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## MATHS

## BOOKS - SELINA MATHS (ENGLISH)

## MATHEMATICS -2017

## Section A

1. If $b$ is the mean proportion between $a$ and $c$, show that :
$\frac{a^{4}+a^{2} b^{2}+b^{4}}{b^{4}+b^{2} c^{2}+c^{4}}=\frac{a^{2}}{c^{2}}$
2. Solve the equation $4 x^{2}-5 x-3=0$ and give your answer correct to two decimal places.

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3. $A B$ and $C D$ are two parallel chords of a circle on opposite sides of a diameter such that $A B=24 \mathrm{~cm}$ and $C D=10 \mathrm{~cm}$. If the radius of the circle is 13 cm , find the distance between the two chords.

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4. Evaluate without using triignometric tables,**
$\sin ^{2} 28^{\circ}+\sin ^{2} 62^{\circ}+\tan ^{2} 38^{\circ}-\cot ^{2} 52^{\circ}+\frac{1}{4} \sec ^{2} 30^{\circ}$

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## 5.

$$
A=\left[\begin{array}{ll}
1 & 3 \\
3 & 4
\end{array}\right], B=\left[\begin{array}{rr}
-2 & 1 \\
-3 & 2
\end{array}\right] \text { and } A^{2}-5 B^{2}=5 C
$$

. find matrix $C$ where $C$ is a 2 by 2 matrix.

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6. Jaya borrowed Rs 50,000 for 2 years. The rates of
interest for two seccessive years are $12 \%$ and $15 \%$
respectively. She repays Rs 33,000 at the end of the first year. Find the amount she must pay at the end of the second year to clear her debt.**

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7. The catalogue price of a computer set is Rs 42000.

The shopkeeper gives a discount of $10 \%$ on the listed price. He further gives an off-season discount of $5 \%$ on the discounted price. However, sales tax at $8 \%$ is charged after successive discounts. Find :
(i) the amount of sales tax a customer has to pay
(ii) the total price to be paid by the customer for the computer set.
8. $P(1,-2)$ is a point on the line segment $A(3,-6)$ and $\mathrm{B}(\mathrm{x}, \mathrm{y})$ such that $A P: P B$ is equal to $2: 3$. Find the coordinates of $B$.

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9. The marks of 10 students of a class in an examination arranged in ascending order are as follows:
$13,35,43,46, x, x+4,55,61,71,80$

If the median marks is 48 , find the value of $x$. Hence find the mode of the given data.

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10. What must be subtracted from
$16 x^{3}-8 x^{2}+4 x+7$ so that the resulting expression has $2 \mathrm{x}+1$ is a factor?

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11. In the given figure $A B C D$ is a rectangle. It consists of a circle and two semi-circles each of which are of
radius 5 cm . Find the area of the shaded region. Give
your answer correct to three significant figures.**

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12. Solve the following inequation and represent the solution set on a number line.
$-8 \frac{1}{2}<-\frac{1}{2}-4 x \leq 7 \frac{1}{2}, x \in I$

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## Section B

1. Given matrix $B=\left[\begin{array}{ll}1 & 1 \\ 8 & 3\end{array}\right]$. Find the matrix $X$ if, $X=B^{2}-4 B$. Hence, solve for a and b given $X\left[\begin{array}{l}a \\ b\end{array}\right]=\left[\begin{array}{c}5 \\ 50\end{array}\right]$.
2. How much should a man invest in Rs 50 shares selling at Rs 60 to obtain an income of Rs 450 , if the rate of dividend declared is $10 \%$. Also find his yield percent, to the nearest whole number.

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2. Sixteen cards are labelled as a, b, c,...... m, n. o,p.

They are put in a box and shuffled. A boy is asked to draw a card from the box. What is the probability
that the card drawn is :
(i) a vowel

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3. Sixteen cards are labelled as a, b, c,...... m, n. o,p.

They are put in a box and shuffled. A boy is asked to draw a card from the box. What is the probability that the card drawn is :
(ii) a consonant

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4. Sixteen cards are labelled as a, b, c,...... m, n. o,p.

They are put in a box and shuffled. A boy is asked to draw a card from the box. What is the probability that the card drawn is :
(iii) none of the letters of the word 'median'.

