# ©゙" doubtnut 

India's Number 1 Education App

## MATHS

## BOOKS - SELINA MATHS (ENGLISH)

## MATHEMATICS-2019

Section A

1. Solve the following inequation and write down the solution set:
$11 x-4<15 x+4 \leq 13 x+14, x \in W$.
2. A man invests Rs. 4,500 in shares of a company which is playing $7.5 \%$ dividend. If Rs.

100 shares are available at a discount of $10 \%$

Find :
(i) number of shares he purchases. (ii) his annual income.
3. In a class of 40 students, marks obatined by
the students in a class test (out of 10) are given below:

| Marks | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Students | 1 | 2 | 3 | 3 | 6 | 10 | 5 | 4 | 3 | 3 |

Calculate the following for the given distribution :
(i) Median
(ii) Mode

- Watch Video Solution

4. Using the factor theorem, show that $(x-2)$ is a factor of $x^{3}+x^{2}-4 x-4$. Hence factorise the polynomial completely.

## - Watch Video Solution

5. Prove that :
$(\operatorname{cosec} \theta-\sin \theta)(\sec \theta-\cos \theta)(\tan \theta+\cot \theta)=1$

- Watch Video Solution

6. In an Arithmetic Progression (A.P.) the fourth
and sixth terms are 8 and 14 respectively. Find
the :
(i) first term
(ii) common difference
(iii) sum of the first 20 terms

## D Watch Video Solution

7. Simplify :
$\sin A\left|\begin{array}{cc}\sin A & -\cos A \\ \cos A & \sin A\end{array}\right|+\cos A\left|\begin{array}{cc}\cos A & \sin A \\ -\sin A & \cos A\end{array}\right|$
8. M and N are two points on the X -axis and Y axis respectively. $P(3,2)$ divides the line segment $M N$ in the ratio $2: 3$.

Find :
(i) the coordinates of $M$ and $N$

## - Watch Video Solution

9. M and N are two points on the X -axis and Y axis respectively. $P(3,2)$ divides the line
segment MN in the ratio $2: 3$.

Find :
slope of the line MN.

## D Watch Video Solution

10. A solid metallic sphere of radius 6 cm is
melted and made into a solid cylinder of height 32 cm . Find the :
(i) radius of the cylinder
(ii) curved surface area of the cylinder
(Take $\pi=3.1$ )

## Watch Video Solution

11. The following numbers, $K+3, K+2,3 K-7$ and $2 \mathrm{~K}-3$ are in proportion. Find K .

## D Watch Video Solution

12. Solve for $x$ the quadratic equation
$x^{2}-4 x-8=0$. Give your answer correct to
three significant figures.

D Watch Video Solution
13. Draw a circle of radius 4 cm . From the point

7 cm away from its centre, construct the pair of tangents to the circle.

## D Watch Video Solution

## Section B

1. There are 25 disc numbered 1 to 25 . They are put in a closed box and shaken throughly. A disc is drawn at random from the box.

Find the probability that the number on the disc is :
(i) an odd number
(ii) divisible by 2 and 3 both
(iii) a number less than 16 .

## D Watch Video Solution

2. Rekha opened a recurring deposite account
for 20 months. The rate of interest is $9 \%$ per annum and Rekha receives Rs 441 as interest
at the time of maturity.

Find the amount Rekha deposited each month.

## D Watch Video Solution

3. Use a graph sheet for this question. Take 1 $\mathrm{cm}=1$ unit along both x and y axes.
(i) Plot the points: $\mathrm{A}(0,5), \mathrm{B}(3,0), \mathrm{C}(1,0)$ and $D(1,-5)$.
(ii) Reflect the point $B, C$ and $D$ on the $y$-axis and name them as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and $\mathrm{D}^{\prime}$ respectively.
(iii) Write down the co-ordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and

D'.
(iv) Join the points $A, B, C, D, D^{\prime}, C^{\prime}, B^{\prime}, A$ in order and give a name to the closed figure ABCDD'C'B'.

## - Watch Video Solution

4. Use graph paper for this question.
(Take $2 \mathrm{~cm}=1$ unit along both $x$-axis and $y$ axis.)

Plot the points $\mathrm{O}(0,0), \mathrm{A}(-4,4), \mathrm{B}(-3,0)$ and $\mathrm{C}(0$,
-3).

