



# MATHS

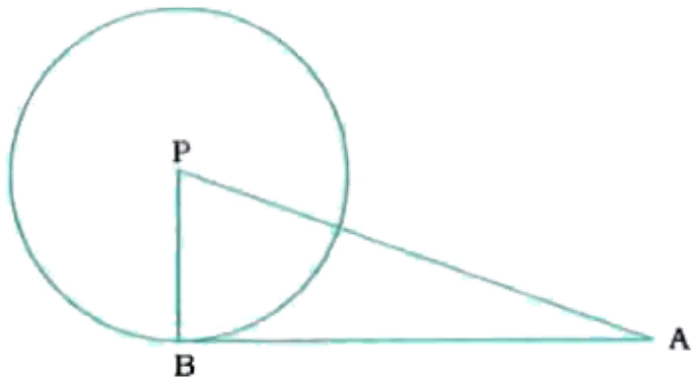
## BOOKS - KUMAR PRAKASHAN

### CIRCLE

#### Other Important Examples

1. Point  $a$  lies in the exterior of a circle with centre  $P$  and radius  $7\text{cm}$ . A tangent through  $A$

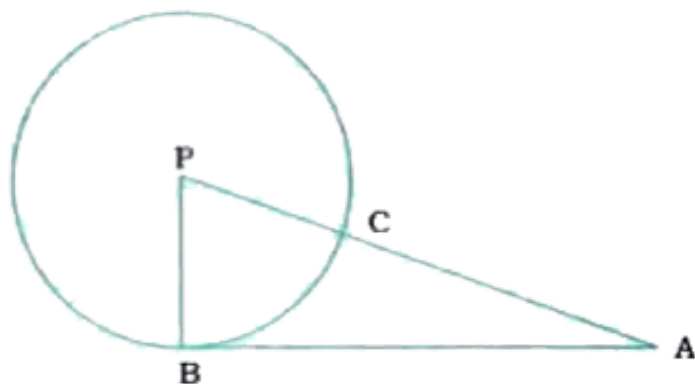
touches the circle at B . If  $AB = 24$  cm . Find PA.



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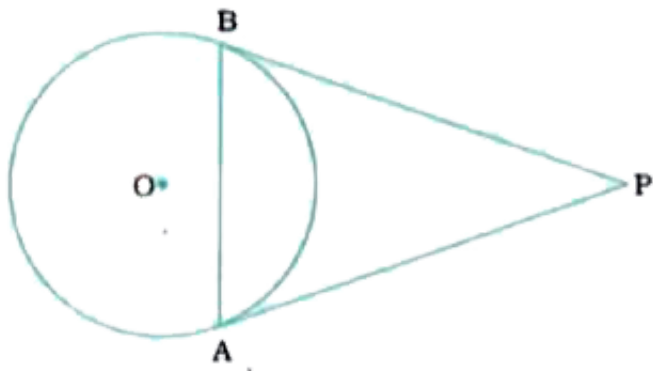
2. AB is a tangent to a circle with centre P and B is the point of contact. PA intersects the circle at C. If  $AB = 15$  cm and  $AC = 9$  cm, find the

radius of the circle.



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**3.** Prove that the tangent drawn at the ends of chord of a circle make equal angle with the



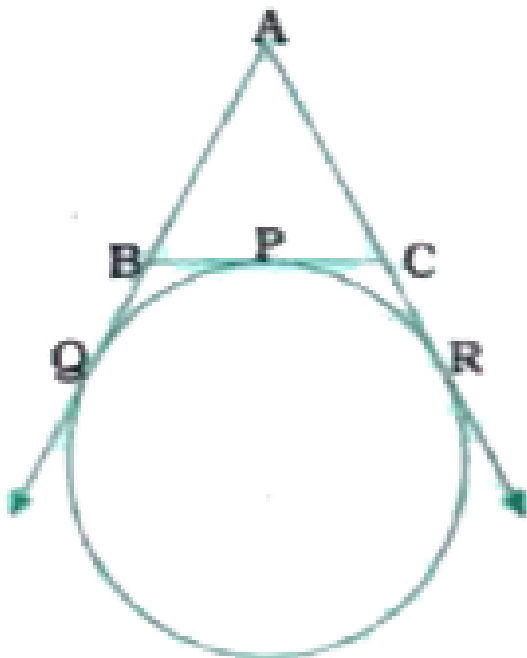
chord.