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5. Using a ruler and a compass, construct a triangle
$A B C$ in which $A B=7 \mathrm{~cm}, \angle C A B=60^{\circ}$ and
$A C=5 \mathrm{~cm}$. construct the locus of:
points equidistant from $B A$ and $B C$. Hence construct
a circle touching the three sides of the triangle internally.

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6. Using a ruler and a compass, construct a triangle

ABC in which $A B=7 \mathrm{~cm}, \angle C A B=60^{\circ}$ and
$A C=5 \mathrm{~cm}$. construct the locus of:
points equidistant from $B A$ and $B C$. Hence construct
a circle touching the three sides of the triangle internally.
7. A conical tent has to accommodate 77 persons.

Each person must have $16 m^{3}$ of air to breathe. Given the radius of the tent as 7 m , find the height of the tent and also its curved surface area.

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8. If $\frac{7 m+2 n}{7 m-2 n}=\frac{5}{3}$ use properties of proportion to find
(i) $m: n$
(ii) $\frac{m^{2}+n^{2}}{m^{2}-n^{2}}$
9. A page fron a savings bank account passbook as given below : **
(i) Calculate the interest for the 6 months from January to June 2016, at 6\% per annum.
(ii) If the account is closed on 1st July 2016, find the amount received by the account holder.

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10. Use a graph paper for this question.
(Take $2 \mathrm{~cm}=1$ unit on both x and y axes)
Plot the following points :
$A(0,4), B(2,3), C(1,1)$ and $D(2,0)$.
11. Use a graph paper for this question.
(Take $2 \mathrm{~cm}=1$ unit on both x and y axes) where $\mathrm{A}(0$,
4), $B(2,3), C(1,1)$ and $D(2,0)$ and reflect points $B^{\prime}, C^{\prime}$,

D' on $y$-axis
Join the points $A, B, C, D, D^{\prime}, C^{\prime}, B^{\prime}$ and $A$ in order, so as
to form a closed figure. Write down the equation of the line about which if this closed figure obtained is folded, the two parts of the figure exactly coincide.

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12. Use a graph paper for this question.
(Take $2 \mathrm{~cm}=1$ unit on both x and y axes) where $\mathrm{A}(0$,
4), $B(2,3), C(1,1)$ and $D(2,0)$ and reflect points $B^{\prime}, C^{\prime}$,
$D^{\prime}$ on $y$-axis
Join the points $A, B, C, D, D^{\prime}, C^{\prime}, B^{\prime}$ and $A$ in order, so as
to form a closed figure. Write down the equation of the line about which if this closed figure obtained is folded, the two parts of the figure exactly coincide.

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13. Calculate the mean of the following distribution using step deviation method.


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14. In the given figure $P Q$ is a tangent to the circle at
A. AB and AD are bisectors of $\angle C A Q$ and $\angle P A C$. If
$\angle B A Q=30^{\circ}$, prove that :
(i) BD is a diameter of the circle.
(ii) $A B C$ is an isosceles triangle


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15. The printed of an air conditioner is Rs 45,000 . The wholesaler allows of $10 \%$ to the shopkeeper. The shopkeeper sells the article to the customer at a discount of $5 \%$ of the marked price. Sales tax (under VAT) is charged at the rate of $12 \%$ at every stage.

Find :**
(i) VAT paid by the shopkeeper to the government.

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16. The printed of an air conditioner is Rs 45,000 . The wholesaler allows of $10 \%$ to ther shopkeeper. The shopkeeper sells the article to the customer at a discount of $5 \%$ of the marked price. Sales tax (under VAT) is charged at the rate of $12 \%$ at every stage. Find :**
(ii) The total amount paid by the customer inclusive of tax.
17. In the figure given, $O$ is the centre of the circle.
$\angle D A E=70^{\circ}$. Find, giving suitable reason, the measure of : (i) $\angle B C D$ (ii) $\angle B O D$ (iii) $\angle O B D$

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18. $A(-1,3), B(4,2)$ and $C(3,-2)$ are the vertices of a triangle.

Find the coordinates of the centroid $G$ of the triangle.

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19. $A(-1,3), B(4,2)$ and $C(3,-2)$ are the vertices of a triangle.

Find the equation of the line through $G$ and parallel to $A C$.

