



MATHS

BOOKS - NAGEEN PRAKASHAN ENGLISH

QUADRATIC EQUATIONS

Solved Examples

1. Check whether the following are quadratic equation

(i) $(x + 1)^2 = 2(x - 3)$

(ii) $x^2 - 2x = (-2)(3 - x)$

(iii) $(x - 2)(x + 1) = (x - 1)(x + 3)$

$$(iv) (x - 3)(2x + 1) = x(x + 5)$$

$$(v) (2x - 1)(x - 3) = (x + 5)(x - 1)$$

$$(vi) x^2 + 3x + 1 = (x - 2)^2$$

$$(vii) (x + 2)^3 = 2x(x^2 - 1)$$

$$(viii) x^3 - 4x^2 - x + 1 = (x - 2)^3$$



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2. Represent the following situations in the form of quadratic equations : (i) The area of a rectangular plot is 528 m^2 . The length of the plot (in metres) is one more than twice its breadth. We need to find the length and breadth of the plot



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3. Which of the following are the solutions of

$$2x^2 - 5x - 3 = 0?$$

(i) $x = 2$

(ii) $x = 3$

(iii) $x = \frac{-1}{2}$

A. only (i)

B. (i) and (ii)

C. (ii) and (iii)

D. (i) , (ii) and (iii)

Answer: C



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4. If $x=2$ and $x=3$ are roots of the equation $3x^2 - mx + 2n = 0$, then find the values of m and n .



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5. Solve the following quadratic equation:

$$(3x - 5)(2x + 3) = 0$$

A. $x = 5$ and $x = -3$

B. $x = \frac{5}{3}$ and $x = \frac{3}{2}$

C. $x = \frac{5}{3}$ and $x = \frac{-3}{2}$

D. none of these

Answer: C

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6. Find the roots of the following quadratic equations by factorisation :

(i) $x^2 - 3x - 10 = 0$ (ii) $2x^2 + x - 6 = 0$ (iii)

$\sqrt{2}x^2 + 7x + 5\sqrt{2} = 0$

(iv) $2x^2 - x + \frac{1}{8} = 0$ (v) $100x^2 - 20x + 1 = 0$ (vi)

$2x^2 + az - a^2 = 0$

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7. Solve the following quadratic equations by factorisation :

(i) $4 - 11x = 3x^2$

(ii) $x^2 - \frac{11}{4}x + \frac{15}{8} = 0$



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8. Solve the following quadratic equations :

$$x^2 - (1 + \sqrt{2})x + \sqrt{2} = 0$$



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9. Solve the following quadratic equation for x :

$$43x+5x-23 = 0$$



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10. Solve the following quadratic equation :

$$10x - \frac{1}{x} = 3$$



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11. Solve the following quadratic equation :

$$a^2b^2x^2 + b^2x - a^2x - 1 = 0$$

A. $\frac{-1}{a}$ and $\frac{1}{b}$

B. $\frac{-1}{a^2}$ and $\frac{1}{b^2}$

C. $\frac{1}{a^2}$ and $\frac{1}{b^2}$

D. $\frac{-1}{a^2}$ and $\frac{-1}{b^2}$

Answer: B



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12. Solve the following quadratic equations by

factorization method: $4x^2 - 2(a^2 + b^2)x + a^2b^2 = 0$

$9x^2 - 9(a + b)x + (2x^2 + 5ab + 2b^2) = 0$



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13. Solve by factorization:

$$\frac{1}{x+4} - \frac{1}{x-7} = \frac{11}{30}, \quad x \neq 4, 7$$



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14. Using factorisation method, solve the following quadratic equations.

$$\frac{2x}{x-4} + \frac{2x-5}{x-3} = \frac{25}{3}; \quad x \neq 4, 3$$

A. $x = 6$ or $x = \frac{45}{13}$

B. $x = 0$ or $x = \frac{40}{13}$

C. $x = 4$ or $x = \frac{40}{13}$

$$D. x = 6 \text{ or } x = \frac{40}{13}$$

Answer: D



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15. Solve for x : $\frac{1}{x+1} + \frac{3}{5x+1} = \frac{5}{x+4}$, $x \neq -1, -1/5, -4$



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16. Solve the equation :

$$\frac{5}{2-x} + \frac{x-5}{x+2} + \frac{3x+8}{x^2-4} = 0$$



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17. Solve the following equation :

$$2\left(\frac{2x - 1}{x + 3}\right) - 3\left(\frac{x + 3}{2x - 1}\right) = 5, (x \neq -3, 1)$$



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18. Solve the equation :

$$\frac{a}{x - b} + \frac{b}{x - a} = 2 \quad (x \neq b, a)$$



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19. Solve the following equation :

$$3^{x+2} + 3^{-x} = 10$$



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20. Find the roots of the following quadratic equations, if they exist, by the method of completing the square: (i) $2x^2 - 7x + 3 = 0$ (ii) $2x^2 + x - 4 = 0$
(iii) $4x^2 + 4\sqrt{3}x + 3 = 0$ (iv) $2x^2 + x + 4 = 0$



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21. Find the roots of following quadratic equations by using quadratic formula, if they exist.