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4. A circle is touching the side  $BC$  of  $\triangle ABC$  at  $P$  and touching  $AB$  and  $AC$  extended at  $Q$  and  $R$  respectively. Prove that,  $AQ = \frac{1}{2}$  (perimeter of

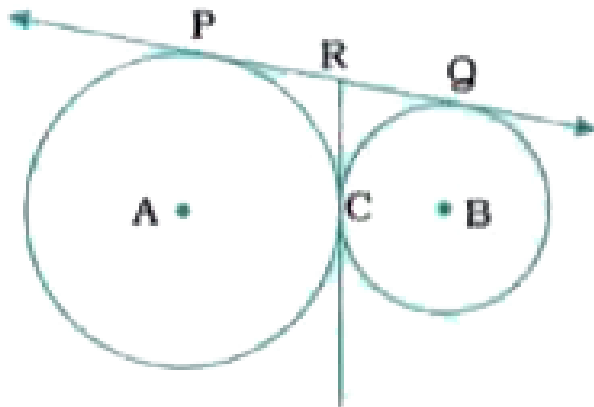
$\triangle ABC$ ).



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5. In the given figure, two circles with centres A and B touch each other at C bisects the

common tangent at P and Q.



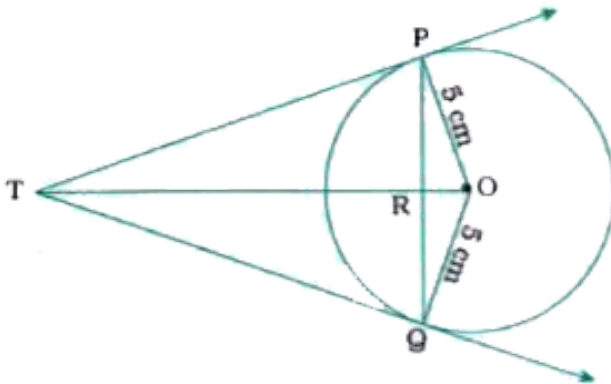
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6. If  $a$ ,  $b$ ,  $c$  are the side of a right triangle where  $c$  is the hypotenuse, prove that the radius of the circle which touches all the side of the triangle is given by  $r = \frac{a + b - c}{2}$ .



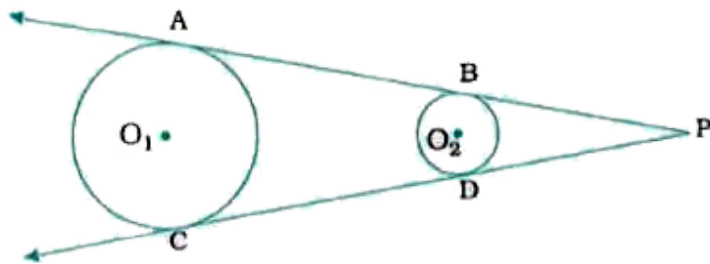
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7. PQ is a chord of length 8cm of circle of radius 5cm. The tangent at P and Q intersect at a point T. Find the length TP.



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8. As shown in the figure, AB and CD are two common tangents to circles with centres  $O_1$  and  $O_2$  and different radius. Prove that



$AB=CD$



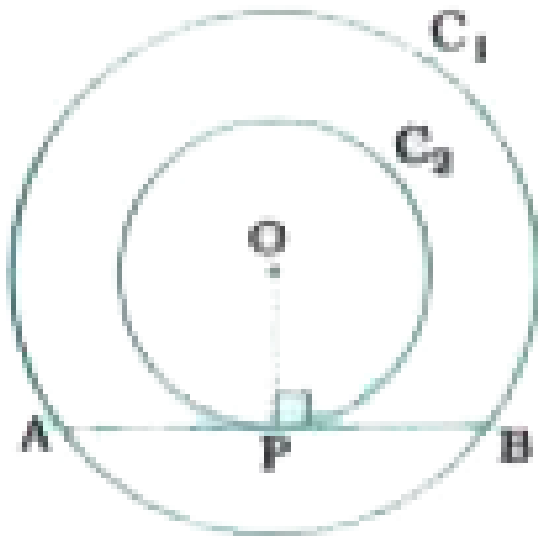
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Textual Examples



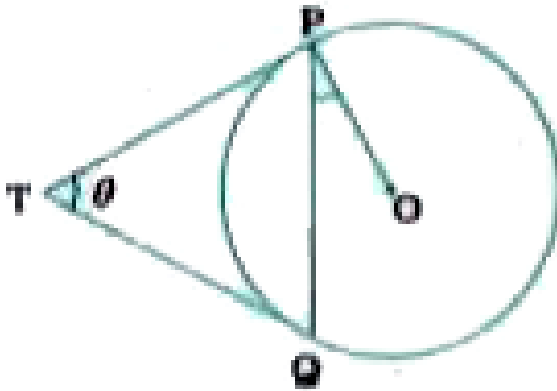
1. Prove that in concentric circles, the chord of the larger circle, which touches the smaller circle, is bisected at the point of contact.

