



# MATHS

## BOOKS - PSEB

### QUADRILATERALS

#### Exercise

1. The angles of quadrilateral are in the ratio 3 : 5 : 9 : 13. Find all the angles of the quadrilateral.



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2. If the diagonals of a parallelogram are perpendicular, then it is a rhombus.



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3. If diagonals of a quadrilateral bisect each other at right angles, then it is a :



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4. Which of the following statements are True or False :

If the diagonals of a quadrilateral are equal and bisect each other at right angles then the quadrilateral is a square.



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5. Which of the following statements are True or False :

If the diagonals of a quadrilateral are equal and

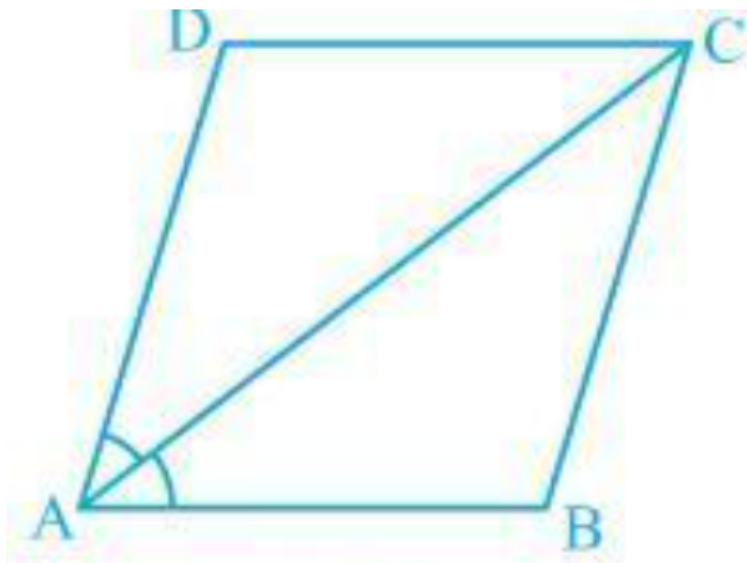
bisect each other at right angles then the quadrilateral is a square.



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**6.** Diagonal  $AC$  of a parallelogram  $ABCD$  bisects  $\angle A$  (see Fig. 8.19). Show that (i) it bisects  $\angle C$

also, (ii) ABCD is a rhombus.



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7. ABCD is a rhombus. Show that the diagonal AC bisects  $\angle A$  as well as  $\angle C$  and diagonal BD bisects  $\angle B$  as well as  $\angle D$ .



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8. ABCD is a rectangle in which diagonal AC

bisects

$\angle A$  as well as  $\angle C$

. Show that  $\widehat{D}$  diagonal BD bisects  $\perp$   $\angle B$

as well as  $\angle D$ .

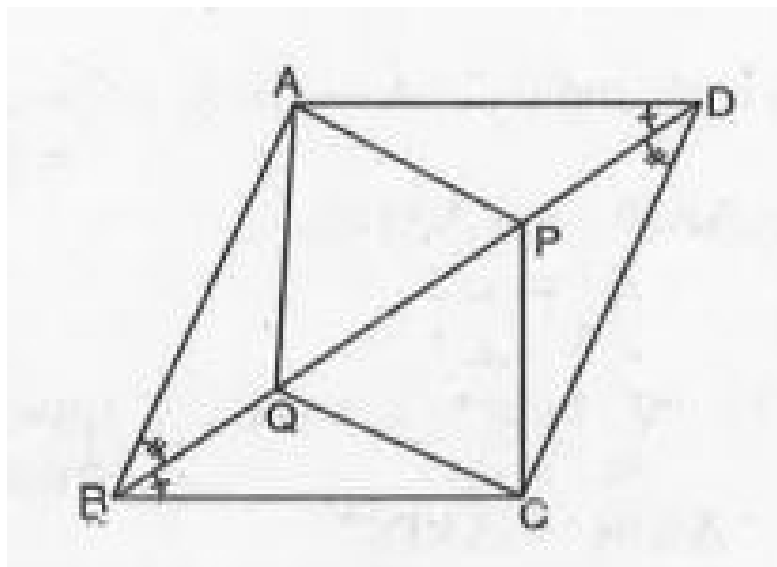


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9. In parallelogram ABCD, two points P and Q

are taken on diagonal BD such that DP = BQ

(see Fig.