(i) $2x^2 + x - 4 = 0$ (ii) $2x^2 + x + 4 = 0$

(iii) $2x^2 + 5\sqrt{3}x + 6 = 0$ (iv)

$\sqrt{3}x^2 + 11x + 6\sqrt{3} = 0$



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22. Find roots of the equation by quadratic formula :

$$x^2 + x - (a + 2)(a + 1) = 0$$



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23. Solved the equation by using quadratic formula

$$a(x^2 + 1) = (a^2 + 1)x, a \neq 0.$$



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24. Solved the following equation by the method of completing the square :

$$4\sqrt{3}x^2 + 5x - 2\sqrt{3} = 0$$



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25. Solved : $x^2 + x - (a + 2)(a + 1) = 0$ by

(i) factorisation (ii) method of completing the square



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26. Let $f(x) = 3x^2 - 5x - 1$. Then solve $f(x)=0$ by

(i) factoring the quadratic

(ii) using the quadratic formula

(iii) completing the square

and then rewrite $f(x)$ in the form $A(x \pm B)^2 \pm C$.



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27. Find the nature of the roots of the following quadratic equations. If the real roots exist, find them:

(i) $2x^2 - 3x + 5 = 0$ (ii) $3x^2 - 4\sqrt{3}x + 4 = 0$ (iii)

$2x^2 - 6x + 3 = 0$



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28. Find the value of k so that the equation $2x^2 - 5x + k = 0$ has two equal roots.

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29. The equation $3x^2 - 12x + (n - 5) = 0$ has repeated roots. Find the value of n .

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30. Find the value of k for which the equation $x^2 + k(2x + k - 1) + 2 = 0$ has real and equal roots.



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31. Find the value of p , for which one root of the quadratic equation $px^2 - 14x + 8 = 0$ is 6 times the other.



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32. The equation $x^2 + 2(m - 1)x + (m + 5) = 0$ has real and equal roots. Find the value of m .



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33. If -4 is a root of the equation $x^2 + px - 4 = 0$ and the equation $x^2 + px + q = 0$ has coincident roots, find the values of p and q .



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34. both roots of the equation

$$(x - a)(x - b) + (x - b)(x - c) + (x - c)(x - a) = 0$$

are



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35. Determine the positive values of ' k ' for which the equation $x^2 + kx + 64 = 0$ and $x^2 - 8x + k = 0$ will both have real roots.



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36. Find the value(s) of k for which the given quadratic equations has real and distinct roots :

(i) $2x^2 + kx + 4 = 0$ (ii) $4x^2 - 3kx + 1 = 0$

(iii) $kx^2 + 6x + 1 = 0$ (iv) $x^2 - kx + 9 = 0$



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37. For what value(s) of λ the quadratic equation

$$x^2 + \lambda x + (\lambda + 1.25) = 0 \text{ has :}$$

(i) coincident roots (ii) real and distinct roots (iii) no real roots?



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38. For what value(s) of k the quadratic equation

$$x^2 + kx + 1 = 0 \text{ can be factorised into a product of}$$

real linear factors?



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39. If the equation $(1 + m^2)x^2 + 2mcx + (c^2 - a^2) = 0$ has equal roots, prove that $c^2 = a^2(1 + m^2)$.

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40. In a $\triangle ABC$ the value of $\angle A$ is given by $5 \cos A - 3 = 0$ then the equation whose roots are $\sin A$ and $\tan A$ is :

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41. For what value of n , the quadratic equation $3^n x^2 + 54x + 81^n = 0$ have coincident roots?



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42. The sum of a number and its reciprocal is $\frac{10}{3}$, find the number(s).



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43. Divide 16 into two parts such that twice the square of the larger part exceeds the square of the smaller part by 164.



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44. The sum of the squares of three consecutive natural numbers is 149. Find the numbers.



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45. A two digit number is such that the product of its digits is 8. When 63 is subtracted from the number digits interchange their places. Find the number.



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46. The denominator of a fraction is one more than twice the numerator. If the sum of the fraction and its reciprocal is $2\frac{16}{21}$, find the fraction.



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47. The hypotenuse of a right triangle is 6 m more than the twice of the shortest side. If the third side is 2 m less than the hypotenuse, find the sides of the triangle.