**H.C.L.**



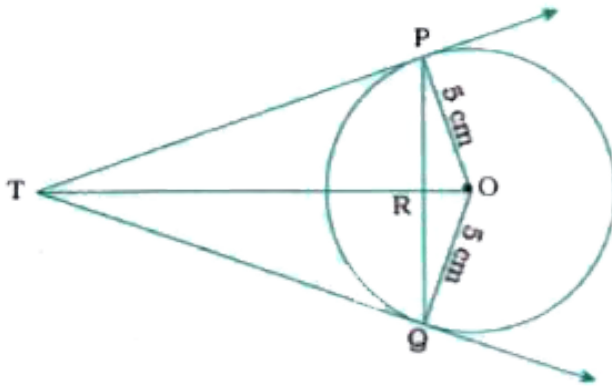
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2. Two tangent TP and TQ are drawn to a circle with centre O from an external point T. prove that  $\angle PTQ = 2\angle OPQ$ .



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3. PQ is a chord of length 8cm of circle of radius 5cm. The tangent at P and Q intersect at a point T. Find the length TP.



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**Test Your Skills**

1. Point S lies in the exterior of a circle with centre P and radius 33cm. A tangent from S touches the circle at T and  $ST=56\text{cm}$ . Find the distance of S from P.



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2. Point M lies in the exterior of a circle with centre A and a tangent from M touches the circle at N. If  $AM=41\text{cm}$  and  $MN=40\text{cm}$ , find the radius of the circle.



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3. XY is a tangent to a circle with centre O touching the circle at Y. If  $OX=61\text{cm}$  and the diameter of the circle is  $22\text{cm}$ , find XY.



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4. AB is a tangent to a circle with centre P touching the circle at B. PA intersects the circle at M. If  $AB=35\text{cm}$  and  $AM=25\text{cm}$ , find the diameter of the circle.



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5. PM is a tangent to a circle with centre O touching the circle at M. If  $OP=85\text{cm}$  and  $PM=77\text{cm}$ , find the radius of the circle.



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6. Out of two cocentric circles, the radius of the outer circle is  $25\text{cm}$  and the chord AC of length  $48\text{cm}$  is a tangent to the inner circle. Find the radius of the inner circle.



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7. Prove that a diameter  $AB$  of a circle bisects all those chords which are parallel to the tangent at the point  $A$ .



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8. Two tangent segments  $PA$  and  $PB$  are drawn to a circle with centre  $O$  such that  $\angle APB = 120^\circ$ . Prove that  $OP = 2AP$ .



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9. A circle touches all the four sides of a quadrilateral ABCD with  $AB=6\text{cm}$ ,  $BC=7\text{cm}$  and  $CD=4\text{cm}$ . Find AD.



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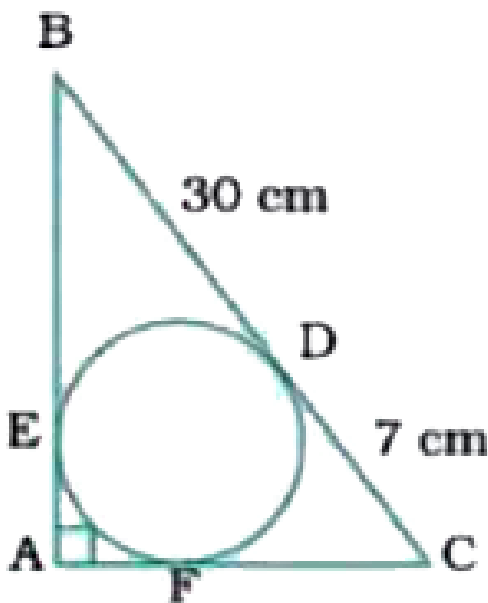
10. In  $\triangle ABC$   $AB=20\text{cm}$ ,  $BC=21\text{cm}$  and  $AC=29\text{cm}$ . Find the radius of the circle touching all the sides of  $\triangle ABC$ .



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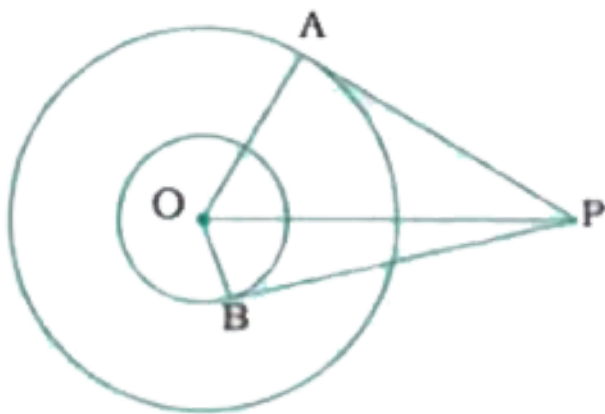


11. In the given figure, BC, BA and AC are tangents to the circle touching the circle at D, E and F respectively. If  $BD=30\text{cm}$ ,  $CD=7\text{cm}$  and  $\angle A = 90^\circ$ , find the radius of the circle.



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12. In the given figure, two concentric circles with centre  $O$  and radii  $5\text{cm}$  and  $3\text{cm}$  are given,  $PA$  and  $PB$  are tangents to those circle at  $A$  and  $B$  respectively. If  $PA = 12\text{cm}$ , find  $PB$ .