) Show

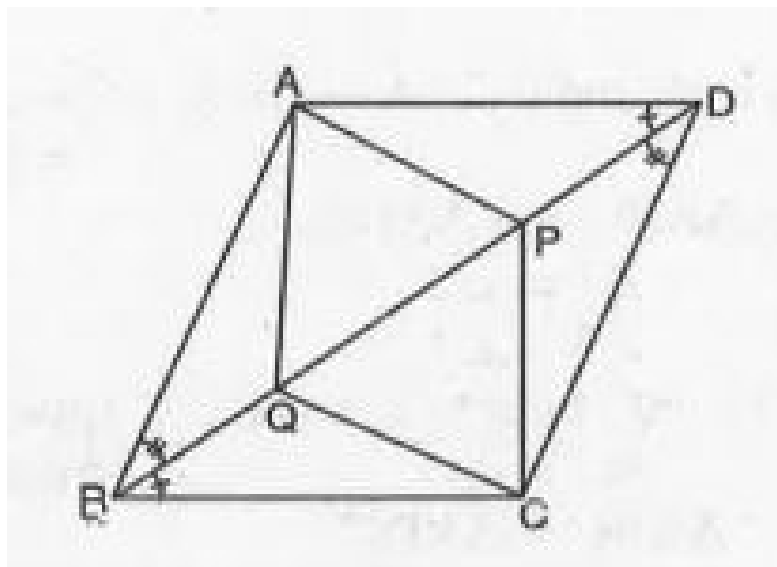
that  $AQ = CP$ .



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**10.** In parallelogram  $ABCD$ , two points  $P$  and  $Q$  are taken on diagonal  $BD$  such that  $DP = BQ$

(see Fig.



) Show

that  $AQ = CP$ .

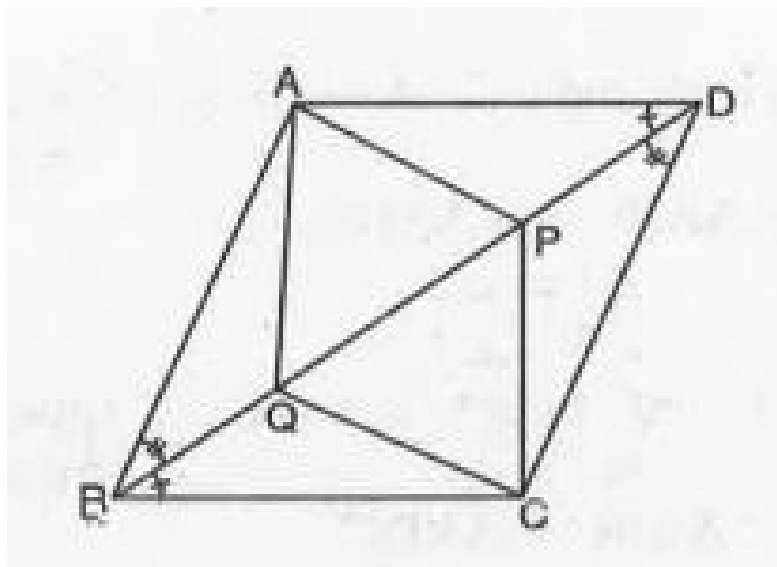


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**11.** In parallelogram  $ABCD$ , two points  $P$  and  $Q$  are taken on diagonal  $BD$  such that  $DP = BQ$



(see Fig.



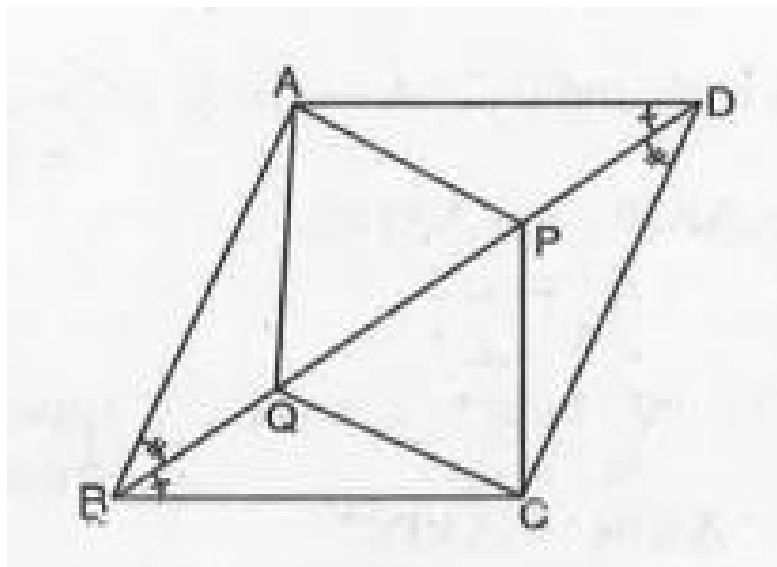
) Show

that  $AQ = CP$ .

