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## MATHS

## BOOKS - SELINA MATHS (ENGLISH)

## MATHEMATICS -2014

## Section A

1. Ranbir borrows रु 20,000 at 12 per cent C.I. If he repays

रु 8,400 at the end of first year and रु 9,680 at the end of
second year, find the amount of loan outstanding at the beginning of the third year.
2. Find the values of $x$, which satisfy the inequation $-2 \frac{5}{6}<\frac{1}{2}-\frac{2 x}{3} \leq 2, x \in W$. Graph the solution set on the number line.

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3. A die has 6 faces marked by the given numbers as shown below :
1


The die is thrown once. What is the probability of getting
(i) a positive integer.
4. A die has 6 faces marked by the given numbers as shown below:
1


The die is thrown once. What is the probability of getting
(ii) an integer greater than -3 .

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5. A die has 6 faces marked by the given numbers as
shown below:
$\square$
$\square$


The die is thrown once. What is the probability of getting
(iii) the smallest integer.
6. Find $x$, $y$ if $\left[\begin{array}{cc}-2 & 0 \\ 3 & 1\end{array}\right]\left[\begin{array}{c}-1 \\ 2 x\end{array}\right]+\left[\begin{array}{c}-2 \\ 1\end{array}\right]=2\left[\begin{array}{l}y \\ 3\end{array}\right]$

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7. Shahrukh opened a Recurring Deposite Account in a bank and deposited Rs 800 per month for $1 \frac{1}{2}$ years. If he received Rs 15,084 at the time of maturity, find the rate of interest per annum.

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8. Calculate the ratio in which the line joining $A(-4,2)$ and
$B(3,6)$ is divided by point $P(x, 3)$. Also, find (i) $x$

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9. Calculate the ratio in which the line joining $A(-4,2)$ and $B(3,6)$ is divided by point $P(x, 3)$. Also, find
(ii) length of AP.

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10. Without using trigonometric tables, evaluate.
$\sin ^{2} 34^{\circ}+\sin ^{2} 56^{\circ}+2 \tan 18^{\circ} \tan 72^{\circ}-\cot ^{2} 30^{\circ}$
11. Using the Remainder and Factor theorem, factorise the following polynomial :
$x^{3}+10 x^{2}-37 x+26$.

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12. In the figure given below, $A B C D$ is a rectangle. $A B=14$ $\mathrm{cm}, \mathrm{BC}=7 \mathrm{~cm}$. From the rectangle, a quarter circle BFEC and a semicircle DGE are removed. Calculate the area of
the remaining piece of the rectangle. (Take $\pi=\frac{22}{7}$ )


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13. The numbers $6,8,10,12,13$, and $x$ are arranged in an ascending order. If the mean of the observation is equal to the median, find the value of $x$.
14. In the given figure, $\angle D B C=58^{\circ}$, BD is diameter of the circle. Calculate :
(i) $\angle B D C$ (ii) $\angle B E C$ (iii) $\angle B A C$


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15. Use graph paper to answer the following questions.
(Take $2 \mathrm{~cm}=1$ unit on both axis).
(i) Plot the points $\mathrm{A}(-4,2)$ and $\mathrm{B}(2,4)$.

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16. Use graph paper to answer the following questions.
(Take $2 \mathrm{~cm}=1$ unit on both axis).
(ii) $\mathrm{A}^{\prime}$ is the image of A when reflected in the Y -axis. Plot it on the graph paper and write the coordinates of $\mathrm{A}^{\prime}$.the points $A(-4,2)$ and $B(2,4)$.
17. Use graph paper to answer the following questions.
(Take $2 \mathrm{~cm}=1$ unit on both axis).

Here $A^{\prime}(4,2), B^{\prime}(-2,4)$ (iii) $B^{\prime}$ is the image of $B$ when reflected in the line $A A^{\prime}$. Write the coordinates of $B^{\prime}$. the points $A(-4,2)$ and $B(2,4)$

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18. Use graph paper to answer the following questions.
(Take $2 \mathrm{~cm}=1$ unit on both axis).
(iv) Write the geometric name of the figure $A B A^{\prime} B^{\prime}$ 'the points $A(-4,2)$ and $B(2,4), A^{‘}(4,2), B^{\prime}(2,0)$.
19. Use graph paper to answer the following questions.
(Take $2 \mathrm{~cm}=1$ unit on both axis).
Here $A^{\prime}(4,2), B^{\prime}(2,0)(v)$ Name a line of symmetry of the figure formed.ABA'B'.the points $A(-4,2)$ and $B(2,4)$

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## Section B

1. A shopkeeper bought a washing machine at a discount of $20 \%$ from a wholesaler, the printed price of the washing machine being Rs 18,000 . The shopkeeper sells it to a consumer at a discount of $10 \%$ on the printed price. If the rate of sales tax is $8 \%$, find :
(i) the VAT paid by the shopkeeper,
(ii) the total amount that the consumer pays for the washing machine.