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## Practice Thoroughly

1. A point P is 26cm away from the centre O of a circle and the length PT of the tangent drawn from P to the circle is 10cm. Find the radius of the circle.



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2. AB is a diameter and AC is a chord of a circle with centre O such that  $\angle BAC = 30^\circ$ . The

tangent at C intersects AB at a point D. Prove that  $BC=BD$ .



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3. Prove that the tangent drawn at the midpoint of an arc of a circle is parallel to the chord joining the end points of the arc.



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4. If  $d_1, d_2 (d_2 > d_1)$  be the diameter of the two cocentric circles and  $c$  be the length of a chord of a circle which is tangent to the other circle, prove that  $d_2^2 = c^2 + d_1^2$ .



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5. From an external point P, tangent PA=PB are drawn to a circle with centre O. If  $\angle PAB = 50^\circ$ , then find  $\angle AOB$ .



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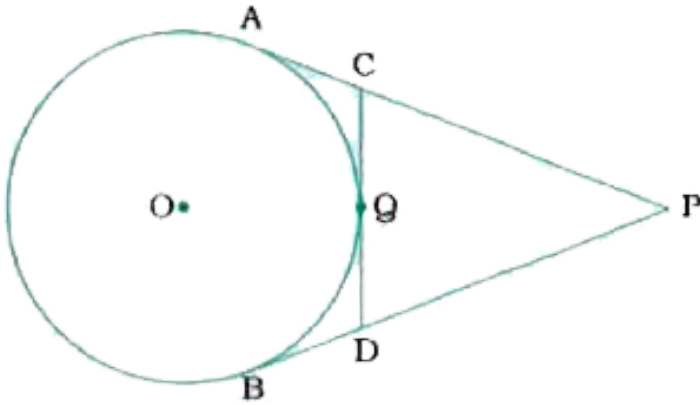
6. Two concentric circles are of diameters 30cm and 18cm. Find the length of the chord of the larger which touches the smaller circle.



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7. In the given figure, PA and PB are tangent to the circle from an external point P. CD is another tangent touching the circle at Q. If

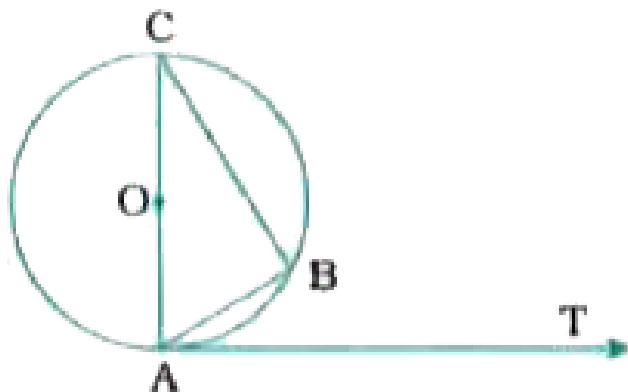
$PA=12\text{cm}$  and  $QC=QD=3\text{cm}$ , then find  $PC+PD$ .



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8.  $AB$  is a chord of a circle with centre  $O$ ,  $AC$  is a diameter and  $AT$  is the tangent at  $A$  as shown

in the figure. Prove that  $\angle BAT = \angle ACB$ .



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## Exercise 10 1

1. How many tangent can a circle have ?



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2. A tangent to a circle intersects it \_\_\_\_ points.



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3. A line intersecting a circle in two points is called a secant.



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4. A circle can have two parallel tangents. parallel to a secant at the most.



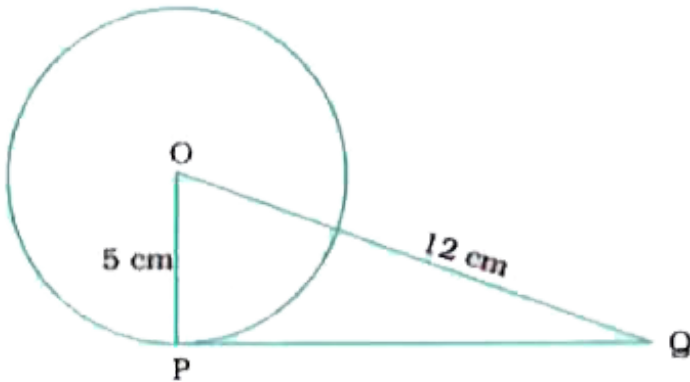
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5. The common point of a tangent to a circle and the circle is called the point of contact.