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**12.** In parallelogram  $ABCD$ , two points  $P$  and  $Q$  are taken on diagonal  $BD$  such that  $DP = BQ$

(see Fig.



) Show


that  $AQ = CP$ .



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**13.** In parallelogram ABCD, two points P and Q are taken on diagonal BD such that  $DP = BQ$

(see Fig.

 Show that APCQ is a parallelogram.



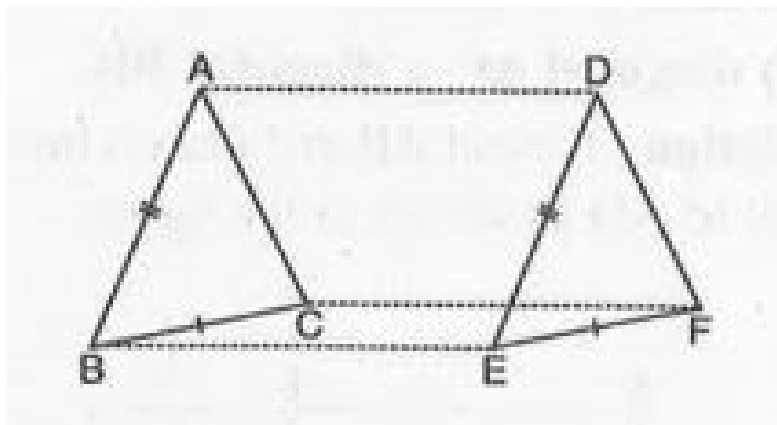
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**14.** ABCD is a parallelogram and AP and CQ are the perpendiculars from vertices A and C on its diagonal BD (See fig.) Show that  $\triangle APB \cong \triangle CQD$ .



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15. In  $\triangle ABC$  and  $\triangle DEF$ ,  $AB = DE$ ,  $AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices A, B and C are joined to vertices D, E and F respectively (See fig.)



Show

that quadrilateral ABED is a parallelogram.



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16. In  $\triangle ABC$  and  $\triangle DEF$  ,  $AB = DE$ ,

$AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ .

Vertices A, B and C are joined to vertices D, E and F respectively (See fig.)



Show that quadrilateral BEFC is a parallelogram.

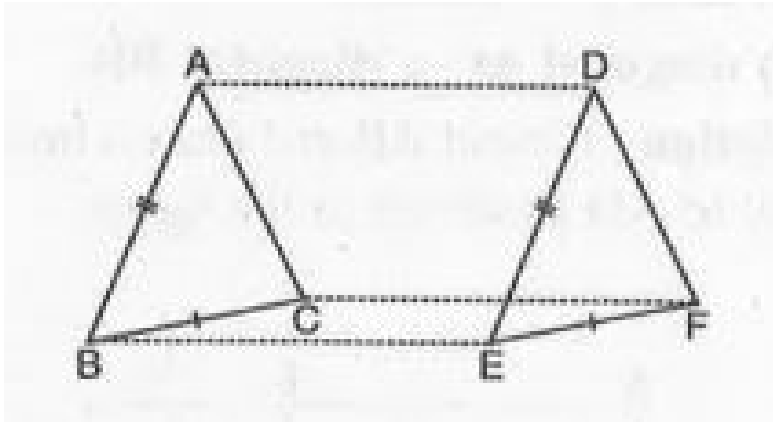


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17. In  $\triangle ABC$  and  $\triangle DEF$  ,  $AB = DE$ ,

$AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices

A, B and C are joined to vertices D, E and F respectively (See fig.)