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2. If $\frac{x^{2}+y^{2}}{x^{2}-y^{2}}=\frac{17}{8}$, using the properties of proportion find the value of:
(i) $x: y$

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3. If $\frac{x^{2}+y^{2}}{x^{2}-y^{2}}=\frac{17}{8}$, using the properties of proportion find the value of:
(ii) $\frac{x^{3}+y^{3}}{x^{3}-y^{3}}$

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4. In $\triangle A B C, \angle A B C=\angle D A C, \mathrm{AB}=8 \mathrm{~cm}, \mathrm{AC}=4 \mathrm{~cm}$ and
$A D=5 \mathrm{~cm}$.

(i) Prove that $\triangle A C D \sim \triangle B C A$.

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5. In $\triangle A B C, \angle A B C=\angle D A C, \mathrm{AB}=8 \mathrm{~cm}, \mathrm{AC}=4 \mathrm{~cm}$ and
$A D=5 \mathrm{~cm}$.

(ii) Find the length of $B C$ and $C D$.

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6. In $\triangle A B C, \angle A B C=\angle D A C, \mathrm{AB}=8 \mathrm{~cm}, \mathrm{AC}=4 \mathrm{~cm}$ and
$A D=5 \mathrm{~cm}$.

(iii) Find area of $\triangle A C D$ : area of $\triangle A B C$.

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7. Find the value of 'a' for which the following points $A(a$,
$3), \mathrm{B}(2,1)$ and $\mathrm{C}(5, a)$ are collinear. Hence, find the equation of the line.
8. Salman invests a sum of money in 50 rs shares paying $15 \%$ dividend quoted at $20 \%$ premium. If his annual dividend is $600 r s$, calculate
(i) the number of shares he bought
(ii) his total investment
(iii) the rate of return on his investment

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9. Salman invests a sumof money in Rs 50 shares, paying
$15 \%$ dividend quoted at $20 \%$ premium. If his annual dividend is Rs 600, calculate :
(ii) his total investment.
10. Salman invests a sumof money in Rs 50 shares, paying $15 \%$ dividend quoted at $20 \%$ premium. If his annual dividend is Rs 600, calculate :
(iii) the rate of return on his investment.

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11. The suface area of a solid metallic sphere is $2464 \mathrm{~cm}^{2}$.

It is melted and recast into solid right circular cones of radius 3.5 cm and height 7 cm . Calculate :
(i) the radius of the sphere.
12. The surface area of a solid metallic sphere is $2464 \mathrm{~cm}^{2}$. It is melted and recast into solid right circular cones of radius 3.5 cm and height 7 cm . Calculate :
the number of cones recast. (Take $\pi=\frac{22}{7}$ )

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13. Calculate the mean of the distribution given below using the short cut method.

| Marks | $11-$ | $21-$ | $31-$ | $41-$ | $51-$ |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 20 | 30 | 40 | 50 | 60 | 70 | 80 |
| No. of students | 2 | 6 | 10 | 12 | 9 | 7 | 4 |

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14. In the figure given below, diameter $A B$ and chord $C D$ of a circle meet at P. PT is a tangent to the circle at T. CD $=7.8$ $\mathrm{cm}, \mathrm{PD}=5 \mathrm{~cm}, \mathrm{~PB}=4 \mathrm{~cm}$. Find
(i) AB.
(ii) The length of tangent PT.


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$A=\left[\begin{array}{ll}2 & 1 \\ 0 & -2\end{array}\right], B=\left[\begin{array}{ll}4 & 1 \\ -3 & -2\end{array}\right]$ and $C=\left[\begin{array}{ll}-3 & 2 \\ -1 & 4\end{array}\right]$
. Find $A^{2}+A C-5 B$.

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16. The compound interest, calculated yearly, on a certain sum of money for the second year is Rs 1320 and for the third year is Rs 1452. Calculate the rate of interest and the original sum of money.