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6. A tangent PQ point P of a circle of radius 5cm meets a line through the centre O at a point Q so that OQ=12 cm. length PQ is :



A. 12cm

B. 13cm

C. 8.5cm

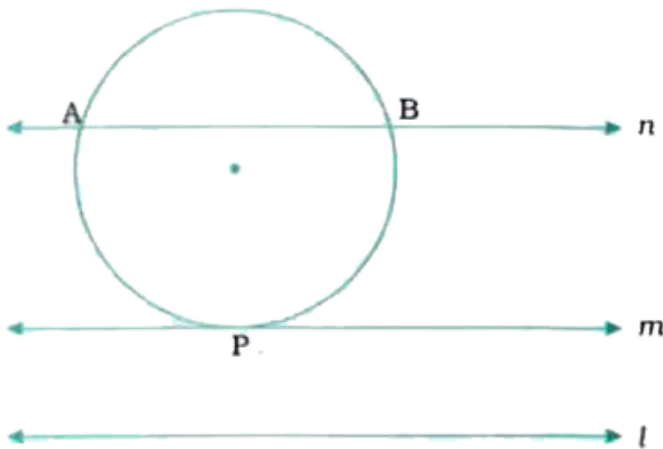
D.  $\sqrt{119}$ cm

**Answer: D**



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7. Draw a circle and two lines parallel to a given line such that one is tangent and the other, a secant to the circle.



## Exercise 10 2

1. From a point  $Q$ , the length of tangent to a circle is 24cm and the distance of  $Q$  from the centre is 25cm. The radius of the circle is.....

A. 7m

B. 12cm

C. 15cm

D. 24.5 cm

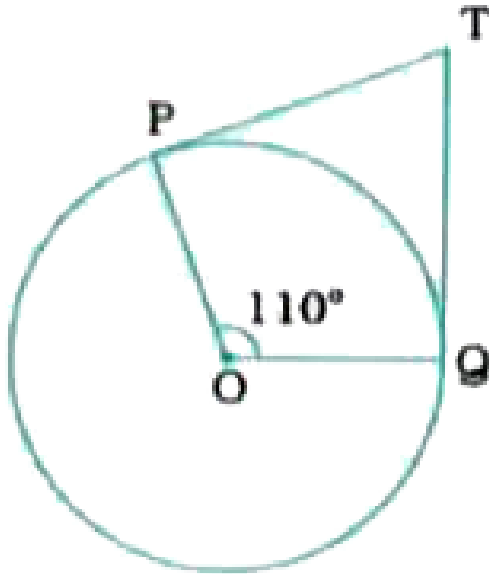
**Answer: A**



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2. In the given figure. If TP and TQ are the two tangents to a circle with centre O so that  $\angle$

$\angle POQ = 110^\circ$ , then  $\angle PTQ$  is equal to .....



A.  $60^\circ$

B.  $70^\circ$

C.  $80^\circ$

D.  $90^\circ$

**Answer: B**



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3. If tangent PA and PB from point P to a circle with centre O are inclined to each other at an angle of  $80^\circ$ . Then  $\angle POA = \dots\dots\dots$

A.  $50^\circ$

B.  $60^\circ$

C.  $70^\circ$

D.  $80^\circ$

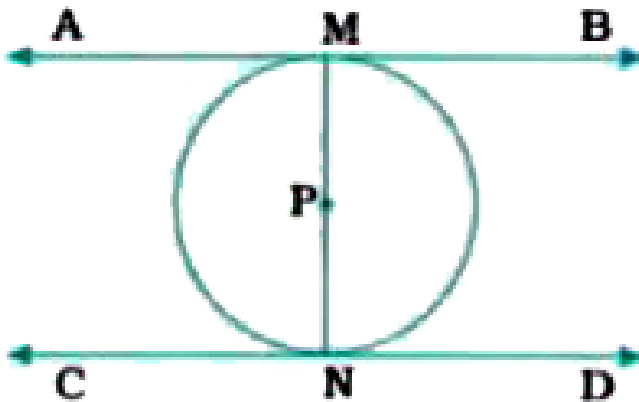


**Answer: A**



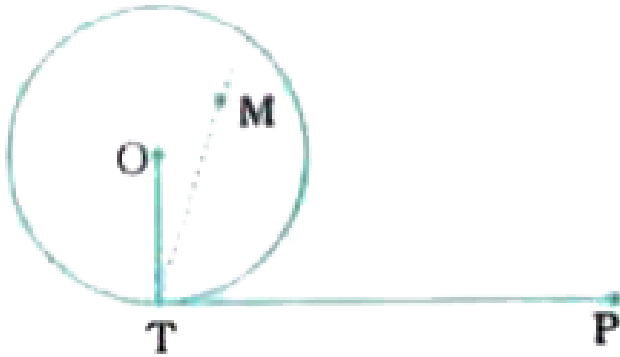
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4. Prove that tangent drawn at the ends of a diameter of a circle are parallel.



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5. Prove that perpendicular at the point of contact to the tangent to circle passes through the centre.