## 20. Prove that

$\frac{\sin \theta-2 \sin ^{3} \theta}{2 \cos ^{3} \theta-\cos \theta}=\tan \theta$

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21. The sum of the age of Vivek and his younger brother Amit is 47 years. The product of their ages in years is 550 . Find their ages.

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22. The daily wages of 80 workers in a project are given below.

| Wages(in Rs.) | $400-$ <br> 450 | $450-$ <br> 500 | $500-$ <br> 550 | $550-$ <br> 600 | $600-$ <br> 650 | $650-$ <br> 700 | $700-$ <br> 750 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No.of <br> workers | 2 | 6 | 12 | 18 | 24 | 13 | 5 |

Use a graph paper to draw an ogive for the above
distribution. (Use a scale of $2 \mathrm{~cm}=\mathrm{Rs} 50$ on X-axis and $2 \mathrm{~cm}=10$ workers on $Y$-axis). Use your ogive to estimate :
the median wage of the workers.

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23. The daily wages of 80 workers in a project are
given below.

| Wages(in Rs.) | $400-$ <br> 450 | $450-$ <br> 500 | $500-$ <br> 550 | $550-$ <br> 600 | $600-$ <br> 650 | $650-$ <br> 700 | $700-$ <br> 750 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No.of <br> workers | 2 | 6 | 12 | 18 | 24 | 13 | 5 |

Use a graph paper to draw an ogive for the above distribution. (Use a scale of $2 \mathrm{~cm}=\mathrm{Rs} 50$ on X -axis and $2 \mathrm{~cm}=10$ workers on $Y$-axis). Use your ogive to estimate :
the lower quartile wage of workers.

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24. The daily wages of 80 workers in a project are
given below.

| Wages(in Rs.) | $400-$ <br> 450 | $450-$ <br> 500 | $500-$ <br> 550 | $550-$ <br> 600 | $600-$ <br> 650 | $650-$ <br> 700 | $700-$ <br> 750 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No.of <br> workers | 2 | 6 | 12 | 18 | 24 | 13 | 5 |

Use a graph paper to draw an ogive for the above
distribution. (Use a scale of $2 \mathrm{~cm}=$ Rs 50 on X-axis
and $2 \mathrm{~cm}=10$ workers on $Y$-axis). Use your ogive to estimate :
the number of workers who earn more than Rs 625 daily.

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25. The angles of depression of two ships a $A$ and $B$ as observed from the top of a light house 60 m high are $60^{\circ}$ and $45^{\circ}$ respectively. If the two ships are on the opposite sides of the light house, find the distance between the two ships. Give your answer correct to the nearest whole number.
26. $P Q R$ is a triangle. $S$ is a point on the side $Q R$ of
$\triangle P Q R$ such that $\angle P S R=\angle Q P R$. Given $\mathrm{QP}=8$ $\mathrm{cm}, \mathrm{PR}=6 \mathrm{~cm}$ and $\mathrm{SR}=3 \mathrm{~cm}$.


Prove $\triangle P Q R \sim \Delta S P R$.

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27. $P Q R$ is a triangle. $S$ is a point on the side $Q R$ of
$\triangle P Q R$ such that $\angle P S R=\angle Q P R$. Given $\mathrm{QP}=8$
$\mathrm{cm}, \mathrm{PR}=6 \mathrm{~cm}$ and $\mathrm{SR}=3 \mathrm{~cm}$.


Find the lengths of QR and PS .

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28. $P Q R$ is a triangle. $S$ is a point on the side $Q R$ of
$\triangle P Q R$ such that $\angle P S R=\angle Q P R$. Given $\mathrm{QP}=8$
$\mathrm{cm}, \mathrm{PR}=6 \mathrm{~cm}$ and $\mathrm{SR}=3 \mathrm{~cm}$.

area of $\triangle P Q R$
area of $\triangle S P R$

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29. Mr. Richard has a recurring deposite account in a bank for 3 years at $7.5 \%$ p.a. simple interest. If he gets Rs 8325 as interest at the time of maturity, find the monthly deposite.

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30. Mr. Richard has a recurring deposite account in a bank for 3 years at $7.5 \%$ p.a. simple interest. If he gets Rs 8325 as interest at the time of maturity, find the maturity value.

