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## MATHS

## BOOKS - EDUCART PUBLICATION

## CIRCLES

Objective Type Questions Multiple Choice
Questions

1. In the figure-3, from an external point $P$, two
tangents PQ and PR are drawn to a circle of
the radius 4 cm with centre O . If $\angle \mathrm{QPR}=90^{\circ}$,

A. 3 cm
B. 4 cm
C. 2 cm

## D. $2 \sqrt{2} \mathrm{~cm}$

Answer: B

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2. In figure $P Q$ is tangent to the circle with centre at O at the point B , if $\angle A O B=100^{\circ}$,
then $\angle A B P$ is equal to

A. $50^{\circ}$
B. $40^{\circ}$
C. $60^{\circ}$
D. $80^{\circ}$

Answer: A
3. In the figure, TP and TQ are tangents drawn to the circle with centre at 0 . If
$\angle P O Q=115^{\circ}$ then $\angle P T Q$ is:

A. $115^{\circ}$
B. $57.5^{\circ}$
C. $55^{\circ}$
D. $65^{\circ}$

Answer: D

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4. In the given figure, If $\angle A O B=125^{\circ}$ then
find $\angle C O D$.

A. $62.5^{\circ}$
B. $45^{\circ}$
C. $35^{\circ}$
D. $55^{\circ}$

## Answer: D

0
5. From an external point Q , the length of the tangents to a circle is 5 cm and the distance of
$Q$ from the centre is 8 cm . The radius of the circle is:
A. 39 cm
B. 3 cm
C. $\sqrt{39} \mathrm{~cm}$
D. 7 cm

Answer: C

# 6. Tangent $P Q$ at a point $P$ of a circle of radius 

5 cm meets a line through the centre $O$ at a point $Q$ so that $Q Q=12 \mathrm{~cm}$. Find length of $P Q$
A. 12 cm
B. 13 cm
C. 8.5 cm
D. $\sqrt{119} \mathrm{~cm}$

Answer: D
7. From a point $P$ which is at a distance of 13 cm from the centre O of a circle of radius 5 cm , the pair of tangents PQ and PR to the circle are drawn. Then the area of the quadrilateral PQOR is :
A. $60 \mathrm{~cm}^{2}$
B. $65 \mathrm{~cm}^{2}$
C. $30 \mathrm{~cm}^{2}$
D. $32.5 \mathrm{~cm}^{2}$

Answer: A

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8. The chord of a circle of radius 10 cm
subtends a right angle at its centre. The length of the chord (in cm ) is
A. 10 cm
B. $10 \sqrt{2} \mathrm{~cm}$
C. 20 cm
D. 12 cm

Answer: B

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9. In a circle of radius 7 cm , tangent PT is drawn from a point $P$ such tht $P T=24 \mathrm{~cm}$. If O
is the centre of circle, then find the length of

OP.
A. 25 cm
B. $15 \sqrt{2}$
C. 18 cm

## D. 17 cm

## Answer: A

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10. At one end $A$ of a diameter $A B$ of a circle of
radius 5 cm , tangent $x a y$ is drawn to the circle. Find the length of the chord cd paralled to $X Y$ and at a distantce 8 cm from A .
A. 4 cm
B. 5 cm
C. 6 cm
D. 8 cm

Answer: D

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11. In figure, AT is a tangent to the circle with centre 0 such that $O T=4 \mathrm{~cm}$ and
$\angle O T A=30^{\circ}$. Then, AT is equal to

A. 4 cm
B. 2 cm
C. $2 \sqrt{3} \mathrm{~cm}$
D. $4 \sqrt{3} \mathrm{~cm}$

Answer:
12. If radii of two concentric circles are 4 cm and 5 cm , then length of each chord of one circle which is tangent to the other circle, is
A. 8 cm
B. 6 cm
C. 10 cm
D. 12 cm
13. In the figure, $O$ is the centre of a circle and

AT is a tangent at point $A$. The measure of
$\angle B A T$ is:

A. $30^{\circ}$
B. $60^{\circ}$
C. $75^{\circ}$
D. $105^{\circ}$

Answer: B

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## Objective Type Questions Fill In The Blanks

1. All concentric circles are..... to each other.

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2. In the figure, $\triangle A B C$ is circumscribing a circle, the length of $B C$ is cm.


