## ©゙"doubtnut India's Number 1 Education App

## MATHS

## BOOKS - HT Olympiad Previous Year Paper

## IMO QUESTION PAPER 2016 SET B

## Mathematical Reasoning

1. Directions (Questions 508 to 509): These questions are based on the following information: 85 children went to an amusement park where they could ride on merry-go-round, roller coaster and Ferris wheel. It was known that 20 of them took all the three rides and 55 of them have taken at least two of the three rides. Each ride costs Re 1, and the total receipt of
the amusement park was Rs 145 . How many children took exactly one ride? (a) 5 (b) 10 (c) 15 (d) 20
A. 10
B. 20
C. 25
D. 15

## Answer: A

## - Watch Video Solution

2. If $\mathrm{x}, \mathrm{y}$ are rational numbers and $\frac{5+\sqrt{11}}{3-2 \sqrt{11}}=x+y \sqrt{11}$.

The values of $x$ and $y$ are

$$
\text { A. } \frac{37}{35}, \frac{-13}{35}
$$

B. $\frac{37}{35}, \frac{13}{35}$
C. $\frac{-37}{35}, \frac{-13}{35}$
D. $\frac{-37}{35}, \frac{13}{35}$

## Answer: C

## D Watch Video Solution

3. For a group of 32 students food lasts for 45 days. For how many days will the same food last for 72 students ?
A. 13
B. 40
C. 20
D. 6

## - Watch Video Solution

4. Which of the following can be the coordinates of $R$, if $P R=Q R$
?

A. $(1,-1)$
B. $(2,-2)$
C. $(2,3)$
D. $(3,3)$

## Answer: C

## - Watch Video Solution

5. Which of the following steps is INCORRECT while constructing a quadrilateral $A B C D$, given that $A B=5 \mathrm{~cm}, B C=7 \mathrm{~cm}, A D=4 \mathrm{~cm}$, diagonal $A C=9 \mathrm{~cm}$ and diagonal $B D=6 \mathrm{~cm}$.
6. Draw $\mathrm{AB}=5 \mathrm{~cm}$
7. With $A$ and $B$ as centres and 4 cm and 6 cm as radii
respectively ,draw arcs to cut each other at D.
8. Join $A D$ and $B C$. With $A$ and $B$ as centres and 9 cm and 7 cm as radii, respectively, draw arcs to cut each other at $C$.
9. Join $A C$ and $B C$. Also join $D C . A B C D$ is the required quadrilateral.
A. Only 1
B. Both 2 and 3
C. Only 3
D. Both 2 and 4

Answer: C

- View Text Solution

6. In the figure given below PQRS is a trapezium . AB is parallel to PQ and cuts PR at O . If $\angle P S R=90^{\circ}, \angle A B R=110^{\circ}$ and $\angle Q P R=40^{\circ}$, find
(i) $\angle P R Q$
(ii) $\angle A O R$
(iii) $\angle O P A$

$\begin{array}{lll}\text { A. } & i & i i \\ 30^{\circ} & 110^{\circ} & \text { iii } \\ 50^{\circ}\end{array}$
B. $\begin{array}{lll}i & i i & i i i \\ 15^{\circ} & 120^{\circ} & 45^{\circ}\end{array}$
C. $\begin{array}{lll}i & i i & i i i \\ 15^{\circ} & 140^{\circ} & 45^{\circ}\end{array}$
D. $\begin{array}{lll}i & i i & i i i \\ 30^{\circ} & 140^{\circ} & 50^{\circ}\end{array}$

Answer: D

## - Watch Video Solution

7. In $\triangle A B C$ it is given that D is the midpoint of $\mathrm{BC}, \mathrm{E}$ is the midpoint of $B D$ and $O$ is the midpoint of $A E$. Then, find ar $(\triangle B O E)$.