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17. Construct a $\Delta A B C$ with $\mathrm{BC}=6.5 \mathrm{~cm}, \mathrm{AB}=5.5 \mathrm{~cm}, \mathrm{AC}=5$
cm . Construct the incircle of the triangle. Measure and record the radius of the incircle.
18. The daily pocket expenses of 200 students in a school are given below : (Use a graph apper for this question.)

| Pocket expenses <br> (in ₹) | Number of students <br> (frequency) |
| :---: | :---: |
| $0-5$ | 10 |
| $5-10$ | 14 |
| $10-15$ | 28 |
| $15-20$ | 42 |
| $20-25$ | 50 |
| $25-30$ | 30 |
| $30-35$ | 14 |
| $35-40$ | 12 |

Draw a histogram representing the above distribution and estimate the mode from the graph.
19. If $(x-9):(3 x+6)$ is the duplicate ratio of $4: 9$, find the value of $x$ using properties of proportion.

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20. Solve the x using the quadratic formula. Write your answer correct to two significant figures. $(x-1)^{2}-3 x+4=0$.

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21. A page from the saving bank account of Priyanka is given below

| Date | Particulars | Amount withdrawn (₹) | Amount deposited (₹) | Balance (₹) |
| :--- | :--- | :--- | :---: | :---: |
| $3 / 4 / 2006$ | B/F |  |  | $4000-00$ |
| $5 / 4 / 2006$ | By Cash |  | $2000-00$ | $6000-00$ |
| $18 / 4 / 2006$ | By Cheque |  | $6000-00$ | $12000-00$ |
| $25 / 5 / 2006$ | To Cheque | $5000-00$ |  | $7000-00$ |
| $30 / 5 / 2006$ | By Cash |  | $3000-00$ | $10000-00$ |
| $20 / 7 / 2006$ | By Self | $4000-00$ |  | $6000-00$ |
| $10 / 9 / 2006$ | By Cash |  | $2000-00$ | $8000-00$ |
| $19 / 9 / 2006$ | To Cheque | $1000-00$ |  | $7000-00$ |

If the interest earned by Priyanka for the period ending
September, 2006 is Rs 175, find the rate of interest.

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22. A two digit positive number is such that the product of its digits is 6 . If 9 is added to the number, the digits interchange their places. Find the number.

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23. The marks obtained by 100 students in a Mathematics test are given below :

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Students | 3 | 7 | 12 | 17 | 23 | 14 | 9 | 6 | 5 | 4 |

Draw an ogive for the given distribution on a graph sheet.
(Use a scale of $2 \mathrm{~cm}=10$ units on both axis).

Use the ogive to estimate the :
(i) median.

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24. The marks obtained by 100 students in a Mathematics test are given below :

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Students | 3 | 7 | 12 | 17 | 23 | 14 | 9 | 6 | 5 | 4 |

Draw an ogive for the given distribution on a graph sheet.
(Use a scale of $2 \mathrm{~cm}=10$ units on both axis).

Use the ogive to estimate the :
(ii) lower quartile.

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25. The marks obtained by 100 students in a Mathematics test are given below :

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Students | 3 | 7 | 12 | 17 | 23 | 14 | 9 | 6 | 5 | 4 |

Draw an ogive for the given distribution on a graph sheet.
(Use a scale of $2 \mathrm{~cm}=10$ units on both axis).

Use the ogive to estimate the number of students who obtained more than $85 \%$ marks in the test.
26. The marks obtained by 100 students in a Mathematics test are given below :

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Students | 3 | 7 | 12 | 17 | 23 | 14 | 9 | 6 | 5 | 4 |

Draw an ogive for the given distribution on a graph sheet.
(Use a scale of $2 \mathrm{~cm}=10$ units on both axis).
Use the ogive to estimate the number of students who
did not pass in the test if the pass percentage was 35 .

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27. In the figure given below, $O$ is the centre of the circle.
$A B$ and $C D$ are two chords of the circle. $O M$ is
perpendicular to $A B$ and $O N$ is perpendicular to $C D . A B=$ $24 \mathrm{~cm}, \mathrm{OM}=5 \mathrm{~cm}, \mathrm{ON}=12 \mathrm{~cm}$. Find the :
(i) radius of the circle
(ii) length of chord CD


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28. Prove the identity
$(\sin \theta+\cos \theta)(\tan \theta+\cot \theta)=\sec \theta+\operatorname{cosec} \theta$

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29. An aeroplane at an altitude of 250 m observes the angle of depression of two boats on the opposite banks of a river to be $45^{\circ}$ and $60^{\circ}$ respectively. Find the width of the river. Write the answer correct to the nearest whole number.