Show

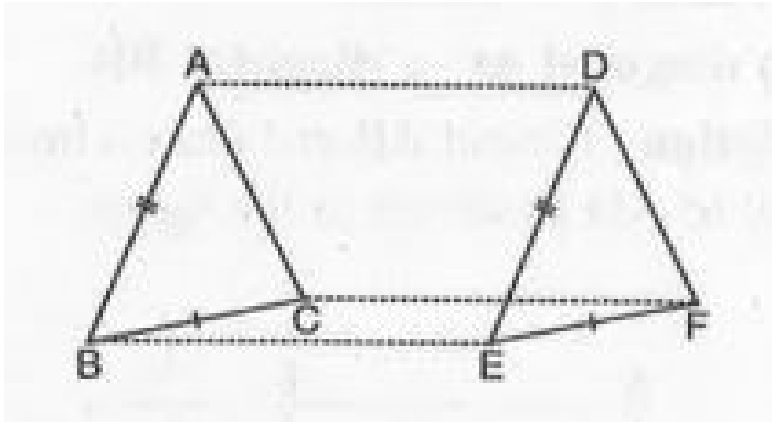
that  $AD \parallel CF$  and  $AD = CF$ .



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**18.** In  $\triangle ABC$  and  $\triangle DEF$ ,  $AB = DE$ ,  
 $AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices

A, B and C are joined to vertices D, E and F respectively (See fig.)  
respectively (See fig.)



Show

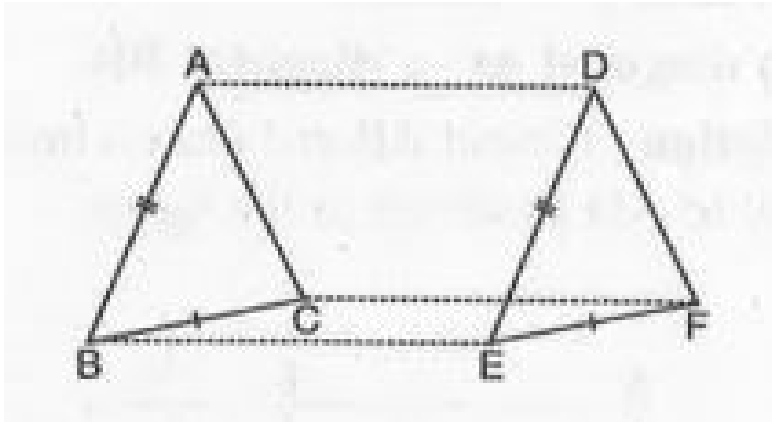
that quadrilateral ACFD is a parallelogram.



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**19.** In  $\triangle ABC$  and  $\triangle DEF$  ,  $AB = DE$ ,  
 $AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices

A, B and C are joined to vertices D, E and F respectively (See fig.)



Show

that  $AC=DF$ .

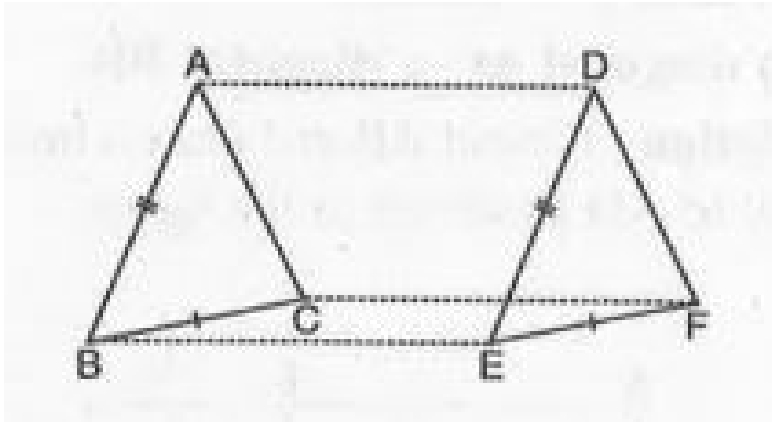


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20. In  $\triangle ABC$  and  $\triangle DEF$ ,  $AB = DE$ ,  
 $AB \parallel DE$ ,  $BC = EF$  and  $BC \parallel EF$ . Vertices



A, B and C are joined to vertices D, E and F respectively (See fig.)  
respectively (See fig.)