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48. a, b and c are the integral sides of a right angled triangle in which c is the hypotenuse measuring $3\sqrt{5}$ metres. If side 'a' is increased by $\frac{400}{3}\%$ and side 'b' is increased by $\frac{50}{3}\%$, then their total becomes 14 metres. Find the area of triangle.



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49. The age of a father is twice the square of the age of his son. Eight years hence, the age of his father will be 4 years more than 3 times the age of the son. Find their present ages.

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50. The sum of the reciprocals of Rehman's ages, (in years) 3 years ago and 5 years from now is $\frac{1}{3}$. Find his present age.

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51. Two taps running together can fill a tank in $3\left(\frac{1}{13}\right)$ hours. If one tap takes 3 hours more than the other to fill the tank, then how much time will each tap take to fill the tank ?

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52. A takes 6 hours less than B to complete a work. If together they complete the work in 13 hours 20 minutes, find how much time will B alone take to complete the work.



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53. The diagonal of a rectangular field is 60 metres more than the shorter side. If the longer side is 30 metres more than the shorter side, find the sides of the field.



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54. An aeroplane takes 1 hour less for a journey of 1200 km if its speed is increased by 100 km/hr from its usual speed. Find its usual speed.



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55. A train travels a distance of 300 km at constant speed. If the speed of the train is increased by 5 km an hour, the journey would have taken 2 hours less. Find the original speed of the train.



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56. The speed of a boat in still water is 15 km/hr. It can go 30 km upstream and return downstream to the original point in 4 hours 30 minutes. Find the speed of the stream.

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57. A dealer sells an article for Rs. 24 and gains as much percent as the cost price of the article. Find the cost price of the article.

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58. One fourth of a herd of camels was seen in the forest. Twice the square root of the herd had gone to mountains and the remaining 15 camels were seen on the bank of a river. Find the total number of camels.



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59. Out of a number of saras birds, one-fourth of the number are moving about in lotus plants, $\frac{1}{9}$ th coupled along with $\frac{1}{4}$ th as well as 7 times the square root of the number move on a hill. 56 birds remain in vakula trees. What is the total number of birds?



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60. The total cost of a certain length of cloth is $Rs200$. If the piece was 5 m longer and each metre of cloth costs $Rs2$ less, the cost of the piece would have remained unchanged. How longer is the piece and what is its original rate per metre?



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61. Some students planned a picnic. The budget for food was $Rs.480$. But, 8 of these failed to go and thus the cost of food for each member increased by $Rs 10$. How many students attended the picnic?



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63. A group of students decided to buy an. F.M. Radio (transistor) from 256 to 300 rupees. But at the last moment two students backed out of the decision so that the remaining students had to pay one rupee each more than they had planned. What was the price of F.M. Radio, if the students paid equal shares?

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64. A swimming pool is filled with three pipes with uniform flow. The first two pipes creating simultaneously, fill the pool in the same time during which the pool is filled by the third pipe alone. The second pipe fills the pool five hours faster than the first pipe and four hours slower than the third pipe. Find the time required by each pipe to fill the pool separately.



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Problems From Ncert Exemplar

1. Solve the following quadratic equations :

(i) $x^2 - 45x + 324 = 0$ (ii) $x^2 - 55x + 750 = 0$



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2. The altitude of a right triangle is 7 cm less than its base. If the hypotenuse is 13 cm, find the other two sides.



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3. A cottage industry produces a certain number of pottery articles in a day. It was observed on a

particular day that the cost of production of each article (in rupees) was 3 more than twice the number of articles produced on that day. If the to

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4. Find the roots of the following equations : (i)

$$x - \frac{1}{x} = 3, x \neq 0 \quad \text{(ii)}$$

$$\frac{1}{x+4} - \frac{1}{x-7} = \frac{11}{30}, x \neq -4, 7$$

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5. The difference of squares of two numbers is 180. The square of the smaller number is 8 times the

larger number. Find the two numbers.



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6. Find the values of k for each of the following quadratic equations, so that they have two equal roots. (i) $2x^2 + kx + 3 = 0$ (ii) $kx(x - 2) + 6 = 0$



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7. Which of the following is a quadratic equation?

(i) $x^2 + 2x + 1 = (4 - x)^2 + 3$ (ii)

$-2x^2 = (5 - x) \left(2x - \frac{2}{5} \right)$

(iii) $(k + 1)x^2 + \frac{3}{2}x = 7$ where $k = -1$ (iv)

$$x^3 - x^2 = (x - 1)^3$$

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8. Find the roots of the following quadratic equations by the factorisation method.

$$2x^2 + \frac{5}{3}x - 2 = 0$$

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9. A natural number when increased by 12, equals 160 times its reciprocal. Find number.