## Watch Video Solution

5. Use a graph sheet for this question. Take 1 $\mathrm{cm}=1$ unit along both x and y axes.
(i) Plot the points: $\mathrm{A}(0,5), \mathrm{B}(3,0), \mathrm{C}(1,0)$ and $D(1,-5)$.
(ii) Reflect the point $\mathrm{B}, \mathrm{C}$ and D on the y -axis and name them as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and $\mathrm{D}^{\prime}$ respectively.
(iii) Write down the co-ordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and D'.
(iv) Join the points A, B, C, D, D', C', B', A in order
and give a name to the closed figure ABCDD'C'B'.

## D Watch Video Solution

6. Use a graph sheet for this question. Take 1 $\mathrm{cm}=1$ unit along both x and y axes.
(i) Plot the points: $\mathrm{A}(0,5), \mathrm{B}(3,0), \mathrm{C}(1,0)$ and $D(1,-5)$.
(ii) Reflect the point $B, C$ and $D$ on the $y$-axis and name them as $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and $\mathrm{D}^{\prime}$ respectively.
(iii) Write down the co-ordinates of $\mathrm{B}^{\prime}, \mathrm{C}^{\prime}$ and

D'.
(iv) Join the points $A, B, C, D, D^{\prime}, C^{\prime}, B^{\prime}, A$ in order and give a name to the closed figure ABCDD'C'B'.

## D Watch Video Solution

7. In the given figure, $\angle P Q R=\angle P S T=90^{\circ}$,
$P Q=5 \mathrm{~cm}$ and $P S=2 \mathrm{~cm}$.
(i) Prove that $\triangle P Q R \sim \Delta P S T$.


- Watch Video Solution

8. In the given figure, $\angle P Q R=\angle P S T=90^{\circ}$
,$P Q=5 \mathrm{~cm}$ and $\mathrm{PS}=2 \mathrm{~cm}$.

Prove that $\triangle P Q R \sim \triangle P S T$


## - Watch Video Solution

9. The first and last term of a geometrical

Pregression (G.P.) are 3 and 96 respectively. If the common ratio is 2 , find :
(i) 'n' the number of terms of the G.P.
(ii) Sum of the n terms.

## D Watch Video Solution

10. A hemispherical and a conical hole is scooped out of a solid wooden cylinder. Find the volume of the remaining solid where the measurements are as follows :

The height of the solid cylinder is 7 cm , radius of each of hemisphere, come and cylinder is 3 cm . height of cone is 3 cm .

Give your answer correct to the nearest whole number.
(Take $\pi=\frac{22}{7}$ )


## - Watch Video Solution

11. In the given figure $A C$ is a tangent to the circle with centre 0.

If $\angle A D B=55^{\circ}$, find x and y . Give reason for
your answer.

(D) Watch Video Solution
12. The model of a building is constructed with
the scale factor $1: 30$.
(i) If the height of the model is 80 cm , find the actual height of the building in metres.

## - Watch Video Solution

13. The model of a building is constructed with
the scale factor 1:30.

If the actual volume of a tank at the top of the
building is $27 m^{3}$, find the volume of the tank on the top of the model.

## - Watch Video Solution

14. Given $\left[\begin{array}{cc}4 & 2 \\ -1 & 1\end{array}\right] M=6 I$, where $M$ is a matrix and I is the unit matrix or order $2 \times 2$.
(i) State the order of matrix $M$.

## - Watch Video Solution

15. Given $\left[\begin{array}{cc}4 & 2 \\ -1 & 1\end{array}\right] M=6 I$, where $M$ is a matrix and I is the unit matrix or order $2 \times 2$.
(ii) Find the matrix $M$.

## D Watch Video Solution

16. The sum of the first three terms of an

Arithmeic Progression (A.P.) is 42 and the product of the first and third term is 52 . Find the first term and the common difference.
17. The vertices of a $\Delta A B C$ are $\mathrm{A}(3,8), \mathrm{B}(-1,2)$ and $C(6,-6)$. Find :
(i) Slope of BC.

## D Watch Video Solution

18. The vertices of a $\Delta A B C$ are $\mathrm{A}(3,8), \mathrm{B}(-1,2)$ and $C(6,6)$. Find :
(i) Slope of BC.
(ii) Equation of a line perpendicular to BC and passing through A.
19. Show that the SHM is projection of uniform circular motion on the diameter of a circle.