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3. In fig., $A B C D$ is a cyclic quadrilatreral. If
$\angle B A C=50^{\circ}$ and $\angle D B C=60^{\circ}$, then find
$\angle B C D$.


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4. From the external point $P$ tangents $P A$ and PB are drawn to a circle with centre O . If $\angle P A B=50^{\circ}$, then find $\angle A O B$.

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5. $P Q$ is a tangent drawn from a point $P$ to a circle with centre $O$ and $Q O R$ is a diameter of the circle such that $\angle P O R=1200$, then $\angle O P Q$ is $60 o$ (b) $45 o$ (c) $30 o$ (d) $90 o$

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6. The length of the tangent to a circle from a point $P$, which is 25 cm away from the centre, is 24 cm . What is the radius of the circle.
7. A tangent $P Q$ at a point $P$ of a circle of radius 5 cm meets a line through the centre $O$ at a point $Q$ so that $O Q=13 \mathrm{~cm}$. Find the length of $P Q$.

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8. A line which intersects a circle at two distinct point is called a $\qquad$

## 9. In the given figure the length $\mathrm{PB}=$

cm.


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## Objective Type Questions Write True Or False

1. If a chord $A B$ subtends and angle of $60^{\circ}$ at
the centre of a circle, then the angle between
the tangents to the circle drawn from $A$ and
$B$ is

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2. The length of tangent from an external point on a circle is always greater than the radius of the circle.

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3. The length of tangent from an external point $P$ on a circlewith centre 0 is always less than OP.
4. The angle between two tangents to a circle may be $0^{\circ}$.

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5. The tangent to the circumcircle of an isosceles $\triangle A B C$ at A , in which $\mathrm{AB}=\mathrm{AC}$, is parallel to $B C$.

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6. If a number of circles touch line segment $P Q$
at a point $A$ then, their centres lie on the perpendicular bisector of PQ. State True or False

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7. If a number of circles pass through the end points $P$ and $Q$ of a line segment $P Q$, then their centres lie on the perpendicular bisector of PQ.
8. $A B$ is a diameter of a circle and $A C$ is its chord such that $\angle B A C=30^{\circ}$. If the tengent at $C$ intersects $A B$ extended at $D$, then $B C=B D$.

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Objective Type Questions Very Short Questions

1. $A B$ and $C D$ are common tangents to two
circles which intersect each other at C as
shown in the figure IF $A B=6 \mathrm{~cm}$, find $C D$.


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2. If Fig, $A O B$ is diameter of a circle with centre
$O$ and $A C$ is a tangent to the circle at $A$. If
$\angle B O C=130^{\circ}$, then find $\angle A C O$.

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3. What is the maximum number of parallel tangents a circle can have on a diameter?
4. In Figure 1, O is the centre of a circle, PQ is a chord and PT is the tangent at P. If angle POQ
$=70^{\circ}$, then angleTPQ is equal to

## D Watch Video Solution

5. If Fig, $A O B$ is diameter of a circle with centre
$O$ and $A C$ is a tangent to the circle at $A$. If
$\angle B O C=130^{\circ}$, then find $\angle A C O$.

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6. If the angle between two tangents drawn
from an external point $P$ to a circle of radius 'a' and center O , is $60^{\circ}$, then find the length of OP.
7. In figure $P Q$ is a tangent at a point $C$ to a circle with centre $O$. If $A B$ is a diameter and
$\angle C A B=30^{\circ}$, find $\angle P C A$


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8. In Figure PQ is a chord of a circle with centre

O and PT is a tangent. If $Q P T=60^{\circ}$ so, find
PRQ.


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9. In the figure, $\angle A P B=90^{\circ}$


Find the length of OP if $A P=2 \mathrm{~cm}$.

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10. PQ is a tangent drawn from an external point P to a circle with center $\mathrm{O}, \angle Q O R$ is the diameter of the circle. If $\angle P O R=120^{\circ}$. What is the measure of $\angle O P Q$ ?


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## 1. In Figure, a quadrilateral $A B C D$ is drawn to

circumscribe a circle .