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10. A train, travelling at a uniform speed for 360 km, would have taken 48 minutes less to travel the same distance if its speed were 5 km/h more. Find the original speed of the train.

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11. The quadratic equation $2x^2 - \sqrt{5}x + 1 = 0$ has
(a) two distinct real roots (b) two equal real roots
(c) no real roots (d) more than 2 real roots

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12. $(x^2 + 1)^2 - x^2 = 0$ has



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13. Does there exist a quadratic equation whose coefficients are rational but both of its roots are irrational? Justify your answer.



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14. Does there exist a quadratic equation whose coefficients are all distinct irrationals but both the roots are rationals?



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15. Find a natural number whose square diminished by 84 is equal to thrice of 8 more than the given number.



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16. If Zeba were younger by 5 years than what she really is, then the square of her age (in years) would have been 11 more than five times her actual age.

What is her age now?



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17. At t minutes past 2 pm, the time needed by the minutes hand of a clock to show 3pm was found to be 3 minutes less than $\frac{t^2}{4}$ minutes. Find t .



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Exercise 4 A

1. Which of the following are quadratic equations?

(i) $x^2 + 8x + 12 = 0$ (ii) $x + \frac{1}{x} = 5$ (iii) $x + \frac{5}{x} = x^2$

(iv) $x^2 - 5\sqrt{x} + 7 = 0$ (v) $x^2 - 5x - \sqrt{x} + 4 = 0$ (vi)

$x^2 - \frac{1}{x^2} = 4$

$$(vii) \quad 5x^2 - 7x = 3x^2 - 7x + 3 \quad (viii)$$

$$\frac{1}{4}x^2 + \frac{7}{6}x - 2 = 0$$

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2. Represent the following situations mathematically:

(i) John and Jivanti together have 45 marbles. Both of them lost 5 marbles each and the product of the number of marbles they now have is 124. We would like to find out how many marbles they had to start with.

A cottage industry produces a certain number of toys in a day. The cost of production of each toy (in

rupees) was found to be 55 minus the number of toys produced in a day. On a particular day, the total cost of production was RS.750. We would like to find out the number of toys produced on that day.



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3. Which of the following are roots of

$$4x^2 - 9x - 100 = 0?$$

(i) -4 (ii) $\frac{3}{4}$ (iii) $\frac{25}{4}$



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4. If one root of the quadratic equation $6x^2 - x - k = 0$ is $\frac{2}{3}$, then find the value of k .



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5. Solve each of the following equations :

$$3x^2 - 243 = 0$$



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6. Solve each of the following equations :

$$5x^2 + 4x = 0$$



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7. Solve each of the following equations :

$$x^2 + 12x + 35 = 0$$



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8. Solve each of the following equations :

$$2x^2 - 5x + 3 = 0$$



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9. Solve each of the following equations :

$$6x^2 - x - 2 = 0$$



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10. Solve the following equatins for x:

$$8x^2 - 22x - 21 = 0$$



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11. Solve each of the following equatins :

$$9x^2 + 6x + 1 = 0$$



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12. Solve each of the following equations :

$$48x^2 - 13x - 1 = 0$$



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13. Solve each of the following equations :

$$6x^2 + 40 = 31x$$



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14. Factorize $\sqrt{3}x^2 + 11x + 6\sqrt{3}$



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15. Solve each of the following equations :

$$3\sqrt{7}x^2 + 4x - \sqrt{7} = 0$$



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16. Solve each of the following equations :

$$2\sqrt{5}x^2 - 3x - \sqrt{5} = 0$$



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17. Solve each of the following equations :

$$x^2 + 5 = \frac{9}{2}x$$



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18. Solve each of the following equations :

$$x = \frac{3x + 1}{4x}$$



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19. Solve each of the following equations :

$$x + \frac{1}{x} = 2.5$$



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20. Solve each of the following equations :

$$5x - \frac{35}{x} = 18, x \neq 0$$



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21. Solve each of the following equations :

$$\frac{2}{x^2} - \frac{5}{x} + 2 = 0, x \neq 0$$



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22. Solve each of the following equations :

$$a^2x^2 + 2ax + 1 = 0$$



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23. Solve each of the following equations :

$$x^2 - (p + q)x + pq = 0$$



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24. Solve each of the following equations :

$$a^2x^2 + (a^2 + b^2)x + b^2 = 0$$



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25. Solve $12abx^2 - 9a^2x + 8b^2x - 6ab = 0$