## - Watch Video Solution

20. The data on the number of patient attending a hospital in a month are given below. Find the average (mean) number of patients attending the hospital in a month by
using the shortcut method.

Take the assumed mean as 45. Give your answer correct to 2 decimal places.

| Number of <br> patients | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Dave | 5 | 2 | 7 | 9 | 2 | 5 |

( Watch Video Solution
21. Using properties of proportion solve for x ,
given
$\sqrt{5 x}+\sqrt{2 x-6}$
$\frac{\sqrt{5 x}-\sqrt{2 x-6}}{\sqrt{5 x}}=4$.

- Watch Video Solution

22. Sachin invests Rs. 8,500 in $10 \%$, Rs. 100 shares at Rs. 170 . He sells the shares when the price of each share rises by Rs. 30 . He invests the proceeds in $12 \%$ Rs. 100 shares at 125 . Find
(i) the scale proceeds.
(ii) the number of Rs. 125 shares he buys.
(iii) the change in his annual income.

## D Watch Video Solution

23. Sachin invests Rs. 8,500 in $10 \%$, Rs. 100 shares at Rs. 170. He sells the shares when the price of each share rises by Rs. 30 . He invests the proceeds in $12 \%$ Rs. 100 shares at 125 . Find
(i) the scale proceeds.
(ii) the number of Rs. 125 shares he buys.
(iii) the change in his annual income.

## - Watch Video Solution

24. Sachin invests Rs. 8,500 in $10 \%$, Rs. 100 shares at Rs. 170 . He sells the shares when the price of each share rises by Rs. 30 . He invests the proceeds in $12 \%$ Rs. 100 shares at 125 . Find
(i) the scale proceeds.
(ii) the number of Rs. 125 shares he buys.
(iii) the change in his annual income.

## - Watch Video Solution

25. Use graph paper for this question.

The marks obtained by 120 students in an

English test are given below :

| Marks | Number of students |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | 9 |
| $20-30$ | 16 |
| $30-40$ | 22 |
| $40-50$ | 26 |
| $50-60$ | 18 |
| $60-70$ | 11 |
| $70-80$ | 6 |



Draw the ogive and hence, estimate :
the median marks.
26. Use graph paper for this question.

The amrks obtained by 120 students in an

English test are given below :

| Marks | Number of students |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | 9 |
| $20-30$ | 16 |
| $30-40$ | 22 |
| $40-50$ | 26 |
| $50-60$ | 18 |
| $60-70$ | 11 |
| $70-80$ | 6 |



Draw the ogive and hence, estimate :
the number of students who did not pass test if the pass percetage was 50 .

## D Watch Video Solution

27. Use graph paper for this question.

The amrks obtained by 120 students in an

English test are given below :

| Marks | Number of students |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | 9 |
| $20-30$ | 16 |
| $30-40$ | 22 |
| $40-50$ | 26 |
| $50-60$ | 18 |
| $60-70$ | 11 |
| $70-80$ | 6 |



## Draw the ogive and hence, estimate :

the upper quartile marks.

D Watch Video Solution
28. A man observes the angle of elevation of
the top of the tower to be $45^{\circ}$. He walks towards it in a horizontal line through its base. On covering 20 m the angle of elevation change to $60^{\circ}$. Find the height of the tower correct to 2 significant figures.

## D Watch Video Solution

29. Using the Remainder Theorem find the remainders obtained when
$x^{3}+(k x+8) x+k \quad$ is divided by
$x-1$ and $x-2$.

Hence find k if the sum of the remainders is 1.

## D Watch Video Solution

30. The product of two consecutive natural numbers which are multliples of 3 is equal to 810. Find the two numbers.
31. In the given figure, $A B C D E$ is a pentagon
inscribed in a circle such that AC is a diameter and side $B C \| A E$. If $B A C=50^{\circ}$, Find angle $B C A$


- Watch Video Solution

32. In the given figure, $A B C D E$ is a pentagon
inscribed in a circle such that AC is a diameter and side $B C \| A E$. If $B A C=50^{\circ}$, Find angle CDE


- Watch Video Solution

33. In the given figure, $A B C D E$ is a pentagone inscribed in a circle such that AC is a diameter and side $\mathrm{BC} / / \mathrm{AE}$. If $\angle B A C=50^{\circ}$, find $\angle B C E$,


D Watch Video Solution