A. $\frac{1}{3} \operatorname{ar}(\triangle A B C)$
B. $\frac{1}{4} \operatorname{ar}(\triangle A B C)$
C. $\frac{1}{6} \operatorname{ar}(\triangle A B C)$
D. $\frac{1}{8} \operatorname{ar}(\triangle A B C)$

## Answer: D

## - Watch Video Solution

8. The factors $8(a-2 b)^{2}-2 a+4 b-1=$ are
A. $(2 a-4 b-1)(4 a-8 b+1)$
B. $(2 a+4 b+1)(4 a-8 b+1)$
C. $(2 a-4 b-1)(4 a-8 b-1)$
D. $(2 a+4 b-1)(4 a+8 b+1)$

## - Watch Video Solution

9. If the point $(3,4)$ lies on the graph of the equation $3 y-a x-7$
$=0$ find the value of a
A. $\frac{2}{3}$
B. 1
C. $\frac{4}{3}$
D. $\frac{5}{3}$

## Answer: D

10. ( Number of students (in thousands) who opted for three different specializations durning the five years in a University )


The total number of students who opted for English in the
years 2012 and 2015 together are approximately what per cent of the total number of students who opted for all three subjects in the same years?
A. 38
B. 28
C. 42
D. 46

## - Watch Video Solution

11. ( Number of students (in thousands) who opted for three different specializations durning the five years in a University )


What is the respective ratio between the number of students
who opted for Mathematics in the years 2012 and 2016 together and the number of students who opted for Hindi in the years 2013 and 2015 together?
A. $2: 3$
B. 12: 7
C. 11: 7
D. $12: 5$

## Answer: A

## ( Watch Video Solution

12. In the given figures, $\triangle A B C$ is an equilateral triangle the length of whose side is equal to 10 cm , and $\triangle D B C$ right angled at D and $\mathrm{BD}=8 \mathrm{~cm}$. Find the area of the shaded region
$[$ Take, $\sqrt{3}=1.732$.

A. $19.3 \mathrm{~cm}^{2}$
B. $43.3 \mathrm{~cm}^{2}$
C. $17.3 \mathrm{~cm}^{2}$
D. $21.3 \mathrm{~cm}^{2}$

Answer: A
13. Given below are the marks scored by a group of 90 students in a Mathematics test of 100 marks.

| Marks | $0-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of students | 7 | 10 | 10 | 20 | 20 | 15 | 8 |

Find the probability that a student obtained :
(i) less than $20 \%$ marks.
(ii) 60 or more marks .
$i$
$i \quad i i$
A.
$17 / 90 \quad 43 / 90$
B. $\begin{array}{ll}i & i i \\ 7 / 90 & 43 / 90\end{array}$
C. $\begin{array}{ll}i & i i \\ 7 / 90 & 23 / 90\end{array}$
D. $\begin{array}{ll}i & i i \\ 17 / 90 & 23 / 90\end{array}$

## Answer: C

## - Watch Video Solution

14. $A B C D$ is a cyclic quadrilateral such that $A B$ is a diameter of the circle circumscribing it and $\angle A D C=140^{\circ}$, then $\angle B A C$ is equal to
A. $80^{\circ}$
B. $50^{\circ}$
C. $40^{\circ}$
D. $30^{\circ}$

## Answer: B

15. A, B, C are three sets of values of $x$ given below. A: $2,3,7,1,3,2,3$

B: $7,5,9,12,5,3,8$
C : $4,4,11,7,2,3,4$

Which one of the following options is correct ?
A. Mean of $A=$ Mode of $C$
B. Mean of $C=$ Median of $B$
C. Median of $B=$ Mode of $A$
D. Mean, Median and Mode of A are equal .

## Answer: D

16. In the adjoining
figure

$$
\angle C A B=62^{\circ}, \angle C B A=76^{\circ} \angle A D E=58^{\circ} \text { and } \angle D F G=66^{\circ}
$$



Find $\angle F G E$ :
A. $44^{\circ}$
B. $34^{\circ}$
C. $36^{\circ}$
D. None of these

## - Watch Video Solution

17. Using Euler's formula find the values of $P, Q, R$ and $S$ respectively .

| Faces | 6 | 5 | 20 | 14 |
| :--- | :---: | :---: | :---: | :---: |
| Vertices | P | Q | 36 | R |
| Edges | 12 | 9 | S | 36 |

A. $8,6,24,54$
B. $6,8,54,24$
C. $6,8,24,54$
D. $8,6,54,24$

## Answer: A

18. It is given that $\triangle A B C \cong \triangle F D E$ and $\mathrm{AB}=5 \mathrm{~cm}$, $\angle B=40^{\circ}$ and $\angle A 80^{\circ}$ then which of the following is true?
A. $D F=5 \mathrm{~cm}, \angle F=60^{\circ}$
B. $D F=5 \mathrm{~cm}, \angle E=60^{\circ}$
C. $D E=5 \mathrm{~cm}, \angle E=60^{\circ}$
D. $D E=5 \mathrm{~cm}, \angle D=60^{\circ}$

