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## India's Number 1 Education App

## MATHS

## BOOKS - ICSE

## TRIANGLES

## Exercise 9 A

1. Which of the following pairs of triangles are congruent ? In each case, state the condition of congruency :
(a) In $\triangle A B C$ and $\triangle D E F, \mathrm{AB}=\mathrm{DE}, \mathrm{BC}=\mathrm{EF}$ and $\angle B=\angle E$.
(b) In $\triangle A B C$ and $\triangle D E F, \angle B=\angle E=90^{\circ}, \mathrm{AC}=\mathrm{DF}$ and $\mathrm{BC}=\mathrm{EF}$.
(c) In $\triangle A B C$ and $\triangle Q R P, \mathrm{AB}=\mathrm{QR}, \angle B=\angle R$ and $\angle C=\angle P$.
(d) In $\triangle A B C$ and $\triangle P Q R, \mathrm{AB}=\mathrm{PQ}, \mathrm{AC}=\mathrm{PR}$ and $\mathrm{BC}=\mathrm{QR}$.
(e) In $\triangle A B C$ and $\triangle P Q R$, $\quad \mathrm{BC} \quad \mathrm{QR}$,
$\angle A=90^{\circ}, \angle C=\angle R=40^{\circ}$ and $\angle Q=50^{\circ}$.
2. The given figure shows a circle with centre $O$. $P$ is mid-point of chord $A B$. Show that OP is perpendicular to AB.


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3. The following figure shows a circle with centre O .

If $O P$ is perpendicular to $A B$, prove that $A P=B P$.

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4. In a triangle $A B C, D$ is mid-point of $B C, A D$ is produced upto $E$ so that $D E$
= AD. Prove that :
(i) $\triangle A B D$ and $\triangle E C D$ are congruent.
(ii) $\mathrm{AB}=\mathrm{EC}$
(iii) AB is parallel to EC .

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5. A triangle ABC has $\angle B=\angle C$. Prove that :
(i) the perpendiculars from the mid-point of $B C$ to $A B$ and $A C$ are equal.
(ii) the perpendicular from $B$ and $C$ to the opposite sides are equal.

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6. The perpendicular bisectors of the sides of a triangle ABC meet at I. Prove that : $\mathrm{IA}=\mathrm{IB}=\mathrm{IC}$.

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7. $A$ line segment $A B$ is bisected at point $P$ and through point $P$ another line segment PQ , which is perpendicular to AB , is drawn. Show that : $\mathrm{QA}=$ QB.

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8. If AP bisects angle BAC and $M$ is any point on AP, prove that the perpendiculars drawn from $M$ to $A B$ and $A C$ are equal.

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9. From the given diagram, in which $A B C D$ is a parallelgram, $A B L$ is a line segment and E is mid point of BC . Prove that :
(i) $\triangle D C E \cong \triangle L B E$
(ii) $\mathrm{AB}=\mathrm{BL}$
(iii) $\mathrm{AL}=2 \mathrm{DC}$

10. In the given figure, $A B=D B$ and $A C=D C$. If $\angle A B D=58^{\circ}, \angle D B C=(2 x-4)^{\circ}, \angle A C B=y+15^{\circ}$ and $\angle D C B=63$
, find the values of $x$ and $y$.

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11. In the given figure : $\mathrm{AB} / / \mathrm{FD}, \mathrm{AC} / / \mathrm{GE}$ and $\mathrm{BD}=\mathrm{CE}$, prove that :
(i) $\mathrm{BG}=\mathrm{DF}$
(ii) $\mathrm{CF}=\mathrm{EG}$


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12. In a triangle $A B C, A B=A C$. Show that the altitude $A D$ is median also.
13. In the following figure, $\mathrm{BL}=\mathrm{CM}$.


Prove that $A D$ is a median of triangle $A B C$.