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26. Solve each of the following equations :

$$4x^2 - 4ax + (a^2 + b^2) = 0$$



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27. Solve each of the following equations :

$$\frac{x + 1}{x - 1} = \frac{3x - 7}{2x - 3}$$



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28. Solve each of the following equations :

$$\frac{5}{2x + 1} + \frac{6}{x + 1} = 3$$



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29. Solve each of the following equations :

$$\frac{x + 3}{x - 2} - \frac{1 - x}{x} = 4\frac{1}{4}$$



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30. Solve the following equations :

$$2\left(\frac{x}{x + 1}\right)^2 - 5\left(\frac{x}{x + 1}\right) + 2 = 0 \quad x \neq -1$$



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31. Solve $\sqrt{\frac{x}{1 - x}} + \sqrt{\frac{1 - x}{x}} = \frac{13}{6}$



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32. Solve each of the following equations :

$$\left(\frac{2x-3}{x-1}\right) - 4\left(\frac{x-1}{2x-3}\right) = 3, x \neq 1, \frac{3}{2}$$



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33. Solve each of the following equations :

$$2^{2x+3} - 57 = 65(2^x - 1)$$



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34. Solve each of the following equations :

$$2^{2x} - 3 \times 2^{x+2} + 32 = 0$$

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35. Solve each of the following equations :

$$x^{2/3} + x^{1/3} - 2 = 0$$

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36. Solve for x :

$$\frac{a}{ax - 1} + \frac{b}{bx - 1} = a + b; x \neq \frac{1}{a}, \frac{1}{b}$$

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37. Solve the following quadratic equations by factorization method:

$$\frac{1}{a + b + x} = \frac{1}{a} + \frac{1}{b} + \frac{1}{x}, \quad a + b \neq 0$$



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Exercise 4 B

1. Find the roots of the following quadratic equations by the method of completing the square :

(i) $x^2 - 10x - 24 = 0$ (ii) $2x^2 - 7x - 39 = 0$

(iii) $5x^2 + 6x - 8 = 0$



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2. Solve the following equations by using quadratic formula:

$$2x^2 - 9x + 7 = 0$$



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3. Solve the following equations by using quadratic formula:

$$5x^2 - 19x + 17 = 0$$



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4. Solve the following equations by using quadratic formula:

$$x^2 - 18x + 77 = 0$$



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5. Solve the following equations by using quadratic formula:

$$\frac{2}{3}x = -\frac{1}{6}x^2 - \frac{1}{3}$$



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6. Solve the following equations by using quadratic formula:

$$\frac{1}{15}x^2 + \frac{5}{3} = \frac{2}{3}x$$



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7. Solve the following equations by using quadratic formula:

$$\sqrt{6}x^2 - 4x - 2\sqrt{6} = 0$$



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8. Solve the following quations by using qaradratic formula:

$$256x^2 - 32x + 1 = 0$$



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9. Solve the following quations:

$$(2x + 3)(3x - 2) + 2 = 0$$



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10. Solve the following quations by using qaradratic formula:

$$\frac{x-2}{x+2} + \frac{x+2}{x-1} = 4$$



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11. Solve the following equations by using quadratic formula:

$$\frac{1}{x-2} + \frac{1}{x-3} + \frac{1}{x-4} = 0$$



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12. Solve the question:

$$x^2 - 16 = 0$$



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13. Solve the following equations by using quadratic formula:

$$36x^2 - 12ax + (a^2 - b^2) = 0$$



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14. Solve the following equations by using quadratic formula:

$$p^2x^2 + (p^2 - q^2)x - q^2 = 0$$



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15. Solve the following equations by using quadratic formula:

$$abx^2 + (b^2 - ac)x - bc = 0$$



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16. Solve the following equations by using quadratic formula:

$$12abx^2 - (9a^2 - 8b^2)x - 6ab = 0$$



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1. Determine the nature of roots of the following quadratic equations:

(i) $2x^2 + 5x - 4 = 0$ (ii) $9x^2 - 6x + 1 = 0$

(iii) $3x^2 + 4x + 2 = 0$ (iv) $x^2 + 2\sqrt{2}x + 1 = 0$

(v) $x^2 + x + 1 = 0$ (vi) $x^2 + ax - 4 = 0$

(vii) $3x^2 + 7x + \frac{1}{2} = 0$

(viii) $3x^2 - 4\sqrt{3}x + 4 = 0$

(ix) $2\sqrt{3}x^2 - 5x + \sqrt{3} = 0$ (x)

$(x - 2a)(x - 2b) = 4ab$



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2. Without determining the roots of the following equations comment their nature:

$$(i) \quad 6\sqrt{3}x^2 - 4x + \sqrt{3} = 0 \quad (ii)$$

$$9a^2b^2x^2 - 48abcdx + 64c^2d^2 = 0$$

$$(iii) \quad a^2x^2 + 2abx = b^2, a^2 \neq 0 \quad (iv)$$

$$2(a^2 + b^2)x^2 + 2(a + b)x + 1 = 0$$

$$(v) \quad (b + c)x^2 - (a + b + c)x + a = 0$$



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3. Find the values of k for which roots of the following equations are real and equal:

