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## MATHS

## BOOKS - SWAN PUBLICATION

## TRIANGLES

Exercise 71

1. In quadrilateral $A B C D, A C=A D$ and $A B$ bisect
$\angle A$ show that $\triangle A B C \approx \triangle A B D$. What can
you say about BC and BD ?


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2. $A B C D$ is a quadrilateral in which $A D$
$=B C$ and $\angle D A B=\angle C B A$ Prove that

$\triangle A B D \approx \triangle B A C$

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3. $A B C D$ is a quadrilateral in which $A D$
$=B C$ and $\angle D A B=\angle C B A$ Prove that

$B D=A C$

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4. $A B C D$ is a quadrilateral in which $A D$
$=B C$ and $\angle D A B=\angle C B A=$ Prove that

$\angle A B D=\angle B A C$

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5. $A D$ and $B C$ are equal perpendicular to a line segment $A B$. Show that $C D$ bisects $A B$


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6. I and m are two parallel lines intersected by
another pair of parallel lines p and q Show
that $\triangle A B C \approx \triangle C D A$.


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7. What is the value of $\sin a$.


D Watch Video Solution
8. Line I is the bisector of an angle $\angle A$ and B is
any point on $I . B P$ and $B Q$ are perpendiculars
from B to the arms of $\angle A$ show that:
$\triangle A P B \equiv \triangle A Q B$


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9. 

$A C=A E, A B=A D$ and $\angle B A D=\angle E A C$.
show that $B C=D E$.


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10. $A B$ is a line segment and $P$ is its midpoint. $D$
and $E$ are points on the same side of $A B$ such
that $\angle B A D=\angle A B E$ and $\angle E P A=\angle D P B$
. Show that $\Delta D A P \cong \Delta E B P$.

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11. $A B$ is a line segment and $P$ is its midpoint. $D$
and $E$ are points on the same side of $A B$ such
that $\angle B A D=\angle A B E$ and $\angle E P A=\angle D P B$
. Show that $A D=B E$.


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12. In right triangle $A B C$, right angled at $C, M$ is
the mid-point of hypotenuse $A B . C$ is joined to
$M$ and produced to a point $D$ such that $D M=$
CM. Point D is joined to point B (See Fig.

) Show
that : $\triangle A M C \cong \triangle B M D$.

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13. In right triangle $A B C$, right angled at $C, M$ is
the mid-point of hypotenuse $A B . C$ is joined to
$M$ and produced to a point $D$ such that $D M=$

## CM. Point D is joined to point B (See Fig.)



Show that: $C M=\frac{1}{2} A B$.

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14. In right triangle $A B C$, right angled at $C, M$ is
the mid point of hypotenuse $A B . C$ is joined to
$M$ and produced to a point $D$ such that
$D M=C M$. point $D$ is joined to point $B$. show that

$\triangle D B C \equiv \triangle A C B$

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15. In right triangle $A B C$, right angled at $C, M$ is
the mid-point of hypotenuse $A B . C$ is joined to $M$ and produced to a point $D$ such that $D M=$
CM. Point D is joined to point B (See Fig.)


Show that : $C M=\frac{1}{2} A B$.

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Exercise 72

1. In an isosclees triangle $A B C$, with $A B=A C$,
the bisectors of $\angle B$ and $\angle C$ intersect each other at O . Join A to O show that: $\mathrm{OB}=\mathrm{OC}$.

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2. In an isosclees triangle $A B C$, with $A B=A C$,
the bisectors of $\angle B$ and $\angle C$ intersect each other at O . Join A to O show that : AO bisects
$\angle A$.
3. In $\triangle A B C, \mathrm{AD}$ is the perpendicular bisector of BC . Show that $\triangle A B C$ is an isosceles triangle in which $A B=A C$


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4. $A B C$ is an isosceles triangle in which altitudes BE and CF are drawn to sides AC and $A B$ respectively (See Fig.

). Show
that these altitudes are equal.
5. $A B C$ is a triangle in which altitudes $B E$ and

CF to sides AC and AB are equal Show that

$\triangle A B E \approx \triangle A C F$

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6. $A B C$ is a triangle in which altitudes $B E$ and
$C F$ to sides $A C$ and $A B$ are equal Show that

$A B=A C$, i.e., ABC is an isosceles

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# 7. ABC and DBC are two isosceles trianges on 

the same base BC Show that
$\angle A B D=\angle A C D$.


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8. $\triangle A B C$ is an isoscelestriangle in which $\mathrm{AB}=$
$A C$. Side $B A$ is produced to $D$ such that $A D=A B$.
Show that $\angle B C D$ is a right angle (see Fig.

).

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9. $A B C$ is a right angled triange in which
$\angle A=90^{\circ}$ and $A B=A C$.
Find
$\angle B$ and $\angle C$.


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10. Show that the angles of an equilateral triangle are $60^{\circ}$ each.

11. $\triangle A B C$ and $\triangle D B C$ are two isosceles
triangles on the same base $B C$ and vertices $A$ and $D$ are on the same side of BC (See Fig. 1UHI.

).If $A D$ is
extended to intersect $B C$ at $P$, show that
$\triangle A B D \cong \triangle A C D$.
12. $\triangle A B C$ and $\triangle D B C$ are two isosceles triangles on the same base BC and vertices $A$ and $D$ are on the same side of BC (See Fig. IUII.

).If $A D$ is
extended to intersect $B C$ at $P$, show that $\triangle A B D \cong \triangle A C D$.