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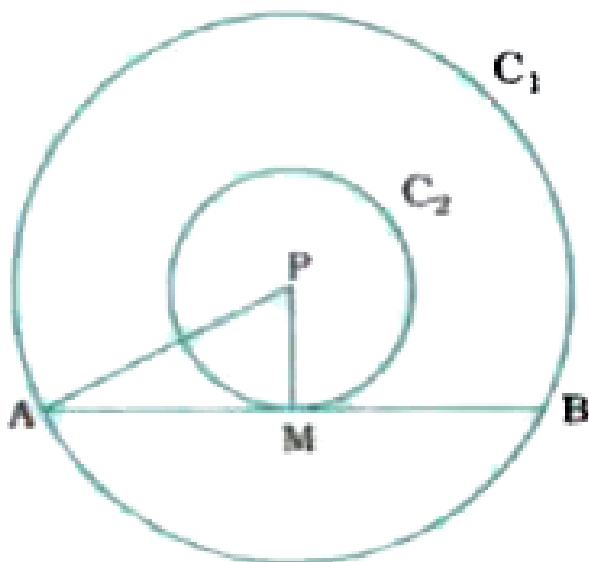
6. The length of a tangent from point A at distance 5cm from the center of the circle is 4cm. Find the radius of the circle.



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7. Two concentric circle are of radii 5cm and 3cm. Find the length of the chord of the larger

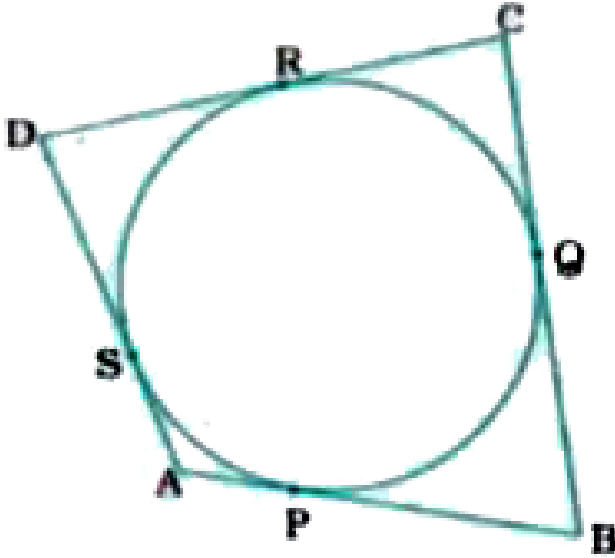
circle which touches the smaller circle.



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8. A quadrilateral  $ABCD$  is drawn to circumscribe a circle (see the given figure).

Prove that  $AB+CD = AD+BC$ .

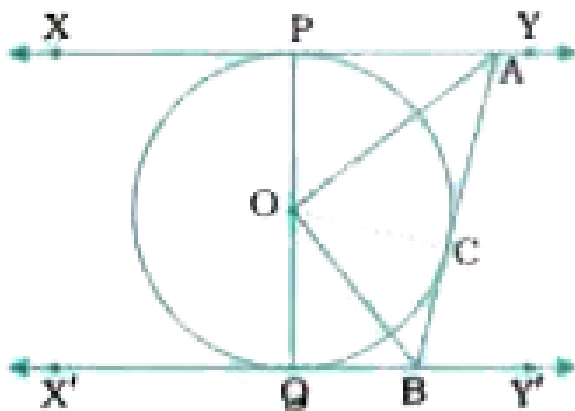


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9. In the given figure.  $XY$  and  $X'Y'$  are two parallel tangent to a circle with centre  $O$  and another tangent  $AB$  with point of contact  $C$  is