(i) $12x^2 + 4kx + 3 = 0$ (ii) $kx^2 - 5x + k = 0$

(iii) $x^2 + k(4x + k - 1) + 2 = 0$



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4. In the following determine the set of values of k for which the given quadratic equation has real roots :

(i) $2x^2 + 5x - k = 0$ (ii) $kx^2 - 6x - 2 = 0$

(iii) $9x^2 + 3kx + 4 = 0$ (iv) $kx^2 + 2x - 3 = 0$



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5. If the roots of the equation $(b - c)x^2 + (c - a)x + (a - b) = 0$ are equal, then

prove that $2b = a + c$



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6. If -5 is a root of the quadratic equation $2x^2 + px - 15 = 0$ and the quadratic equation $p(x^2 + x) + k = 0$ has equal roots, find the value of k .



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7. If 1 is a root of the quadratic equation $3x^2 + ax - 2 = 0$ and the quadratic equation

$a(x^2 + 6x) - b = 0$ has equal roots, find the value of b .

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8. If the equation $(a^2 + b^2)x^2 - 2(ac + bd)x + c^2 + d^2 = 0$ has equal roots, then

(a) $ab = cd$ (b) $ad = bc$ (c) $ad = \sqrt{bc}$ (d) $ab = \sqrt{cd}$

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9. Prove that the equation $x^2(a^2 + b^2) + 2x(ac + bd) + (c^2 + d^2) = 0$ has no

real root, if $ad \neq bc$.



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10. If the roots of the equation $(c^2 - ab)x^2 - 2(a^2 - bc)x + b^2 - ac = 0$ are equal, prove that either $a = 0$ or $a^3 + b^3 + c^3 = 3abc$.



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11. Show that the equation $2(a^2 + b^2)x^2 + 2(a + b)x + 1 = 0$ has not real roots, when $a \neq b$.



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12. If $a, b, c \in R$, show that roots of the equation $(a - b)x^2 + (b + c - a)x - c = 0$ are real and unequal,



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Exercise 4 D

1. the sum of a number and its reciprocal is $\frac{61}{30}$ Find the number



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2. Divide 15 into two parts such that the sum of their reciprocals is $\frac{3}{10}$.

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3. Find two natural numbers which differ by 3 and whose squares have the sum 117.

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4. Divide 57 into two parts whose product is 782.

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5. The sum of the squares of three consecutive natural numbers is 77. Find the numbers.



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6. Find two consecutive odd natural numbers whose product is 323.



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7. The product of two numbers is 12. If their sum added to the sum of their squares is 32, find the numbers.



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9. Determine two consecutive multiples of 3 whose product is 270.



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10. Three consecutive positive integers are such that the sum of the square of the first and the product of

other two is 46, find the integers.



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11. A number consists of two digits. The product of these digits is 14. If 45 is subtracted from the number, the digits interchange their places. Find the number.



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12. A two digit number is four times the sum and three times the product of its digits.



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13. In a two digit number, the ten's digit is bigger. The product of the digits is 27 and the difference between two digits is 6. Find the number.



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14. A two digit number is made of two consecutive digits such that the sum of their squares is 4 less than the number. Find the two digit number.



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15. In a certain positive fraction, the denominator is greater than the numerator by 3. If 1 subtracted from both the numerator and denominator, the fraction is decreased by $\frac{1}{14}$. Find the fraction.



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16. The denominator of a positive fraction is one more than twice the numerator. If the sum of the fraction and its reciprocal is 2.9, find the fraction,



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17. The numerator of a fraction is 4 less than the denominator. If 1 is added to both its numerator and denominator, it becomes $\frac{1}{2}$. Find the fraction.

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18. The numerator of a fraction is 4 less than denominator. If 1 is added to both its numerator and denominator, it becomes $\frac{1}{2}$. Find the fraction.

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19. The sides of a right angled triangle containing the right angle are $4x$ cm and $(2x-1)$ cm. If the area of the triangle is 30cm^2 calculate the lengths of its sides.



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20. The hypotenuse of a right triangle is 13 cm and the difference between the other two sides is 7cm. Find the two unknown side of the triangle.



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21. The longest side of a right angled triangle is 4cm longer than one side and 2 cm longer than the other side. Find the longest side.



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22. In a triangle the measure of the greatest angle is square of measure of the smallest angle and the other angle is double of the smaller angle. Find the greatest angle of the triangle.



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23. The hypotenuse of a right triangle is $3\sqrt{10}cm$. If the smaller leg is tripled and the longer leg doubled, new hypotenuse will be $9\sqrt{5}cm$. How long are the legs of the triangle?



