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## MATHS

## BOOKS - SELINA MATHS (ENGLISH)

## MATHEMATICS- 2015

## Section A

1. A shopkeeper bought an article for Rs 3,450 . He marks the price of the article $16 \%$ above the cost price. The rate of sale tax charged on the article is $10 \%$. Find the :
(i) marked price of the article.
(ii) price paid by a customer who buys the article.

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2. Solve the following ineqaution and write the solution set :
$13 x-5<15 x+4<7 x+12, x \in R$
Represent the solution on a real number line

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3. Without using trigonometric tables evaluate.

$$
\frac{\sin 65^{\circ}}{\cos 25^{\circ}}+\frac{\cos 32^{\circ}}{\sin 58^{\circ}}-\sin 28^{\circ} \cdot \sec 62^{\circ}+\operatorname{cosec}^{2} 30^{\circ}
$$

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4. If $A=\left[\begin{array}{cc}3 & x \\ 0 & 1\end{array}\right]$ and $B=\left[\begin{array}{cc}9 & 16 \\ 0 & -y\end{array}\right]$ find x and y when $A^{2}=B$.

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5. The present population of a town is 2,00,000. Its population increase by $10 \%$ in the first year and $15 \%$ in the second year. Find the population of the town at the end of the two years.
6. Three vertices of a parallelogram $A B C D$ taken in order are $A(3,6), B(5,10)$ and $C(3,2)$ find :
(i) the coordinates of the fourth vertex D .

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7. Three vertices of a parallelogram $A B C D$ taken in order are $A(3,6), B(5,10)$ and $C(3,2)$ find :
(ii) length of diagonal BD.

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8. Three vertices of a parallelogram $A B C D$ taken in order are $A(3,6), B(5,10)$ and $C(3,2)$ find :
(iii) equation of side $A B$ of the parallelogram $A B C D$.

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9. In the given figure, $A B C D$ is a square of side 21 cm .
$A C$ and $B D$ are two diagonals of the square. Two semi
circles are drawn with $A D$ and $B C$ as diameters. Find
the area of the shaded region
(Take $\pi=\frac{22}{7}$ )


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10. The marks obtained by 30 students in a class assessment of 5 subjects is given below :

| Marks | 0 | 1 | 2 | 3 | 4 | 5 |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Students | 1 | 3 | 6 | 10 | 5 | 5 |

Calculate the mean, median and mode of the above distribution.

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11. In the figure given below, $O$ is the centre of the cirlce and SP is a tangent. If $\angle S R T=65^{\circ}$, find the value of $\mathrm{x}, \mathrm{y}$ and z .

12. Katrina opened a recurring deposit account with a Nationalised Bank for a period of 2 years. If the bank pays interest at the rate of $6 \%$ per annum and the monthly instalment is Rs 1,000 , find the :
(i) interest earned in 2 years.

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13. Katrina opened a recurring deposit account with a Nationalised Bank for a period of 2 years. If the bank pays interest at the rate of $6 \%$ per annum and the
monthly instalment is Rs 1,000 , find the :
(ii) maturity value.

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14. Find the value of ' $k$ ' for which $x=3$ is a solution
of the quadratic equation, $(k+2) x^{2}-k x+6=0$
Hence, find the other root of the equation.

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15. Draw a regular hexagon of side 5 cm .

1. Use a graph paper for this question take $1 \mathrm{~cm}=1$ unit along both the $X$ and $Y$ axis :
(i) Plot the points $A(0,5), B(2,5), C(5,2), D(5,-2), E(2,-5)$ and $F(0,-5)$.

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2. Use a graph paper for this question taking $1 \mathrm{~cm}=1$ unit along both the x and y axis:
(i) Plot the points $A(0,5), B(2,5), C(5,2), D(5,-2), E(2,-5)$ and $\mathrm{F}(0,-5)$.
(ii) Reflect the points B, C, D and E on the $y$-axis and name them respectively as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.

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3. Use a graph paper for this question taking $1 \mathrm{~cm}=1$ unit along both the x and y axis:
(i) Plot the points $A(0,5), B(2,5), C(5,2), D(5,-2), E(2,-5)$ and $\mathrm{F}(0,-5)$.
(ii) Reflect the points B, C, D and E on the $y$-axis and name them respectively as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
(iii) Write the coordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
4. Use a graph paper for this question taking $1 \mathrm{~cm}=1$ unit along both the x and y axis:
(i) Plot the points $A(0,5), B(2,5), C(5,2), D(5,-2), E(2,-5)$ and $\mathrm{F}(0,-5)$.
(ii) Reflect the points $B, C, D$ and $E$ on the $y$-axis and name them respectively as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
(iii) Write the coordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
(iv) Name the figure formed by BC DEE'D'C'B'.