intersecting  $XY$  at  $A$  and  $X'Y'$  at  $B$ . Prove that

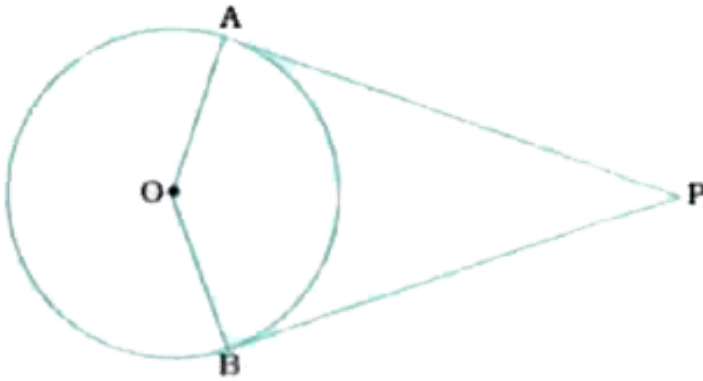
$$\angle AOB = 90^\circ$$



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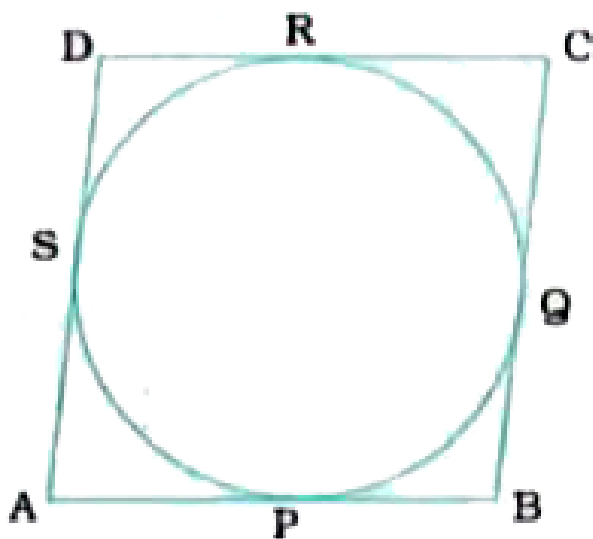
**10.** Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle

subtended by the line segment joining the point of contact at the centre.



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**11.** Prove that the parallelogram circumscribing a circle is a rhombus.

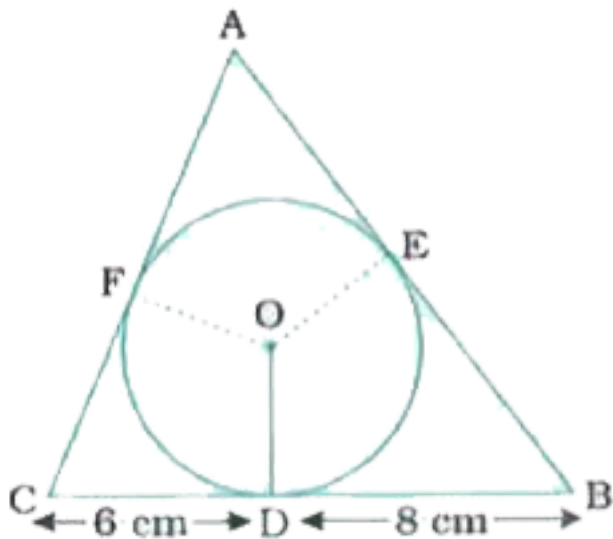


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**12.** A triangle  $ABC$  is drawn to circumscribe a circle of radius  $4\text{cm}$  such that the segment  $BD$  and  $DC$  into which  $BC$  is divided by the point of contact  $D$  are of lengths  $8\text{cm}$  and  $6\text{cm}$



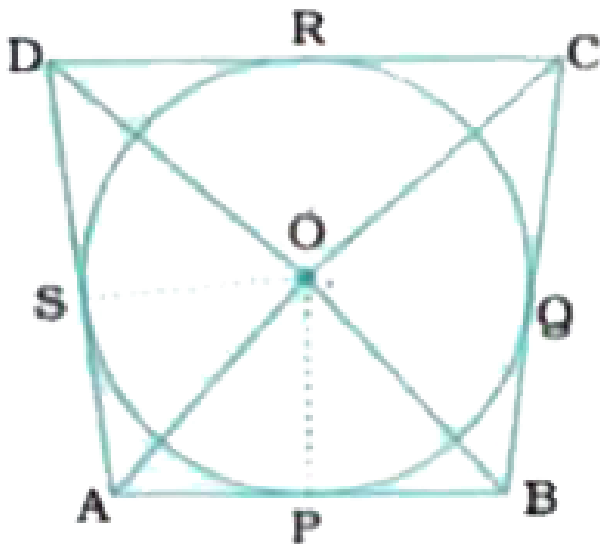
respectively. Find the sides AB and AC.



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**13.** Prove that opposite side of a quadrilateral circumscribing a circle subtend supple.

Central angle at the center of the circle.



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Objective Questions Fill In The Blanks

1. From a point Q. the length of tangent to a circle is 24cm and the distance of Q from the centre is 25cm. The radius of the circle is.....



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2. If tangent PA and PB from point P to a circle with centre O are inclined to each other at an angle of  $80^\circ$ . Then  $\angle POA = \dots\dots\dots$



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3. PQ is a tangent to a circle with centre O at the point P. If  $\triangle OPQ$  is an isosceles triangle, then  $\angle OQP = \dots\dots\dots$



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4. Two equal circle touch each other externally at C and AB is a common tangent to the circle. Then.  $\angle ACB = \dots\dots\dots$



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5. The four sides of quadrilateral ABCD are tangential to a circle. If  $AB = 7.2$  cm  $CD = \dots\dots\dots$ cm



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## Objective Questions

1. PQ is tangent drawn from point P to a circle with centre O and QR is a diameter of the circle, such that  $\angle POR = 120^\circ$ . Then,  $\angle OPQ = \dots\dots\dots$

