a parallelogram enclose a parallelogram (b) rhombus rectangle (d) square

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5. In parallelogram ABCD, the bisector of angle

A meets DC at P and AB = 2AD.

Prove that :

(i) BP bisects angle B.

(ii) Angle APB =  $90^{\circ}$ 



6. In a quadrilateral ABCD, AB = AD and CB = CD.

Prove that :

(i) AC bisects angle BAD

(ii) AC is perpendicular bisector of BD.

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**7.** The following figure shows a trapezium ABCD in which AB is parallel to DC and AD = BC.



Prove that :

- (i)  $\angle DAB = \angle CBA$
- (ii)  $\angle ADC = \angle BCD$
- (iii) AC = BD

(iv) OA = OB and OC = OD