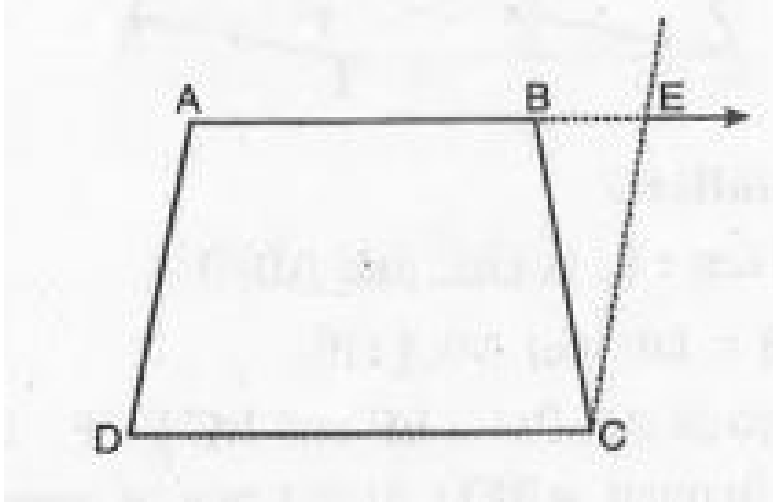
Show

that  $\triangle ABC \cong \triangle DEF$ .



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21. ABCD is a trapezium in which  $AB \parallel CD$   
and  $AD = BC$  (See Fig.)



Show

that  $\angle A = \angle B$ .



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22. ABCD is a trapezium in which  $AB \parallel CD$

and  $AD = BC$  (See Fig.)



Show that  $\angle C = \angle D$ .



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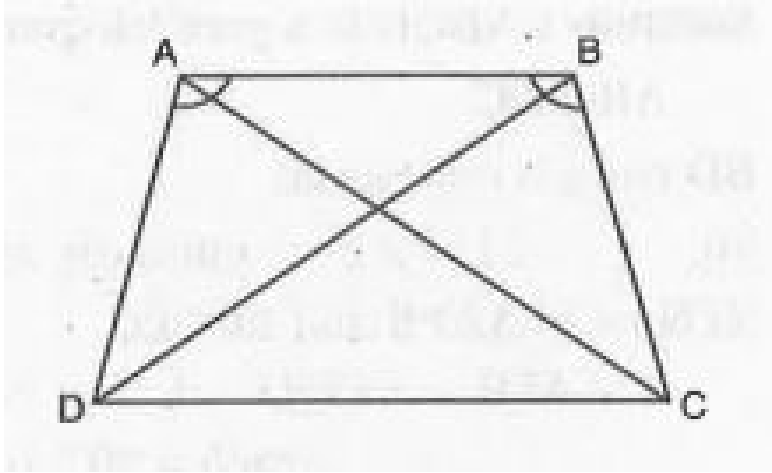
**23.** ABCD is a trapezium in which  $AB \parallel CD$   
and  $AD = BC$  (See Fig.)

 Show that  $\triangle ABC \cong \triangle BAD$ .



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**24.** ABCD is a trapezium in which  $AB \parallel CD$   
and  $AD = BC$  (See Fig.)



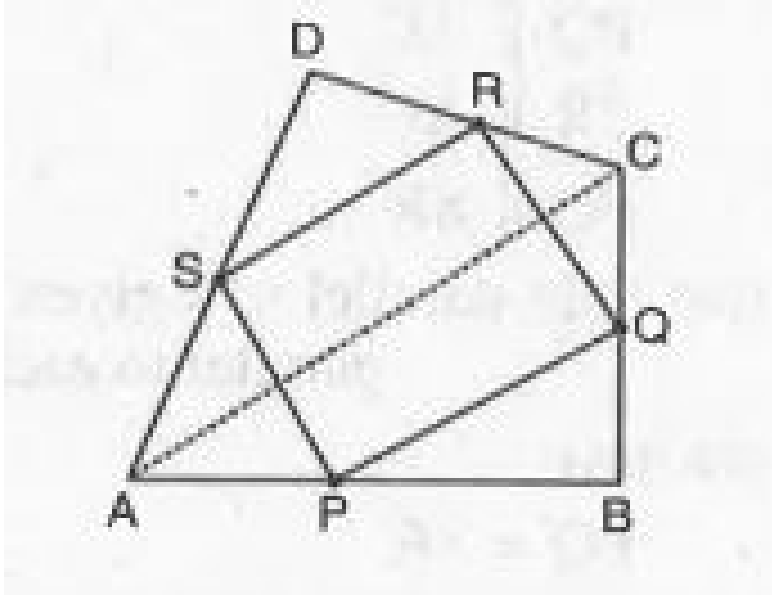
Show

that diagonal  $AC =$  diagonal  $BD$ .