## Answer: B

## - Watch Video Solution

19. The length and bredth of a hall are in the ratio $4: 3$ and its height is 5.5 metres. The cost of decorating its walls (including doors and windows) at $R s .6 .60$ per squaremetre is $R s .5082$. Find the length and breadth of the room.
A. $13 \mathrm{~m}, 7 \mathrm{~m}$
B. $45 \mathrm{~m}, 37 \mathrm{~m}$
C. $40 \mathrm{~m}, 30 \mathrm{~m}$
D. $50 \mathrm{~m}, 50 \mathrm{~m}$

## Answer: C

## - Watch Video Solution

20. Based on Playfair's axiom, for every line I and every point $P$ not lying on I, there exists $\qquad$ line (s) passing through $P$ and parallel to I.
A. Two distinct
B. A unique
C. Three distinct
D. None of these

## Answer: B

## - Watch Video Solution

## Everyday Mathematics

1. Saif purchased 20 dozens of toys at the rate of Rs. 375 per dozen. He sold each one at the rate of Rs. 33 . What was his percentage profit??
A. $3.5 \%$
B. $4.5 \%$
C. $5.6 \%$
D. $6.5 \%$

## Answer: C

## - Watch Video Solution

2. Water flows through a cylindrical pipe of diameter 5 mm at the rate of 10 m per minute and falls into a conical vessel having 40 cm as the diameter of its base and 24 cm as its height. How long will it take to fill the vessel ?
A. 48 mins 15 secs
B. 51 mins 2 secs
C. 52 mins 1 sec
D. 51 mins 12 secs

## D Watch Video Solution

3. A man take a 5 hours 45 mins in walking to a certain place and riding back. He would have gained 2 hours by riding both ways . The time he would take to walk both ways, is $\qquad$ .
A. 3 hrs 45 mins
B. 7 hrs 30 mins
C. 7 hrs 45 mins
D. 11 hrs 45 mins

## Answer: C

4. From the salary of an officer, $10 \%$ is deducted as house rent, $15 \%$ of the rest he spends on children's education and $10 \%$ of the balance, he spends on clothes. After this expenditure he is left with Rs. 1,377 . His salary is
A. Rs. 2000
B. Rs. 2040
C. Rs. 2100
D. Rs 2200

## Answer: A

## (D) Watch Video Solution

5. A man borrows 12,500 at $20 \%$ compound interest. At the end of every year he pays 2000 as part repayment. How much does he still owe after three such instalments?
A. Rs. 12,000
B. Rs. 12,864
C. Rs. 15,600
D. None of these

## Answer: D

## (D) Watch Video Solution

6. 10 women can complete a work in 7 days and 10 children take 14 days to complete the same work. How many days will 5
women and 10 children take to complete the same work ?
A. 3
B. 5
C. 7
D. Cannot be determined

## Answer: C

## - Watch Video Solution

7. Four different electronic devices make a beep after every 30 minutes, 1 hour, $1 \frac{1}{2}$ hour and 1 hour 45 minutes respectively.

All the devices beeped together at 12 noon. They will again beep together at:
A. 12 midnight
B. 3 a.m.
C. 6 a.m.
D. 9 a.m.

## Answer: D

## - Watch Video Solution

8. If the price of eraser is reduced by $25 \%$ a person can buy 2 more erasers for a rupee. How many erasers are available for a rupee?
A. 8
B. 6
C. 4
D. 2

## Answer: B

## - Watch Video Solution

9. The income of $A B$ and $C$ are in the ratio 7:9:12 and their spendings are in the ratio $8: 9: 15$. If A saves $\frac{1}{4}$ th of his income, then the savings of $A, B$ and $C$ are in the ratio of:
A. $56: 99: 69$
B. 99:56: 69
C. 69:56:99
D. 99: 69:56

## - Watch Video Solution

10. A tradesman gives $4 \%$ discount on the marked price and gives 1 article free for buying every 15 articles and thus gains $35 \%$. The marked price is increased above the cost price by
A. $20 \%$
B. $39 \%$
C. $40 \%$
D. $50 \%$