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14. In the following figure, $A B=A C$ and $A D$ is perpendicular to $B C$. $B E$ bisects angle $B$ and $E F$ is perpendicular to $A B$. Prove that :
(i) $B D=C D$
(ii) $\mathrm{ED}=\mathrm{EF}$


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15. Use the information in the given figure to prove :
(i) $\mathrm{AB}=\mathrm{FE}$
(ii) $\mathrm{BD}=\mathrm{CF}$

## A



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Exercise 9 B

1. On the sides $A B$ and $A C$ of triangle $A B C$, equilateral triangles $A B D$ and

ACE are drawn. Prove that :
(i) $\angle C A D=\angle B A E$
(ii) $C D=B E$

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2. In the following diagrams, $A B C D$ is a square and $A P B$ is an equilateral triangle. In each case,
(i) Prove that: $\triangle A P D \cong \triangle B P C$
(ii) Find the angles of $\triangle D P C$


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3. In the figure, given below, triangle ABC is right-angled at B. ABPQ and ACRS are squares. Prove that :
(i) $\triangle A C Q$ and $\triangle A S B$ are congruent.
(ii) $\mathrm{CQ}=\mathrm{BS}$


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4. In a $\triangle A B C, \mathrm{BD}$ is the median to the side $\mathrm{AC}, \mathrm{BD}$ is produced to E such that $B D=D E$. Prove that : $A E$ is parallel to $B C$.
5. In the adjoining figure, $Q X$ and $R X$ are the bisectors of the angles $Q$ and $R$ respectively of the triangle $P Q R$.

If $X S \perp Q R$ and $X T \perp P Q$, prove that :
$\Delta X T Q \cong \triangle X S Q$


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6. In the parallelogram ABCD, the angles $A$ and $C$ are obtuse. Points $X$ and $Y$ are taken on the diagonal BD such that the angles XAD and YCB are right angles. Prove that : $\mathrm{XA}=\mathrm{YC}$

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7. $A B C D$ is a parallelogram. The sides $A B$ and $A D$ are produced to $E$ and $F$ respectively, such that $A B=B E$ and $A D=D F$. Prove that : $\triangle B E C \cong \triangle D C F$.

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8. In the following figures, the sides $A B$ and $B C$ and the median $A D$ of triangle $A B C$ are respectively equal to the sides $P Q$ and $Q R$ and median $P S$
of the triangle PQR . Prove that $\triangle A B C$ and $\triangle P Q R$ are congruent.


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9. In the following diagram, AP and BQ are equal and parallel to each other.


Prove that:
(i) $\triangle A O P \cong \triangle B O Q$
(ii) AB and PQ bisect each other.

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10. In the following figure, $O A=O C$ and $A B=B C$. Prove that:
(i) $\angle A O B=90^{\circ}$
(ii) $\triangle A O D \cong \triangle C O D$
(iii) $A D=C D$


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11. The following figure shows a triangle $A B C$ in which $A B=A C . M$ is a point on $A B$ and $N$ is a point on $A C$ such that $B M=C N$. Prove that :
(i) $\mathrm{AM}=\mathrm{AN}$
(ii) $\Delta A M C \cong \triangle A N B$
(iii) $\mathrm{BN}=\mathrm{CM}$
(iv) $\triangle B M C \cong \triangle C N B$


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12. In a triangle $A B C, A B=B C, A D$ is perpendicular to side $B C$ and $C E$ is perpendicular to side $A B$. Prove that : $A D=C E$.

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13. $P Q R S$ is a parallelogram. $L$ and $M$ are points on $P Q$ and $S R$ respectively such that $P L=M R$. Show that $L M$ and $Q S$ bisect each other.

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14. In the following figure, $A B C$ is an equilateral triangle in which $Q P$ is parallel to $A C$. Side $A C$ is produced upto point $R$ so that $C R=B P$.


Prove that QR bisects PC.

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15. In the following figure, $\angle A=\angle C$ and $\mathrm{AB}=\mathrm{BC}$.


Prove that : $\triangle A B D \cong \triangle C B E$

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16. $A D$ and $B C$ are equal perpendiculars to a line segment $A B$. If $A D$ and $B C$ are on different sides of $A B$ prove that $C D$ bisects $A B$.

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17. In $\Delta A B C, \mathrm{AB}=\mathrm{AC}$ and the bisectors of angles B and C intersect at point O. Prove that:
(i) $\mathrm{BO}=\mathrm{CO}$
(ii) AO bisects angle BAC.

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18. In the following figure, $\mathrm{AB}=\mathrm{EF}, \mathrm{BC}=\mathrm{DE}$ and $\angle B=\angle E=90^{\circ}$.


Pove that $A D=F C$.

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19. A point $O$ is taken inside a rhombus $A B C D$ such that its distances from the vertices $B$ and $D$ are equal. Show that AOC is a straight line.