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**25.** ABCD is a quadrilateral in which P, Q, R and S are the mid-points of sides AB, BC, CD and DA respectively (See Fig.



AC is a

diagonal

Show

that

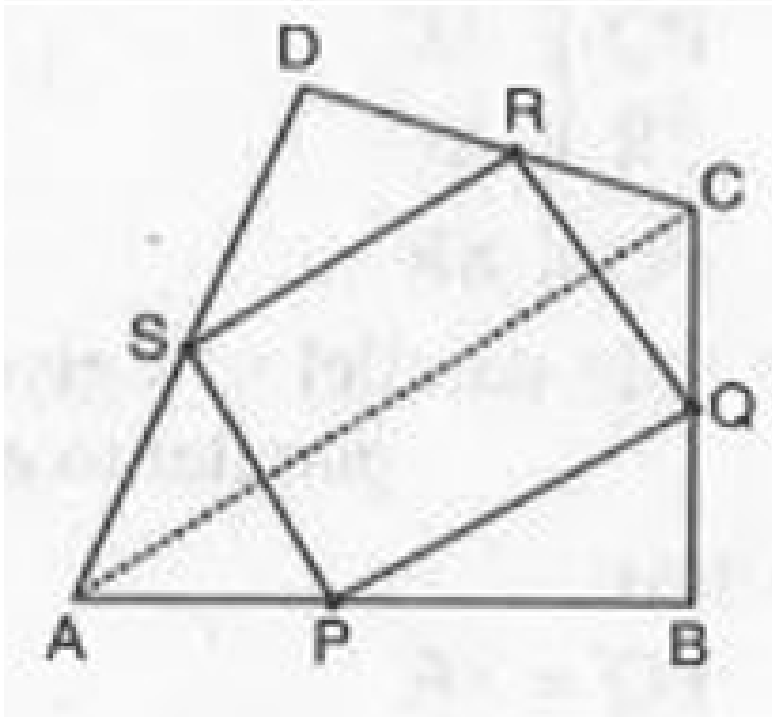
$$SR \parallel AC \text{ and } SR = \frac{1}{2} AC.$$



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**26.** ABCD is a quadrilateral in which P, Q, R and S are the mid-points of sides AB, BC, CD and DA

respectively (See Fig.)




AC is a

diagonal Show that  $PQ = SR$ .



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27. ABCD is a quadrilateral in which P, Q, R and S are the mid-points of sides AB, BC, CD and DA respectively (See Fig.)

 AC is a diagonal Show that PQRS is a parallelogram.



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28. ABCD is a rhombus and P, Q, R, S are the mid-points of AB, BC, CD and DA respectively.

Prove that quadrilateral PQRS is a rectangle.





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**29.** ABCD is a rectangle and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rhombus.




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**30.** ABCD is a trapezium, in which  $AB \parallel DC$ , BD is a diagonal and E is the mid-point of AD. A line is drawn through E, parallel to AB




intersecting BC at F (See Fig.)

 Show that F is the mid-point of BC.

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**31.** In a parallelogram ABCD, E and F are the mid-points of sides AB and CD respectively (See Fig)

 Show that the line segments AF and EC trisect the diagonal BD.

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**32.** Show that the line segments joining the mid-points of opposite sides of a quadrilateral bisect each other.



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**33.** ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that D is the mid-point of AC.



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**34.** ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that  $MD \perp AC$ .



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**35.** ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that  $CM = MA = \frac{1}{2}AB$ .