Prove that
$A B+C D=B C+A D$


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2. In Fig, $O$ is the centre of a circle, $P Q$ is a chord and the tangent PR at P makes an angle of $50^{\circ}$ with PQ . Find $\angle P O Q$.


R
(D) Watch Video Solution
3. In the figure, find the perimeter of $\triangle A B C$, if $\mathrm{AP}=12 \mathrm{~cm}$.


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4. In the given, if $A B=A C$. prove the $B E=E C$.


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5. Prove that the tangents drawn at the ends of a diameter of a circle are parallel.

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6. In the given figure, PA and PB are tangents
to the circle from an external point P. CD is
another tangent touching the circle at Q . If PA
$=12 \mathrm{~cm}, \mathrm{QC}=3 \mathrm{~cm}$, then find $\mathrm{PC}+\mathrm{PD}$.


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## 7. In the figure, $O$ is the centre of the circle and

$L N$ is a diameter. If $P Q$ is a tangent to the circle at $K$ and $\angle K L N=30^{\circ}$, find $\angle P K L$.


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8. The incircle of an isosceles triangle $A B C$, in which $A B=A C$, touches the sides $B C, C A$ and $A B$ at $\mathrm{D}, \mathrm{E}$ and F respectively. Prove that $\mathrm{BD}=\mathrm{DC}$.


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9. From a point P, two tangents PT and PS are drawn to a circle with center O.Such that
$\angle S P T=120^{\circ}$. Prove that $\mathrm{OP}=2 \mathrm{PS}$.

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10. In the given figure, a circle inscribed in a triangle $A B C$, touches the sides $A B, B C$ and $A C$ at points $D, E$ and $F$ respectively. If $A B=12 \mathrm{~cm}$, $B C=8 \mathrm{~cm}$ and $A C=10 \mathrm{~cm}$, find the lengths of $A D, B E$ and $C F$.
11. In Fig AP and BP are tangents to a circle with centre $O$, such that $A P=5 \mathrm{~cm}$, and
$\angle A P B=60^{\circ}$. Find the length of chord AB .


## D Watch Video Solution

12. Prove that the rectangle circumscribing a circle is a square

## D Watch Video Solution

13. In Fig.2, a quadrilateral $A B C D$ is drawn to circumscribe a circle, with centre $O$, in such a way that the sides $A B, B C, C D$ and $D A$ touch the circle at the points $P, Q, R$ and $S$ respectively. Prove that $A B+C D=B C+D A$.
14. In Figure $1, O$ is the centre of a circle, $P Q$ is a chord and PT is the tangent at P. If angle $P O Q=70^{\circ}$, then angleTPQ is equal to

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15. $P Q$ is a tangent drawn from a point $P$ to a circle with centre $O$ and $Q O R$ is a diameter of
the circle such that $\angle P O R=120 o$, then
$\angle O P Q$ is $60 o$ (b) $45 o$ (c) $30 o$ (d) $90 o$
16. In Fig. two tangents RQ and RP are drawn
from an external point $R$ to the circle with centre 0 . If $\angle P R Q=120^{\circ}$, then prove that
$O R=P R+R Q$.

17. Prove that the tangents drawn at the end points of a chord of a circle make equal angles with the chord.

## D Watch Video Solution

18. There are two concentric circles with centre
O. PRT and PQS are tangents to the inner
circle. If $P R=5 \mathrm{~cm}$, find the length of $P S$.


## D Watch Video Solution

19. A circle touches the side BC of $\triangle A B C$ at F and touches $A B$ and $A C$ at $D$ and $E$,
respectively. If $A D=8 \mathrm{~cm}$, then find the perimeter of $\triangle A B C$.


D Watch Video Solution
20. From the external point $P$ tangents $P A$ and

PB are drawn to a circle with centre O . If
$\angle P A B=50^{\circ}$, then find $\angle A O B$.