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5. Use a graph paper for this question taking $1 \mathrm{~cm}=1$
unit along both the x and y axis:
(i) Plot the points $\mathrm{A}(0,5), \mathrm{B}(2,5), \mathrm{C}(5,2), \mathrm{D}(5,-2), \mathrm{E}(2,-5)$ and $\mathrm{F}(0,-5)$.
(ii) Reflect the points $B, C, D$ and $E$ on the $y$-axis and name them respectively as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
(iii) Write the coordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}, \mathrm{D}^{\prime}$ and $\mathrm{E}^{\prime}$.
(iv) Name the figure formed by BC DEE'D'C'B'.
(v) Name a line of symmetry for the figure formed.

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6. Virat opened a Saving Bank account in a bank on $16^{\text {th }}$ April, 2010. His pass book shows the following enteries.

| Date | Particulars | Withdrawal (₹) | Deposit (₹) | Balance (₹) |
| :---: | :---: | :---: | :---: | :---: |
| April 16, 2010 | By Cash | - | 2500 | 2500 |
| April $28^{\text {th }}$ | By Cheque | - | 3000 | 5500 |
| May $9^{\text {th }}$ | To Cheque | 850 | - | 4650 |
| May 15 ${ }^{\text {th }}$ | By Cash | - | 1600 | 6250 |
| May $24^{\text {th }}$ | To Cash | 1000 | - | 5250 |
| June $4^{\text {th }}$ | To Cash | 500 | - | 4750 |
| June $30^{\text {th }}$ | By Cheque | - | 2400 | 7150 |
| July $3^{\text {rd }}$ | By Cash | - | 1800 | 8950 |

Calculate the interest Virat earned at the end of $31^{\text {st }}$
July, 2010 at 4\% per annum interest. What sum of money will he receive if he closes the account on $1^{\text {st }}$

August, 2010 ?

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7. If $a, b, c$ are in continued proportion, prove that $(a+b+c)(a-b+c)=a^{2}+b^{2}+c^{2}$.
8. In the given figure $A B C$ is a triangle and $B C$ is parallel to the $Y$-axis. $A B$ and $A C$ intersects the $y$-axis at Pand Q respectively.

(i) Write the coordinates of $A$.
9. In the figure, given, $A B C$ is a triangle and $B C$ is parallel to the $y$-axis. $A B$ and $A C$ intersect the $y$-axis at $P$ and $Q$ respectively.


Find the length of $A B$ and $A C$.

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10. In the given figure $A B C$ is a triangle and $B C$ is parallel to the $Y$-axis. $A B$ and $A C$ intersects the $y$-axis at Pand Q respectively.

(iii) Find the ratio in which Q divides AC .
11. In the given figure $A B C$ is a triangle and $B C$ is parallel to the $Y$-axis. $A B$ and $A C$ intersects the $y$-axis at Pand Q respectively.

(iv) Find the equation of the line $A C$.
12. Calculate the mean of the following distribution:

| Class In- <br> terval | $0-10$ | $10-$ <br> 20 | $20-$ | 30 | 30 | $40-$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | $50-$ |  |  |  |  |  |
| Frequen- <br> cy | 8 | 5 | 12 | 35 | 24 | 16 |

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13. Two solid spheres of radii 2 cm and 4 cm are melted and recast into a cone of height 8 cm . Find the radius of the cone so formed.
14. Find 'a' if the two polynomials $a x^{3}+3 x^{2}-9$ and $2 x^{3}+4 x+a$, leaves the same remainder when divided by $\mathrm{x}+3$.

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15. Prove that $\frac{\sin \theta}{1-\cot \theta}+\frac{\cos \theta}{1-\tan \theta}=\cos \theta+\sin \theta$

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16. $A B$ and $C D$ are two chords of a circle intersecting at P. Prove that $A P \times P B=C P \times P D$


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17. A bag contains 5 white balls, 6 red balls and 9
green balls. A ball is drawn at random from the bag.
Find the probability that the ball drawn is :
(i) a green ball.
18. A bag contains 5 white balls, 6 red balls and 9 green balls. A ball is drawn at random from the bag.

Find the probability that the ball drawn is :
(ii) a white or a red ball.

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19. A bag contains 5 white balls, 6 red balls and 9
green balls. A ball is drawn at random from the bag.
Find the probability that the ball drawn is :
(iii) neither a green ball nor a white ball.
20. Rohit invested 9600 rs on 100 rs shares at 20 rs premium paying $8 \%$ dividend. Rohit sold the shares when the price rose to 160 rs . He invested the proceeds (excluding dividend) in $10 \% 50 \mathrm{rs}$ shares at $40 r s$ find the
(i) original number of shares
(ii) sale proceeds
(iii) new number of shares
(iv) change in the two dividends

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21. Rohit invested 9600 rs on 100 rs shares at 20 rs premium paying $8 \%$ dividend. Rohit sold the shares when the price rose to 160 rs . He invested the proceeds (excluding dividend) in $10 \% 50 \mathrm{rs}$ shares at $40 r s$ find the
(i) original number of shares
(ii) sale proceeds
(iii) new number of shares
(iv) change in the two dividends

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22. Rohit invested 9600 rs on 100 rs shares at 20 rs premium paying $8 \%$ dividend. Rohit sold the shares when the price rose to 160 rs . He invested the proceeds (excluding dividend) in $10 \% 50 \mathrm{rs}$ shares at $40 r s$ find the
(i) original number of shares
(ii) sale proceeds
(iii) new number of shares
(iv) change in the two dividends

- Watch Video Solution

23. Rohit invested 9600 rs on 100 rs shares at 20 rs premium paying $8 \%$ dividend. Rohit sold the shares when the price rose to 160 rs . He invested the proceeds (excluding dividend) in $10 \% 50 \mathrm{rs}$ shares at $40 r s$ find the
(i) original number of shares
(ii) sale proceeds
(iii) new number of shares
(iv) change in the two dividends

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24. The horizontal distance between two tower is 120
$m$. The angle of elevation of the top and angle of depression of the bottom of the first tower as observed from the second tower is $30^{\circ}$ and $24^{\circ}$
respectively.