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## Example

1. Show that each angle of a rectangle is a right angle.



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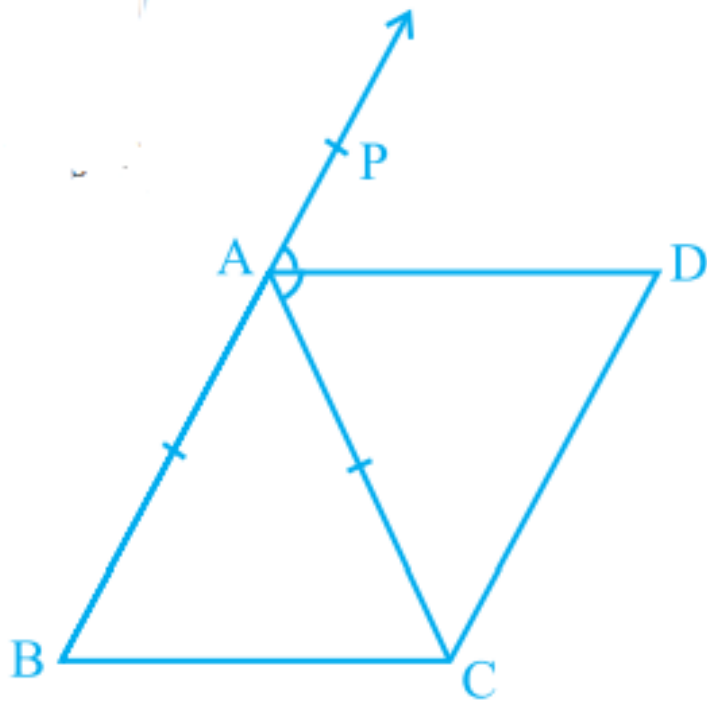
2. The diagonals of a rhombus are perpendicular to each other .



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**3.** ABC is an isosceles triangle in which  $AB = AC$ . AD bisects exterior angle PAC and  $CD \parallel AB$  (see Fig. 8.14). Show that (i)  $\angle DAC = \angle BCA$  and

(ii) ABCD is a parallelogram.



**Fig. 8.14**



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4. Two parallel lines  $l$  and  $m$  are intersected by a transversal  $p$  (see Fig. 8.15). Show that the quadrilateral formed by the bisectors of interior angles is a rectangle.

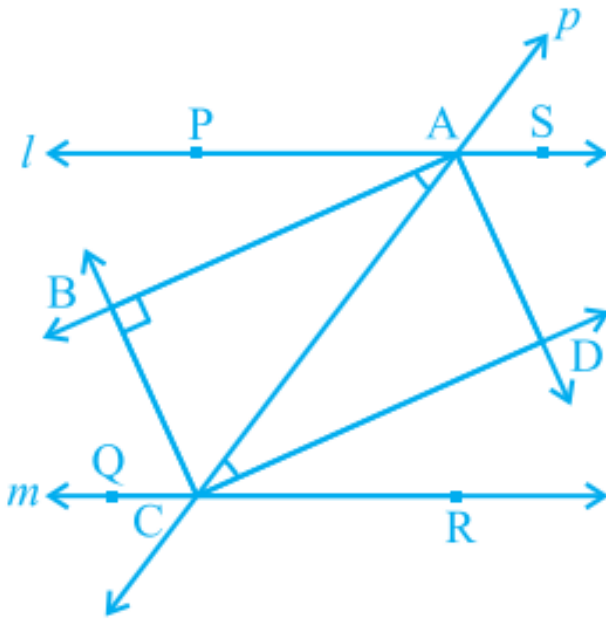


Fig. 8.15



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5. The bisectors of angles of a parallelogram from a :

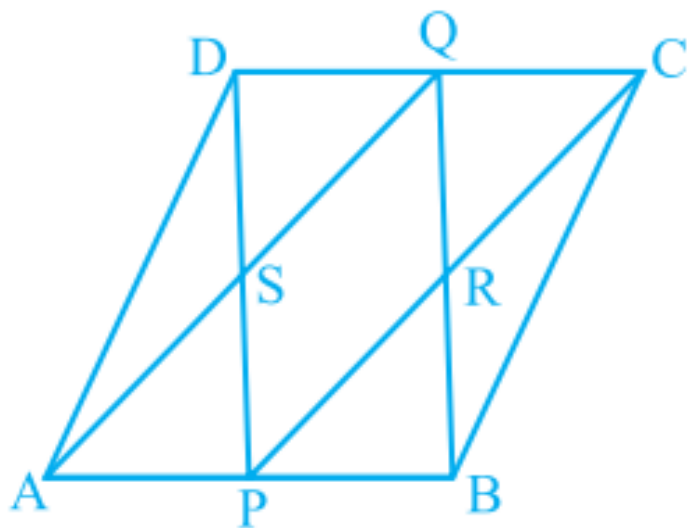


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6. ABCD is a parallelogram in which P and Q are mid-points of opposite sides AB and CD (see Fig. 8.18). If AQ intersects DP at S and BQ intersects CP at R, show that: APCQ is a



parallelogram.