## D Watch Video Solution

21. If the angle between two tangents drawn
from an external point $P$ to a circle of radius ' $a$ ' and center O , is $60^{\circ}$, then find the length of

OP.
22. In the figure, $\angle A D C=90^{\circ}$,

$B C=38 \mathrm{~cm}, C D=28 \mathrm{~cm}$ and $B P=25 \mathrm{~m}$
. Find the radius of the circle.
23. चित्र में एक वृत्त त्रिभुज $A B C$ की भुजा $B C$ को प पर स्पर्श करता है । तथा $A B$ व $A C$ को बढ़ाये जाने पर क्रमश :

Q व R पर स्पर्श |
सिद्ध कीजिए $A Q=\frac{1}{2}$ ( $\triangle A B C$ का परिमाप )

24. Out of the 2 concentric circle the radius of
the outer circle is 5 cm and the chord AC of the length 8 cm is a tangent to the inner circle find the radius of the inner circle

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25. In Fig. 10.21, two circles touch each other at
the point $C$. Prove that the common tangent
to the circles at $C$, bisects the common
tangent at $P$ and $Q$. (FIGURE)
26. Prove that the parallelogram
circumscribing a circle is a rhombus.

## - Watch Video Solution

27. In figure, common tangents $A B$ and $C D$ to
two circles intersect at $E$. Prove that $A B=C D$.


## - Watch Video Solution

28. In Fig , AB is a chord of a circle, with centre
$O$, such that $A B=16 \mathrm{~cm}$ and radius of circle is
10 cm . Tangents at $A$ and $B$ intersect each other at P. Find the length of PA.


Short Answer Sa li Type Questions

1. In Fig XY and $X^{\prime} Y^{\prime}$ are two parallel tangents to a circle with centre O and another tangent $A B$ with point of contact $C$ intersecting $X Y$ and $\mathrm{X}^{\prime} \mathrm{Y}^{\prime}$ at B , prove that $\angle A O B=90^{\circ}$

2. Two tangents $P Q$ and $P R$ are drawn from an external point to a circle with centre 0 . Prove that QORP is cyclic quadrileral.

## D Watch Video Solution

3. In the adjoining figure, common tangents
$A B$ and $C D$ to two circles intersect at $P$.

Prove that $A B=C D$.


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4. ABC is a right triangle in which $\angle B=90^{\circ}$.

If $A B=8 \mathrm{~cm}$ and $B C=6 \mathrm{~cm}$. find the diameter of the circle inscribed in the triangle.
5. $P Q$ and RS are two parallel tangents to a circle with centre $O$ and another tangent $A B$ wih point of contact $C$ intersect $P Q$ at $A$ and RS at B . then find $\angle A O B$

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6. In Figure 4, PQ and PR are tangents drawn to a circle with centre $O$ from an external
point P . If $\angle P R Q=70^{\circ}$, then find
$\angle Q P R$ and $\angle O Q R$

## D Watch Video Solution

7. In the given figure, PA and PB are tangents
to a circle from an external point $P$ such that
$\mathrm{PA}=4 \mathrm{~cm}$ and $\angle B A C=135^{\circ}$. Find the length
of dhord $A B$.


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8. A chord PQ of a circle is parallel to the tangent drawn at a point R of the circle,Prove that R bisects the $\operatorname{arc} P R Q$.

## Watch Video Solution

9. Prove that a diameter $A B$ of a circle bisects
all those chords which are parllel to the tangent at the point A .

## - Watch Video Solution

10. $A B$ is a diameter of a circle with centre $O$
and AT is a tangent. If $\angle A O Q=58^{\circ}$ find
$\angle A T Q$.


## - Watch Video Solution

11. In the given figure, $O$ is the centre of $a$ circle, BOA is its diameter and the tangent at
the point $P$ meets $B A$ extended at $T$. If
$\angle P B O=30^{\circ}$, then $\angle P T A$ is equal to


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12. Prove that the length of the tangents drawn from an external point to a circle are equal.

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13. In Fig, PQ is a tangent from an external point $P$ to a circle with centre $O$ and $O P$ cuts the circle at $T$ and $Q O R$ is a diameter. If
$\angle P O R=130^{\circ}$ and S is a point on the circle, find $\angle 1+\angle 2$.

## D Watch Video Solution

14. In Fig , are two concentric circles of radii 6 cm and 4 cm with centre O . If AP is a tangent to the larger circle and BP to the smaller circle
and length of $A P$ is 8 cm , find the length of $B P$.