## Answer: D

## Achievers Section

1. Length of a mathematics lab is $1 \frac{1}{3}$ of its breadth and its height is $\frac{1}{2}$ of its length. The cost of whitewashing the walls at the rate of Rs. 2.60 per $m^{2}$ is Rs. 291.20 . Find the cost of tiling the floor at the rate of Rs. 6.75 per $m^{2}$.
A. Rs. 324
B. Rs. 624
C. Rs. 570
D. Rs. 420

## Answer: A

## Column I

## Column II

(a) Angle bisectors of a (p) Parallelogram parallelogram form a
$\qquad$ _.
(b) The quadrilateral formed (q) Rectangle by joining the mid-points of the pairs of adjacent sides of a square is a
$\qquad$ _.
(c) The quadrilateral formed (r) Square by joining the mid-points of the pairs of adjacent sides of a rectangle is a
$\qquad$ -
(d) The figure formed by (s) Rhombus joining the mid-points of the pairs of adjacent sides of a quadrilateral is a $\qquad$ .
2.
$\begin{array}{llll}a & b & c & d\end{array}$
A.
$r \quad q \quad s \quad p$
B.
$q \quad r \quad p \quad s$
$\begin{array}{llll}a & b & c & d\end{array}$
$q \quad r \quad s \quad p$
D. $\begin{array}{llll}a & b & c & d \\ s & r & q & p\end{array}$
3. State True or False and select the correct option .
P. In a $\triangle A B C$ in which $\mathrm{AB}=\mathrm{AC}$, the altitude AD bisects BC .
Q. The sum of any two sides of a triangle is greater than twice the median drawn to the third side .
$R$. If $D$ is the mid-point of the hypotenuse $A C$ of a right $\Delta A B C$, then $\mathrm{BD}=\mathrm{AC}$.
S. Perimeter of a triangle is equal to the sum of its three medians.
T. If the altitudes $\mathrm{AD}, \mathrm{BE}$ and CF of $\triangle A B C$ are equal, then $\triangle A B C$ is equilateral .
$\begin{array}{lllll}P & Q & R & S & T \\ \text { A. } & \begin{array}{ll}\text { True } & \text { True }\end{array} & \text { False } & \text { False } & \text { True }\end{array}$
${ }_{B} \begin{array}{lllll}P & Q & R & S & T\end{array}$
True False True False True
c. $\begin{array}{lllll}P & Q & R & S & T\end{array}$
False True False True True
${ }_{\mathrm{D}}{ }^{P}$

## Answer: A

## - Watch Video Solution

4. Fill in the blanks and select the correct option .
(I) There is (are) __P__ circle (s) passing through three noncollinear points .
(II) A continuous piece of a circle is called the __Q__ of the circle .
(III) If two arcs of a circle are congruent then their corresponding chords are __R_.
(IV) A line segment joining the centre to any point on the circle is called its __S_.
(V) The sum of either pair of opposite angles of a cyclic quadrilateral is __ ${ }^{\top}$._
$\begin{array}{lllll}P & Q & R & S & T \\ \text { Anfinite } & \text { Chord } & \text { Not equal } & \text { Diameter } & 360^{\circ}\end{array}$
B. $\begin{array}{lllll}P & Q & R & S & T \\ \text { Two } & \text { Arc } & \text { Equal } & \text { Diameter } & 360^{\circ}\end{array}$
C. $\begin{array}{lllll}P & Q & R & S & T \\ \text { One } & \text { Chord } & \text { Equal } & \text { Radius } & 180^{\circ}\end{array}$
D. $\begin{array}{lllll}P & Q & R & S & T \\ \text { One } & \text { Arc } & \text { Equal } & \text { Radius } & 180^{\circ}\end{array}$

## Answer: D

## - Watch Video Solution

5. Given below is a question followed by three statements. You have to study the question and the ststements and decide which of the statement is/are necessary to answer the question.

What is Arun's present age ?
I. Five years ago, Arun's age was double that of his son's age at that time .
II. Present ages of Arun and his son are in the ratio of $11: 6$ respectively .
III. Five years hence, the respective ratio of Arun's age and his son's age will become 12:7.
A. Only I and II
B. Only II and III
C. Only I and III
D. Any two of the three

## Answer: D