D Watch Video Solution
3. $\triangle A B C$ and $\triangle D B C$ are two isosceles triangles on the same base $B C$ and vertices $A$ and $D$ are on the same side of BC (See Fig.

extended to intersect $B C$ at $P$, show that $A P$ bisects $\angle A$ as well as $\angle D$.

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4. $\triangle A B C$ and $\triangle D B C$ are two isosceles
triangles on the same base $B C$ and vertices $A$
and $D$ are on the same side of BC (See Fig.
nuli.

).If $A D$ is
extended to intersect $B C$ at $P$, show that
$\triangle A B D \cong \triangle A C D$.

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5. $A D$ is an altitude of an isosceles triangle $A B C$
in which $A B=A C$. Show that:- $A D$ bisects $B C$

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6. $A D$ is an altitude of an isosceles triangle $A B C$ in which $A B=A C$. Show that:- $A D$ bisects $B C$
7. Two sides $A B$ and $B C$ and median $A M$ of one
triangle $A B C$ are respectively equal to sides $P Q$
and QR and median PN of $\triangle P Q R$ (See Fig

). Show
that : $\triangle A B M \cong \triangle P Q N$.

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8. Two sides $A B$ and $B C$ and median $A M$ of one
triangle $A B C$ are respectively equal to sides $P Q$
and QR and median PN of $\triangle P Q R$ (See Fig

). Show
that : $\triangle A B M \cong \triangle P Q N$.

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9. BE and CF are two equal altitudes of a triangle $A B C$. Using RHS congruence rule, prove that the triangle $A B C$ is isosceles.


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10. $A B C$ is an isosceles triangle with $A C=B C$. If
$A B^{2}=2 A C^{2}$, prove that ABC is right triangle.

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## Exercise 74

1. Show that in a right angled triangle, the hypotenuse is the longest side.


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2. sides AB and AC of $A B C$ are extended to points $P$ and $Q$ respectively. Also
$\angle P B C<\angle Q C B$. Show that $A C>A B$.


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3. $\angle B<\angle A$ and $\angle C<\angle D$. Show that $A D<B C$.


- Watch Video Solution

4. $A B$ and $C D$ are respectively the smallest and
longest sides of a quadrilateral $A B C D$ (see Fig.
7.50). Show that $\angle A>\angle C$ and $\angle B>\angle D$.

5. In Fig 7.51, $\mathrm{PR}>\mathrm{PQ}$ and PS bisects $\angle Q P R$.

Prove that $\angle P S R>\angle P S Q$.

A. $\angle P S Q$
B.
C.
D.

## Answer:

## D Watch Video Solution

6. Show that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.

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Exercise 75

1. $A B C$ is a triangle. Locate a point in the interior of $\triangle A B C$ which is equidistant from all the vertices of $\triangle A B C$.

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2. In a triangle locate a point in its interior which is equidistant from all the sides of the triangle.

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3. In a huge park, people are concentrated at the points

A: where there are difference slides for children

B: near which a man-made lake is situated

C: which is near to a large parking and each
where should an icecream parlour be set up
that maximum number of persons can

## approach it

## - A

-c

D Watch Video Solution
4. Complete the hexagonal rangoli and the star Rangolies (see Figs.

filling them with as many equilateral triangles of side 1 cm as you can. Count the number of triangles in each case. Which has more triangles?

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## Objective Type Questions

1. State whether the statement are true (T) or false (F):

Zero is a rational number.

## - Watch Video Solution

2. If .... And the included angle of one triangle are equal to two sides and the included angle of the other triangle then two triangles are congruent.
3. State whether the statement are true (T) or false (F):

Zero is a rational number.

D Watch Video Solution
4. The sides opposite to two equal angles of a triangle are :

D Watch Video Solution
5. The sides opposite to two equal angles of a triangle are :

D Watch Video Solution
6. Two right triangles are congruent if hypotenuse and one side of first-triangle are respectively equal to the hypoteņuse and one corresponding side of the second triangle
7. The measure of each angle of an equilateral triangle is :

## - Watch Video Solution

8. State whether the statement are true (T) or false (F):

In a triangle side opposite to the larger (greater) angle is longer .
9. In a triangle, the angle opposite to the longer side is :

## D Watch Video Solution

10. Sum of any two sides of a triangle is greater than the third side.

## D Watch Video Solution

11. If three angles of one triangle are equal to corresponding three angles of an other
triangle then triangles are congruent.

## - Watch Video Solution

12. Fill in the blank

If in
two
triangles
$A B=Q R, \angle A=\angle Q, \angle B=\angle R$,
then
$\triangle A B C \approx$

D Watch Video Solution
13. If $M$ is the mid point of hypotenuse $A C$ of $r t$.
$\Delta A B C$ then $B M=\frac{1}{2} \ldots$.

- Watch Video Solution

14. If in two triangles $\triangle P Q R$ and $\triangle D E F$,
$Q R=D E, P Q=F D$,
then
$\triangle P Q R \equiv \ldots . . . . . . . . . . . . .$.

D Watch Video Solution
15. The sides opposite to two equal angles of a triangle are :

- Watch Video Solution

16. Fill in the blank

Each angle of an equilateral triangle is
( Watch Video Solution

## 17. Fill in the blank

In a triangle
ABC,
if
$B C=A B$ and $\angle C=80^{\circ}, \quad$ then $\angle B=$

## D Watch Video Solution

18. Fill in the blank

In a triangle PQR , if $\angle P=\angle R$ then $\mathrm{PQ}=$

## D Watch Video Solution

## 19. Fill in the blank

In a right triangle the hypotenuse is

Side.

- Watch Video Solution

20. If two sides of a triangle are unequal, then
the larger side has the ................ angle opposite
to it.

- Watch Video Solution

