# ©゙doubtnut 

## MATHS

# BOOKS - HT Olympiad Previous Year Paper 

## SURFACE AREAS AND VOLUMES

## Mathematical Reasoning

1. If the height of a cylinder is doubled, by what
number must the radius of the base be multiplied
so that the resulting cylinder has the same
volume as the original cylinder? 4 (b) $\frac{1}{\sqrt{2}}$ (c) 2 (d)
$\frac{1}{2}$
A. 4
B. $\frac{1}{\sqrt{2}}$
C. 2
D. $\frac{1}{2}$

Answer: B

- Watch Video Solution

2. An aluminium sheet 27 cm long, 8 cm broad and

1 cm thick is melted into a cube. The difference in
the surface areas of the two solids would be (a)

Nil (b) 284 cm 2 (c) 286 cm 2 (d) 296 cm 2
A. $280 \mathrm{~cm}^{2}$
B. $284 \mathrm{~cm}^{2}$
C. $296 \mathrm{~cm}^{2}$
D. $286 \mathrm{~cm}^{2}$

Answer: D

D Watch Video Solution
3. If the height of a cone is equal to its base diameter, then its slant height is
A. $\sqrt{2 r^{2}+h^{2}}$
B. $r \sqrt{5}$
C. $h \sqrt{5}$
D. $r h \sqrt{5}$

Answer: B

- Watch Video Solution

4. The length of the longest rod that can be placed in a room of dimensions
$(10 m \times 10 m \times 5 m)$ is
A. 16 m
B. 10 m
C. 15 m
D. 12 m

Answer: C

- Watch Video Solution

5. A hollow cylindrical pipe is 28 dm long. Its outer
and inner diameters are 12 cm and 8 cm
respectively. Find the volume of the copper used in making the pipe.
A. $17600 \mathrm{~cm}^{3}$
B. $17000 \mathrm{~cm}^{3}$
C. $16600 \mathrm{~cm}^{3}$
D. $16000 \mathrm{~cm}^{3}$

## Answer: A

6. The volume of a cylinder of radius $r$ is $\frac{1}{4}$ of the volume of a rectangular box with a square base of side length $x$. If the cylinder and the box have equal heights, what is $r$ in terms of $x ? \frac{x^{2}}{2 \pi}$ (b)
$\frac{x}{2 \sqrt{\pi}}$ (c) $\frac{\sqrt{2 x}}{\pi}$ (d) $\frac{\pi}{2 \sqrt{x}}$
A. $\frac{x^{2}}{2 \pi}$
B. $\frac{x}{2 \sqrt{x}}$
C. $\frac{\sqrt{2 x}}{\pi}$
D. $\frac{x}{\sqrt{\pi}}$

Answer: B
7. The edge of a cube is 20 cm . How many small cubes of edge 5 cm can be formed from this cube?
A. 4
B. 32
C. 64
D. 100

Answer: C

D Watch Video Solution
8. The volume of two spheres are in the ratio 216 :
125. The difference of their surface areas, if the sum of their radii is 11 units, is
A. $38 \pi$ sq. units
B. $45 \pi$ sq. units
C. $50 \pi$ sq. units
D. $44 \pi$ sq. units

## Answer: D

## - Watch Video Solution

9. The radii of two cylinders are in the ratio 3:4
and their heights are in the ratio 6: 5. The ratio of
their curved surface areas is
A. $5: 4$
B. 3: 4
C. 9:10
D. $4: 5$

## Answer: C

- Watch Video Solution

Everyday Mathematics

1. An open rectangular box has the external measures as $98 \mathrm{~cm}, 84 \mathrm{~cm}, 77 \mathrm{~cm}$ and the thickness of wood is 2 cm . Then the volume of the wood is $\qquad$
A. $70000 \mathrm{cu} . \mathrm{cm}$
B. $64865 \mathrm{cu} . \mathrm{cm}$
C. $60000 \mathrm{cu} . \mathrm{cm}$
D. $84904 \mathrm{cu} . \mathrm{cm}$
2. A spherical ball of radius 3 cm is melted and recast into three spherical balls. The radii of two of these balls are 1.5 cm and 2 cm . The radius of the third ball is
A. 2.66 cm
B. 2.5 cm
C. 3 cm
D. 3.5 cm

Answer: B

## Watch Video Solution

3. How many metres of cloth 5 m wide will be required to make a conical tent, the radius of whose base is 7 m and whose height is 24 m ?