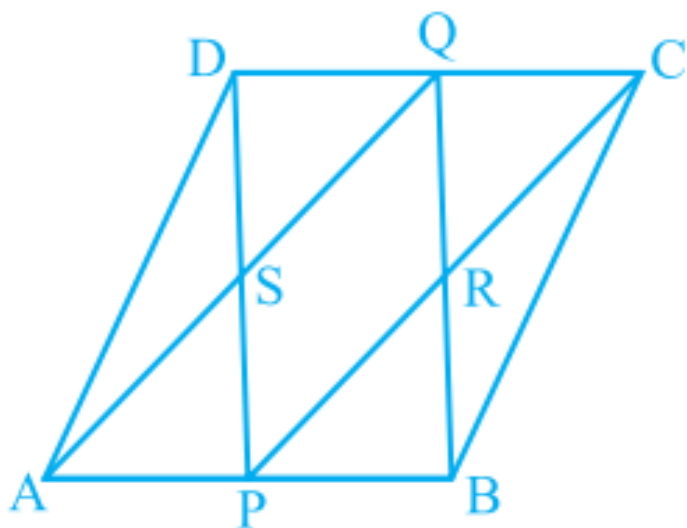
**Fig. 8.18**



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7. ABCD is a parallelogram in which P and Q are mid-points of opposite sides AB and CD (see

Fig. 8.18). If  $AQ$  intersects  $DP$  at  $S$  and  $BQ$  intersects  $CP$  at  $R$ , show that:  $APCQ$  is a parallelogram.

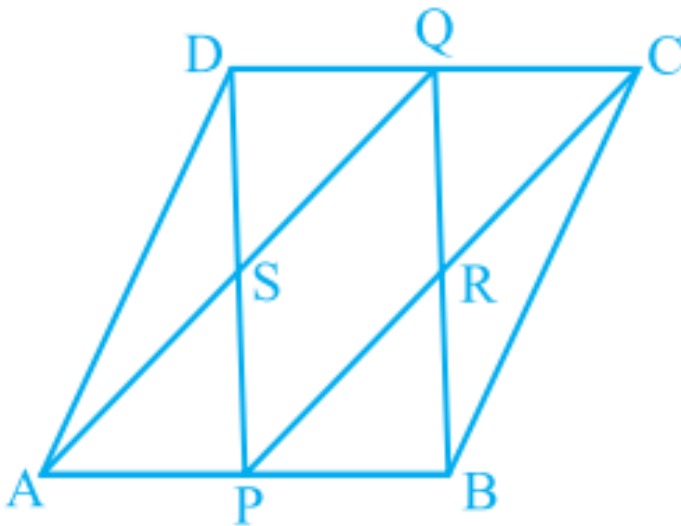


**Fig. 8.18**



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8. ABCD is a parallelogram in which P and Q are mid-points of opposite sides AB and CD (see Fig. 8.18). If AQ intersects DP at S and BQ intersects CP at R, show that: DQBP is a parallelogram.



**Fig. 8.18**



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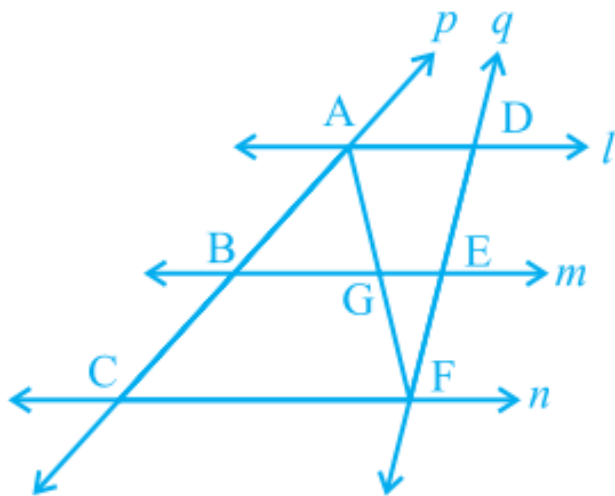
**9.** In  $\triangle ABC$ , D, E and F are respectively the mid-points of sides AB, BC and CA . Show that  $\triangle ABC$  is divided into four congruent triangles by joining D, E and F.



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**10.** l, m and n are three parallel lines intersected by transversals p and q such that l, m and n cut off equal intercepts AB and BC on

$p$  (see Fig. 8.28). Show that  $l$ ,  $m$  and  $n$  cut off equal intercepts  $DE$  and  $EF$  on  $q$  also.



**Fig. 8.28**



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