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15. From an external point $P$, two tangents PT and PS are drawn to a circle with centre $O$ and
radius r. if $O P=2 r$, show that
$\angle O T S=\angle O S T=30^{\circ}$

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16. Two tangents $P A$ and $P B$ are drawn to a circle with centre $O$ from an external point $P$. Prove that $\angle A P B=2 \angle O A B$


## - Watch Video Solution

17. Prove that the tangent at any point of circle
is perpendicular to the radius through the point of contact.

## - Watch Video Solution

18. Prove that tangent drawn at the mid point of the are of a circle is pallelar to the chord joing the ends of point of the are
19. Two circles touch each other externally at $P$.
$A B$ is a common tangent to the circle touching them at $A$ and $B$. The value of $\angle A P B$ is $30 o$ (b) $45 o$ (c) $60 o$ (d) $90 o$

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2. $P Q$ is a chord of length 8 cm of a circle of radius 5 cm . The tangents at $P$ and $Q$ intersect at a point $T$. Find the length $T P$.

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3. Let $s$ denotes the semi-perimeter of $a$
$\triangle A B C$ in which $\mathrm{BC}=\mathrm{a}, \mathrm{CA}=\mathrm{b}$ and $\mathrm{AB}=\mathrm{c}$. If a circle touches the sides $B C, C A, A B$, at $D, E, F$, respectively. Prove that $B D=s-b$.

## D Watch Video Solution

4. From an external point $P$, two tangents, PA
and PB are drawn to a circle with centre 0 . At
one point $E$ on the circle tangent is drawn which intersects $P A$ and $P B$ at $C$ and $D$, respectively. If $\mathrm{PA}=10 \mathrm{~cm}$, find the preimeter of the trianlge PCD.

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5. $O$ is the centre of a circle of radius $5 \mathrm{~cm} . T$ is
a point such that $O T=13$ cmandOT
intersects the circle at $E$. If $A B$ is the tangent to the circle at $E$, find length of $A B$.
6. In Fig XY and $X^{\prime} Y^{\prime}$ are two parallel tangents
to a circle with centre O and another tangent
$A B$ with point of contact $C$ intersecting $X Y$ and
$\mathrm{X}^{\prime} \mathrm{Y}^{\prime}$ at B , prove that $\angle A O B=90^{\circ}$


## D Watch Video Solution

7. If an isosceles triangle $A B C$ in which
$A B=A C=6 \mathrm{~cm}$ is inscribed in a circle of radius 9 cm , find the area of the triangle.

## D Watch Video Solution

8. In a right angle triangle $\triangle A B C$ is which
$\angle B=90^{\circ}$ a circle is drawn with AB diameter
intersecting the hypotenuse AC at P.Prove that
the tangent to the circle at $P Q$ bisects $B C$.
9. In a figure the common tangents, AB and CD to two circles with centers O and $\mathrm{O}^{\prime}$ intersect at E . Prove that the points $\mathrm{O}, \mathrm{E}$ and O are collinear.


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10. $A$ is a point at a distance 13 cm from the centre $O$ of a circle of radius 5 cm . AP and AQ are the tangents to the circle at P and Q . If a tangent $B C$ is drawn at a point $R$ lying on the minor $\operatorname{arc} P Q$ to intersect $A P$ at Band $A Q$ at $C$, find the perimeter of the $\triangle A B C$

## D Watch Video Solution

11. . In the given figure, two equal circles, with centres O and $\mathrm{O}^{\prime}$, touch each other at X . $\mathrm{OO}^{\prime}$
produced me the circle with centre $O^{\prime}$ at $A$. AC is tangent to the circle with centreO, at the point C. O'D is perpendicular to AC. Find the value of $\frac{D O^{\prime}}{C O}$.

## D Watch Video Solution

12. A triangle $A B C$ is drawn to circumscribe a circle of radius 4 cm such that the segments $B D$ and $D C$ into which $B C$ is divided by the point of contact $D$ are of lengths 8 cm and 6 cm respectively. Find the sides $A B$ and $A C$.

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13. $P Q$ is a chord of length 8 cm of a circle of radius 5 cm . The tangents at $P$ and $Q$ intersect at a point $T$. Find the length $T P$.

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