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24. A square lawn has a path 2m wide around it. The area of the path is 196 sq. m. Find the length of the side of the lawn.



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25. the number of seats in a row is equal to the total number of rows in a hall .the total number of seats in the hall will increase by 375. If the number of rows is doubled and the number of seats in each row is reduced by 5 find the number of rows in the hall



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26. The area of a rectangular field is $260m^2$. Had its length been 5 m less and the breadth 2m more, the field would have been in the shape of a square. Find the perimeter of the field.



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27. A chess board contains 64 equal squares and the area of each square is 6.25 cm^2 . A border round the board is 2 cm wide. Find the length of the side of the chess board.



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28. A girl is twice as old as her sister. Four years hence, the product of their ages (in years) will be 160. Find their present ages.



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29. The product of Ramus age (in years) five years ago with his age (in years) 9 years later is 15. Find Ramus present age.



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30. Mrs. Mehra has two sons, one being exactly one year older than the other. At present, her age is equal to the sum of squares of ages of her sons. If 4 years hence her age becomes five times the age of the elder son then find the present ages of her sons.



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31. The sum of ages of a boy and his brother is 25 years, and the product of their ages in years is 126. Find their ages.



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32. A takes 6 days less than the time taken by B to finish a piece of work. If both A and B together can finish it in 4 days . Find the time taken by B to finish the work.



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33. One pipe can fill a cistern in 3 hours less than the other. The two pipes together can fill the cistern in 6 hours 40 minutes. Find the time that each pipe will take to fill the cistern.



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34. A train travels a distance of 300 km at constant speed. If the speed of the train is increased by 5 km an hour, the journey would have taken 2 hours less. Find the original speed of the train.



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35. A plane left 30 minutes late than its scheduled time and in order to reach the destination 1500 km away in time, it had to increase the speed by 100 km/h from the usual speed. Find its usual speed.



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37. The distance by road between two towns A and B, is 216 km, by rail it is 208 km. If car travels at a speed

of x km/h, and train travel at a speed which is 16 km/h fastest than the car. Calculate (i) The time taken by the car, to reach town B from A, in terms of x .



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38. The speed of a boat in still water is 15 km/hr. It can go 30 km upstream and return downstream to the original point in 4 hours 30 minutes. Find the speed of the stream.



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39. The speed of a boat in still water is 9 km/hr. It can go 12 km upstream and 12 km downstream in 3 hours. Find the speed of the stream.



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41. A trader bought a number of articles for RS.1200. Ten were damaged and he sold each of the rest at RS. 2 more than what he paid for it, thus clearing a profit

of RS.60 on the whole transaction. Find the number of articles he bought.



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42. Mohan sold an article for RS.56 which cost him RS.x. He finds that he has gained $x\%$ on his outlay. Find x.



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43. A shopkeeper purchase a certain number of books for Rs 960. If the cost per books was Rs 8 less, the number of books that could be purchased for Rs 960

would be 4 more. Write an equation, taking the original cost of each book to be Rs x , and solve it to find their original cost of the books.



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44. The hotel bill for a number of persons for overnight stay is Rs 4,800. If there were four more persons, the bill each person had to pay would have reduced by Rs 200. Find the number of persons staying overnight.



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45. In an auditorium, seats are arranged in rows was equal to the number of seats in each row. When the number of rows was doubled and the number of seats in each row was reduced by 10, the total number of seats increased by 300. Find the number of rows in original arrangement.



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46. At an annual function of a school each student gives gift to every other student. If the number of gifts is 1980, find the number of students.



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47. A line segment AB is 8 cm in length. AB is produced to P such that $BP^2 = AB \cdot AP$, find the length of BP .



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48. The product of 12% of an integer and 20% of the next integer is 61.2. Find the integer.



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49. Girl! Out of a group of swans, $\frac{7}{2}$ times the square root of the number are playing on the shore of a tank. The two remaining ones are playing, with amorous fight, in the water. What is the total number of swans?

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50. In a class test, the sum of the marks obtained by P in Mathematics and science is 28. Had he got 3 marks more in Mathematics and 4 marks less in Science. The product of his marks, would have been 180. Find his marks in the two subjects.

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51. The angry Arjun carried some arrows for fighting with Bheeshm. With half the arrows, he cut down the arrows thrown by Bheeshm on his and with six other arrows he killed the rath driver of Bheeshm. With one arrow each he knocked down respectively the rath, flag and the bow of Bheeshm. Finally, with one more than four times the square root of arrows he laid Bheeshm unconscious on an arrow bed. Find the total number of arrows Arjun had.



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52. A piece of cloth costs RS.75. If the piece were 4 metre longer and each metre costs RS.5 less, the total cost would remain unchanged. How long is the piece?