Find the height of the two towers. Give youe answer correct to 3 significant figures.

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25. The weight of 50 workers is given below :

$\left.$| Weight <br> in kg | $50-$ <br> 60 | $60-$ <br> 70 | $70-$ <br> 80 | $80-$ <br> 90 | 90 <br> 100 | 100 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 110 |  |  |  |  |  |  | | $110-$ |
| :---: |
| 120 | \right\rvert\, | No. of |
| :--- |
| Workers | 4

Draw an ogive of the given distribution using a graph sheet. Take $2 \mathrm{~cm}=10 \mathrm{~kg}$ on one axis and $2 \mathrm{~cm}=5$ workers along the other axis. Use a graph to estimate the following the upper and lower quartiles.
26. The weight of 50 workers is given below :
$\left.\begin{array}{|l|c|c|c|c|c|c|c|}\hline \begin{array}{l}\text { Weight } \\ \text { in kg }\end{array} & \begin{array}{c}50- \\ 60\end{array} & \begin{array}{c}60- \\ 70\end{array} & \begin{array}{c}70- \\ 80\end{array} & \begin{array}{c}80- \\ 90\end{array} & \begin{array}{c}90- \\ 100\end{array} & 100- & 110\end{array}\right)$

Draw an ogive of the given distribution using a graph
sheet. Take $2 \mathrm{~cm}=10 \mathrm{~kg}$ on one axis and $2 \mathrm{~cm}=5$
workers along the other axis. Use a graph to estimate
the following: if weight 95 kg and above is considered overweight find the number of workers who are overweight.

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27. A wholesaler buys a TV from the manufacturer for

Rs 25,000 . He marks the price of the TV $20 \%$ above his cost price and sells it to a retailer at a $10 \%$ discount on the marked price. If the rate of VAT is $8 \%$, Find the :
(i) marked price.
(ii) retailer's cost price inclisive of tax.
(iii) VAT paid by the wholsaler.

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28. 

$A=\left[\begin{array}{ll}3 & 7 \\ 2 & 4\end{array}\right], B=\left[\begin{array}{ll}0 & 2 \\ 5 & 3\end{array}\right]$ and $C=\left[\begin{array}{ll}1 & -5 \\ -4 & 6\end{array}\right]$
Find $A B-5 C$.

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29. ABC is a right angled triangle with $\angle A B C=90^{\circ}$,
$D$ is any point on $A B$ and $D E$ is perpendicular to $A C$.
Prove that :

(i) $\triangle A D E \sim \triangle A C B$.

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30. ABC is a right angled triangle with $\angle A B C=90^{\circ}$,
$D$ is any point on $A B$ and $D E$ is perpendicular to $A C$.

(ii) If $\mathrm{AC}=13 \mathrm{~cm}, \mathrm{BC}=5 \mathrm{~cm}$ and $\mathrm{AE}=4 \mathrm{~cm}$. Find DE and

AD.
31. ABC is a right angled triangle with $\angle A B C=90^{\circ}$,
$D$ is any point on $A B$ and $D E$ is perpendicular to $A C$.
Prove that :

(iii) Find area of $\Delta$ ADE : area of quadrilateral BCED.If
$A C=13 \mathrm{~cm}, \mathrm{BC}=5 \mathrm{~cm}$ and $\mathrm{AE}=4 \mathrm{~cm}$.
32. Sum of two natural number is 8 and the difference of their reclprocal is $\frac{2}{15}$. Find the numbers.

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33. Given $\frac{x^{3}+12 x}{6 x^{2}+8}=\frac{y^{3}+27 y}{9 y^{2}+27}$.

Using
componendo and devidendo find $\mathrm{x}: \mathrm{y}$.

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34. In a right triangle $\mathrm{ABC}, \angle B=90^{\circ}$ If $\mathrm{AC}=5 \mathrm{~cm}, \mathrm{BC}$
$=3 \mathrm{~cm}$, Find $A B$.
35. In a right triangle $\mathrm{ABC}, \angle B=90^{\circ}$

If $A B=6 \mathrm{~cm}, B C=8 \mathrm{~cm}$, Find $A C$,

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36. Construct the kite EASY if $\mathrm{AY}=8 \mathrm{~cm}, \mathrm{EY}=4 \mathrm{~cm}$ and

SY $=6 \mathrm{~cm}$. Which properties of the kite did you use in the process?