$$
\left(\text { Take } \pi=\frac{22}{7}\right)
$$

A. 550 m
B. 168 m
C. 110 m
D. 33.6 m

## Answer: C

## Watch Video Solution

4. Water flows in a tank $150 m x 100 m$ at the base,
through a pipe whose cross-section is
$2 d m$ by $1.5 d m$ at the speed f 15 km per hour. In what time, will the water be 3 metres deep?
A. 50 hours
B. 150 hours
C. 100 hours
D. 200 hours

## Answer: C

## - Watch Video Solution

5. A hemispherical dome of a building needs to be painted from outside. If the circumference of the base of the dome is 17.6 m , then find the cost of painting it at the rate of Rs. 8 per $100 \mathrm{~cm}^{2}$
A. Rs. 35680
B. Rs. 28650
C. Rs. 39424
D. None of these

## Answer: C

## - Watch Video Solution

6. A circus tent is cylindrical to a height of 3 metres and conical above it. If its diameter is 105
m and the slant height of the conical portion is 53
m , calculate the length of the canvas 5 m wide to
make the required tent.

# A. 1996 m 

B. 2096 m
C. 1947 m
D. 1800 m

## Answer: C

## Watch Video Solution

## 7. A school provides milk to the studenst daily in a

 cylinder glasses of diameter 7 cm . If the glass isfilled with milk upto an height of 12 cm , find how
many liters of milk is needed to server 1600 students.
A. 739.2 litres
B. 538 litres
C. 742 litres
D. 400 litres

Answer: A
8. A small village having a population of 5000 , requires 75 L of water per head per day. The
village has got an overhead tank of measurement
$40 m \times 25 m \times 15 m$.For how days will the water of this tank last?
A. 30 days
B. 32 days
C. 40 days
D. 45 days

## Achievers Section Hots

1. Read the following statements carefully and write 'T' for true and 'F' for false.
(i) Volume of a cylinder is three times the volume of a cone on the same base and of same height
(ii) Volume of biggest sphere in cube of edge 6 cm is $30 \pi \pi \mathrm{~cm}^{3}$
(iii) Total surface area of a cone of radius $r$ and stant height r is $\pi r l+\pi r^{2}$
(i) (ii) (iii)
A.
T
F T
(i) (ii) (iii)
$\mathrm{T} \quad \mathrm{T} \quad \mathrm{T}$
$\begin{array}{cccc}\text { C. } & \text { (i) } & \text { (ii) } & \text { (iii) } \\ \mathrm{F} & \mathrm{T} & \mathrm{F}\end{array}$
D. $\begin{array}{ccc}\text { (i) } & \text { (ii) } & \text { (iii) } \\ \mathrm{F} & \mathrm{T} & \mathrm{T}\end{array}$

Answer: B

Watch Video Solution

## 2. Match the following

## Column-I

$(P)$ A cylinder of radius 3 cm is inscribed in
a sphere of radius
5 cm , then volume of cylinder is $\qquad$
(Q) A conical tent of base diameter 24 cm is 10 cm in height, the slant height of tent is $\qquad$ .
(R) If the length of a diagonal of a cube is $6 \sqrt{3} \mathrm{~cm}$, then its volume is $\qquad$
(S) The volume of a conical vessel with height 12 cm and slant height 13 cm is $\qquad$
A.

$$
(P) \rightarrow(2),(Q) \rightarrow(3),(R) \rightarrow(4),(S) \rightarrow(1)
$$

B.

$$
(P) \rightarrow(1),(Q) \rightarrow(3),(R) \rightarrow(2),(S) \rightarrow(4)
$$

C.

$$
(P) \rightarrow(3),(Q) \rightarrow(1),(R) \rightarrow(2),(S) \rightarrow(4)
$$

D.

$$
\begin{equation*}
(P) \rightarrow(4),(Q) \rightarrow(1),(R) \rightarrow(3),(S) \rightarrow \tag{2}
\end{equation*}
$$

## Answer: C

## D Watch Video Solution

3. Study the following statements carefully and select the correct option.

Statement-1 : If diameter of a sphere is decreased
by $25 \%$, then its curved surface area is decreased by $43.75 \%$.

Statement-il : Curved surface area is increased when diameter decreases.
A. Both Statement-I and Statement-II are true.
B. Statement-I is true but Statement-II is false.
C. Statement-I is false but Statement-II is true.
D. Both Statement-I and Statement- II are false.

Answer: B