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53. Everybody in a room shakes hands with everybody else. If the total number of handshakes is 66, then the total number of handshakes is 66, then the total number of persons in the room is:



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54. P and Q are centres of circles of radii 9 cm and 2 cm respectively. $PQ = 17$ cm. R is the centre of a circle of radius x cm which touches the above circles externally. Given that $\angle PRQ = 90^\circ$, write an equation in x and solve it.



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55. There is a two-digit number whose digits are the same, and has got the following property : when squared, it produces a four-digit number, whose first two digits are the same and equal to the original's

minus one, and whose last two digits are the same and equal to half of the original's. Find that number.



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Revision Exercise Very Short Answer Questions

1. Show that $x = 3$ is the solution of $2x^2 - 5x - 3 = 0$



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2. Show that $x = -2\sqrt{2}$ is the solution of

A. $x^2 + \sqrt{2}x - 4 = 0$

B. $x^2 + \sqrt{2}x - 8 = 0$

C. $x^2 + \sqrt{4}x - 8 = 0$

D. none of these

Answer: N/A



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3. If $x = -\frac{1}{2}$ is a solution of the quadratic equation

$3x^2 + 2kx - 3 = 0$, find the value of k .



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4. Solve $(x - 2)(x + 3) = 0$.



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5. Solve $8x^2 - 16x = 0$.



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6. Solve $6x^2 - x - 2 = 0$.



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7. If $x = 1$ is a root of $x^2 + kx + 5 = 0$,

A. $k = 5$

B. $k = 6$

C. $k = -6$

D. none of these

Answer: C



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8. Show that the equation $x^2 + 5x - 6 = 0$ has real roots.

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9. If the roots of the quadratic equation

$2x^2 + 8x + k = 0$ are equal, find the value of k .

A. $k = 0$

B. $k = 4$

C. $k = 8$

D. $k = 2$

Answer: C

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10. Find the nature of roots of the quadratic equation

$$4x^2 - 5x + 3 = 0.$$



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11. Check whether the equation

$(x + 1)^3 = x^3 + x + 6$ is a quadratic equation or not.

A. yes, it is a quadratic equation

B. it will be cubic equation

C. it will be a linear equation

D. none of these

Answer: A



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12. Solve the equation $x^2 - 45x + 324 = 0$.



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13. Find the value of k if the quadratic equation

$kx(x - 2) + 6 = 0$ has two equal roots.



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14. Find the value(s) of k so that, the quadratic equation $x^2 - 4kx + k = 0$ has equal roots.



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15. If one root of the quadratic equation $3x^2 - 10x + k = 0$ is reciprocal of the other, find the value of k .



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Revision Exercise Short Answer Questions

1. Solve by factorization: $4\sqrt{3}x^2 + 5x - 2\sqrt{3} = 0$

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2. Solve $9x^2 - 9(a + b)x + 5ab + 2b^2 = 0$.

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3. Find the value of k for which the quadratic equation $(k + 4)x^2 + (k + 1)x + 1 = 0$

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4. Solve by factorization: $2x^2 + ax - a^2 = 0$



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5. Solve $x^2 - (\sqrt{3} + 1)x + \sqrt{3} = 0$.



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6. Solve $x^2 + 5x - (a^2 + a - 6) = 0$.



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7. Solve the following quadratic equation for x .

$$x^2 - 4ax - b^2 + 4a^2 = 0$$



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8. The sum of two natural number is 28 and their product in 192. Find the numbers.



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9. Find the value of p for which the quadratic equation

$$(p + 1)x^2 + - 6(p + 1)x + 3(p + 9) = 0, p \neq - 1$$

has equal roots. Hence, find the roots of the equation.



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10. 5. Solve $12abx^2 - 9a^2x + 8b^2x - 6ab = 0$



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Revision Exercise Long Answer Questions

1. Solve the following quadratic equations by factorization method:

$$\frac{1}{a + b + x} = \frac{1}{a} + \frac{1}{b} + \frac{1}{x}, \quad a + b \neq 0$$



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2. Solve $5^{x+1} + 5^{2-x} = 5^3 + 1$



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3. find the roots of the following equation by applying the quadratic formula

$$x^2 - (2b - 1)x + (b^2 - b - 20) = 0$$



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4. Solve each of the following quadratic equations:

$$\frac{a}{(x-b)} + \frac{b}{(x-a)} = 2, x \neq b, a$$

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5. Solve for: $\frac{1}{2a+b+2x} = \frac{1}{2a} + \frac{1}{b} + \frac{1}{2x}$

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6. Using quadratic formula, solve the following equation for x : $abx^2 + (b^2 - ac)x - bc = 0$

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