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20. In quadrilateral $A B C D, A D=B C$ and $B D=C A$. Prove that :
(i) $\angle A D B=\angle B C A$
(ii) $\angle D A B=\angle C B A$

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## Questions

1. $P$ is any point in the angle $A B C$ such that the perpendicular drawn from $P$ on $A B$ and $B C$ are equal. Prove that $B P$ bisects angle $A B C$.

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2. If the diagonals of a quadrilateral bisect each other at right angle, prove that the quadrilateral is a rhombus.

A rhombus has all its four sides equal.


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3. In triangle $A B C$, the sides $A B$ and $A C$ are equal. If $P$ is a point on $A B$ and
$Q$ is a point on $A C$ such that $A P=A Q$, prove that :
(i) triangle APC and AQB are congruent.
(ii) triangle BPC and CQB are congruent.


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4. In the given figure, $\mathrm{AC}=\mathrm{AE}, \mathrm{AB}=\mathrm{AD}$ and $\angle B A D=\angle E A C$. Show that : $B C=D E$.


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5. Use the information given in the adjoining figure, to prove :
(i) $\triangle D B C \cong \triangle E A C$.
(ii) $\mathrm{DC}=\mathrm{EC}$.


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6. The given figure shows a parallelogram ABCD. Squares ABPQ and ADRS are drawn on sides $A B$ and $A D$ of the parallelogram $A B C D$. Prove that :
(i) $\angle S A Q=\angle A B C$
(ii) $\mathrm{SQ}=\mathrm{AC}$


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7. In the given figure, $A B C D$ and $A B E F$ are parallelograms. If $O$ is the midpoint of $B C$, show that: $D C=C F=F E$.


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8. In the given figure, $A B C D$ is a square. $M$ is the mid-point of $A B$ and $P Q$ is perpendicular to CM . CB produced meets PQ at point Q . Prove that :
(i) $P A=B Q$
(ii) $\mathrm{CP}=\mathrm{AB}+\mathrm{PA}$


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## 3 Marks Questions

1. The perpendicular bisectors of the sides of a triangle $A B C$ meet at $I$.

Prove that : $I A=I B=I C$.
2. If AP bisects angle BAC and $M$ is any point on AP, prove that the perpendiculars drawn from $M$ to $A B$ and $A C$ are equal.

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3. In the following figure, $B L=C M$


Prove that AD is a Median of triangle ABC

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4. In the figure, given below, triangle ABC is right-angled at B. ABPQ and

ACRS are squares.
Prove that:
$\triangle A C Q$ and $\triangle A S B$ are congruent


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5. In the figure, given below, triangle $A B C$ is right-angled at $B$. $A B P Q$ and ACRS are squares.

Prove that:

$$
C Q=B S
$$



[^0]6. $A B C D$ is a parallelogram. The sides $A B$ and $A D$ are produced to $E$ and $F$ respectively, such that $A B=B E$ and $A D=D F$. Prove that : $\triangle B E C \cong \triangle D C F$.

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7. $P Q R S$ is a parallelogram. $L$ and $M$ are points on $P Q$ and $S R$ respectively such that PL = MR. Show that LM and QS bisect each other.

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8. In the following figure, ABC is an equilateral triangle in which QP is parallel to $A C$. Side $A C$ is produced upto point $R$ so that $C R=B P$.


Prove that QR bisects PC.

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9. In $\triangle A B C, A B=A C$ and the bisectors of angles B and C intersect at point O. Prove that
$B O=O C$

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10. In $\triangle A B C, \mathrm{AB}=\mathrm{AC}$ and the bisectors of angles B and C intersect at point O. Prove that:
(i) $\mathrm{BO}=\mathrm{CO}$
(ii) AO bisects angle BAC.

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11. In the following, $\mathrm{AB}=\mathrm{EF}, \mathrm{BC}=\mathrm{De}$ and $\angle E=90^{\circ}$


Prove that $A D=F C$

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1. In a triangle $A B C, D$ is mid-point of $B C, A D$ is produced upto $E$ so that $D E$ = AD. Prove that:
(i) $\triangle A B D$ and $\triangle E C D$ are congruent.
(ii) $\mathrm{AB}=\mathrm{EC}$
(iii) $A B$ is parallel to $E C$.

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2. In a triangle $A B C, D$ is the mid - point of $B C, A D$ is produced upto $E$ so that $D E=A D$.