A.  $60^\circ$

B.  $45^\circ$

C.  $30^\circ$

D.  $90^\circ$

**Answer: C**



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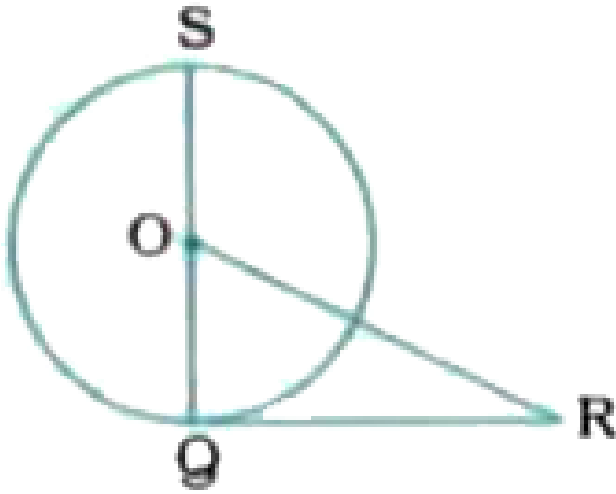
2. In the given figure, Rq is a tangent to the circle with centre O. if  $SQ = 6\text{cm}$  and  $QR = 4\text{cm}$ .

Then.

OR

=

.....cm.



A. 8

B. 3

C. 2.5

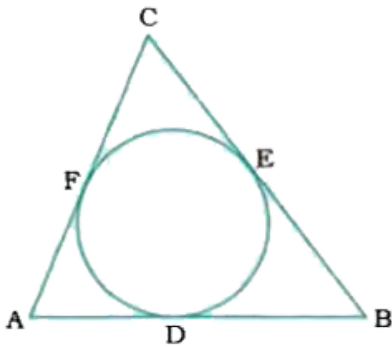
D. 5

**Answer: D**



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3. In the given figure, if  $AB = 12\text{cm}$ ,  $BC = 8\text{cm}$  and  $AC = 10\text{cm}$ , then  $AD = \dots\dots\dots\text{cm}$



A. 5

B. 4



C. 6

D. 7

**Answer: D**



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4. AP and AQ are tangent drawn from a point A to a circle with centre O and radius 9cm. If OA = 15 cm. then  $AP + AQ = \dots\dots$  Cm.

A. 12

B. 18

C. 24

D. 36

**Answer: C**



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5. At one end A of a diameter AB of a circle of radius 5 cm, tangent XAY is drawn to the circle. The length of the chord CD parallel to XY and at a distance 8 cm from A is ..... cm .

A. 4

B. 5

C. 6

D. 8

**Answer: D**



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6. If two tangent inclined at an angle of  $60^\circ$  are drawn to a circle of radius 3cm, then the length of each tangent is.....cm.

A.  $\frac{3\sqrt{3}}{2}$

B. 6

C. 3

D.  $3\sqrt{3}$

**Answer: D**



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7. In a right triangle ABC, right angled at B ; BC = 12 cm and AB = 5 cm. Then the radius of the circle inscribed in the triangle is.....cm.

A. (A) 4

B. (B) 3

C. (C) 2

D. (D) 1

**Answer: C**



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**8.** If the angle between two radii of a circle is  $130^\circ$ , the angle between the tangents at the ends of the radii is.....

A.  $90^\circ$

B.  $50^\circ$

C.  $70^\circ$

D.  $40^\circ$

**Answer: B**



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**9.** If radii of the two concentric circles are 15cm and 17cm, then the length of each chord of one circle which is tangent to other is:

A. 8

B. 16

C. 30

D. 17

**Answer: D**



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**10.** The pair of tangents AP and AQ drawn from an external point to a circle with centre O are perpendicular to each other and the length of

each tangent is 4 cm. Then, the radius of the circle is ... cm.

A. 10

B. 7.5

C. 5

D. 2.5

**Answer: D**



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## Objective Questions Answer The Following By A Number Or A Word Or A Sentence

1. If the radii of two circles with centres  $O$  and  $O'$  are 7 cm and 10 cm and the distance between their centres is 12 cm. In how many points do the circles intersect?



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2. What is the radius of a circle inscribed in a triangle with sides of length 12cm, 35cm and

37cm?



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**3.** Two tangents TA and TB to circle with centre O are inclined to each other angle of  $70^\circ$ .

Then, Find  $\angle OAB$ .



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**4.** A circle is inscribed in a quadrilateral PQRS.

If PQ= 5cm QR=8.2cm and RS = 9.3 cm, what is

the length of SP?



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5. The radii of two concentric circles are 40 cm and 41 cm. What is the length of a chord of the bigger circle which is tangent to the smaller circle?



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**Objective Questions True False**

1. The radii of two circles with centres  $O$  and  $O'$  are 9 cm and 7 cm and the distance between their centres is 20 cm. Then those circles will have \_\_\_\_\_ common tangents.



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2. A rectangle circumscribing a circle is a square.



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3. A quadrilateral ABCD circumscribes a circle. In ABCD. If AB is the longest side, then CD is the shortest side.



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4. Diameter of circle is 20 cm. Then, the length of each tangent to that are less than 20 cm.

True or false



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