Prove that:
$A B=E C$

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3. In a triangle $A B C, D$ is mid-point of $B C, A D$ is produced upto $E$ so that $D E$
= AD. Prove that :
(i) $\triangle A B D$ and $\triangle E C D$ are congruent.
(ii) $\mathrm{AB}=\mathrm{EC}$
(iii) $A B$ is parallel to $E C$.

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4. From the given diagram, in which $A B C D$ is a Parallelogram, $A B L$ is a line segment and $E$ is a mid - point of $B C$.

Prove that :
$\triangle D C E \cong \triangle L B E$


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5. From the given diagram, in which $A B C D$ is a Parallelogram, $A B L$ is a line segment and E is a mid - point of BC .

## Prove that :

$A B=B L$


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6. From the given diagram, in which $A B C D$ is a Parallelogram, $A B L$ is a line segment and $E$ is a mid - point of $B C$.

Prove that :
$A L=2 D C$


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7. In the given figure, $A B=D B$ and $A C=D C$. If $\angle A B D=58^{\circ}, \angle D B C=(2 x-4)^{\circ}, \angle A C B=y+15^{\circ} \quad$ and $\angle D C B=63^{\circ}$, Find the value of x and y .


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8. In the following figure, $A B=A C$ and $A D$ is perpendicular to $B C$. $B E$ bisects angle $B$ and $E F$ is perpendicular to $A B$.

## Prove that : ED=EF



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9. In the following figure, $A B=A C$ and $A D$ is perpendicular to $B C$. $B E$ bisects angle $B$ and $E F$ is perpendicular to $A B$.

Prove that :

$E D=E F$

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10. On the sides $A B$ and $A C$ of triangle $A B C$, equilateral triangles $A B D$ and ACE are drawn. Prove that :
$\angle C A D=\angle B A E$

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11. On the sides $A B$ and $A C$ of triangle $A B C$, equilateral triangles $A B D$ and ACE are drawn. Prove that :
(i) $\angle C A D=\angle B A E$
(ii) $C D=B E$

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12. In the adjoining figure, $O X$ and $R X$ are the bisectors of the angle $Q$ and R respectively of the triangle PQR . If $X S \perp Q R$ and $X T \perp P Q$.


Prove that:
$\Delta X T Q \cong \triangle X S Q$

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13. In the adjoining figure, $O X$ and $R X$ are the bisectors of the angle $Q$ and R respectively of the triangle PQR . If $X S \perp Q R$ and $X T \perp P Q$.


Prove that :

PX bisects angle P.

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14. In the following figure, $O A=O C$ and $A B=B C$.


Prove that :
$\angle A O B=90^{\circ}$

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15. In the following figure, $O A=O C$ and $A B=B C$.


Prove that :
$\triangle A O D \cong \triangle C O D$

## - Watch Video Solution

16. In the following figure, $O A=O C$ and $A B=B C$.


Prove that :
$A D=C D$

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17. The following figure shows a triangle $A B C$ in which $A B=A C . M$ is a point on $A B$ and $N$ is a point on $A C$ such that $B M=C N$. Prove that

$A M=A N$

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18. The following figure shows a triangle $A B C$ in which $A B=A C . M$ is a point on $A B$ and $N$ is a point on $A C$ such that $B M=C N$. Prove that

$\Delta A M C \cong \triangle A N B$

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19. The following figure shows a triangle $A B C$ in which $A B=A C . M$ is a point on $A B$ and $N$ is a point on $A C$ such that $B M=C N$. Prove that

$B N=C M$

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20. The following figure shows a triangle $A B C$ in which $A B=A C . M$ is a point on $A B$ and $N$ is a point on $A C$ such that $B M=C N$. Prove that
$\Delta B M C \cong \triangle C N B$

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21. In the given diagram ABCD is a parallelogram. $\triangle A P D$ and $\triangle B Q C$ are equilateral triangles.


Prove that:
$\angle P A B=\angle Q C D$
22. In the given diagram ABCD is a parallelogram. $\triangle A P D$ and $\triangle B Q C$ are equilateral triangles.


Prove that :
$P B=Q D$

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23. In the given figure $A B C$ is a triangle and $D$ is the mid-point of $B C$. $A D$ is produced to E . BM and CN are two perpendiculars dropped from B and C respectively on AE .


Prove that :
$\Delta B M D \cong \triangle C N D$

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24. In the given figure $A B C$ is a triangle and $D$ is the mid-point of $B C$. $A D$ is produced to E . BM and CN are two perpendiculars dropped from B and C respectively on AE .


Prove that:
$B M=C N$

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